

# Lectures Outline

## Lecture 1-6: Chapter # 1

### Lecture 1:

- Introduction

### Motivation of DM

- Applications of DM

- Logic and its applications

### Lecture 2:

- Logic types

  - Classical, Fuzzy

### Classical Logic

- Simple Logic

  - Proposition

- Compound Logic

  - Logical Connectors

    - AND, OR, NOT, IMPLICATION, BI-Implication

  - Logical Equivalence

### Lecture 3:

- Quiz

- Tautology

- Contradiction

- Logical Equivalence using Tautology

- Converse

- Inverse

- Contradiction

- Negation

### Lecture 4:

- Predicate Logic

  - Motivation

- Quantification

  - Prefix and Quantifiers

  - Proposition Function

  - Types of Quantifiers

    - Existential

    - Universal

  - Negation of quantifiers

Lecture 5:

- Translation English into Quantifiers
- Binding and Free Variables
- Nested Quantifiers

Lecture 6:

- Logical Proofs
- Types of Proof
  - Direct proof
  - Indirect Proof
    - Proof by Contraposition
    - Proof by Contradiction

**Lecture 7-9: Chapter # 2**

Lecture 7:

- Set Theory
  - Set Representation
    - Set Builder Notation
    - Venn Diagrams
    - Subset and its Derivatives
  - Set Operations
  - Representation of Set Concepts using Predicate Logic
  - Proof of Set Properties using Set Builder Notation
  - Representation of Set in Computers using Bit strings
  - Set Operations using Bit strings

**Self Study:** Cartesian Product

- Intro to Functions
  - What is a Function
  - Domain, Range, Co-Domain and Image of a Function

Lecture 8:

- Types of Functions
  - Onto functions
  - One-to-one
  - Bijjective
- Inverse of Functions
- Composition of Functions
- Widely used functions
  - Increasing, Strictly-Increasing, Decreasing, Strictly Decreasing, Ceiling, Floor
  - Representation of increasing and decreasing functions using predicate logic

Sequence and Summations  
    Recurrence Relations  
    Base Conditions  
    Expressing Summations

Lecture 9:

Class Feedback  
Closed-Form Solutions vs Recurrence relations  
Closed-Form Solution of Geometric Series  
    Limit Shifting  
    Summation Expansion

### **Lecture 10-12: Chapter # 5**

Lecture 10:

Long Quiz  
Introduction to Induction  
    Sample Questions

Lecture 11:

Weak Induction  
Practice Examples  
Strong Induction

Lecture 12:

Weak Induction Quiz  
Strong Induction  
Recursion

Lecture 13:

Long Quiz Solution  
Recurrence relations and Recursion

Lecture 14:

Revision of set concepts  
Function Growth

# Practice Questions

## Chapter 1: Logic

### Propositional Logic:

Exercise (starting Page 12): Q#1-12, 16-18, 31-39

Read De-Morgan's law from Page 26

### Logical Equivalence

Exercise (starting Page 34): Q#1-10, 13-33

### Quantification

Exercise (starting Page 53): Q# 1-18, 21, 22, 25, 28, 29

### Nested Quantifiers

Exercise (starting Page 64): Q# 1-4, Q5 part (a)-(d), 25-27, 29

### Proof practice Questions

Page 91: Q# 1-9, 15-17

Reading:

Rules of Inference: Page # 71-72

Proofs: Page # 81-87

### Fuzzy Logic

Page 16: Q# 45-47

## Chapter 2: Sequence and Summations[2.1-2.4]

### Set Theory:

## Basics of Set Theory

Page 125: Q# 1-44

Topic: Set operations, BitStrings, multi-sets, fuzzy-sets

V2: Page 136: Q# 1-11, 25-35, 52-65

V1: Page 136-137: Questions 1-4, 25, 26, 27, 29, 30, 31, 32, 52, 53, 63, 64, 65

Reading:

Set Identities Page # 130

## Function

Page 152: Q# 1-33, 77 (Partial Function)

Reading:

Section 2.3 starting Page 138-145

## Summation

Page 167: Q#1-6(a)-(f), 7-10, 18(a), 19(a), 29-34

Reading : Page # 156-160, Page # 164-166, Theorem 1 at Page 164

## Chapter 5: Induction and Recursion

### Induction:

Page # 329: Q# 1-24, 31-36