

```
U۷
            CONSTEYAL THE HAMITHAGES - COTTINHT NACVETS/NTTSLELLOSS///
 63
            constexpr int num_warps = num_buckets / kWarpSize;
 64
 65
            __shared__ int sums[num_warps];
 66
            __shared__ int histogram_smem[num_buckets];
            const int tid = blockIdx.x * blockDim.x + threadIdx.x;
 67
 68
            for (int i = tid; i < num_buckets; i += blockDim.x)</pre>
 69
 70
            {
 71
                histogram_smem[i] = histogram[i];
                histogram[i] = 0; // 设置histogram的所有值为0, 用于初始化下一次pass
 72
 73
            __syncthreads();
 74
 75
 76
            int lane_id = tid % kWarpSize;
 77
            int warp_id = threadIdx.x / kWarpSize;
 78
            int value = histogram_smem[tid];
 79
            // using a shfl instruction for a scan. (Hillis Steele scan)
 80
            for (int i = 1; i < kWarpSize; i *= 2)</pre>
 81
 82
 83
                uint mask = 0xffffffff;
 84
                int n = __shfl_up_sync(mask, value, i, kWarpSize);
 85
                if (lane_id >= i)
 86
                {
                    value += n;
 87
 88
                }
            }
 89
 90
 91
            // write the sum of the warp to smem
            if (threadIdx.x % kWarpSize == kWarpSize - 1)
 92
 93
 94
                sums[warp_id] = value;
 95
            __syncthreads();
 96
 97
 98
            // scan sum the warp sums
 99
            if (warp_id == 0 && lane_id < num_warps)</pre>
100
            {
101
                int warp_sum = sums[lane_id];
                uint mask = (0\times01 << num\_warps) - 1;
102
                for (int i = 1; i < num_warps; i *= 2)</pre>
103
104
105
                    int n = __shfl_up_sync(mask, warp_sum, i, num_warps);
                    if (lane_id >= i)
106
107
                    {
108
                        warp_sum += n;
109
                    }
                }
110
111
                sums[lane_id] = warp_sum;
112
113
            }
            __syncthreads();
114
115
116
            // perform a uniform add across warps in the block
117
            // read neighbouring warp's sum and add it to threads value
118
            int block_sum = 0;
119
            if (warp_id > 0)
120
                block_sum = sums[warp_id - 1];
121
122
            histogram_smem[tid] = value + block_sum;
123
124
            // choose bucket
125
            int k = counter->k;
126
            int len = counter->len;
127
            __syncthreads();
128
129
            for (int i = tid; i < num_buckets; i += blockDim.x)</pre>
130
            {
131
                int pre = (i == 0) ? 0 : histogram_smem[i - 1];
132
                int cur = histogram_smem[i];
133
134
                // one and only one thread will satisfy this condition, so counter is written by only one thread
135
                if (pre < k && cur >= k)
136
                {
137
```

```
// how many values still are there to find
138
                    counter->k = k - pre;
139
                    counter->len = cur - pre; // number of values in next pass
                    counter->prev_len = len;
140
                    counter->bucket_bits = i; // bucket
141
                }
142
            }
143
144
            if (tid == 0)
145
146
            {
147
                counter->filter_cnt = 0; // 重新设置filter_cnt的值为0
            }
148
        }
149
150
151
        template <int BitsPerPass>
152
        static __global__ void filter_kernel(const uint* in_buf, const int* in_idx,
153
                                             uint* out_buf, int* out_idx,
154
                                             int* out_index, Counter* counter,
155
                                             const int pass, const bool select_min)
        {
156
157
            constexpr int num_buckets = cal_num_buckets<BitsPerPass>();
158
            uint select_bucket = counter->bucket_bits;
            uint bucket_bits = (select_min ? select_bucket : (select_bucket ^ ((0x01 << BitsPerPass) - 1)));</pre>
159
160
161
            const int tid = blockIdx.x * blockDim.x + threadIdx.x;
162
            for (int idx = tid; idx < counter->prev_len; idx += gridDim.x * blockDim.x)
163
164
                uint mask = float_flip(in_buf[idx]);
165
                mask = mask >> (32 - BitsPerPass * (pass + 1));
166
                uint bits = mask & ((0x01 << BitsPerPass) - 1);
167
168
                if (bits == bucket_bits)
169
                    // int pos = atomicAdd(&counter->filter_cnt, 1);
170
171
                    int pos = atomicAggInc_cg(&counter->filter_cnt);
172
                    out_buf[pos] = in_buf[idx];
173
                    out_idx[pos] = in_idx[idx];
174
                }
175
                else if ((bits < bucket_bits) == select_min)</pre>
176
177
                    // int pos = atomicAdd(&counter->output_cnt, 1);
178
                    int pos = atomicAggInc_cg(&counter->output_cnt);
179
                    out_index[pos] = in_idx[idx];
180
                    // 如果实际的topk的值,在数据集中有多个相等的值,(这里收集到的值肯定小于topk)
181
                    // 则在最后一个pass后,将out_idx的指标都附加到out_index后面,直到数据个数为topk个
182
                }
            }
183
184
185
        }
186
187
        static __global__ void gather_kernel(int* out_index, int* in_index,
188
                                             Counter* counter, const int* num_elements,
189
                                             const int topk)
190
        {
            const int output_len = MIN(*num_elements, topk);
191
192
            const int tid = blockIdx.x * blockDim.x + threadIdx.x;
            for (int idx = tid; idx < (output_len - counter->output_cnt); idx += gridDim.x * blockDim.x)
193
194
            {
                out_index[counter->output_cnt + idx] = in_index[idx];
195
196
197
198
        }
199
        // topk operator
200
201
202
            for (int pass = 0; pass < num_passes; ++pass)</pre>
203
204
                // 1. Calculate histogram
                constexpr int TS_topk = 16;
205
206
                const int GS_topk = (total_num_score_ + (BS * TS_topk) - 1) / (BS * TS_topk);
                histogram kernel<BitsPerPass><<<GS topk, BS, 0, cu stream>>>
207
208
                                (in_buf, histogram, counter, pass, select_min);
209
210
                // 2. Scan the histogram (Inclusive prefix sum)
                // 3. Choose the bucket (Find the bucket j of the histogram that the k-th value falls into)
211
                scan select kernel<BitsPerPass><<<1, num buckets, 0, cu stream>>>
212
213
                                    (histogram, counter);
```

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214
               // 4. Filtering (Input elements whose digit value <j are the top-k elements)</pre>
215
                filter_kernel<BitsPerPass><<<GS_topk, BS, 0, cu_stream>>>
216
217
                                (in_buf, in_idx, out_buf, out_idx,
218
                                output_index, counter, pass, select_min);
219
                in_buf = (pass % 2 == 0) ? buf_value_1 : buf_value_2;
220
                in_idx = (pass % 2 == 0) ? buf_index_1 : buf_index_2;
221
                out_buf = (pass % 2 == 0) ? buf_value_2 : buf_value_1;
222
                out_idx = (pass % 2 == 0) ? buf_index_2 : buf_index_1;
223
           }
224
225
            gather_kernel<<<1, BS, 0, cu_stream>>>(output_index, in_idx, counter, ws1_data, total_num_out_);
226
227
       }
```