2022

Assignment 2

(Image Segmentation)

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1. Download the Dataset and Understand the Format:

[we work only on 50 images from the test images]

A function used to read images from a folder in the drive and save it in np array

```
Function for reading images

[2] import numpy as np import cv2

def read_images(folder,count):
    data = []
    for i in range(1, count+1):
        img = cv2.imread('/content/gdrive/MyDrive/assigm2_data/'+folder+'/'+folder+str(i)+'.jpg')
        img_col = np.array(img)
        #image will be flatten further more...
        subject = int(i)
        data.append(img_col)
        return np.array(data)

[3] test=read_images('test',50)
```

Read_mat_boderlines is a function used to load the borderlines of the ground truth from the mat file and save them as a jpg image

Read_mat_colored_segment is a function used to load the colored segments of the ground truth from the mat file and save them as a jpg image

Function to read ground truth and save as jpg image

```
[4] from scipy import io
        import os
         from imageio import imwrite
         import matplotlib.image as mpimg
        Import matpatetationage def read mat_borderlines(folder,count):
    save_pth1='/content/gdrive/MyDrive/assigm2_data/'+folder+'/'+'border_lines/'
           os.makedirs(save_pth1,exist_ok=True)
           for i in range(1,count+1):

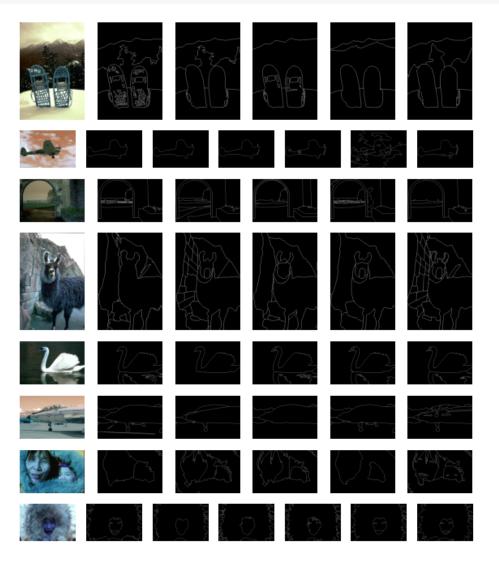
data = io.loadmat('/content/gdrive/MyDrive/assigm2_data/'+folder+'/'+folder+str(i))
              for j in range (len(data['groundTruth'][0])):
               edge_data = (data['groundTruth'][0][j][0][0][1]).astype(np.uint8)
                edge_data_255 = edge_data * 255
                new_img_name = folder.split('.')[0]+'_border_lines'+str(i)+'_'+str(j)+'.jpg'
               imwrite(os.path.join(save_pth1,new_img_name), edge_data_255)
[5] def read_mat_colored_segment(folder,count):
           save\_pth2='/content/gdrive/MyDrive/assigm2\_data/'+folder+'/'+'colored\_segments'+'/'os.makedirs(save\_pth2,exist\_ok=True)
           for i in range(1,count+1):
    data = io.loadmat('/content/gdrive/MyDrive/assigm2_data/'+folder+'/'+folder+str(i))
    for j in range (len(data['groundTruth'][0])):
               edge_data = (data['groundTruth'][0][j][0][0][0]).astype(np.uint8)
               edge_data_255 = edge_data * 255

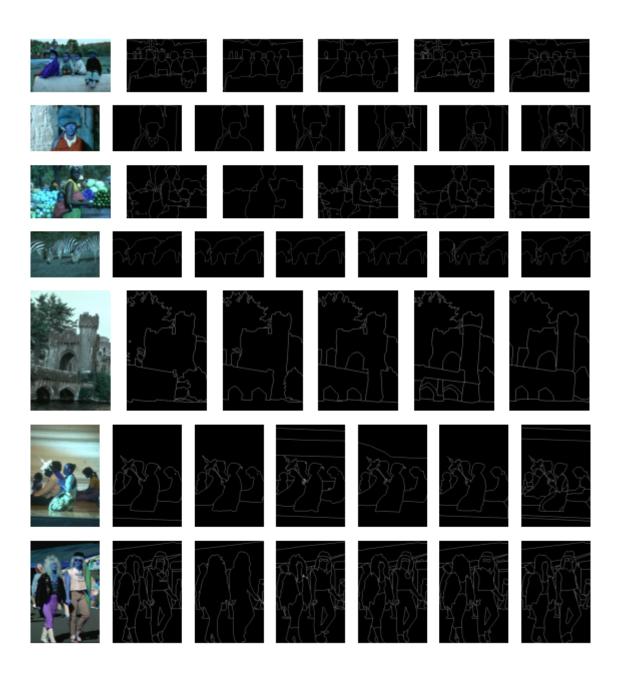
new_img_name = folder.split('.')[0]+'_colored'+str(i)+'_'+str(j)+'.jpg'
                path=os.path.join(save_pth2+new_img_name)
                mpimg.imsave(path,edge_data_255)
  [ ] ground truth test borderlines=read mat borderlines('ground truth test',50)
   [ ] ground truth test colored=read mat colored segment('ground truth test',50)
```

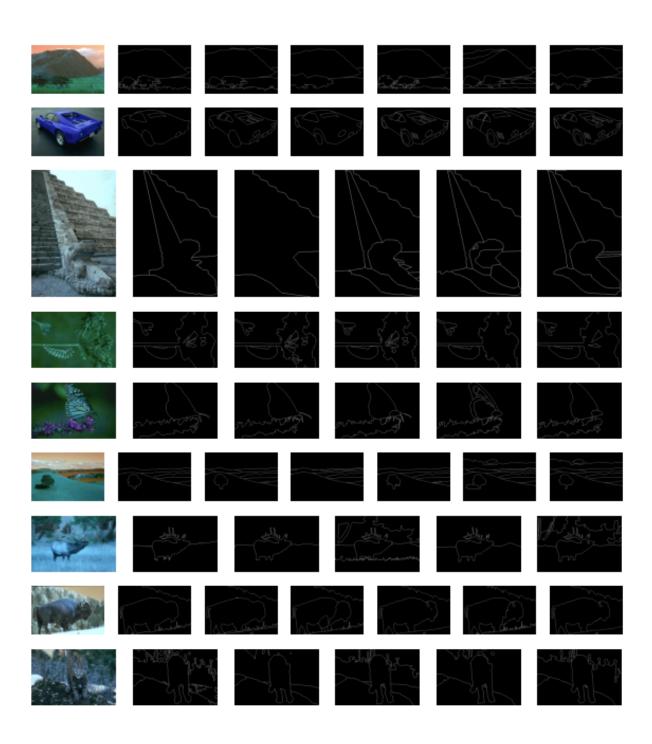
2. Visualize the image and the ground truth segmentation

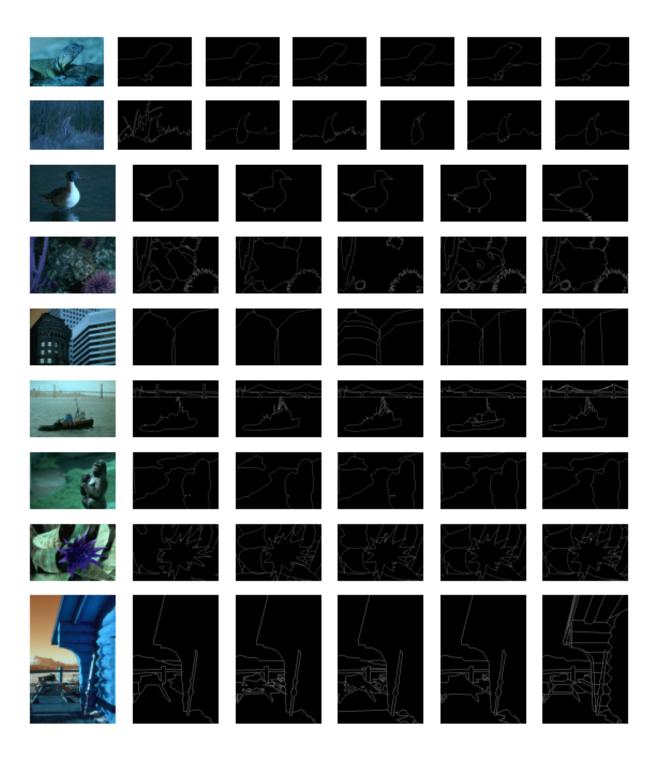
A function used to plot the image with all the corresponding borderlines ground truth and save them in the drive

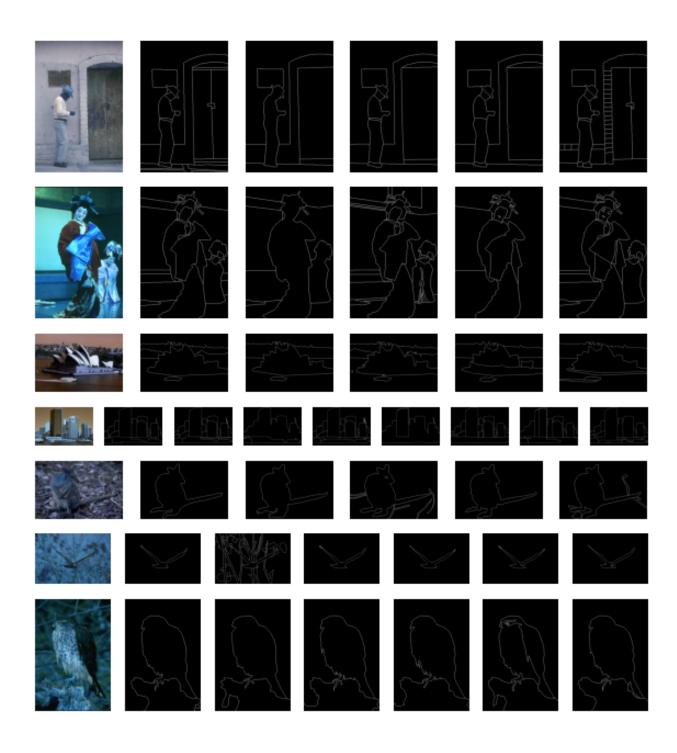
```
[ ] from matplotlib import pyplot as plt
     import cv2
     def view_edges(image_num):
       fig = plt.figure(figsize=(10,10))
data = io.loadmat('/content/gdrive/MyDrive/assigm2_data/ground_truth_test/ground_truth_test'+str(image_num))
       columns = 1+len(data['groundTruth'][0])
       original = cv2.imread('/content/gdrive/MyDrive/assigm2_data/test/test'+str(image_num)+'.jpg')
       fig.add_subplot(rows, columns,1)
       plt.imshow(original)
       plt.axis('off')
       for j in range(len(data['groundTruth'][0])):
         egge = cv2.imread('/content/gdrive/MyDrive/assigm2_data/ground_truth_test/border_lines/ground_truth_test_border_lines'+str(image_num)+'_'+str(j)+'.jpg')
         fig.add_subplot(rows, columns,1+j+1)
         plt.imshow(edge)
         plt.axis('off')
       fig.save fig('/content/gdrive/MyDrive/assigm2\_data/Figures/Original \&edges/fig'+str(image\_num)+'.jpg',bbox\_inches='tight')
[ ] for i in range(50):
    view_edges(i+1)
```

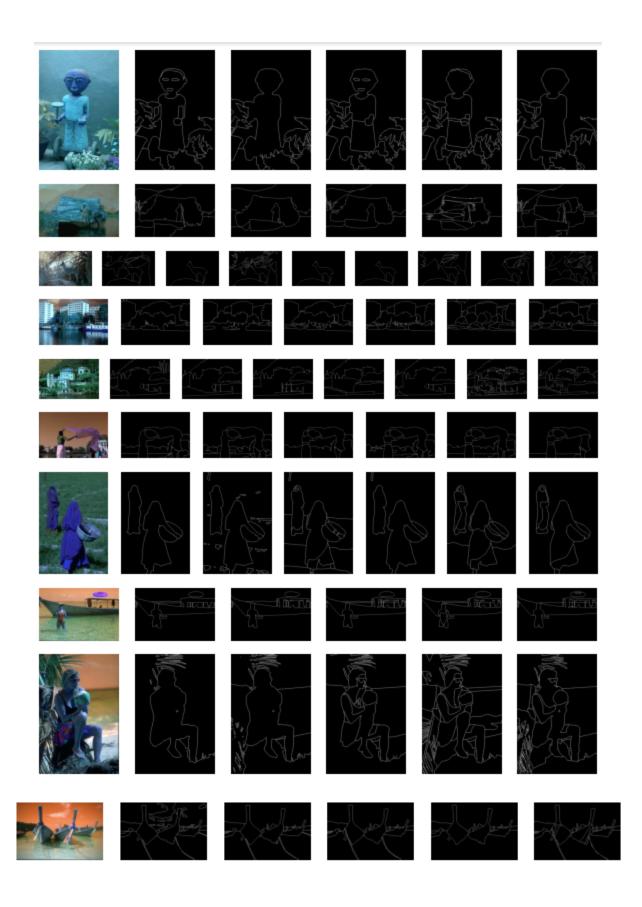












3. Segmentation using K-means

a)

A function used to calculate the k means of given image and return the cluster index for every pixel in the image.

We initialize random centroids at the first run. The function keeps working until it finds that the centroids places remain the same for 2 loops. If we have an empty cluster, we initialize new random centroid for it.

```
import random
def k_means(data,k):
 centroids = []
  for i in range(0,k):
    centroids.append(random.choice(data))
  while True:
    cluster_set = np.empty((k, 0)).tolist()
    newCentroids = []
    cluster_index = []
    distance = []
    for i in range(0,len(data)):
      row = []
     for j in range(0,k):
       row.append(np.linalg.norm(data[i] - centroids[j]))
     distance.append(row)
    distance = np.array(distance)
    for i in range(0,len(data)):
     for j in range(0,k):
       if (np.argmin(distance[i]))==j:
          cluster_set[j].append(data[i])
          cluster_index.append(j)
    cluster_set= np.array(cluster_set)
    for n in range(k):
      if len(cluster_set[n])==0:
        centroids[n]=random.choice(data)
      else:
        row =sum((cluster_set[n])[:])/len(cluster_set[n])
        newCentroids.append(row)
    newCentroids=centroids.copy()
    if np.sum(newCentroids) != np.sum(centroids):
        centroids= newCentroids
    else:
  cluster_index=np.array(cluster_index)
  return cluster_index
```

A function used to save the images resulting from the k_means function in the drive to use them later

```
[7] def save_images(folder,pixels,k,j,number,name):
    save_pth='/content/gdrive/MyDrive/assigm2_data/'+folder+'/'+name+str(number)+'/'
    os.makedirs(save_pth,exist_ok=True)
    new_img_name =str(j)+'_kmeans_'+'_'+str(k)+'.jpg'
    path=os.path.join(save_pth+new_img_name)
    mpimg.imsave(path,pixels)
```

We make the k means 5 times (M=5) to use them for calculating the average f measure and conditional entropy for every image

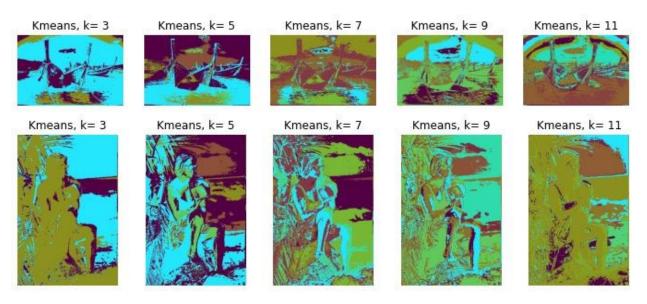
```
import matplotlib.pyplot as plt
for k in range (1,6):
    for i in range(0,50):
        for j in range (3,12,2):
            pixels=k_means(test[i].reshape(test[i].shape[0]*test[i].shape[1],test[i].shape[2]),j)
        pixels = pixels.reshape(test[i].shape[0],test[i].shape[1])
        save_images('ground_truth_test',pixels,j,i,k,'images')
```

A function used to plot the 5 k means (3-5-7-9-11) for every image

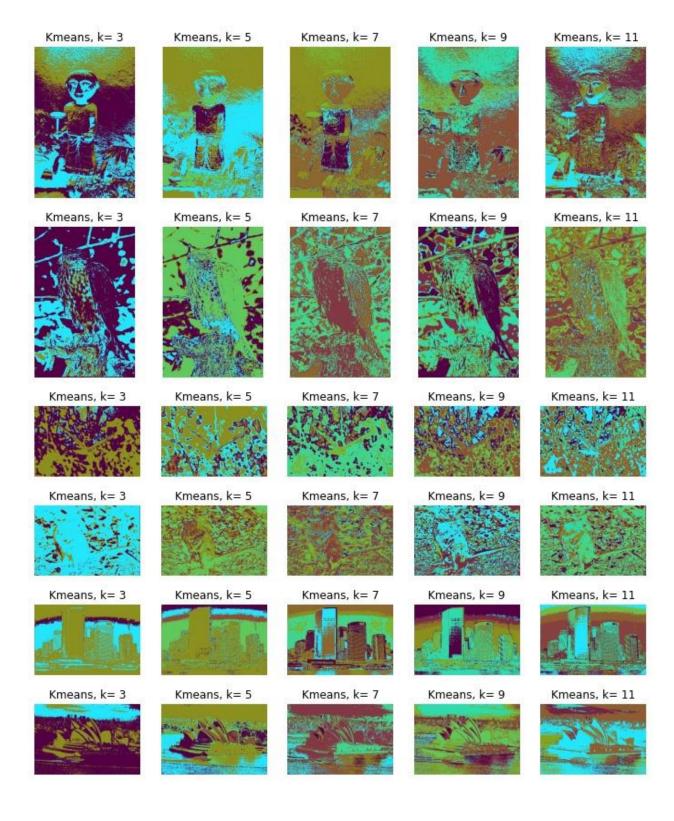
```
[ ] def view_kmeans(image_num):
    fig = plt.figure(figsize=(12,3))
    data = io.loadmat('/content/gdrive/MyDrive/assigm2_data/ground_truth_test/ground_truth_test'+str(image_num))
    rows = 1
    columns = 5
    k=3
    for i in range(1,6):
        kmeans = cv2.imread('/content/gdrive/MyDrive/assigm2_data/ground_truth_test/images1/'+str(image_num)+'_kmeans_'+str(k)+'.jpg')
        fig.add_subplot(rows, columns,i)
        plt.imshow(kmeans)
        plt.title('Kmeans, k= '+str(k))
        plt.axis('off')
        k=k+2
    fig.savefig('/content/gdrive/MyDrive/assigm2_data/Figures/Kmeans/fig'+str(image_num)+'.jpg',bbox_inches='tight')

[ ] for i in range (1,51):
        view_kmeans(i)
```

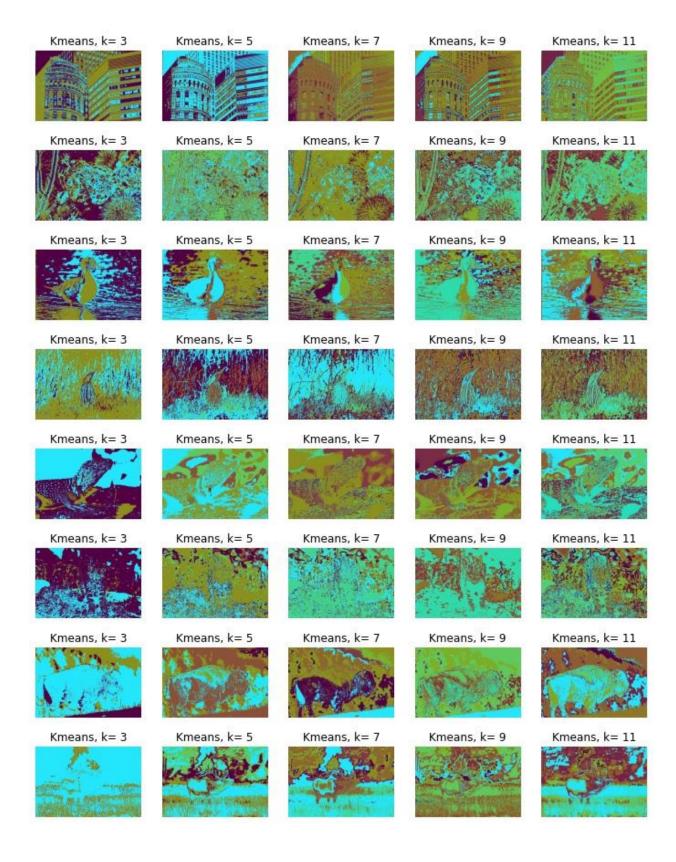
K-means for every image

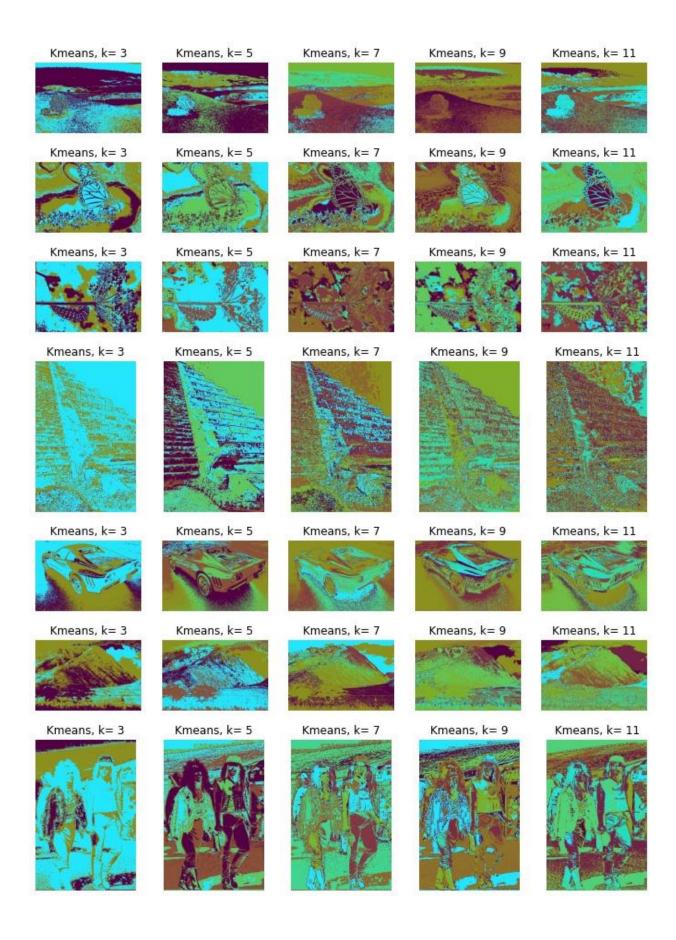




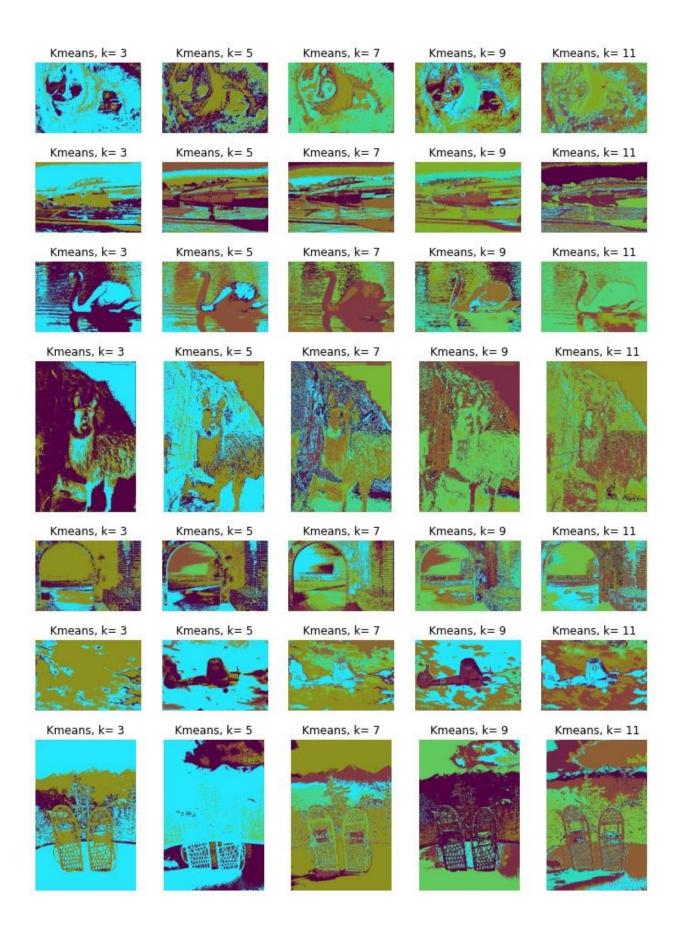












A function used to make masking for the k means clusters and ground truth clusters we collect all the extra clusters we have in the last cluster so both k means and ground truth have the same number of clusters

```
def mask(kmeans,ground_truth):
      x,y=np.unique(kmeans,return_counts=True)
      kmeans_unique=sort_lists(x, y)
      x,y=np.unique(ground_truth,return_counts=True)
      ground truth unique=sort lists(x, y)
      if len(kmeans_unique)<=len(ground_truth_unique):</pre>
        for i in range(0,len(kmeans_unique)-1):
          ground_truth=np.where(ground_truth==ground_truth_unique[i],kmeans_unique[i]+500,ground_truth)
        ground_truth=np.where(ground_truth<500,kmeans_unique[-1]+500,ground_truth)</pre>
        ground_truth=[x - 500 for x in ground_truth]
      else:
        for i in range(0,len(ground_truth_unique)-1):
          kmeans=np.where(kmeans==kmeans_unique[i],ground_truth_unique[i]+500,kmeans)
        \verb|kmeans=np.where| (\verb|kmeans<500|, ground_truth_unique[-1]+500|, kmeans)|
        kmeans=[x - 500 for x in kmeans]
      return kmeans,ground_truth
```

A function used to sort 1 list according to the elements of the second list we used this function in the masking function

```
[20] def sort_lists(list1, list2):
    zipped_pairs = zip(list2, list1)
    z = [x for _, x in sorted(zipped_pairs,reverse=True)]
    return z
```

A function used to print the measure results in a good table view

```
[60] from prettytable import PrettyTable
    def print_results(f_measure,conditional_entropy,i):
        print('Image :',i+1)
    # Specify the Column Names while initializing the Table
    myTable = PrettyTable(["k_means", "F measure", "Conditional entropy"])

# Add rows
myTable.add_row(["3", f_measure[(i*5)], conditional_entropy[(i*5)]])
myTable.add_row(["5", f_measure[(i*5)+1], conditional_entropy[(i*5)+1]])
myTable.add_row(["7", f_measure[(i*5)+2], conditional_entropy[(i*5)+2]])
myTable.add_row(["9", f_measure[(i*5)+3], conditional_entropy[(i*5)+3]])
myTable.add_row(["11", f_measure[(i*5)+4], conditional_entropy[(i*5)+4]])

print(myTable)
```

A function used to calculate the f measure and conditional entropy measure for every image using the contingency matrix

```
from sklearn.metrics.cluster import contingency_matrix
     import math
    def measures():
      f_measure_list=[]
      Conditional_Entropy_list=[]
       for i in range (1,51):
        data = io.loadmat('/content/gdrive/MyDrive/assigm2_data/'+'ground_truth_test'+'/'+'ground_truth_test'+str(i))
        #print('-----
        #print('Image Number ',i)
        #print('-----
        for k in range(3,12,2):
          f measure=0
          f_score=0
          Conditional_Entropy=0
          Conditional_Entropy_score=0
          for j in range(0,len(data['groundTruth'][0])):
            ground_truth = (data['groundTruth'][0][j][0][0][0]).astype(np.uint8)
            test = cv2.imread('_/content/gdrive/MyDrive/assigm2_data/test/test'+str(i)+'.jpg')
            pixels=k_means(test.reshape(test.shape[0]*test.shape[1],test.shape[2]),k)
            kmeans_labels,groundTruth_labels=mask(pixels,ground_truth)
            contingency_mat = contingency_matrix (groundTruth_labels,kmeans_labels)
            for x in range (len(contingency_mat[0,:])):
              max = np.argmax(contingency_mat[:,x])
              precision =contingency_mat[max,x]/np.sum(contingency_mat[:,x])
              recall = contingency_mat[max,x]/np.sum(contingency_mat[max,:])
              f_measure+=(2*precision*recall)/(precision+recall)
            for y in range (len(contingency_mat[0,:])):
              entropy = 0
              Conditional_Entropy=0
              for z in range (len(contingency_mat)):
               if(contingency_mat[z][y]!=0.0):
                  temp = contingency_mat[z][y]/sum(contingency_mat[:,y])
                  entropy-=(temp)*math.log2(temp)
              Conditional_Entropy+=(sum(contingency_mat[:,y])/(len(pixels)))*entropy
              Conditional_Entropy_score+=Conditional_Entropy
            f_measure=f_measure/len(contingency_mat[0,:])
            f_score+=f_measure
           f_score=f_score/len(data['groundTruth'][0])
           f_measure_list.append(f_score)
          Conditional_Entropy_score=Conditional_Entropy_score/len(data['groundTruth'][0])
          {\tt Conditional\_Entropy\_list.append(Conditional\_Entropy\_score)}
          #print('f_measure (',k,'means) = ',f_score)
          #print('Conditional_Entropy (',k,'means) = ',Conditional_Entropy_score)
      return f_measure_list,Conditional_Entropy_list
```

We calculate the f measures and conditional entropy and print them for all the images

```
[61] f_measure1,conditional_entropy1=measures()
```

```
for i in range (0,int(len(f_measure1)/5)):
    print_results(f_measure1,conditional_entropy1,i)
```

f measure and conditional entropy for every image

.mage : 1	+	++	₽	k means	F measure	Conditional entro
k_means	F measure	Conditional entropy		+		+
3	+ 0.5754384809868774	1.300240078294118		3	0.5790632183720736	1.45113193241790
5	0.42764476846281163	1.7911298914538005		5	0.46317167081342847	1.58475195943073
7	0.39831946530711865	1.826494292168676		7	0.42584685882522966	1.35506946127212
9	0.33460854304829074	1.900435125392765		9	0.35265916095515804	1.44402703620020
11	0.32368553076403483	1.8772767758791613		11	0.3498131021004127	1.33220540633725
	+	++		Image : 7		
k_means	++ F measure	Conditional entropy		k_means	F measure	Conditional entro
3	++ 0.7118976391482597	0.6610827735962425		3	0.5955551563814219	1.28461992428001
5				5	0.4076024793523426	1.38057964985273
7	0.6158729341420218	0.7264442222773774 0.7274175959620076		7	0.36336435888716073	1.44471314893998
,	0.6004715424152759			j 9 j	0.33842746354551884	1.40766528343464
9 11	0.6227956311254709 0.5303982164575859	0.652890263553881 0.6968891125965325		11	0.29609342339661626	1.41392251550628
	· +	· -		Image : 8		+
	+	·		+		+
k_means	F measure	Conditional entropy		k_means	F measure	Conditional entro
3	+ 0.6227581588165327	 1.1579050986815196		3	0.5708498871383675	0.92757476300836
5	0.40512664519762326	1.7508618576819708		5	0.3353738165784252	1.08328890433338
7	0.36026947957395583	2.0922238624080767		7	0.3236743095459316	0.99491841809018
9	0.3573178809731741	2.132438688804999		9	0.23513311484106528	1.06365994301623
11	0.33485841576394976	2.2379792563009957		11	0.22951549845383465	1.01438094236156
	+	++		Image : 9		
k_means	+ F measure	 Conditional entropy		k_means	F measure	Conditional entro
	+	++		3	0.6412437558355959	1.1801272581966
3	0.6427654818380726	1.1782337739824764		5 1	0.47477002489576137	1.52159553240677
5	0.45320028079621133	1.694242060069644		1 7 1	0.3832400406483903	1.84932988524815
7	0.3313426753579686	2.033297426966823		9 1	0.3224895232975663	2.04113172776454
9	0.2997951649935695	2.231852637400592		1 11	0.2967511693759366	2.13648114867450
11	0.2779467828479073 +	2.2191103546029187		+		+
image : 5				Image : 10		+
k_means	F measure	Conditional entropy		k_means	F measure	Conditional entro
3	+ 0.7300156189145788	 0.9885528336616524		3	0.6687599345308426	1.23136434858626
5	0.6023812406425422	0.9697129865133525		j 5 j	0.4406825421842436	1.67336774001135
7	0.47776874291881233	0.9329060502070581		j 7 j	0.38271835413044886	1.90987925723029
9	0.4388650570042829	0.9689988917037551		j 9 j	0.39389711025517765	1.75302885270608
11	0.4286449293461663	0.9250985096527904		11 1	0.3040202087882909	1.87571499581051

	+	
k_means		Conditional entropy
+ 3	0.5758897730315778	+ 1.1922004604731415
5	0.3328647860922726	1.8071734757997224
7	0.2827833261415299	2.116247046276522
9 11	0.27290624968503097 0.27325245352324845	2.3369109338957617 2.532546926652418
+	+	+
Image : 12	+	+
k_means	F measure	Conditional entropy
+ 3	0.6527795354383115	
5	0.4153438207296265	
	0.33382868979986036	
	0.32046626523335114	1.7108110349912007
+	+	+
Image : 13 +	+	+
k_means	F measure	Conditional entropy
	0.57355827526547	1.299698196437608
	0.37792514262469823	1.9286018233643056
7 9	0.3464104379185577 0.325342377576974	2.145612629230664
	0.2850759858915902	2.2797650401347047
+ Image : 14	+	+
+	++	
k_means	F measure	Conditional entropy
	0.6575392095646718	
5	0.4518393352212979	1.6729125796073154
	0.3674971401315427 0.311904358538341	
	0.3083803542418088	
+	· 	
Image : 15 	•	+
k_means		Conditional entropy
3		0.9511391780882111
5	0.3425366505156184	1.5535226310070813
7	0.28685796888125803 0.2792380778844779	1.8374807567586713
-	0.2502549055543729	
Image : 21 +	+	+ Conditional entropy
+	+	+
	0.7763126999679031	1.1960435768369402
5	0.7763126999679031 0.558535008062316 0.40418056169738376	1.1960435768369402 1.1999986127569668 1.3111761571311586
5 7 9	0.40418056169738376 0.36918392911018993	1.3111761571311586 1.3428167454473836
5 7 9 11	0.40418056169738376 0.36918392911018993 0.34817270777535775	1.3111761571311586 1.3428167454473836
5 7 9 11 +	0.40418056169738376 0.36918392911018993 0.34817270777535775	1.3111761571311586 1.3428167454473836
5 7 9 11 + Image : 22	0.40418056169738376 0.36918392911018993 0.34817270777535775	1.3111761571311586 1.3428167454473836 1.229174620351982
5 7 9 11 +	0.40418056169738376 0.36918392911018993 0.34817270777535775 	1.3111761571311586
5 7 9 11 +	0.40418055169738376 0.36918392911018893 0.34817270777535775 F measure 0.7426842892890987	1.3111761571311586
5 7 9 11 +	0.40418055169738376 0.36918392911018993 0.34817270777535775 F measure 0.7426842892890987 0.504374764484373 0.5043747643847761	1.3117/61571311586 1.342816734473836 1.229174620351982
5 7 9 11 11 12 13 3 5 7	0.40418055169738376 0.36918392911018993 0.34817270777535775 F measure 0.7426842892890987 0.5933670164843737 0.5942747643847761 0.4620055843511886	1.3117/61571311586 1.342816734473836 1.229174620351982 Conditional entropy 1.1517747752267704 1.4115738099408972 1.3784843861846248 1.453081409077514
5 7 9 11 1 1 1 1 1 1 1	0.40418055169738376 0.36918392911018993 0.34817270777535775 F measure 0.7426842892890987 0.5933670164843737 0.5942747643847761 0.4620055843511886	1.3117/61571311586 1.342816734473836 1.229174620351982
5 7 9 11	0.40418055169738376 0.36918392911018993 0.34817270777535775 F measure 0.7426842892890987 0.5033670164843737 0.5042747643847761 0.46200556843511886 0.43476875848748825	1.3117/61571311586 1.342816734473836 1.229174620351982 Conditional entropy 1.1517747752267704 1.4115738099408972 1.3784843861846248 1.453081409077514
5	0.40418055169738376 0.36918392911018993 0.34817270777535775 F measure 0.7426842892890987 0.5033670164843737 0.5042747643847761 0.46200556843511886 0.43476875848748825	1.3117/61571311586 1.342816734473836 1.229174620351982 Conditional entropy 1.1517747752267704 1.4115738099408972 1.3784843861846248 1.452301490272514 1.45201490272514 1.45201746182009957
5	0.40418055169738376 0.36918392911018993 0.34817270777535775 F measure 0.7426842892890987 0.5933679164843737 0.5042747643847761 0.46200556843511886 0.43476875848748825	1.3117/61571311586 1.342816734473836 1.229174620351982 Conditional entropy 1.1517747752267704 1.1517738099408972 1.3784843861846248 1.4523001490272514 1.4501746182009057
5	0.40418055169738376 0.36918392911018993 0.34817270777535775 F measure 0.7426842892890987 0.5933679164843737 0.5042747643847761 0.46200556843511886 0.43476875848748825	1.3117/61571511586 1.3428167454473836 1.229174620351982 Conditional entropy Conditional entropy 1.1517747752267704 1.41157380994089772 1.3784043861946248 1.4523001490272514 1.4501746182009057
5	0.40418055169738376 0.36918392911018993 0.34817270777535775 F measure 0.7426842892890987 0.5033670164843737 0.5042747643847761 0.43476875848748825 F measure 0.6817430246763627 0.5292744067704654 0.432214803474824	1.3117/61571311586 1.342816734473836 1.229174620351982 Conditional entropy 1.1517747752267704 1.415738099408972 1.3784843861346248 1.4523001490272514 1.4501746182009057 Conditional entropy Conditional entropy
5	0.40418056169738376 0.36918392911018993 0.34817270777535775 F measure 0.7426842892890987 0.5033670164843737 0.5042747643847761 0.4620055643511886 0.43476875848748825 F measure 0.6817439246763627 0.5292744067704654 0.43221480344774824 0.43425738047985397	1.3117/61571311586 1.342816734473836 1.229174620351982 Conditional entropy Conditional entropy 1.1517747752267704 1.4115738099408972 1.3784943861946248 1.4523041499272514 1.45201746182009057 Conditional entropy Conditional entropy 1.3663709647935118 1.45715072560833 1.4341060932496477 1.3884228592634748
5	0.40418055169738376 0.36918392911018993 0.34817270777535775 F measure 0.7426842892890987 0.5933679164843737 0.5942747643847761 0.46200555843511886 0.43476875848748825 F measure 0.6817430246763627 0.5292744067704654 0.4322148934474824 0.345219834474824 0.345219834477824	1.3117/61571311586 1.342816734473836 1.229174620351982 Conditional entropy Conditional entropy 1.1517747752267704 1.4115738099408972 1.3784843861846248 1.452001490272514 1.45201746182009057 Conditional entropy Conditional entropy 1.3663709647935118 1.45715072560833 1.4341060932496477 1.3884228502634748
5	0.40418056169738376 0.36918392911018993 0.34817270777535775 F measure 0.7426842892890987 0.50336701648437761 0.46200556843511886 0.43476875848748825 F measure 0.6817430246763627 0.5292744067704654 0.4322148034474824 0.34595738047985397 0.3440371780529506	1.3117/61571311586 1.3428167454473836 1.229174620351982 Conditional entropy Conditional entropy 1.1517747752267704 1.4115738099408972 1.3784943861946248 1.4523041499272514 1.452014490272514 Conditional entropy Conditional entropy 1.3663709647935118 1.45715072560833 1.4341060932496477 1.3884228502634748 1.388422850263478 1.388422850263478
5	0.40418055169738376 0.36918392911018993 0.34817270777535775 F measure	1.3117/61571311586 1.3428167454473836 1.229174620351982 Conditional entropy Conditional entropy 1.1517747752267704 1.4115738099408972 1.3784943861946248 1.4523041499272514 1.452014490272514 Conditional entropy Conditional entropy 1.3663709647935118 1.45715072560833 1.4341060932496477 1.3884228502634748 1.388422850263478 1.388422850263478
5 7 9 11 11 1 1 1 1 1 1	0.40418055169738376	1.3117/61571311586 1.342816734473836 1.229174620351982 Conditional entropy 1.1517747752267704 1.1517747752267704 1.4157380994089772 1.3784043861946248 1.4523001490272514 1.452301490272514 1.45210746182009057 Conditional entropy 1.3663709647935118 1.45715072560833 1.4341060932496477 1.3884228502634748 1.2861010850299153
5	0.40418055169738376	1.3117/61571511586 1.342816734473836 1.229174620351982 Conditional entropy 1.1517747752267704 1.4115738099408972 1.3784843861846248 1.4523001490272514 1.45201746182009057 Conditional entropy 1.3663709647935118 1.45715072560833 1.43410609324096477 1.3884228502634748 1.2861010850299153
5	0.40418056169738376	1.3117/61571311586 1.342816734473836 1.229174620351982 Conditional entropy 1.1517747752267704 1.1517747752267704 1.4157380994089772 1.3784043861946248 1.4523001490272514 1.452301490272514 1.45210746182009057 Conditional entropy 1.3663709647935118 1.45715072560833 1.4341060932496477 1.3884228502634748 1.2861010850299153
5	0.40418055169738376 0.36918392911018993 0.34817270777535775 F measure 0.7426842892890987 0.5033670164843737 0.5042747643847761 0.46200556843511886 0.43476875848748825 F measure 0.6817430246763627 0.5292744067704654 0.4322148034474824 0.343597330847985397 0.3440371780529506 F measure 0.58981892117779723 0.3824575532891501 0.30829730903336056 0.2721840669900318	1.3117/61571311586 1.342816734473836 1.229174620351982 Conditional entropy 1.1517747752267704 1.4115738099408972 1.3784843861846248 1.452014990272514 1.4501746182009057 Conditional entropy 1.3663709647935118 1.45715072560833 1.4341060932496477 1.3884225502634748 1.2861010850229153
5	0.40418055169738376 0.36918392911018993 0.34817270777535775 F measure 0.7426842892890987 0.5033670164843737 0.5042747643847761 0.46200556843511886 0.43476875848748825 F measure 0.6817430246763627 0.5292744067704654 0.4322148034474824 0.343597330847985397 0.3440371780529506 F measure 0.58981892117779723 0.3824575532891501 0.30829730903336056 0.2721840669900318	1.3117/61571311586 1.342816734473836 1.229174620351982 Conditional entropy
5	0.40418055169738376	1.3117/61571311586 1.342816734473836 1.229174620351982 Conditional entropy
5	0.40418055169738376	1.3117/61571311586 1.342816734473363 1.229174620351982 Conditional entropy 1.1517747752267704 1.4115738099408972 1.3784843861846248 1.452001490272514 1.4501746182009057 Conditional entropy 1.3663709647935118 1.45715072560833 1.43410609324096477 1.3884228502634748 1.28610108502299153
5	0.40418056169738376	1.3117/61571311586 1.342816734473836 1.229174620351982 Conditional entropy Conditional entropy 1.1517747752267704 1.4115738099408972 1.3784843861946248 1.4523041490272514 1.4523041490272514 1.4520614190272514 1.3663709647935118 1.35415072560833 1.4341060932496477 1.3864278592634748 1.2861010850299153 Conditional entropy 1.3664787928467874 1.8367942475369368 2.0234821061174753 1.9417378659201713 Conditional entropy
5	0.40418055169738376	1.3117/61571311586 1.342816734473363 1.229174620351982 Conditional entropy
5	0.40418056169738376	1.3117/61571311586 1.342816734473363 1.229174620351982 Conditional entropy
5	0.40418055169738376	1.3117/61571311586 1.342816734473836 1.229174620351982 Conditional entropy

k means	F measure	Conditional entro
+	++	
	0.7634101108377175	1.14980475312659
	0.5486097587294617 0.5099451635256352	1.37633833232116
	0.4078415651499521	1.32806719155920 1.46015573939103
11	0.422881941587336	1.20417673333657
+		
Image : 17 +	++	
	F measure	Conditional entro
+	0.6061061685441994	1 10600615117100
	0.489254154005639	
	0.3365575826223841	1.29634274696123
	0.2683041743125962	
11	0.2274279956431512	1.36775194645465
Image : 18		
k means	F measure	Conditional entr
+		+
	0.5706497193331088 0.48386113190398927	
	0.42338060543916456	
9	0.42536990703032734	1.7024055947623
	0.40018114362842405	1.7182735923043
Image : 19		
	F measure	
+		+
3		1.4732016143582
5 7	0.39714720614402943	1.9390753348532
	0.2957460238980659 0.25613904436071544	1.9735776677254
	0.22873097641004322	2.0010277835174
+ Image : 20	+	+
+		
k_means	F measure	Conditional entro
3	0.6372785255600598	1.18538444541399
	0.4562685924012605	
	0.3318893317504831	1.36669423635644
11 	0.3094351660262912 0.2676909356620542	1.31455837191915 1.34444922353808
11 	0.3094351660262912 0.2676909356620542	1.31455837191915 1.34444922353808
11 	0.3094351660262912 0.2676909356620542	1.31455837191915 1.34444922353808
Image : 2	0.3094351660262912 0.2676909356620542 6 F measure 0.6049924552513585 0.4705456264700365	1.31455837191915 1.34444922353808 Conditional ent 1.013781744200 1.06628574095
Image : 2	0.3094351660262912 0.2676909356620542 6 F measure 0.6049924552513585 0.4705456264700365 0.46931047238953355	1.3455837191915 1.3444492353808 Conditional ent 1.013781744200 1.0665874095 1.074963912888
Image : 2 +	0.3094351660262912 0.2676909356620542 6 F measure 0.6649924552513585 0.4705456264700365 0.46931047238953355 0.44735838355125979	1.3444922353808 1.34444922353808 Conditional ent 1.013781744200 1.066628574095 1.074963912888 1.068398644166
Image : 2	0.3094351660262912 0.2676909356620542 0.2676909356620542 0.2676909356620542 0.604992452513585 0.4705456264700365 0.46931047238953355 0.46931047238953505 0.46931047238953505 0.4693104723895505 0.469310472389505 0.469310472389505 0.469310472389505 0.469310472389505 0.469310472389505 0.469310472389505 0.469310472389505 0.46931047258505 0.46951047505 0.46951047505 0.46951047505 0.46951047505 0.46951047505 0.46951047505 0.46951047505 0.46951047505 0.46951047505 0.46951047505 0.46951047505 0.4695104505 0.4695104505 0.4695104505 0.4695104505 0.4695104505 0.4695104505 0.4695104505 0.4695104505 0.4695104505 0.4695104505 0.469510505 0.469510505 0.46951050505 0.469510505 0.46951050505 0.46951050505 0.469510505050505 0.46951050505 0.4695105050505 0.4695105050505 0.469510505050505 0.46951050505050505005005000000000000000000	1.3444922353808 1.34444922353808 Conditional ent 1.013781744200 1.066628574095 1.074963912888 1.068398644166
Image : 2 +	0.3094351660262912 0.2676909356620542 6 F measure 0.6049924552513585 0.4705456264700365 0.46931047238933551 0.417358355125972 0.3821963973981431	1.31455837191915 1.34444922353808 Conditional ent 1.013781744200 1.066628574095 1.074963912888 1.068398644166
Image : 2 k_means 3 5 7 9 11 Image : 2	0.3094351660262912 0.2676909356620542 6 F measure 0.6049924552513585 0.4705456264700365 0.46931047238933551 0.417358355125972 0.3821963973981431	1.3445837191915 1.34444922353808 Conditional ent 1.013781744200 1.0668574095 1.074963912888 1.068398644166 1.079426352994
Image : 2 k_means 3 5 7 9 11 Image : 2 k_means 1 1 k_means k_m	0.3094351660262912 0.2676909356620542 0.2676909356620542 0.2676909356620542 0.269292452513585 0.4705456264700365 0.46931047238953355 0.46931047238953355 0.3623963973981431 7 F measure	1.3445837191915 1.34444922353808 Conditional ent 1.013781744200 1.066628574095 1.074963912888 1.068398644166 1.079426352994
Image: 2 k_means 3 5	0.3094351660262912 0.2676909356620542 6.2676909356620542 6 F measure 0.6049924552513585 0.4705456264708365 0.46931047238953355 0.437358835512597 0.3821963973981431 7 F measure 0.9332523273947265	1.3444922353808 Conditional ent Conditional ent 1.013781744200 1.066628574095 1.074963912888 1.08398644166 1.079426352994 Conditional entr
Image: 2 k_means 3 5 7 9 11 Image: 2 k_means 3 5 7 7 9 11 Image: 2 1 1 1 1 1 1 1 1 1	0.3094351660262912 0.2676909356620542 0.2676909356620542 0.2676909356620542 0.269292452513585 0.4705456264700365 0.46931047238953355 0.46931047238953355 0.3623963973981431 7 F measure	1.3444922353808 Conditional ent 1.013781744200 1.066628574095 1.079426352994 1.0
Image : 2 k_means 3 5 7 9 11 Image : 2 k_means 3 5 7 7 9	0.3994351662052912 0.2676909356620542 6.2676909356620542 6 F measure 0.6049924552513585 0.4705456264709365 0.46931047238953355 0.4370588355125972 0.3821963973981431 7 F measure 0.9332523273947265 0.8813096213558026 0.88285335813261309 0.8411762954033708 0.841176296403708 0.841176296403708 0.841176296403708 0.841176296403708 0.841176296403708 0.841176296403708 0.841176296403708 0.841176296403708 0.841176298 0.84	1.3445837191915 1.34444922353808 Conditional ent 1.013781744200 1.066628574095 1.074963912888 1.068398644166 1.079426352994 Conditional entr 0.6498238397266 0.6171283309745 0.6372298011755 0.6264520556144
Image: 2 k_means 3 5 7 9 11 Image: 2 k_means 5 7 7 11 Image: 2 5 7 7 11 Image: 2 5 7 7 11 1 1 1 1 1 1	0.3094351660262912 0.2676909356620542 6.2676909356620542 6 F measure 0.6049924552513585 0.4705456264700365 0.4693104723895355 0.4173588355125972 0.3821963973981431 7 F measure 0.9332523273947265 0.8813096213558026 0.828533531351261309 0.828535351351261309	1.3445837191915 1.34444922353808 Conditional ent 1.013781744200 1.066628574095 1.074963912888 1.068398644166 1.079426352994 Conditional entr 0.6498238397266 0.6171283309745 0.6372298011755 0.6264520556144
Image : 2	0.3994351662052912 0.2676909356620542 0.2676909356620542 0.2676909356620542 0.2676909356620542 0.269253355 0.46931047238953355 0.46931047238953355 0.4673588355125972 0.3821963973981431 7 F measure 0.9332523273947265 0.8813096213558026 0.88285335813261358026 0.88137713394147036 0.8387713394147036	1.3445837191915 1.34444922353808 Conditional ent 1.013781744200 1.066628574095 1.074963912888 1.068398644166 1.079426352994 Conditional entr 0.6498238397266 0.6171283309745 0.6264520556144 0.5810283501185
Image : 2	0.3094351660262912 0.2676909356620542 6.2676909356620542 6	1.3445837191915 1.34444922353808 Conditional ent 1.013781744200 1.066628574095 1.074963912888 1.068398644166 1.079426352994 Conditional entr 0.6498238397266 0.6372298011755 0.6264520556144 0.5810283501185
Image : 2	0.3994351662052912 0.2676909356620542 0.2676909356620542 0.2676909356620542 0.2676909356620542 0.269326264708365 0.46931047238953355 0.4795456264708365 0.46931047238953355 0.4173588355125972 0.3821963973981431 7	1.3445837191915 1.34444922353808 Conditional ent 1.013781744200 1.066628574095 1.074963912888 1.068398644166 1.079426352994 Conditional entr 0.6498238397266 0.6371283309745 0.6372298011755 0.62645205561185
Image : 2	0.3994351662052912 0.2676909356620542 6.2676909356620542 6.2676909356620542 6.2676909356620542 6.26931047238953355 0.4673588355125972 0.3821963973981431 7 F measure 0.9332523273947265 0.8813096213558026 0.82853358126937398 0.8387713394147036 8 F measure 0.5932144706686485 6.5932144706686485 C.5932144706686485 0.5932144706686485 0.5932144706686485 0.5932144706686485 0.5932144706686485 0.5932144706686485 0.5932144706686485 0.5932144706686485 0.5932144706686485 0.5932144706686485 0.5932144706686485 0.5932144706686485 0.5932144706686485 0.5932144706686485 0.5932144706686485 0.5932144706686485 0.5932144706686485 0.5932144706686485 0.5932144706686485 0.5932144706686485 0.5932144706686485 0.5932144706686485 0.5932144706686485 0.5932144706686485 0.5932144706686485 0.5932144706686485 0.59321447068686485 0.5932	1.3445837191915 1.34444922353808 Conditional ent 1.013781744200 1.066628574095 1.074963912888 1.068398644166 1.079426352994 Conditional entr 0.6498238397266 0.6171283300745 0.6372298011755 0.626452805765144 0.5810283501185
Image : 2 k_means 3 5 7 9 11 Image : 2 k_means 1 3 5 7 9 11 Image : 2 k_means 1 1 1 1 1 1 1 1 1	0.3994351660262912 0.2676909356620542 6.2676909356620542 6	1.3445837191915 1.34444922353808 Conditional ent 1.013781744200 1.066628574095 1.079426352994 Conditional entr 0.6498238397266 0.6372298011755 0.6264520556144 0.5810283501165 Conditional entr
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Image : 2 k_means 3 5 7 9 11 Image : 2 k_means 3 5 7 9 11 Image : 2	0.3994351662052912 0.2676909356620542 0.2676909356620542 0.2676909356620542 0.2676909356620542 0.2676909356620542 0.26931047238953355 0.4673588355125972 0.3821963973981431 7 F measure	1.3445837191915 1.34444922353808 Conditional entrolled

Image : 31	*		-	Image : 36		
k_means	F measure	Conditional entropy	ž	k_means	F measure	Conditional entre
+	+			+	0.6471726776426802	+
5	0.44875151516856454	1.6895626249080613		5	0.49729332669893295	1.6262444021345
7	0.3900063117800712 0.3847486571928056	1.7051708443789135			0.38074469052980486	
	0.4076789800830885				0.37906904077822107 0.3751781223851293	
mage : 32	+			+		+
	+			+		+
	F measure	Conditional entropy			F measure	
3	0.5681558922967175	1.148573046350994		3	0.7168536678633312	1.1506686974379
-	0.4541107204791911 0.260233128801769				0.47723645910032547 0.42189646009012427	
	0.30203482275811344				0.35609416926219467	
	0.2732919352979167				0.3151990727064026	
age : 33				Image : 38		+
	t			+	F measure	+
	F measure			+	r measure	+
	0.6315414482870059				0.6783725964009513	
	0.41779634903760315				0.5878564601313193 0.5240627706877918	
9	0.29177845970491323	1.7846208974339308		9	0.5024591131166448	1.0512291526301
11	0.28975121913544066	1.7472378955723393		11	0.48203708757317143	1.0454016845858
age : 34				Image : 39		
k means	+ F measure	Conditional entropy		k means	F measure	Conditional entro
	+			+		
	0.6982575773955135				0.7667999910942763 0.6151032382283034	
	0.4113997518012735 0.37516651733188927			7	0.5704479497886791	0.54223358061580
9	0.3172758807295718	1.8646404006828026		9	0.5553248743006172	0.58810843805593
	0.2979428019305176	1.839980598737815		1 11	0.5472412568599674	0.02102434669/92
age : 35				Image : 40		
k_means		Conditional entropy		k_means	F measure	Conditional entr
3	0.5714264325006583	1 1602717052561900 I			0.6041871451227547	
	0.39799825497990843				0.4406333885914076	
	0.39437987790903384				0.42414965654791564	
	0.3758889322178095 0.318728769074771			9 1	0.3858108081706248 0.39194438295634626	1.2852625334910
	+ F measure	+ Conditional entropy			s F measure	
3	0.6041871451227547	1 3137367389994868		1 3	0.62542958995419	
5	0.4406333885914076	1.3388126665640858		5	0.490493770145336	46 1.4149147491
	0.42414965654791564			7	0.335317602569719	
	0.3858108081706248 0.39194438295634626				0.303252362205403	
· · · · · · · · · · · · · · · · · · ·	+	+		+	+	
nage : 41		+		Image :	47	+
k_means	F measure	Conditional entropy		k_mean	s F measure	Conditional e
3		1.3092922836861534		3	0.62227974391106	84 1.1540595840
	0.36415724669904026	1.7087736285117194			0.40261484870647	
	0.30710931677169984	2102010000000010020		7	0.334437619667815	
	0.2290039528856201			11	0.28164534308086	
age : 42	+	+		+ Image :	48	+
	+	+		+	s F measure	Conditions
κ_means	h measure	Conditional entropy		K_mean	+	+
	0.6335905823377284			3	0.70098452119727	
5	0.41101717850215413	1.6964526912475582		5 7	0.51044330992509	
	0.393819808690974	1.6804687471916264		9	0.37076460703495	36 1.3433744826
	0.3659456543638172				0.29719890068127	
age : 43				Image :		
		+ Conditional entropy		k_mean	s F measure	Conditional en
	+	+		+	+	+
		1.1270567767368067		3 5	0.551571909756153	
5 7	0.43277830456937855 0.36457703541475656	1.635431695971985		7	0.358709379725911	9 1.87648803577
9	0.3318369297204693	1.6769073463482866		9	0.323835876485367	
		1.6440663271512448			0.282922966243823	
age : 44				Image :	50	
k_means	F measure	Conditional entropy		k_mean	s F measure	
	+	+		+ l 3	0.673364431225166	
-	0.575905742132922 0.3367183409716701			3	0.526899474032938	8 1.52000739018
7	0.32322021147667457	2.178871001809207		7	0.344555235889751	9 1.79437365523
9	0.2519620683697891	2.342295201803195		9	0.308117491250567	
	0.23860311330881145	2.400104388223649			+	

4. Big picture

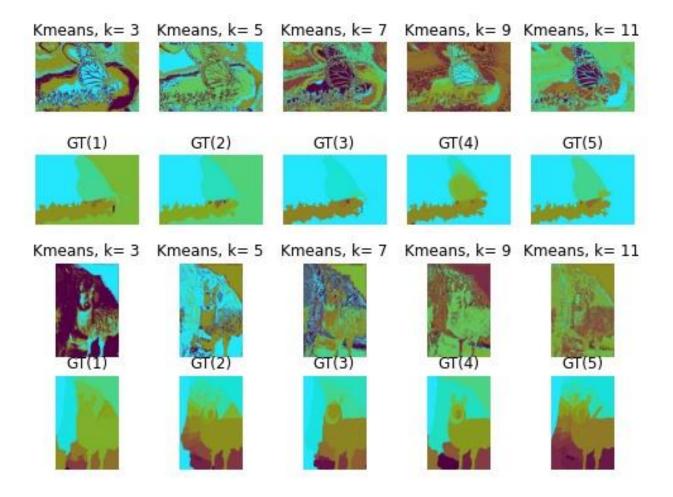
a)

A function used to plot the 5 k means (3-5-7-9-11) and the ground truth for 5 selected images

```
[ ] def view_kmeansAndGround(image_num):
    fig * pit.figure(figsize*(12,3))
    data = io.loadmat('/content/gdrive/hyOrive/assigm2_data/ground_truth_test/ground_truth_test'*str(image_num))
    rows = 2
    columns = 7
    k=3
    for i in range(1,6):
        kmeans = cv2.imread('/content/gdrive/hyOrive/assigm2_data/ground_truth_test/images1/'*str(image_num)+'_kmeans__'*str(k)+'.jpg')
        fig.add_subplot(rows, columns,i)
        plt.title('kmeans, k= '*str(k))
        plt.axis('off')
        kek+2
        for j in range(len(data['groundTruth'][0])):
        edge = cv2.imread('/content/gdrive/hyOrive/assigm2_data/ground_truth_test/colored_segments/ground_truth_test_colored'*str(image_num)+'_'*str(j)+'.jpg')
        fig.add_subplot(rows, columns,i+j+l+5+1)
        plt.simsNow(edge)
        plt.axis('off')
        plt.axis('off')
        plt.title('GT('*str(j+1)*)')')

        fig.savefig('/content/gdrive/hyOrive/assigm2_data/Figures/Kmeans&Ground/fig'*str(image_num)+'.jpg',bbox_inches*'tight')

[ ] view_kmeansAndGround(2)
        view_kmeansAndGround(3)
        view_kmeansAndGround(3)
        view_kmeansAndGround(30)
        view_kmeansAndGround(30)
        view_kmeansAndGround(40)
        view_kmeansAndGround(20)
        view_kmeansAndGround(20)
        view_kmeansAndGround(40)
        view_kmeansAndGround(20)
        view_kmeansAndGround(40)
        view
```





b)

A function used to resize the original image by taking 25% of the width and 25% of the length to use it in the normalized cut

```
[13] def readAndResize(folder,count,scale_percent):
    for i in range(l,count+1):
        img = cv2.imread('/content/gdrive/MyDrive/assigm2_data/'+folder+'/'+folder+str(i)+'.jpg') #need to be edited
    width = int(img.shape[1] * scale_percent / 100)
    height = int(img.shape[0] * scale_percent / 100)
    dim = (width, height)
    resized_image = cv2.resize(img, dim, interpolation = cv2.INTER_AREA)
    save_pth='/content/gdrive/MyDrive/assigm2_data/'+'resized'+'/'+'res'+str(i)+'.jpg'
    cv2.imwrite(save_pth,resized_image)
[ ] readAndResize('test',50,25)
```

A function used to calculate the distance matrix

```
12] def calcDistanceMatrix(data):
    data=data.reshape(data.shape[0]*data.shape[1],data.shape[2])
    distanceMat=[]
    for i in range(data.shape[0]):
        distanceMat.append(np.linalg.norm((data[i]-data),axis=1))
    return np.array(distanceMat)
```

A function used to calculate the normalization cut

```
[11] from sklearn.cluster import KMeans
    from sklearn.neighbors import kneighbors_graph

def normCut(data, k, knn):

    distMatrix=calcDistanceMatrix(data)
    #connectivity here referes to ones and zeros not distance _include self refers to not to consider the point itself to be neighbor adj = kneighbors_graph(distMatrix , knn , mode='connectivity', include_self=False).toarray()
    degree = np.diag(np.sum(adj, axis=1))
    L = np.subtract(degree,adj)
    eigen_values, eigen_vectors = np.linalg.eig(np.dot(np.linalg.inv(degree),L))

sorted_eigen_vectors = eigen_vectors[:,eigen_values.argsort()][:,0:k]
    for i in range(k):
        sorted_eigen_vectors[:,i] = sorted_eigen_vectors[:,i] / np.linalg.norm(sorted_eigen_vectors[:,i])

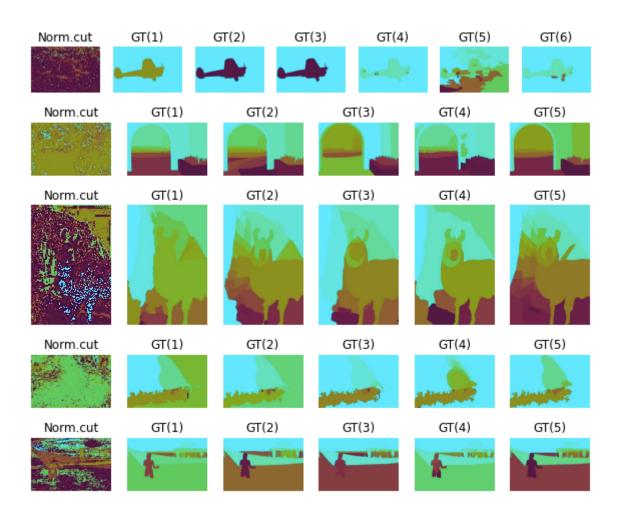
km = kMeans(n_clusters=k).fit(np.real(sorted_eigen_vectors))
    return km_labels
```

A function used to calculate the normalized cut and save the image resulted from it in the drive

A function used to plot the normalized cut and the ground truth for 5 selected images

```
[] def view_groundAndNorm(image_num):
    fig = plt.figure(figsize=(10,18))
    data = io.loadmat('/content/gdrive/MyDrive/assigm2_data/ground_truth_test'+str(image_num))
    rows = 1
    columns = 1+len(data['groundTruth'][0])
    normut = cv2.imread('/content/gdrive/MyDrive/assigm2_data/normalized_cut/'+str(image_num)+'_Normcut.jpg')
    fig.add_subplot(rows, columns,1)
    plt.imshow(normcut)
    plt.axis('off')
    plt.title("Norm.cut")
    for j in range(len(data['groundTruth'][0])):
    edge = cv2.imread('/content/gdrive/MyDrive/assigm2_data/ground_truth_test/colored_segments/ground_truth_test_colored'+str(image_num)+'_'+str(j)+'.jpg')
    fig.add_subplot(rows, columns,1+j+1)
    plt.imshow(edge)
    plt.axis('off')
    plt.title('GT('+str(j+1)+')')
    fig.savefig('/content/gdrive/MyDrive/assigm2_data/Figures/Normalized&Ground/fig'+str(image_num)+'.jpg',bbox_inches='tight')

[] view_groundAndNorm(2)
    view_groundAndNorm(3)
    view_groundAndNorm(4)
    view_groundAndNorm(40)
    view_groundAndNorm(40)
    view_groundAndNorm(40)
    view_groundAndNorm(40)
    view_groundAndNorm(41)
```



A function used to plot the 5 k means (3-5-7-9-11) and the normalized cut for 5 selected images

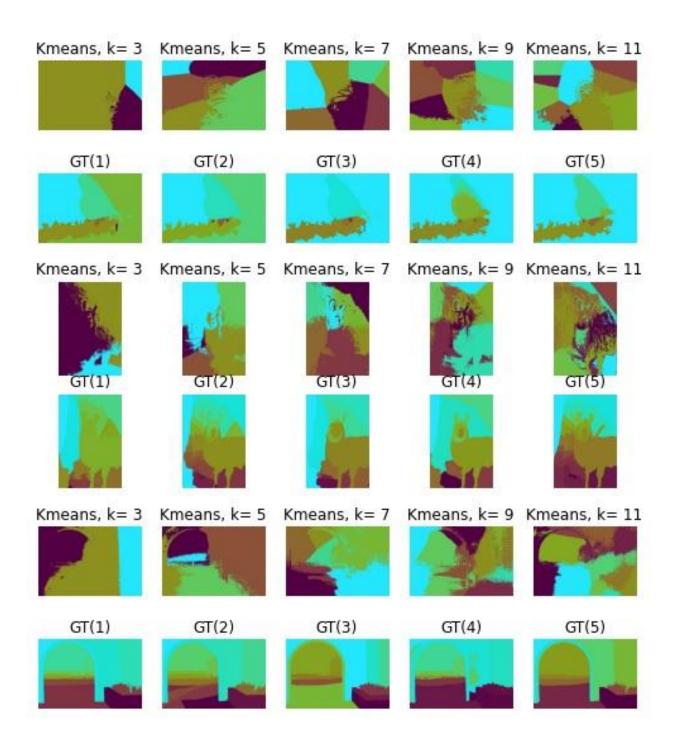
```
[ ] def viewkmeansAndNormalized(num):
      fig = plt.figure(figsize=(15,15))
      rows = 1
      columns = 6
      normalized_cut = cv2.imread('/content/gdrive/MyDrive/assigm2_data/normalized_cut/'+str(num)+'_Normcut.jpg')
      fig.add_subplot(rows, columns,1)
      plt.imshow(normalized_cut)
      plt.axis('off')
      plt.title('Normalized cut')
      k=3
      for j in range(2,7):
        kmeans = cv2.imread('/content/gdrive/MyDrive/assigm2_data/ground\_truth\_test/images1/'+str(num)+'\_kmeans\__'+str(k)+'.jpg')
        fig.add_subplot(rows, columns,j)
        plt.imshow(kmeans)
        plt.title('Kmeans, k= '+str(k))
        plt.axis('off')
        k=k+2
      fig.savefig('/content/gdrive/MyDrive/assigm2_data/Figures/Normalized&Kmeans/fig'+str(num)+'.jpg',bbox_inches='tight')
[ ] viewkmeansAndNormalized(2)
    viewkmeansAndNormalized(3)
    viewkmeansAndNormalized(4)
    viewkmeansAndNormalized(20)
    viewkmeansAndNormalized(48)
Normalized cut
                      Kmeans, k= 3
                                              Kmeans, k= 5
                                                                    Kmeans, k= 7
                                                                                           Kmeans, k= 9
                                                                                                                 Kmeans, k= 11
                                                                    Kmeans, k= 7
Normalized cut
                      Kmeans, k= 3
                                              Kmeans, k= 5
                                                                                           Kmeans, k= 9
                                                                                                                 Kmeans, k= 11
Normalized cut
                      Kmeans, k= 3
                                              Kmeans, k= 5
                                                                    Kmeans, k= 7
                                                                                           Kmeans, k= 9
                                                                                                                 Kmeans, k= 11
Normalized cut
                                                                    Kmeans, k= 7
                                                                                           Kmeans, k= 9
                      Kmeans, k= 3
                                              Kmeans, k= 5
                                                                                                                 Kmeans, k= 11
Normalized cut
                      Kmeans, k= 3
                                              Kmeans, k= 5
                                                                    Kmeans, k= 7
                                                                                           Kmeans, k= 9
                                                                                                                 Kmeans, k= 11
```

5. Extra

A function used to bring the x, y coordinates for every point in the image and calculate the k means for this image after modification (adding x, y to it)

```
[ ] import cv2
     def kmeans_xy(image_num):
      image = cv2.imread('_/content/gdrive/MyDrive/assigm2_data/test/test'+str(image_num)+'.jpg')
       image=np.array(image)
       rows=image.shape[0]
      col=image.shape[1]
      x=[]
      y=[]
       for i in range (rows):
        for j in range(col):
    x.append(i)
          y.append(j)
       x= np.array(x).reshape(rows*col,1)
       y=np.array(y).reshape(rows*col,1)
       image = image.reshape(rows*col,3)
      image = np.append(image,x,axis = 1)
image = np.append(image,y,axis = 1)
       image=image.reshape(rows*col,5)
       for k in range(3,12,2):
        result=k_means(image,k)
         result = result.reshape(rows,col)
         mpimg.imsave('/content/gdrive/MyDrive/assigm2\_data/kmeans\_xy/img'+str(image\_num)+'\_k='+str(k)+'.jpg', result)
    import numpy as np
     kmeans_xy(2)
     kmeans_xy(3)
     kmeans_xy(4)
     kmeans xv(20)
    kmeans_xy(48)
```

A function used to plot the resulted images with the ground truth for 5 selected images





project on google colabDrive having all the results