Guidelines For Finding a Taylor Series

1. Differentiate f with respect to x serveral times and evaluate each derivative at c

$$f(c), f'(c), f''(c), \dots, f^{(n)}(c), \dots$$

Try to recognize a pattern in these numbers.

2. Use the sequence developed in the first step to form the Taylor coefficients $a_n = \frac{f^{(n)}(c)}{n!}$ and determine the interval of convergence for the resulting power series

$$f(c) + f'(c)(x-c) + \frac{f''(c)}{2!}(x-c)^2 + \ldots + \frac{f^{(n)}(c)}{n!}(x-c)^n + \ldots$$

3. Within this interval of convergence, determine whether the series converges to f(x).