

*See the Assessment Guide for information on how to interpret this report.*

## ASSESSMENT SUMMARY

Compilation: PASSED (0 errors, 2 warnings)  
API: PASSED

SpotBugs: PASSED  
PMD: PASSED  
Checkstyle: PASSED

Correctness: 49/49 tests passed  
Memory: 113/133 tests passed  
Timing: 193/193 tests passed

Aggregate score: 98.50%  
[ Compilation: 5%, API: 5%, Style: 0%, Correctness: 60%, Timing: 10%, Memory: 20% ]

## ASSESSMENT DETAILS

The following files were submitted:

```
-----
4.3K Aug 17 01:38 Deque.java
 789 Aug 17 01:38 Permutation.java
3.9K Aug 17 01:38 RandomizedQueue.java
```

```
*****
*   COMPILING
*****
```

```
% javac Deque.java
```

```
*-----
```

```
% javac RandomizedQueue.java
```

```
*-----
```

```
RandomizedQueue.java:21: warning: [unchecked] unchecked cast
```

```

    queue = (Item[]) new Object[1];
                ^
    required: Item[]
    found:    Object[]
    where Item is a type-variable:
      Item extends Object declared in class RandomizedQueue
RandomizedQueue.java:69: warning: [unchecked] unchecked cast
    Item[] copy = (Item[]) new Object[capacity];
                ^
    required: Item[]
    found:    Object[]
    where Item is a type-variable:
      Item extends Object declared in class RandomizedQueue
2 warnings

```

```
% javac Permutation.java
```

```
*-----
```

```
=====
```

```
Checking the APIs of your programs.
```

```
*-----
```

```
Deque:
```

```
RandomizedQueue:
```

```
Permutation:
```

```
=====
```

```
*****
```

```
* CHECKING STYLE AND COMMON BUG PATTERNS
```

```
*****
```

```
% spotbugs *.class
```

```
*-----
```

```
=====
```

```
% pmd .
```

```
*-----
```

```
=====
```

```
% checkstyle *.java
```

```
*-----
```

```
% custom checkstyle checks for Deque.java
```

```
*-----
```

```
% custom checkstyle checks for RandomizedQueue.java
```

```
*-----
```

```
% custom checkstyle checks for Permutation.java
```

```
*-----
```

```
=====
```

```
*****
```

```
* TESTING CORRECTNESS
```

```
*****
```

```
Testing correctness of Deque
```

```
*-----
```

```
Running 19 total tests.
```

Tests 1-8 make random intermixed calls to `addFirst()`, `addLast()`, `removeFirst()`, `removeLast()`, `isEmpty()`, and `size()`, and `iterator()`. The probabilities of each operation are ( $p_1$ ,  $p_2$ ,  $p_3$ ,  $p_4$ ,  $p_5$ ,  $p_6$ ,  $p_7$ ), respectively.

Test 1: check random calls to `addFirst()`, `addLast()`, and `size()`

```
* 5 random calls (0.4, 0.4, 0.0, 0.0, 0.0, 0.2, 0.0)
```

```
* 50 random calls (0.4, 0.4, 0.0, 0.0, 0.0, 0.2, 0.0)
```

```
* 500 random calls (0.4, 0.4, 0.0, 0.0, 0.0, 0.2, 0.0)
```

```
* 1000 random calls (0.4, 0.4, 0.0, 0.0, 0.0, 0.2, 0.0)
```

```
==> passed
```

Test 2: check random calls to `addFirst()`, `removeFirst()`, and `isEmpty()`

```
* 5 random calls (0.8, 0.0, 0.1, 0.0, 0.1, 0.0, 0.0)
```

```
* 50 random calls (0.8, 0.0, 0.1, 0.0, 0.1, 0.0, 0.0)
```

```
* 500 random calls (0.8, 0.0, 0.1, 0.0, 0.1, 0.0, 0.0)
```

```
* 1000 random calls (0.8, 0.0, 0.1, 0.0, 0.1, 0.0, 0.0)
```

```
* 5 random calls (0.1, 0.0, 0.8, 0.0, 0.1, 0.0, 0.0)
```

```
* 50 random calls (0.1, 0.0, 0.8, 0.0, 0.1, 0.0, 0.0)
```

```
* 500 random calls (0.1, 0.0, 0.8, 0.0, 0.1, 0.0, 0.0)
```

```
* 1000 random calls (0.1, 0.0, 0.8, 0.0, 0.1, 0.0, 0.0)
```

```
==> passed
```

Test 3: check random calls to addFirst(), removeLast(), and isEmpty()

- \* 5 random calls (0.8, 0.0, 0.0, 0.1, 0.1, 0.0, 0.0)
- \* 50 random calls (0.8, 0.0, 0.0, 0.1, 0.1, 0.0, 0.0)
- \* 500 random calls (0.8, 0.0, 0.0, 0.1, 0.1, 0.0, 0.0)
- \* 1000 random calls (0.8, 0.0, 0.0, 0.1, 0.1, 0.0, 0.0)
- \* 5 random calls (0.1, 0.0, 0.0, 0.8, 0.1, 0.0, 0.0)
- \* 50 random calls (0.1, 0.0, 0.0, 0.8, 0.1, 0.0, 0.0)
- \* 500 random calls (0.1, 0.0, 0.0, 0.8, 0.1, 0.0, 0.0)
- \* 1000 random calls (0.1, 0.0, 0.0, 0.8, 0.1, 0.0, 0.0)

==> passed

Test 4: check random calls to addLast(), removeLast(), and isEmpty()

- \* 5 random calls (0.0, 0.8, 0.0, 0.1, 0.1, 0.0, 0.0)
- \* 50 random calls (0.0, 0.8, 0.0, 0.1, 0.1, 0.0, 0.0)
- \* 500 random calls (0.0, 0.8, 0.0, 0.1, 0.1, 0.0, 0.0)
- \* 1000 random calls (0.0, 0.8, 0.0, 0.1, 0.1, 0.0, 0.0)
- \* 5 random calls (0.0, 0.1, 0.0, 0.8, 0.1, 0.0, 0.0)
- \* 50 random calls (0.0, 0.1, 0.0, 0.8, 0.1, 0.0, 0.0)
- \* 500 random calls (0.0, 0.1, 0.0, 0.8, 0.1, 0.0, 0.0)
- \* 1000 random calls (0.0, 0.1, 0.0, 0.8, 0.1, 0.0, 0.0)

==> passed

Test 5: check random calls to addLast(), removeFirst(), and isEmpty()

- \* 5 random calls (0.0, 0.8, 0.1, 0.0, 0.1, 0.0, 0.0)
- \* 50 random calls (0.0, 0.8, 0.1, 0.0, 0.1, 0.0, 0.0)
- \* 500 random calls (0.0, 0.8, 0.1, 0.0, 0.1, 0.0, 0.0)
- \* 1000 random calls (0.0, 0.8, 0.1, 0.0, 0.1, 0.0, 0.0)
- \* 5 random calls (0.0, 0.1, 0.8, 0.0, 0.1, 0.0, 0.0)
- \* 50 random calls (0.0, 0.1, 0.8, 0.0, 0.1, 0.0, 0.0)
- \* 500 random calls (0.0, 0.1, 0.8, 0.0, 0.1, 0.0, 0.0)
- \* 1000 random calls (0.0, 0.1, 0.8, 0.0, 0.1, 0.0, 0.0)

==> passed

Test 6: check random calls to addFirst(), removeFirst(), and iterator()

- \* 5 random calls (0.8, 0.0, 0.1, 0.0, 0.0, 0.0, 0.1)
- \* 50 random calls (0.8, 0.0, 0.1, 0.0, 0.0, 0.0, 0.1)
- \* 500 random calls (0.8, 0.0, 0.1, 0.0, 0.0, 0.0, 0.1)
- \* 1000 random calls (0.8, 0.0, 0.1, 0.0, 0.0, 0.0, 0.1)
- \* 5 random calls (0.1, 0.0, 0.8, 0.0, 0.0, 0.0, 0.1)
- \* 50 random calls (0.1, 0.0, 0.8, 0.0, 0.0, 0.0, 0.1)
- \* 500 random calls (0.1, 0.0, 0.8, 0.0, 0.0, 0.0, 0.1)
- \* 1000 random calls (0.1, 0.0, 0.8, 0.0, 0.0, 0.0, 0.1)

==> passed

Test 7: check random calls to all methods except iterator()

- \* 5 random calls (0.3, 0.3, 0.1, 0.1, 0.1, 0.1, 0.0)
- \* 50 random calls (0.3, 0.3, 0.1, 0.1, 0.1, 0.1, 0.0)
- \* 500 random calls (0.3, 0.3, 0.1, 0.1, 0.1, 0.1, 0.0)

```
* 1000 random calls (0.3, 0.3, 0.1, 0.1, 0.1, 0.1, 0.0)
*   5 random calls (0.1, 0.1, 0.3, 0.3, 0.1, 0.1, 0.0)
*  50 random calls (0.1, 0.1, 0.3, 0.3, 0.1, 0.1, 0.0)
* 500 random calls (0.1, 0.1, 0.3, 0.3, 0.1, 0.1, 0.0)
* 1000 random calls (0.1, 0.1, 0.3, 0.3, 0.1, 0.1, 0.0)
==> passed
```

Test 8: check random calls to all methods, including iterator()

```
*   5 random calls (0.2, 0.2, 0.1, 0.1, 0.1, 0.1, 0.2)
*  50 random calls (0.2, 0.2, 0.1, 0.1, 0.1, 0.1, 0.2)
* 500 random calls (0.2, 0.2, 0.1, 0.1, 0.1, 0.1, 0.2)
* 1000 random calls (0.2, 0.2, 0.1, 0.1, 0.1, 0.1, 0.2)
*   5 random calls (0.1, 0.1, 0.2, 0.2, 0.1, 0.1, 0.2)
*  50 random calls (0.1, 0.1, 0.2, 0.2, 0.1, 0.1, 0.2)
* 500 random calls (0.1, 0.1, 0.2, 0.2, 0.1, 0.1, 0.2)
* 1000 random calls (0.1, 0.1, 0.2, 0.2, 0.1, 0.1, 0.2)
==> passed
```

Test 9: check removeFirst() and removeLast() from an empty deque

```
* removeFirst()
* removeLast()
==> passed
```

Test 10: check whether two Deque objects can be created at the same time

```
* n = 10
* n = 1000
==> passed
```

Test 11: check iterator() after n calls to addFirst()

```
* n = 10
* n = 50
==> passed
```

Test 12: check iterator() after random calls to addFirst(), addLast(),  
removeFirst(), and removeLast() with probabilities (p1, p2, p3, p4)

```
* 20 random operations (0.8, 0.0, 0.2, 0.0)
* 20 random operations (0.8, 0.0, 0.0, 0.2)
* 20 random operations (0.0, 0.8, 0.0, 0.2)
* 20 random operations (0.0, 0.8, 0.2, 0.0)
* 20 random operations (0.4, 0.4, 0.1, 0.1)
* 20 random operations (0.2, 0.0, 0.8, 0.0)
* 20 random operations (0.2, 0.0, 0.0, 0.8)
* 20 random operations (0.0, 0.2, 0.0, 0.8)
* 20 random operations (0.0, 0.2, 0.8, 0.0)
* 20 random operations (0.1, 0.1, 0.4, 0.4)
* 100 random operations (0.4, 0.4, 0.1, 0.1)
* 1000 random operations (0.4, 0.4, 0.1, 0.1)
==> passed
```

Test 13: create two nested iterators to same deque of size n

\* n = 10

\* n = 50

==> passed

Test 14: create two parallel iterators to same deque of size n

\* n = 10

\* n = 50

==> passed

Test 15: create an iterator and check calls to next() and hasNext()

\* 10 consecutive calls to hasNext() on a deque of size 10

\* 10 consecutive calls to next() on a deque of size 10

\* 50 random intermixed calls to next() and hasNext() on a deque of size 10

\* 1000 random intermixed calls to next() and hasNext() on a deque of size 100

==> passed

Test 16: create Deque objects of different parameterized types

==> passed

Test 17: call addFirst() and addLast() with null argument

==> passed

Test 18: check that remove() and next() throw the specified exceptions in iterator()

==> passed

Test 19: call iterator() when the deque is empty

==> passed

Total: 19/19 tests passed!

=====

Testing correctness of RandomizedQueue

\*-----

Running 21 total tests.

Tests 1-6 make random intermixed calls to enqueue(), dequeue(), sample(), isEmpty(), size(), and iterator(). The probabilities of each operation are (p1, p2, p3, p4, p5, p6), respectively.

Test 1: check random calls to enqueue() and size()

\* 5 random calls (0.8, 0.0, 0.0, 0.0, 0.2, 0.0)

\* 50 random calls (0.8, 0.0, 0.0, 0.0, 0.2, 0.0)

\* 500 random calls (0.8, 0.0, 0.0, 0.0, 0.2, 0.0)

\* 1000 random calls (0.8, 0.0, 0.0, 0.0, 0.2, 0.0)

==> passed

Test 2: check random calls to enqueue() and dequeue()

```
* 5 random calls (0.7, 0.1, 0.0, 0.1, 0.1, 0.0)
* 50 random calls (0.7, 0.1, 0.0, 0.1, 0.1, 0.0)
* 500 random calls (0.7, 0.1, 0.0, 0.1, 0.1, 0.0)
* 1000 random calls (0.7, 0.1, 0.0, 0.1, 0.1, 0.0)
* 5 random calls (0.1, 0.7, 0.0, 0.1, 0.1, 0.0)
* 50 random calls (0.1, 0.7, 0.0, 0.1, 0.1, 0.0)
* 500 random calls (0.1, 0.7, 0.0, 0.1, 0.1, 0.0)
* 1000 random calls (0.1, 0.7, 0.0, 0.1, 0.1, 0.0)
```

==> passed

Test 3: check random calls to enqueue() and sample()

```
* 5 random calls (0.8, 0.0, 0.2, 0.0, 0.0, 0.0)
* 50 random calls (0.8, 0.0, 0.2, 0.0, 0.0, 0.0)
* 500 random calls (0.8, 0.0, 0.2, 0.0, 0.0, 0.0)
* 1000 random calls (0.8, 0.0, 0.2, 0.0, 0.0, 0.0)
* 5 random calls (0.2, 0.0, 0.8, 0.0, 0.0, 0.0)
* 50 random calls (0.2, 0.0, 0.8, 0.0, 0.0, 0.0)
* 500 random calls (0.2, 0.0, 0.8, 0.0, 0.0, 0.0)
* 1000 random calls (0.2, 0.0, 0.8, 0.0, 0.0, 0.0)
```

==> passed

Test 4: check random calls to enqueue() and iterator()

```
* 5 random calls (0.8, 0.0, 0.0, 0.0, 0.0, 0.2)
* 50 random calls (0.8, 0.0, 0.0, 0.0, 0.0, 0.2)
* 500 random calls (0.8, 0.0, 0.0, 0.0, 0.0, 0.2)
* 1000 random calls (0.8, 0.0, 0.0, 0.0, 0.0, 0.2)
```

==> passed

Test 5: check random calls to all methods except iterator()

```
* 5 random calls (0.6, 0.1, 0.1, 0.1, 0.1, 0.0)
* 50 random calls (0.6, 0.1, 0.1, 0.1, 0.1, 0.0)
* 500 random calls (0.6, 0.1, 0.1, 0.1, 0.1, 0.0)
* 1000 random calls (0.6, 0.1, 0.1, 0.1, 0.1, 0.0)
* 5 random calls (0.1, 0.6, 0.1, 0.1, 0.1, 0.0)
* 50 random calls (0.1, 0.6, 0.1, 0.1, 0.1, 0.0)
* 500 random calls (0.1, 0.6, 0.1, 0.1, 0.1, 0.0)
* 1000 random calls (0.1, 0.6, 0.1, 0.1, 0.1, 0.0)
```

==> passed

Test 6: check random calls to all methods, including iterator()

```
* 5 random calls (0.5, 0.1, 0.1, 0.1, 0.1, 0.1)
* 50 random calls (0.5, 0.1, 0.1, 0.1, 0.1, 0.1)
* 500 random calls (0.5, 0.1, 0.1, 0.1, 0.1, 0.1)
* 1000 random calls (0.5, 0.1, 0.1, 0.1, 0.1, 0.1)
* 5 random calls (0.1, 0.5, 0.1, 0.1, 0.1, 0.1)
* 50 random calls (0.1, 0.5, 0.1, 0.1, 0.1, 0.1)
* 500 random calls (0.1, 0.5, 0.1, 0.1, 0.1, 0.1)
* 1000 random calls (0.1, 0.5, 0.1, 0.1, 0.1, 0.1)
```

==> passed

Test 7: call dequeue() and sample() from an empty randomized queue

- \* dequeue()

- \* sample()

==> passed

Test 8: create multiple randomized queue objects at the same time

- \* n = 10

- \* n = 100

==> passed

Test 9: check that iterator() returns correct items after a sequence of n enqueue() operations

- \* n = 10

- \* n = 50

==> passed

Test 10: check that iterator() returns correct items after intermixed sequence of m enqueue() and dequeue() operations

- \* m = 10

- \* m = 1000

==> passed

Test 11: create two nested iterators over the same randomized queue of size n

- \* n = 10

- \* n = 50

==> passed

Test 12: create two parallel iterators over the same randomized queue of size n

- \* n = 10

- \* n = 50

==> passed

Test 13: create two iterators over different randomized queues, each of length 10

==> passed

Test 14: create an iterator and check calls to next() and hasNext()

- \* 10 consecutive calls to hasNext() on a deque of size 10

- \* 10 consecutive calls to next() on a deque of size 10

- \* 50 random intermixed calls to next() and hasNext() on a deque of size 10

- \* 1000 random intermixed calls to next() and hasNext() on a deque of size 100

==> passed

Test 15: create RandomizedQueue objects of different parameterized types

==> passed

Test 16: check randomness of sample() by enqueueing n items, repeatedly calling



```

    sample(), and counting the frequency of each item
* n = 3, trials = 12000
* n = 5, trials = 12000
* n = 8, trials = 12000
* n = 10, trials = 12000
==> passed

```

Test 17: check randomness of dequeue() by enqueueing n items, dequeueing n items, and seeing whether each of the n! permutations is equally likely

```

* n = 2, trials = 12000
* n = 3, trials = 12000
* n = 4, trials = 12000
* n = 5, trials = 12000
==> passed

```

Test 18: check randomness of iterator() by enqueueing n items, iterating over those n items, and seeing whether each of the n! permutations is equally likely

```

* n = 2, trials = 12000
* n = 3, trials = 12000
* n = 4, trials = 12000
* n = 5, trials = 12000
==> passed

```

Test 19: call enqueue() with a null argument

```

==> passed

```

Test 20: check that remove() and next() throw the specified exceptions in iterator()

```

==> passed

```

Test 21: call iterator() when randomized queue is empty

```

==> passed

```

Total: 21/21 tests passed!

```

=====
*****
* TESTING CORRECTNESS (substituting reference RandomizedQueue and Deque)
*****

```

Testing correctness of Permutation

```

*-----

```

Tests 1-5 call the main() function directly, resetting standard input before each call.

Running 9 total tests.

Test 1a: check formatting for sample inputs from assignment specification

```
% java Permutation 3 < distinct.txt
```

```
H
```

```
C
```

```
A
```

```
% java Permutation 3 < distinct.txt
```

```
F
```

```
E
```

```
D
```

```
% java Permutation 8 < duplicates.txt
```

```
BB
```

```
CC
```

```
BB
```

```
BB
```

```
BB
```

```
CC
```

```
AA
```

```
BB
```

==> passed

Test 1b: check formatting for other inputs

```
% java Permutation 8 < mediumTale.txt
```

```
the
```

```
the
```

```
was
```

```
the
```

```
it
```

```
was
```

```
of
```

```
times
```

```
% java Permutation 0 < distinct.txt
```

```
[no output]
```

==> passed

Test 2: check that main() reads all data from standard input

```
* filename = distinct.txt, k = 3
```

```
* filename = distinct.txt, k = 3
```

```
* filename = duplicates.txt, k = 8
```

```
* filename = mediumTale.txt, k = 8
```

==> passed

Test 3a: check that main() prints each item from the sequence at most once  
(for inputs with no duplicate strings)

```
* filename = distinct.txt, k = 3
```

```
* filename = distinct.txt, k = 1
```

```
* filename = distinct.txt, k = 9
* filename = permutation6.txt, k = 6
* filename = permutation10.txt, k = 10
==> passed
```

Test 3b: check that main() prints each item from the sequence at most once  
(for inputs with duplicate strings)

```
* filename = duplicates.txt, k = 8
* filename = duplicates.txt, k = 3
* filename = permutation8.txt, k = 6
* filename = permutation8.txt, k = 2
* filename = tinyTale.txt, k = 10
==> passed
```

Test 3c: check that main() prints each item from the sequence at most once  
(for inputs with newlines)

```
* filename = mediumTale.txt, k = 10
* filename = mediumTale.txt, k = 20
* filename = tale.txt, k = 10
* filename = tale.txt, k = 50
==> passed
```

Test 4: check main() when k = 0

```
* filename = distinct.txt, k = 0
* filename = distinct.txt, k = 0
==> passed
```

Test 5a: check that permutations are uniformly random  
(for inputs with no duplicate strings)

```
* filename = permutation4.txt, k = 1
* filename = permutation4.txt, k = 2
* filename = permutation4.txt, k = 3
* filename = permutation4.txt, k = 4
* filename = permutation6.txt, k = 2
==> passed
```

Test 5b: check that permutations are uniformly random  
(for inputs with duplicate strings)

```
* filename = permutation5.txt, k = 1
* filename = permutation5.txt, k = 2
* filename = permutation5.txt, k = 3
* filename = duplicates.txt, k = 3
* filename = permutation8.txt, k = 2
==> passed
```

Total: 9/9 tests passed!

=====

\*\*\*\*\*

\* TIMING (substituting reference RandomizedQueue and Deque)

\*\*\*\*\*

Timing Permutation

\*-----

Running 23 total tests.

Test 1: count calls to methods in StdIn

\* java Permutation 5 < distinct.txt  
 \* java Permutation 10 < permutation10.txt  
 \* java Permutation 1 < mediumTale.txt  
 \* java Permutation 20 < tale.txt  
 \* java Permutation 100 < tale.txt  
 \* java Permutation 16412 < tale.txt



Test 2: count calls to methods in Deque and RandomizedQueue

\* java Permutation 5 < distinct.txt  
 \* java Permutation 10 < permutation10.txt  
 \* java Permutation 1 < mediumTale.txt  
 \* java Permutation 20 < tale.txt  
 \* java Permutation 100 < tale.txt  
 \* java Permutation 16412 < tale.txt



Test 3: count calls to methods in StdRandom

\* java Permutation 5 < distinct.txt  
 \* java Permutation 10 < permutation10.txt  
 \* java Permutation 1 < mediumTale.txt  
 \* java Permutation 20 < tale.txt  
 \* java Permutation 100 < tale.txt  
 \* java Permutation 16412 < tale.txt



Test 4: Time main() with k = 5, for inputs containing n random strings

	n	seconds
=> passed	1000	0.00
=> passed	2000	0.00
=> passed	4000	0.00
=> passed	8000	0.00
=> passed	16000	0.01
=> passed	32000	0.01
=> passed	64000	0.02
=> passed	128000	0.04
=> passed	256000	0.08
=> passed	512000	0.16

==> 10/10 tests passed

Test 5: Time main() with k = 1000, for inputs containing n random strings

	n	seconds
=> passed	1000	0.00
=> passed	2000	0.00
=> passed	4000	0.00
=> passed	8000	0.00
=> passed	16000	0.01
=> passed	32000	0.01
=> passed	64000	0.02
=> passed	128000	0.04
=> passed	256000	0.08
=> passed	512000	0.17

==> 10/10 tests passed

Total: 23/23 tests passed!

=====

```
*****
*  MEMORY
*****
```

Analyzing memory of Permutation

\*-----

Running 2 total tests.

Test 1: check that only one Deque or RandomizedQueue object is created

```
* filename = distinct.txt, n = 9, k = 1
* filename = distinct.txt, n = 9, k = 2
* filename = distinct.txt, n = 9, k = 4
* filename = tinyTale.txt, n = 12, k = 10
* filename = tale.txt, n = 138653, k = 50
==> passed
```

Test 2: check that the maximum size of any Deque or RandomizedQueue object created is between k and n

```
* filename = distinct.txt, n = 9, k = 1
* filename = distinct.txt, n = 9, k = 2
* filename = distinct.txt, n = 9, k = 4
* filename = tinyTale.txt, n = 12, k = 10
```

```
* filename = tale.txt, n = 138653, k = 5
* filename = tale.txt, n = 138653, k = 50
* filename = tale.txt, n = 138653, k = 500
* filename = tale.txt, n = 138653, k = 5000
* filename = tale.txt, n = 138653, k = 50000
==> passed
```

Test 3 (bonus): check that maximum size of any or Deque or RandomizedQueue object created is equal to k

```
* filename = tale.txt, n = 138653, k = 5
  - max size of RandomizedQueue object = 138653

* filename = tale.txt, n = 138653, k = 50
  - max size of RandomizedQueue object = 138653

* filename = tale.txt, n = 138653, k = 500
  - max size of RandomizedQueue object = 138653

* filename = tale.txt, n = 138653, k = 5000
  - max size of RandomizedQueue object = 138653

* filename = tale.txt, n = 138653, k = 50000
  - max size of RandomizedQueue object = 138653
```

==> **FAILED**

Total: 2/2 tests passed!

=====

\*\*\*\*\*

\* MEMORY

\*\*\*\*\*

Analyzing memory of Deque

\*-----

For tests 1-4, the maximum amount of memory allowed for a Deque containing  $n$  items is  $48n + 192$ .

Running 49 total tests.

Test 1a-1i: total memory usage after inserting  $n$  items,  
where  $n$  is a power of 2

$n$	bytes
-----	-------

-----

```

=> passed      32      1576
=> passed      64      3112
=> passed     128      6184
=> passed     256     12328
=> passed     512     24616
=> passed    1024     49192
=> passed    2048     98344
=> passed    4096    196648
=> passed    8192    393256
==> 9/9 tests passed

```

Memory: 48.00 n + 40.00 (R<sup>2</sup> = 1.000)

Test 2a-2i: Total memory usage after inserting n items,  
when n is one more than a power of 2.

	n	bytes
-----		
=> passed	33	1624
=> passed	65	3160
=> passed	129	6232
=> passed	257	12376
=> passed	513	24664
=> passed	1025	49240
=> passed	2049	98392
=> passed	4097	196696
=> passed	8193	393304
==> 9/9 tests passed		

Memory: 48.00 n + 40.00 (R<sup>2</sup> = 1.000)

Test 3a-3i: Total memory usage after inserting 2n-1 items, and then  
deleting n-1 items, when n is one more than a power of 2.

	n	bytes
-----		
=> passed	33	1624
=> passed	65	3160
=> passed	129	6232
=> passed	257	12376
=> passed	513	24664
=> passed	1025	49240
=> passed	2049	98392
=> passed	4097	196696
=> passed	8193	393304
==> 9/9 tests passed		

Memory: 48.00 n + 40.00 (R^2 = 1.000)

Test 4a-4e: Total memory usage after inserting n items,  
and then deleting all but one item  
(should not grow with n or be too large of a constant).

	n	bytes
=> passed	32	88
=> passed	64	88
=> passed	128	88
=> passed	256	88
=> passed	512	88
=> passed	1024	88
=> passed	2048	88
=> passed	4096	88
=> passed	8192	88
==> 9/9 tests passed		

Memory: 88.00 (R^2 = 1.000)

Test 5a-5e: Total memory usage of iterator after inserting n items  
(should not grow with n or be too large of a constant).

	n	bytes
=> passed	32	32
=> passed	64	32
=> passed	128	32
=> passed	256	32
=> passed	512	32
=> passed	1024	32
=> passed	2048	32
=> passed	4096	32
=> passed	8192	32
==> 9/9 tests passed		

Memory: 32.00 (R^2 = 1.000)

Test 6a: Insert n strings; delete them one at a time, checking for  
loitering after each deletion. The probabilities of addFirst()  
and addLast() are (p1, p2), respectively. The probabilities of  
removeFirst() and removeLast() are (q1, q2), respectively.

- \* 100 random insertions (1.0, 0.0) and 100 random deletions (1.0, 0.0)
- \* 100 random insertions (1.0, 0.0) and 100 random deletions (0.0, 1.0)
- \* 100 random insertions (0.0, 1.0) and 100 random deletions (1.0, 0.0)



```
* 100 random insertions (0.0, 1.0) and 100 random deletions (0.0, 1.0)
* 100 random insertions (0.5, 0.5) and 100 random deletions (0.5, 0.5)
==> passed
```

Test 6b: Perform random operations, checking for loitering after each operation. The probabilities of addFirst(), addLast(), removeFirst(), and removeLast() are (p1, p2, p3, p4), respectively.

```
* 100 random operations (0.8, 0.0, 0.2, 0.0)
* 100 random operations (0.8, 0.0, 0.0, 0.2)
* 100 random operations (0.0, 0.8, 0.2, 0.0)
* 100 random operations (0.0, 0.8, 0.0, 0.2)
* 100 random operations (0.4, 0.4, 0.1, 0.1)
* 100 random operations (0.2, 0.2, 0.3, 0.3)
==> passed
```

Test 7: Perform m random add/remove operations in the deque and check that only constant memory is allocated/deallocated per operation

```
* m = 128
* m = 256
* m = 512
==> passed
```

Test 8: Insert m items into deque; then iterate over deque and check that only constant memory is allocated/deallocated per operation

```
* m = 64
* m = 128
* m = 256
==> passed
```

```
Min observed memory for Deque: 48.00 n + 40.00 (R^2 = 1.000)
Max observed memory for Deque: 48.00 n + 40.00 (R^2 = 1.000)
```

Total: 49/49 tests passed!

=====

Analyzing memory of RandomizedQueue

```
*-----
For Tests 1-5, the maximum amount of memory allowed for
a RandomizedQueue containing n items is  $48n + 192$ .
```

```
For Test 6, the maximum amount of memory allowed for
a RandomizedQueue iterator over n items is  $8n + 72$ .
```

Test 1a-1i: Total memory usage after inserting n items  
when n is a power of 2.

	n	bytes
=> passed	32	312
=> passed	64	568
=> passed	128	1080
=> passed	256	2104
=> passed	512	4152
=> passed	1024	8248
=> passed	2048	16440
=> passed	4096	32824
=> passed	8192	65592
==> 9/9 tests passed		

Memory:  $8.00 n + 56.00$  ( $R^2 = 1.000$ )

Test 2a-2i: Total memory usage after inserting n items,  
when n is one more than a power of 2.

	n	bytes
=> passed	33	568
=> passed	65	1080
=> passed	129	2104
=> passed	257	4152
=> passed	513	8248
=> passed	1025	16440
=> passed	2049	32824
=> passed	4097	65592
=> passed	8193	131128
==> 9/9 tests passed		

Memory:  $16.00 n + 40.00$  ( $R^2 = 1.000$ )

Test 3a-3i: Total memory usage after inserting  $2n-1$  items, and then  
deleting  $n-1$  items, when n is one more than a power of 2.

	n	bytes
=> passed	33	1080
=> passed	65	2104
=> passed	129	4152
=> passed	257	8248
=> passed	513	16440
=> passed	1025	32824

```
=> passed      2049      65592
=> passed      4097     131128
=> passed      8193     262200
==> 9/9 tests passed
```

Memory: 32.00 n + 24.00 (R<sup>2</sup> = 1.000)

Test 4a-4i: Total memory usage after inserting n items, deleting n items, then inserting n times, when n is a power of 2.

	n	bytes
-----		
=> passed	32	312
=> passed	64	568
=> passed	128	1080
=> passed	256	2104
=> passed	512	4152
=> passed	1024	8248
=> passed	2048	16440
=> passed	4096	32824
=> passed	8192	65592
==> 9/9 tests passed		

Memory: 8.00 n + 56.00 (R<sup>2</sup> = 1.000)

Test 5a-5i: Total memory usage after inserting n items, and then deleting all but one item.

	n	bytes
-----		
=> passed	32	72
=> passed	64	72
=> passed	128	72
=> passed	256	72
=> passed	512	72
=> passed	1024	72
=> passed	2048	72
=> passed	4096	72
=> passed	8192	72
==> 9/9 tests passed		

Memory: 72.00 (R<sup>2</sup> = 1.000)

Test 6a-6i: Total memory usage of iterator after inserting n items.

n	bytes
---	-------

```

-----
=> FAILED      32      1064    (3.2x)
=> FAILED      64      2088    (3.6x)
=> FAILED     128      4136    (3.8x)
=> FAILED     256      8232    (3.9x)
=> FAILED     512     16424    (3.9x)
=> FAILED    1024     32808    (4.0x)
=> FAILED    2048     65576    (4.0x)
=> FAILED    4096    131112    (4.0x)
=> FAILED    8192    262184    (4.0x)
==> 0/9 tests passed

```

Memory: 32.00 n + 40.00 (R^2 = 1.000)

Test 6j-6r: Total memory usage of iterator after inserting n items.

```

           n      bytes
-----
=> FAILED     34      1128    (3.3x)
=> FAILED     66      2152    (3.6x)
=> FAILED    130      4200    (3.8x)
=> FAILED    258      8296    (3.9x)
=> FAILED    514     16488    (3.9x)
=> FAILED   1026     32872    (4.0x)
=> FAILED   2050     65640    (4.0x)
=> FAILED   4098    131176    (4.0x)
=> FAILED   8194    262248    (4.0x)
==> 0/9 tests passed

```

Memory: 32.00 n + 40.00 (R^2 = 1.000)

Test 7a: Insert 100 strings; delete them one at a time, checking for loitering after each deletion.

- loitering observed during 31 of 100 deletions
- maximum number of loitered objects at one time = 1

==> **FAILED**

Test 7b: Perform random operations, checking for loitering after each operation. The probabilities of enqueue(), dequeue(), and sample() are (p1, p2, p3), respectively.

- \* 200 random operations (0.8, 0.2, 0.0)
- \* 200 random operations (0.2, 0.8, 0.0)
  - loitering detected after operation 2 of 200
  - sequence of operations was:
 

```
rq.enqueue("FPFJLVXVMT")
rq.dequeue()      ==> "FPFJLVXVMT"
```

```

- loitered object(s):
  FPFJLVXVMT

* 200 random operations (0.6, 0.2, 0.2)
- loitering detected after operation 3 of 200
- sequence of operations was:
  rq.enqueue("JOIHOLFCCD")
  rq.sample()      ==> "JOIHOLFCCD"
  rq.dequeue()     ==> "JOIHOLFCCD"
- loitered object(s):
  JOIHOLFCCD

* 200 random operations (0.2, 0.4, 0.4)
- loitering detected after operation 4 of 200
- sequence of operations was:
  rq.enqueue("JCSFGYQNBT")
  rq.sample()      ==> "JCSFGYQNBT"
  rq.enqueue("DMFAPSNIIE")
  rq.dequeue()     ==> "DMFAPSNIIE"
- loitered object(s):
  DMFAPSNIIE

```

==> **FAILED**

Test 8: Insert  $m$  items into queue; then iterate over deque and check that only constant memory is allocated/deallocated per operation

```

* m = 64
* m = 128
* m = 256

```

==> passed

Test 9: Total memory usage after inserting  $n$  items, seeking to identify values of  $n$  where memory usage is minimized as a function of  $n$ .

	$n$	bytes
=> passed	32	312
=> passed	64	568
=> passed	128	1080
=> passed	256	2104
=> passed	512	4152
=> passed	1024	8248
=> passed	2048	16440

==> 7/7 tests passed

Memory:  $8.00 n + 56.00$  ( $R^2 = 1.000$ )

Test 10: Total memory usage after inserting 4096 items, then successively

deleting items, seeking values of n where memory usage is maximized  
as a function of n

	n	bytes
=> passed	2049	65592
=> passed	1025	32824
=> passed	513	16440
=> passed	257	8248
=> passed	129	4152
=> passed	65	2104
=> passed	33	1080
=> passed	17	568
=> passed	9	312

==> 9/9 tests passed

Memory: 32.00 n + 24.00 (R<sup>2</sup> = 1.000)

Min observed memory for RandomizedQueue: 8.00 n + 56.00 (R<sup>2</sup> = 1.000)

Max observed memory for RandomizedQueue: 32.00 n + 24.00 (R<sup>2</sup> = 1.000)

Running 82 total tests.

Total: 62/82 tests passed!

=====

\*\*\*\*\*  
\* TIMING  
\*\*\*\*\*

Timing Deque

\*-----

Running 103 total tests.

Test 1a-1k: make n calls to addFirst() followed by n calls to removeFirst()

	n	seconds
=> passed	1024	0.00
=> passed	2048	0.00
=> passed	4096	0.00
=> passed	8192	0.00
=> passed	16384	0.00
=> passed	32768	0.00
=> passed	65536	0.00

```
=> passed      128000      0.00
=> passed      256000      0.00
=> passed      512000      0.01
=> passed     1024000      0.02
==> 11/11 tests passed
```

Test 2a-2k: make n calls to addLast() followed by n calls to removeLast()  
n seconds

```
-----
=> passed      1024      0.00
=> passed      2048      0.00
=> passed      4096      0.00
=> passed      8192      0.00
=> passed     16384      0.00
=> passed     32768      0.00
=> passed     65536      0.00
=> passed     128000     0.01
=> passed     256000     0.00
=> passed     512000     0.01
=> passed     1024000    0.02
==> 11/11 tests passed
```

Test 3a-3k: make n calls to addFirst() followed by n calls to removeLast()  
n seconds

```
-----
=> passed      1024      0.00
=> passed      2048      0.00
=> passed      4096      0.00
=> passed      8192      0.00
=> passed     16384      0.00
=> passed     32768      0.00
=> passed     65536      0.00
=> passed     128000     0.00
=> passed     256000     0.00
=> passed     512000     0.01
=> passed     1024000    0.02
==> 11/11 tests passed
```

Test 4a-4k: make n calls to addLast() followed by n calls to removeFirst()  
n seconds

```
-----
=> passed      1024      0.00
=> passed      2048      0.00
=> passed      4096      0.00
=> passed      8192      0.00
=> passed     16384      0.00
```

```

=> passed      32768      0.00
=> passed      65536      0.00
=> passed     128000      0.00
=> passed     256000      0.00
=> passed     512000      0.01
=> passed    1024000      0.02
==> 11/11 tests passed

```

Test 5a-5g: make n random calls to addFirst(), removeFirst(), isEmpty(), and size()  
with probabilities (0.7, 0.1, 0.1, 0.1)

	n	seconds
-----		
=> passed	1024	0.00
=> passed	2048	0.00
=> passed	4096	0.00
=> passed	8192	0.00
=> passed	16384	0.00
=> passed	32768	0.00
=> passed	65536	0.00
=> passed	128000	0.00
=> passed	256000	0.01
=> passed	512000	0.01
=> passed	1024000	0.03
=> passed	2048000	0.06
==> 12/12 tests passed		

Test 6a-6g: make n random calls to addLast(), removeLast(), isEmpty(), and size(),  
with probabilities (0.7, 0.1, 0.1, 0.1)

	n	seconds
-----		
=> passed	1024	0.00
=> passed	2048	0.00
=> passed	4096	0.00
=> passed	8192	0.00
=> passed	16384	0.00
=> passed	32768	0.00
=> passed	65536	0.00
=> passed	128000	0.00
=> passed	256000	0.01
=> passed	512000	0.02
=> passed	1024000	0.03
=> passed	2048000	0.06
==> 12/12 tests passed		



Test 7a-7g: make n random calls to addFirst(), addLast(), removeFirst(), removeLast(), isEmpty(), and size() with probabilities (0.3, 0.3, 0.1, 0.1, 0.1, 0.1)

	n	seconds
=> passed	1024	0.00
=> passed	2048	0.00
=> passed	4096	0.00
=> passed	8192	0.00
=> passed	16384	0.00
=> passed	32768	0.00
=> passed	65536	0.00
=> passed	128000	0.00
=> passed	256000	0.01
=> passed	512000	0.02
=> passed	1024000	0.03
=> passed	2048000	0.07

==> 12/12 tests passed

Test 8a-8g: make n calls to addFirst(); iterate over the n items by calling next() and hasNext()

	n	seconds
=> passed	1024	0.00
=> passed	2048	0.00
=> passed	4096	0.00
=> passed	8192	0.00
=> passed	16384	0.00
=> passed	32768	0.00
=> passed	65536	0.00
=> passed	128000	0.00
=> passed	256000	0.00
=> passed	512000	0.01
=> passed	1024000	0.02
=> passed	2048000	0.04

==> 12/12 tests passed

Test 9a-9k: make n calls to addFirst()/addLast(); interleave n calls each to removeFirst(), removeLast(), addFirst(), and addLast()

	n	seconds
=> passed	1025	0.00
=> passed	2049	0.00
=> passed	4097	0.00
=> passed	8193	0.00

```

=> passed      16385      0.00
=> passed      32769      0.00
=> passed      65537      0.01
=> passed     128001      0.01
=> passed     256001      0.01
=> passed     512001      0.03
=> passed    1024001      0.05
==> 11/11 tests passed

```

Total: 103/103 tests passed!

=====

Timing RandomizedQueue

\*-----

Running 67 total tests.

Test 1: make n calls to enqueue() followed by n calls to dequeue();  
count calls to StdRandom

```

* n = 10
* n = 100
* n = 1000

```

==> passed

Test 2: make n calls to enqueue() followed by n calls to sample();  
count calls to StdRandom

```

* n = 10
* n = 100
* n = 1000

```

==> passed

Test 3: make n calls to enqueue() and iterate over the n items;  
count calls to StdRandom

```

* n = 10
* n = 100
* n = 1000

```

==> passed

Test 4a-k: make n calls to enqueue() followed by n calls to dequeue()

n seconds

-----

```

=> passed      1024      0.00
=> passed      2048      0.00
=> passed      4096      0.00
=> passed      8192      0.00

```

```

=> passed      16384      0.00
=> passed      32768      0.00
=> passed      65536      0.00
=> passed     128000      0.01
=> passed     256000      0.01
=> passed     512000      0.02
=> passed    1024000      0.03
==> 11/11 tests passed

```

Test 5a-k: make n calls to enqueue() followed by n random calls to enqueue(), sample(), dequeue(), isEmpty(), and size() with probabilities (0.2, 0.2, 0.2, 0.2, 0.2)

	n	seconds
-----		
=> passed	1024	0.00
=> passed	2048	0.00
=> passed	4096	0.00
=> passed	8192	0.00
=> passed	16384	0.00
=> passed	32768	0.00
=> passed	65536	0.01
=> passed	128000	0.01
=> passed	256000	0.02
=> passed	512000	0.04
=> passed	1024000	0.10
==> 11/11 tests passed		

Test 6a-k: make n calls to enqueue() followed by n random calls to enqueue(), sample(), dequeue(), isEmpty(), and size() with probabilities (0.6, 0.1, 0.1, 0.1, 0.1)

	n	seconds
-----		
=> passed	1024	0.00
=> passed	2048	0.00
=> passed	4096	0.00
=> passed	8192	0.00
=> passed	16384	0.00
=> passed	32768	0.00
=> passed	65536	0.00
=> passed	128000	0.01
=> passed	256000	0.01
=> passed	512000	0.03
=> passed	1024000	0.07
==> 11/11 tests passed		

Test 7a-k: make n calls to enqueue() followed by n random calls to enqueue(), sample(), dequeue(), isEmpty(), and size() with probabilities (0.1, 0.1, 0.6, 0.1, 0.1)

	n	seconds
=> passed	1024	0.00
=> passed	2048	0.00
=> passed	4096	0.00
=> passed	8192	0.00
=> passed	16384	0.00
=> passed	32768	0.00
=> passed	65536	0.00
=> passed	128000	0.01
=> passed	256000	0.02
=> passed	512000	0.04
=> passed	1024000	0.11

==> 11/11 tests passed

Test 8a-k: make n calls to enqueue() followed by n calls each to next() and hasNext().

	n	seconds
=> passed	1024	0.00
=> passed	2048	0.00
=> passed	4096	0.00
=> passed	8192	0.00
=> passed	16384	0.00
=> passed	32768	0.00
=> passed	65536	0.01
=> passed	128000	0.01
=> passed	256000	0.02
=> passed	512000	0.04
=> passed	1024000	0.11

==> 11/11 tests passed

Test 9a-i: make 100 calls to enqueue; 99 calls to dequeue; n calls to enqueue(); then call dequeue() three times, followed by enqueue() three times, and repeat n times.

	n	seconds
=> passed	1024	0.00
=> passed	2048	0.00
=> passed	4096	0.00

```
=> passed      8192      0.00
=> passed     16384      0.00
=> passed     32768      0.00
=> passed     65536      0.01
=> passed    128000      0.02
=> passed    256000      0.05
==> 9/9 tests passed
```

Total: 67/67 tests passed!

=====