## CSCI 561 Foundation for Artificial Intelligence

## Discussion Section (Week 4)

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Given a Gridworld domain, where terminal states (1,3), (4,3), and (4,2) have rewards 50, 500, and -50 respectively, the set of possible actions are {N,E,S,W, or X for terminal states}, the agent moves deterministically, all V and Q values for non-terminal states have been initialized to 0.0, answer the questions below.

	atxto			
3	50	155	な	500
2	vs		125	-50
1	17-92	31.72	125	31-25
	1	2	3	4

Circle the letter that corresponds to the best answer for the question.

What are the optimal utility values V for each state in the above grid if y = 0.5, c(a)=0, R(s)=0 for the nonterminal states?

(Remember  $V_{t+1}(s) = R(s) + Max_{a\epsilon A}\{c(a) + \gamma \Sigma_{s'\epsilon S} P(s'|a,s) V_t(s')\}$ )

- $\begin{array}{l} V_{(1,1)} \! = \! 15.75, \, V_{(1,2)} \! = \! 25, \, V_{(2,1)} \! = \! 31.25, \, V_{(2,3)} \! = \! 125, \, V_{(3,1)} \! = \! 62.5, \, V_{(3,2)} \! = \! 125, \, V_{(3,3)} \! = \! 250, \, V_{(4,1)} \! = \! 25 \\ V_{(1,1)} \! = \! 12.5, \, V_{(1,2)} \! = \! 25, \, V_{(2,1)} \! = \! 31.25, \, V_{(2,3)} \! = \! 125, \, V_{(3,1)} \! = \! 62.5, \, V_{(3,2)} \! = \! 125, \, V_{(3,3)} \! = \! 250, \, V_{(4,1)} \! = \! 31.25 \\ V_{(1,1)} \! = \! 15.625, \, V_{(1,2)} \! = \! 25, \, V_{(2,1)} \! = \! 31.25, \, V_{(2,3)} \! = \! 125, \, V_{(3,1)} \! = \! 62.5, \, V_{(3,2)} \! = \! 125, \, V_{(3,3)} \! = \! 250, \, V_{(4,1)} \! = \! 31.25 \\ V_{(1,1)} \! = \! 12.5, \, V_{(1,2)} \! = \! 25, \, V_{(2,1)} \! = \! 25, \, V_{(2,3)} \! = \! 25, \, V_{(3,1)} \! = \! 50, \, V_{(3,2)} \! = \! 100, \, V_{(3,3)} \! = \! 250, \, V_{(4,1)} \! = \! 25 \\ V_{(4,1)} \! = \! 25, \, V_{(2,1)} \! = \! 25, \, V_{(2,3)} \! = \! 25, \, V_{(3,1)} \! = \! 50, \, V_{(3,2)} \! = \! 100, \, V_{(3,3)} \! = \! 250, \, V_{(4,1)} \! = \! 25 \\ V_{(4,1)} \! = \! 25, \, V_{(2,1)} \! = \! 25, \, V_{(2,3)} \! = \! 25, \, V_{(3,1)} \! = \! 50, \, V_{(3,2)} \! = \! 100, \, V_{(3,3)} \! = \! 250, \, V_{(4,1)} \! = \! 25 \\ V_{(4,1)} \! = \! 25, \, V_{(2,1)} \! = \! 25, \, V_{(2,3)} \! = \! 25, \, V_{(3,1)} \! = \! 50, \, V_{(3,2)} \! = \! 100, \, V_{(3,3)} \! = \! 250, \, V_{(4,1)} \! = \! 25 \\ V_{(4,1)} \! = \! 25, \, V_{(4,1)} \! = \! 25, \, V_{(2,1)} \! = \! 25, \, V_{(2,3)} \! = \! 25, \, V_{(3,1)} \! = \! 50, \, V_{(3,2)} \! = \! 100, \, V_{(3,2)} \! = \! 250, \, V_{(4,1)} \! = \! 25, \, V_{(4,1)} \! = \!$
- None of the above

## **Q-Learning**

What are the Q values of state (3,2) in the above grid if  $\gamma = 0.5$ , c(a)=0, R(s)=-2 for non-terminal states?

(Remember 
$$Q_{t+1}(a,s) = R(s) + c(a) + \gamma \Sigma_{s' \in S} P(s'|a,s) \max_{a' \in A} Q_t(a's')$$
)

a. 
$$Q_{((3,2),N)}=122$$
,  $Q_{((3,2),E)}=-27$ ,  $Q_{((3,2),S)}=59$ 

**b** 
$$Q_{((3,2),N)}=122, Q_{((3,2),E)}=-27, Q_{((3,2),S)}=27.5$$

c. 
$$Q_{((3,2),N)}=125$$
,  $Q_{((3,2),E)}=-25$ ,  $Q_{((3,2),S)}=62.5$ 

d. 
$$Q_{((3,2),N)} = 120$$
,  $Q_{((3,2),E)} = -27$ ,  $Q_{((3,2),S)} = 31.5$ 

e. None of the above

