

Theory of Computations

Assignment 1

Regular Expressions

1. Construct a regular expression for all words in which 'a' appears tripled, if at all. This means that every clump of a's contains 3 or 6 or 9 or 12... a's.
2. Construct a regular expression for all words that contain at least one of the strings s1, s2, s3, or s4.
3. Construct a regular expression for all strings that have exactly one double letter in them.
Note: 'exactly one double letter' implies two equal touching letters; triples etc are excluded.
4. Construct a regular expression for all strings in which the letter b is never tripled. This means that no word contains the substring bbb.
Note: Words can be empty and start and end with a or b. A compulsory 'a' is inserted between all repetitions of b's.
5. Construct a regular expression for:
 - (ii) all words that do not have both the substrings bba and abb.
6. Construct a regular expression for:
 - all strings in which any b's that occur are found in clumps of an odd number at a time, such as abaabbbab.
 - all strings that have an even number of a's and an odd number of b's.
 - all strings that have an odd number of a's and an odd number of b's.
7. State whether each pair of regular expressions are equivalent or not.
 - (a^*b^*) and $(ab)^*$
 - $(ab) a^*$ and $a(ba)^*$
 - $(a^* + b)^*$ and $(a + b)^*$
 - $(a^* + b^*)^*$ and $(a + b)^*$
8. Describe in English the languages represented by the following RE:
 - $(a(a + bb)^*)^*$
 - $(b(bb)^*)^*(a(aa)^*b(bb)^*)^*$
 - $((a+b)a)^*$
9. Describe in English phrases the languages associated with the following regular expression:
 - $baa + abbb + bababa$
 - $a(a + bb)^*$
 - $(a(aa)^*b(bb)^*)^*$
 - $(b(bb)^*)^*(a(aa)^*b(bb)^*)^*$
 - $((a + bb)a)^*$

- $(a + b)^*(aa + bb)(a + b)^*$
- $(a + b)^*a(\wedge + bbbb)$

Submission :

- **Deadline is Thursday 8-April @11:59PM**
- **The assignment is individual.**
- **Cheating could lead to serious consequences.**