

Max Heaps and Heapsort

.add() Method

The .add() method is used in the MaxHeap class to add new values to a max-heap while maintaining the max-heap property that a parent must have a larger value than its children.

```
def add(self, element):
    self.count += 1
    print("Adding: {0} to
{1}".format(element, self.heap_list))
    self.heap_list.append(element)
    self.heapify up()
```

.heapify_up() Method

The .heapify_up() method is used in the MaxHeap class to rebalance the heap data structure after an element is added to it.

Starting at the end of the heap where the new element is placed, the new element is compared to its parent value. If the parent has a smaller value than the child, the values swap places. This process repeats itself until an element has no parent value.

```
def heapify_up(self):
    print("Heapifying up")
    idx = self.count
    while self.parent_idx(idx) > 0:
        child = self.heap_list[idx]
        parent =
    self.heap_list[self.parent_idx(idx)]
        if parent < child:
            print("swapping {0} with
        {1}".format(parent, child))
            self.heap_list[idx] = parent
    self.heap_list[self.parent_idx(idx)] = child
        idx = self.parent_idx(idx)
        print("Heap Restored
        {0}".format(self.heap list))</pre>
```



Heapsort

Heapsort is a sorting algorithm that utilizes the heap data structure to sort an unordered list of data. To implement a heapsort algorithm, take the following steps:

- Add items of an unsorted list into a max-heap.
- While there is at least one element in the heap, remove the root of the heap and place it at the beginning of a list that will hold the sorted values. Whenever the root is extracted, the heap must be rebalanced.
- Once the heap is empty, return the sorted list.

```
def heapsort(lst):
  sort = []
 max heap = MaxHeap()
  # Add items of an unsorted list into a
max-heap.
  for idx in 1st:
    max heap.add(idx)
  # While there is at least one element
in the heap, remove the root of the heap
and place it at the beginning of a list
that will hold the sorted values.
Whenever the root is extracted, the heap
must be rebalanced.
  while max heap.count > 0:
    max value = max heap.retrieve max()
    sort.insert(0, max value)
  # Return the sorted list
  return sort
my list = [99, 22, 61, 10, 21, 13, 23]
sorted list = heapsort(my list)
print(sorted list) # Prints: [10, 13, 21,
22, 23, 61, 99]
```



.retrieve_max() Method

The <code>.retrieve_max()</code> method is used in the heapsort algorithm to return the largest value in a heap. In this method, the root of the heap is extracted and replaced by the last element in the heap. Then, the method rebalances the heap data structure using <code>.heapify_down()</code> . Finally, the method returns the largest value.

```
def retrieve max(self):
  if self.count == 0:
   print("No items in heap")
    return None
  # Store the largest value in a variable
  max value = self.heap list[1]
  print("Removing: {0} from
{1}".format(max value, self.heap list))
  # Replace the root of the heap with the
last element in the list
  self.heap list[1] =
self.heap list[self.count]
  # Decrease the count
  self.count -= 1
  # Remove the last element in the list
  self.heap list.pop()
  print("Last element moved to first:
{0}".format(self.heap list))
  # Rebalance the heap
  self.heapify down()
  # Return the largest value
  return max value
```



.heapify_down() Method

The .heapify_down() method is used in the heapsort algorithm to rebalance the heap data structure after the root is removed and replaced with the last element in the heap.

While an element contains a child value, the parent value is compared with the value of its largest child. The larger child is determined using the

.get_larger_child_idx() method. If the parent has a smaller value than the child, the two elements are swapped. Once an element has no children, the heap is restored.

```
def heapify down(self):
  idx = 1
  # This while loop will execute as long
as a child element is present
  while self.child present(idx):
    print("Heapifying down!")
    # Get the index of the child element
with the larger value
    larger child idx =
self.get larger child idx(idx)
    child =
self.heap list[larger child idx]
    parent = self.heap list[idx]
    # If the parent value is less than
the child value, swap the values
    if parent < child:</pre>
      self.heap list[idx] = child
      self.heap list[larger child idx] =
parent
    idx = larger child idx
  print("HEAP RESTORED!
{0}".format(self.heap list))
```



.get_larger_child_idx() Method

The .get_larger_child_idx() method, which is used in the heapsort algorithm, compares the values of an element's children and returns the index of the child with the larger value.

```
def get larger child idx(self, idx):
  # Check if a right child exists
  if self.right child idx(idx) >
self.count:
    print("There is only a left child")
    return self.left child idx(idx)
  else:
    left child =
self.heap list[self.left child idx(idx)]
    right child =
self.heap list[self.right child idx(idx)]
    # Compare the left and right child
values and return the index of the larger
child
    if left child > right child:
      print("Left child "+
str(left child) + " is larger than right
child " + str(right child))
      return self.left child idx(idx)
    else:
      print("Right child " +
str(right child) + " is larger than left
child " + str(left child))
      return self.right child idx(idx)
```