## Chapter-4 Multiple Correlation and Regression

Multiple Correlation: - In multiple correlation we study about the association (or relation) between three or more than

Let x2, x2 and x3 be three variables where x is dependent variable and x 4 xz are independent variable. The correlation coefficient between dependent variable x and joint effect of independent variable so and x3 is called multiple correlation coefficient between x and joint effect of 22 and 23 and it is denoted by R1.23.

Also denoted by R2.13 -> If x2 is dependent variable and x fix3 are independent variables.

R3.12 -> If x3 -1s dependent variable and x1 4x2 are independent variables.

Multiple Correlation es given by
$$R_{1.23} = \sqrt{\frac{\gamma_1^2 + \gamma_3^2 - 2\gamma_2\gamma_3}{1 - \gamma_{23}^2}}$$
Similarly (or 0)

Similarly for R2.13 and R3.12.

For two variables

Correlation coefficient 
$$r = n\Sigma XY - \Sigma X \cdot ZY$$

$$\sqrt{n\Sigma X^2 - (\Sigma X)^2} \sqrt{n\Sigma Y^2 - (\Sigma Y)^2}$$

Properties of multiple Correlation Coefficient:

1) Multiple correlation coefficient lies between 0 to 1. 4ig 0 ≤ R1.23 ≤ 1

04 R2.13 41 0 = R3.12 = 1

99 > Here, R1.23 = K1.32 R2.13 = R2.31 R3.12 = R3.21

je, Correlation between x andy 48 smith

# Coefficient of Multiple determination:

Coefficient of multiple determination 18 the square of coefficient of multiple correlation so, R<sub>1,23</sub>, R<sub>2,13</sub> and R<sub>3,12</sub> are the coefficients of multiple determination.

het R1.23=0.9 then, Coefficient of multiple determination (R1.23) = (0.9)

Interpretation of (Re23) - This means total variation on dependent variables  $x_1$  18 81% that 18 explained by independ variables  $x_2$  and  $x_3$  and remaining (100-81)%=19% variation on depending variable is due to the effect of other independent variables other than x and x3.

Numerical Problems:

Q1. If M2 = 0.6, 3=0.4, 723=0.35 then,

Find the multiple correlation coefficient between x and joint effect of x2 and x3.

(P) Find the multiple correlation coefficient between x2 and joint effect of x1 and x3.

Given, 712=0.6

Here, Multiple correlation coefficient between as and joint effect

of 
$$x_1$$
 and  $x_3$  48  $R_{1.23} = \sqrt{\frac{x_1^2 + x_1^2 - 2x_{12}x_{13}^2}{1 - x_{23}^2}}$ 

$$= \sqrt{\frac{(0.6)^2 + (0.4)^2 - 2 \times 0.6 \times 0.4 \times 0.35}{1 - (0.35)^2}}$$

(P). Multiple correlation coefficient between x and joint effect of ocyand ocy 18 R2.13 =  $\frac{\gamma_{12}^2 + \gamma_{23}^2 - 2\gamma_{12} \cdot \gamma_{23} \cdot \gamma_{13}}{1 - \gamma_{13}^2}$ 

$$= \frac{(0.6)^2 + (0.35)^2 - 2 \times 0.6 \times 0.4}{1 - (0.4)^2}$$

=0.003

Nate: If (R1.23 OR R2.13 OR R3.12) > 1 then . 12, 13 and 23 are inconsistent. 92. A sample of 10 values of three variables x1, x2 and x3 were  $\leq 2x_2x_3=64$ ,  $\leq x_1^2=20$ ,  $\leq 2x_2^2=68$ ,  $\leq 2x_3^2=170$ . Hind the partial correlation coefficient between 24 and 23 eliminating first find the multiple correlation coefficient of & with x and x3. Solution, Here,  $r_{12} = \frac{n \leq x_1 \cdot x_2 - z_1 \cdot x_1 - (z_1 \cdot x_1)^2}{n \leq x_1 - (z_1 \cdot x_1)^2} \sqrt{n \leq x_2 - (z_1 \cdot x_2)^2}$ 10×10-10×20 10x20-100 10x68-400  $\Upsilon_{13} = \chi_{2} \times_{1} \times_{2} - \chi_{2} \times_{2} \times_{3}$ n 2 2 2 (2 2 1) 2 n 2 2 - (2 x3)2 10×15-10×30  $\sqrt{10\times20-(10)^2}$   $\sqrt{10\times170-(30)^2}$ 723 = n = x2x2x3- 2x2 2x3 n 2 x22 (2 x2)2 / n 2 x32 (2 x32) 10×64-20×30  $\sqrt{10\times68-(20)^2}\sqrt{10\times170-(30)^2}$ P Partial correlation coefficient between of and on eliminating the effect of on 182 98 73.2 = 713-720732 1-72 1-72  $= (-0.53) - (0.598) \times 0.085$ 1-(-0.598)2 11-(0.085)2

= 0.729

ii) Multiple correlation coefficient of x with x and x 18,

$$R_{1.23} = \sqrt{\frac{\gamma_{12}^{2} + \gamma_{13}^{2} - 2\gamma_{13}\gamma_{23}}{1 - \gamma_{23}^{2}}}$$

$$= \sqrt{\frac{(-0.598)^{2} + (-0.53)^{2} - 2\times(-0.598)\times(-0.53)\times0.085}{1 - (0.085)^{2}}}$$

$$= 0.7(7)$$

Partial Correlation Coefficient:

correlation coefficient between  $x_1$  and  $x_2$  when  $x_3$  is taken as constant is given denoted by  $R_{12.3}$  and given as:

Similarly for 13.2 and 723.1

Properties:

is Partial correlation coefficient lies between -1 to +1.

اروباری 
$$-1 \leq \gamma_{12,3} \leq +1$$
 $-1 \leq \gamma_{13,2} \leq +1$ 
 $-1 \leq \gamma_{23,2} \leq +1$ 
 $-1 \leq \gamma_{23,2} \leq +1$ 

11> Here, 721.3 = 712.3 731.2=713.2  $\gamma_{32.1} = \gamma_{23.1}$ 

Coefficient of partial determination: Coefficient of partial determination As the square of coefficient of partial correlation. So, 72.3, 72.3 and 723. 1 are the coefficient of partial determination.

Interpretation > het coefficient of partial correlation ( $\tau_{3.2}$ ) =0.8

Then coefficient of partial determination is ( $\tau_{3.2}^2$ ) = (0.8)<sup>2</sup> = 0.64

This means the total variation on dependent variable is 64% that is explained by independent variable  $\tau_3$  when the independent variable  $\tau_2$  is taken as constant and remaining 36% variation on  $\tau_3$  is due to the effect of other independent variation.

93. From the data given below find  $\eta_{12.3}$ ,  $R_{1.23}$ ,  $\tau_{23.1}$  and  $R_{2.13}$   $\Xi_{1}x_{1}x_{2}=40$ ,  $\Xi_{1}x_{3}=55$ ,  $\Xi_{2}x_{2}x_{3}=35$   $\Xi_{1}x_{1}^{2}=90$ ,  $\Xi_{1}x_{2}^{2}=60$ ,  $\Xi_{1}x_{3}^{2}=50$ 

Solution where  $x_1, x_2$  and  $x_3$  are variables measured from their mean.

Given,  $\leq x_1 x_2 = 40$ ,  $\leq x_1 x_3 = 55$ ,  $\leq x_2 x_3 = 35$ .

 $\leq x_1^2 = 90, \leq x_2^2 = 60, \leq x_3^2 = 50$ 

Since, x1, x2 and x3 are measured from their mean.

So, 
$$Y_{12} = \frac{\leq x_1 x_2}{\sqrt{2} x_1^2}$$

$$= \frac{40}{\sqrt{90} \sqrt{60}}$$

$$= 0.54$$

Now,  $\gamma_{12.3} = \gamma_{12} - \gamma_{13}\gamma_{23}$   $= \sqrt{1 - \gamma_{13}^2} \sqrt{1 - \gamma_{23}^2}$   $= 0.54 - 0.639 \times 0.819$   $= \sqrt{1 - (0.639)^2} \sqrt{1 - (0.819)^2}$ 

0.038

Rough

We know that

$$T = \frac{Cov(X,Y)}{\nabla x}$$
 $T = \frac{\nabla x}{\nabla y}$ 
 $T = \frac{\nabla x}{\nabla y}$ 

check the answers

check the answers

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while using them as normal

consider them as normal

errors and correct yourself.

$$R_{1.23} = \int \frac{\gamma_{12}^2 + \gamma_{13}^2 - 2\gamma_{12} \gamma_{13} \gamma_{23}}{1 - \gamma_{23}^2}$$

$$= \int \frac{(0.54)^2 + (0.639)^2 - 2 \times 0.54 \times 0.639 \times 0.819}{1 - (0.819)^2}$$

$$= 0.64$$

$$\gamma_{23,1} = \gamma_{23} - \gamma_{12} \cdot \gamma_{13}$$

$$= 0.819 - 0.54 \times 0.639$$

$$= 0.73$$

$$R_{2.13} = \sqrt{\gamma_{12}^2 + \gamma_{23}^2 - 2\gamma_{12} \cdot \gamma_{23} \cdot \gamma_{13}}$$

$$= 1 - \gamma_{12}^2$$

$$= \sqrt{\frac{(0.54)^2 + (0.819)^2 - 2 \times 0.54 \times 0.819 \times 0.639}{1 - (0.639)^2}}$$

= 0.82

94 From the information given below calculate 7,2.3, 8,3,2 and 7,23.1.

74	6	8	9	11	12	14
$x_2$	-			18		23
$x_3$	21 .	22	27	29	31	32.

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	16/25		_						A STATE OF				
	24	$\infty_1$	$\alpha_2$	u=x-	$v = x_2 - 6$ $= x_2 - 1$		u <sup>2</sup>	102	W2	uv	Lw	vw	Mary -
	6	14	21	-3	-3	-8	9	9	64	9	24	24	
	8	16	22	-1	_1					100			
	9	1.7	27	0		+	1	1	49	1	7	チ	
	11	13	29	2	1	-2	0	0	4	0	0	0	
	10					O	4	1	0	2	0	0	
	12	20	31	3	3	2	9	9	4	9	6	6	
	14	23	32	5	6	3	0-						
T							25	36	9	30.	15	18	
			-	<b>≤</b> 1u=6	20=6.	≤w=12	2H=	Zv²=	Źw²	Suv	£4₩ =52	ZVW	Ĺ
-							48	56	=130	=51	=52	=55	١

$$\gamma_{23} = n \leq vw - \leq v \cdot \leq w$$

$$\sqrt{n \leq v^2 - (\leq v)^2} \sqrt{n \leq w^2 - (\leq w)^2}$$

$$= 6 \times 55 - 6 \times (-12)$$

$$\sqrt{6 \times 56 - (6)^2} \sqrt{6 \times 130 - (-12)^2}$$

= 0.92

=0.95°

$$\gamma_{13.2} = \gamma_{13} - \gamma_{12} \cdot \gamma_{23}$$

$$\sqrt{1 - \gamma_{12}^2} \sqrt{1 - \gamma_{23}^2}$$

$$= 0.95 - 0.98 \times 0.92$$

$$\sqrt{1 - (0.98)^2} \sqrt{1 - (0.92)^2}$$

$$= 0.65$$

$$\gamma_{23.1} = \gamma_{23} - \gamma_{12} \cdot \gamma_{13} \\
= \frac{\sqrt{1 - \gamma_{12}^2} \sqrt{1 - \gamma_{13}^2}}{\sqrt{1 - (0.98)^2} \sqrt{1 - (0.95)^2}} \\
= \frac{0.92 - 0.98 \times 0.95}{\sqrt{1 - (0.95)^2}}$$

Are the following data consistent;  $Y_{23} = 0.8, Y_{31} = -0.5, Y_{12} = 0.6.$ Soly For testing it is consistency we need to find multiple correlation coefficient  $R_{1.23}$ . (We take  $R_{1.23}$ , also we can take  $R_{2.13}$  or  $R_{3.12}$  for testing

Now, 
$$R_{1.23} = \sqrt{\frac{\gamma_{12}^2 + \gamma_{13}^2 - 2\gamma_{12} \cdot \gamma_{13} \cdot \gamma_{23}}{1 - \gamma_{23}^2}}$$
  

$$= \sqrt{\frac{(0.6)^2 + (-0.5)^2 - 2 \times 0.6 \times (-0.5) \times 0.8}{1 - (0.8)^2}}$$

Since R1.23 ± 1.218 > 1. (Not in the range of 0 to 1). So, the data are inconsistent.

Multiple Regression:—
Multiple Regression 18 the functional relationship
between three or more than three variables where one variable
18 dependent and remaining are independent variable, by the
use of regression model we can be able to estimate the value
of dependent variable with the help of independent variable. dependent and  $x_2$  and  $x_3$  are three variables, of  $x_1$  of  $x_2$  and  $x_3$  are independent then, the multiple regression equation es,  $_{7}X_{1} = a + b_{1}X_{2} + b_{2}X_{3}$ also we conface)
take y implace) where, a -> ×1 Intercept. b\_1 + regression coeff. of x1 on X2 when X3 is taken as constant. b2 + regression coeff. of x3 on x3 when X3 is taken as constant. For finding the values of a, b, and b, we have, By using least square method the normal equations aret Solving these three equations (P), (IP) and (P) we get the value of a, b, 4 b, Finally substituting values of a, b, 4 b, in eqn (9) we get the solution.

9.N.6 The table shows the corresponding values of the three, variables X1, X2 and X3. X1: 5 7 8.6 10 9 X2: 12 20 30 40 33 25 X3: 51 55 58 60 70 66 Find the regression equation of X1 on X2 and X3. Estimate, X1 when X2=50 and X3=100. Where X1 represents pull length, X2 represents wire length and X3 represents die height. regression equation 48; Salso we can write to in place of a For finding the value of a, b, and b, we have the following normal equations,  $\leq 1 \times_2 = na + b_2 \leq 1 \times_2 + b_2 \leq 1 \times_3 - (P)$ ZIX1X2= aZX2+bZX2+bZX2+bZX2-000 ZX1X3 = a ZX3+b ZX2X3+b2 ZX3-60. for the calculation of ZIX1, ZIX2, ZIX3, ZIX2, ZIX3, Six1x2, Six2x3, Six1x3 we proceed as following table.  $\chi_2$  $\chi_3$  $X_1X_2$  $X_1 X_3$  $\chi_2\chi_3$ 

EX1=45 EX2=160 EX3=360 EX2=4758 EX2=21846 EX1X2=1235 EX1X3=2758 EXX2X3=9812

Now, we put the values of \$\( X\_1, \in X\_2 \) \( X\_3, \in X\_2^2, \in X\_3^2, \in X\_4 X\_2 \), Zi X2 X3, Zi X1 X3 and n m m m m m and m. 160a + 4758b1+9812b2 = 1235 - VP 360a +9812b1+21846b2 = 2758 \_\_\_ (vir). Using Cramer's Rule (OR, we can find a, b, b2 by directly solving equations). Coefficient of be coefficient of be coefficient of be Constant 160 3.60 45 4758 21846 9812 2758  $D = \begin{vmatrix} 6 & 100 \\ 160 & 4758 & 9812 \\ 360 & 9812 & 21846 \end{vmatrix}$ =6(103943268-96275344)-160(3495360-3532320) + 360 (1569920-1712880) - 455544 Similarly  $D_{1} = \begin{vmatrix} 45 & 160 & 360 \\ 1235 & 4758 & 9812 \\ 2758 & 9812 & 21846 \end{vmatrix}$ = 45(103943268-96275344)-160(26979810-27061496) +360(12117820-13122564) = -3581500 $D_2 = \begin{vmatrix} 6 & 45 & 360 \\ 160 & 1235 & 9812 \\ \hline 360 & 2758 & 21846 \end{vmatrix}$ = 6 (26979810-27061496)-45(3495360-3532320)

+360(441280-444600)

= -22116.

$$D_3 = \begin{vmatrix} 6 & 160 & 45 \\ 160 & 4758 & 1235 \\ 360 & 9.812 & 2758 \end{vmatrix}$$

$$= 6(13122564 - 12117820) - 160(441280 - 444600) + 45(1569920 - 1712880)$$
  
= 126464

Here,
$$0 = \frac{D_1}{D} = \frac{-3581500}{4.55544} = -7.862$$

$$0_1 = \frac{D_2}{D} = \frac{-22116}{4.55544} = -0.048$$

$$0_2 = \frac{D_3}{D} = \frac{126464}{4.55544} = 0.277$$

Now putting values of a, b\_1 & b\_2 on (3) we get regression equation of x\_1 on x\_2 and x\_3 as;

$$X_1 = -7.862 - 0.048 \times_2 + 0.277 \times_3$$
.

Again, 
$$X_1$$
 when  $X_2 = 50$  and  $X_3 = 100$  48,  $X_1 = -7.862 - 0.048 \times 50 + 0.277 \times 100$   $= -7.862 - 2.4 + 27.7$   $= 27.7 - 10.262$   $= 17.438$ 

## 8. Measure of variation:

Total variation: (Total sum of square) = explained variation (sum of

Square due to regression) + unexplained variation (sum

of square due to error.

or we con write

.. TSS = SSR + SSE

or, SSR = TSS - SSE

where;  $TSS = \leq (Y - \overline{Y})^2$ =  $\leq Y^2 - n\overline{Y}^2$ 

derived from

Y=b+b,X1+b2X2

2 6, EY-b, EYX-6, EXX

4 SSE= ZI (Y-Y)2 = ZIYZ-b\_ZYX\_-b\_ZYX\_

## @ Coefficient of Determination:

Coefficient of determination is also determined

as 
$$(R^2) = \frac{SSR}{TSS}$$
  
or,  $R^2 = \frac{TSS - SSE}{TSS}$  ("SSR=TSS-SSE)  
or,  $R^2 = 1 - \frac{SSE}{TSS}$ 

Interpretation: > Coefficient of determination that measures the total variation on dependent variable explained by Independent variable.

## @. Standard Error of Estimate (S.E):

Standard error of estimate (S.E) = 
$$\int SSE$$
 $N=k-1$ 

Where,  $n=n0$ , of observations.
 $k=n0$ . of independent variable.

Q.N.7 From following Information of variables X1, X2 and X3  $\leq 10^{-13}$ ,  $\leq 10^{-11}$ ,  $\leq X_2 X_3 = 136, \leq X_1 X_2 = -240, \leq X_3^2 = 450, n = 10.$ Find the regression equation of X3 on X1 and X2 and. interpret the regression coefficients,

Predict X3 when X1=1 and X2=4. (1) Compute TSS, SSR and SSE.

(V) Compute standard error of estimate. () Compute the coefficient of multiple determination and interpret. Given, the regression equation of X3 on X1 and X2 18 For finding bo, be 4 be we need to solve the following normal equations:  $\leq X_3 = nb_0 + b_1 \leq X_1 + b_2 \leq X_2 - 0$ = X1X3=b0=X1+b1=X1+b2=X1X2-00 Now, putting the given values in an (1), (11) and (10),  $10b_0 + 13b_1 + 11b_2 = 51$ . 13bo +63b1-240b2=77 # 1160 - 24061+956,=136 Using Cramers Rule.

Coeff. bo	Coeff. b.	Coeff. b2	Constants
10	13	11	51
13	63	-240	77
11	-240	95	136

 $D = \begin{vmatrix} 10 & 13 & 11 \\ 13 & 63 & -240 \\ 11 & -240 & 95 \end{vmatrix}$ 

=10(5985-57600)-13(1235+2640)+11(-3120-693)

$$= -516150 - 50375 - 41943$$

$$= -608468$$

$$\mathcal{D}_{1} = \begin{vmatrix} 51 & 13 & 11 \\ 77 & 63 & -240 \\ 136 & -240 & 95 \end{vmatrix}$$

$$= 51(5985 - 57600) - 13(7315 + 32640) + 11(-18480 - 8568)$$

$$= -2632365 - 519415 - 297528$$

$$= -3449308$$

$$\mathcal{D}_{2} = \begin{vmatrix} 10 & 51 & 11 \\ 13 & 77 & -240 \\ 11 & 136 & 95 \end{vmatrix}$$

$$= 10(7315 + 32640) - 51(1235 + 2640) + 11(1768 - 847)$$

$$= 399550 - 197625 + 10131$$

$$= 212056$$

$$\mathcal{D}_{3} = \begin{vmatrix} 10 & 13 & 51 \\ 13 & 63 & 77 \\ 11 & -240 & 136 \end{vmatrix}$$

$$= 10(8568 + 19480) - 13(1768 - 847) + 51(-3120 - 693)$$

$$= 270480 - 11973 - 194463$$

$$= 64044$$

$$Now, b_{0} = \frac{\mathcal{D}_{1}}{\mathcal{D}} = \frac{-3449308}{-608468} = 5.66$$

$$b_{1} = \frac{\mathcal{D}_{2}}{\mathcal{D}} = \frac{-212056}{-608468} = -0.348$$

$$b_{2} = \frac{\mathcal{D}_{3}}{\mathcal{D}} = \frac{64044}{-608468} = -0.105$$

$$\text{The Only putting values of b_{0}, b_{1}4b_{2}+m \text{ The get regression equation}$$

of  $X_3$  on  $X_1$  and  $X_2$  as:  $X_3 = 5.7 - 0.348 X_1 - 0.105 X_2$ .

If  $X_3$  when  $X_1 = 1$  and  $X_2 = 4.8$ :  $X_3 = 5.7 - 0.348 \times 1 - 0.105 \times 4$   $X_3 = 5.7 - 0.348 \times 1 - 0.105 \times 4$   $X_4 = 4.932$ 

i) ((ontinue) part: Interpretation -> Since, b\_=-0.348, this means the value of dependent variable 18 decreased by -0.348 as per unit change in the value of  $x_1$  and  $b_2 = -0.105$ , this means value of endependent variable 18 decreased by -0.105 as per unit change in value of X2.

Here, TSS=ZIX3-nX3  $\left( \begin{array}{c} \begin{array}{c} \begin{array}{c} \begin{array}{c} \end{array} \\ \end{array} \begin{array}{c} X_3 \end{array} \end{array} \right) = \frac{X_3^2}{X_3}$  $=450-10\times(8.82)^{2}$ =450-778.5467= -328.5467

> SSE = = 1x32-b = 1x3-b = 1x3x1-b2 = 1x3x2  $=450-5.66 \times 51+0.348 \times 77+0.105 \times 136$ 二 450-288.66+26,796+14.28 = 202.416

& SSR = TSS-SSE = -328.5467 - 202.416=-530,9627

iv) Standard error of estimate (S.F) = 1 SSE  $=\sqrt{\frac{202.416}{10-2-1}}$ -5.377

v) Coefficient of multiple determination es given by, This question is from 9. N.20

(R3.12) = SSK TSS -530.9627- 328.5 467

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यो १ भन्दी समी

D. Significance lest of regression Coefficient: Warder 9.No.8: Given the following information from a multiple regression attalysis; n=20, b1=4, b2=3, Sb1=1.2, Sb2=0.8. At 0.05 level of significance determine whether each of explanatory (dependent) variable makes a significant contribution to the regression model. Sb\_1=1.2 (i.e, standard, error of b\_1) Sb\_2 = 0.8 (i.e, standard error of b\_2). level of significance = < = 0.05. Problem to test: Null hypothesis (Ho);  $f_1 = 0$  i.e. there is no linear relationship between dependent variable  $X_1$ . Alternative hypothesis (H1); \$ \$ = 0 ie, there is linear relationship Test statistics:  $t_{cal} = \frac{b_1}{5b_2} = \frac{4}{1.2} = 3.33$ between dependent variable Y and independent variable X1. Creffical value— the tabulated value of 't' at 0.05 level of significant with n-k-1 degree of freedom 18 (to.05, 20-2-1) from table given back of book in page no 318  $= t_{0.05}, 17$ = 2.110 Decision: > Since toul =3.33 > tous = 2.110

So, Ho 48 rejected in H1 48 accepted. Conclusion - Hence, there is linear relation between dependent variable Y & independent variable Xi. Note: - We have done for 1/2, Similarly we can do same for 1/2.

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Q.N.9: In order to establish the functional relationship between. anual salaries (y), years of educated high school (x1) and years Variables were collected from a random sample of 10 persons working in a large firm. Analysis of data produces the following results. The sum of squares  $\Xi(Y-Y)^2 = 397.6.5$  um of squares due to enone  $\Xi(Y-Y)^2 = 397.6.5$  un of significance of regression coefficients at 5% level of significance. We have, regression model, Y=bo+b1 X1+b2 X2. Z(Y-Y)2=T5S=397.6  $= (Y-Y)^2 = SSE = 235$ So, SSR=TSS-SSE = 397.6 - 23.5= 1374.1. Null hypothesis (Ho); B=B=0. Ties there 78 no linear relationship between dependent variable Y and independent variables X &X2. Alternative hypothesis (H1); 1 + 12 + 0. vie there is linear Question III overall word 3117
ZIT Fear method ATIZ JIP where, MSR-> Mean square due to regression.
MSE-> Mean square due to error. and MSR = SSR defree of freedom (d.f) MSF = SSE dif

Now, we construct ANOVA table for regression analysis:

			0	· V
Source of Variation	dégree of freedom	Sum of Square	MSS	Fal.
Regression	F=2	SSR=374,1	$MSR = \frac{SSR}{d_1 \cdot f}$ = $\frac{374.1}{2}$ = 187.05	$F_{col} = \frac{MSR}{MSE}$ = 187.05
Error	n-F-1=7	SSE= 23.5	MSE= <u>23.5</u> 7 =3.35	= 55.83
Total	m-1 = 10-1	TSS=397. 6	5	

Critical valve—the tabulated value of Fat 0.05 level of significance with (2,7) d.f 18 fo.05 (2,7). from table from table given in book

Decision -> Since Feal = 55.835 Feab = 4.74 So, Ho 18 rejected.

41.8 H1 18 accepted.

Equals to or smaller

3777 accept 5-6

Conclusion -> Hence we can conclude that there is linear relationship between Y and independent variables.