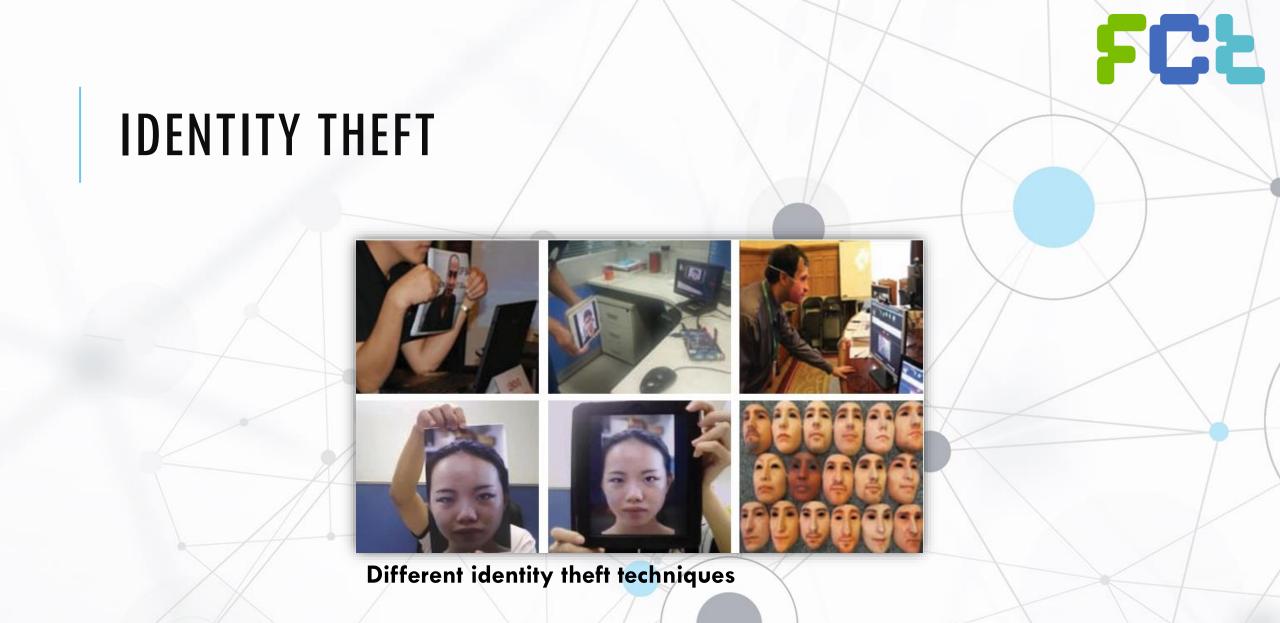


# AN EMPITICAL EVALUATION OF GENERIC CONVOLUTIONAL AND RECURRENT NETWORKS FOR SEQUENCE MODELING

Nova Search Reading Group — June 4th 2020 Ruslan Padnevych

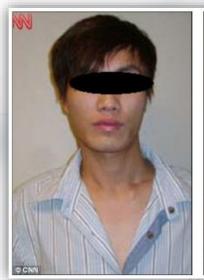
Shaojie Bai, J. Zico Kolter and Vladlen Koltun. April 2018

https://arxiv.org/pdf/1803.01271.pdf





# IDENTITY THEFT (CONT.)





In 2011, a passenger boarded the plane in Hong Kong wearing an elderly man's mask and successfully landed in Canada.

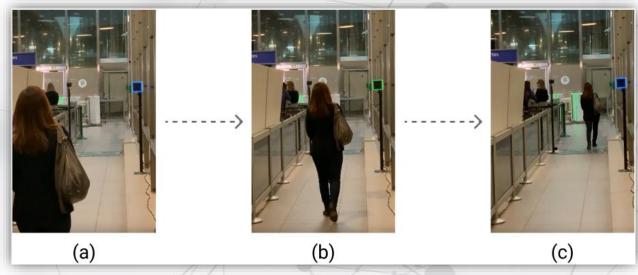
#### Photos taken from Google





### CONTEXT: BORDERS WITHOUT BARRIERS

#### Use case



Biometrics on the Move (SmartyFlow project)

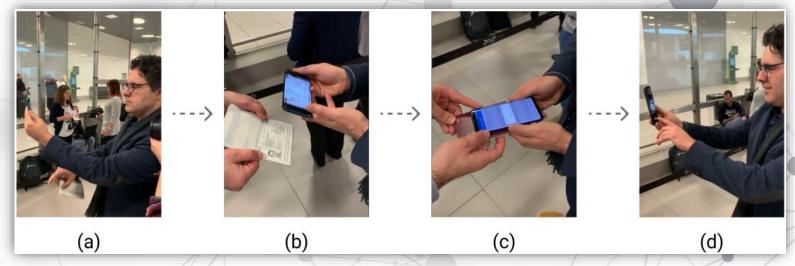


Queues to show documents to border guards



### CONTEXT: BORDERS WITHOUT BARRIERS

#### **Registration Phase**

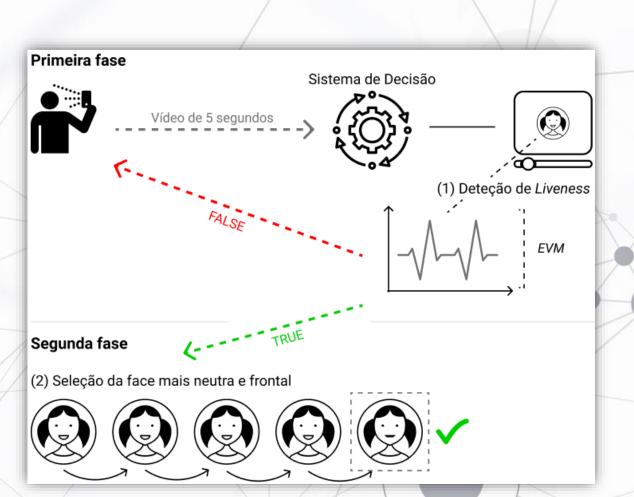


- (a) → liveliness detection (5s video)
- (b) passport registration
- (c) reading the passport chip
- (d) verification of correspondence

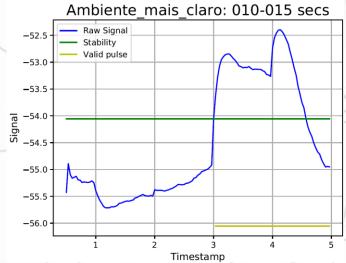
### GOAL

Liveliness detection

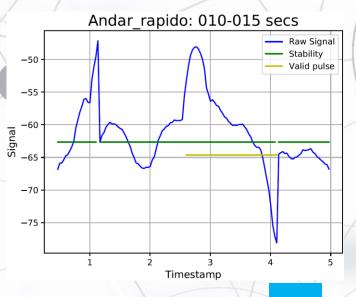
Neutral face selection



#### Fake



#### Real





#### SEQUENCE MODELING

- Suppose that we are given an input sequence x0, ...., xT, and wish to predict some corresponding outputs y0, ...., yT at each time.
- The key constraint is that to predict the output yt for some time t, we are constrained to only use those inputs that have been previously observed: x0, ...., xt.
- \* Formally, a sequence modeling network is any function:

$$f: \mathcal{X}^{T+1} 
ightarrow \mid \mathcal{Y}^{T+1} \mid$$

$$f: \mathcal{X}^{T+1} o \mathcal{Y}^{T+1}$$
 that produces the mapping  $\hat{y}_0, \dots, \hat{y}_T = f(x_0, \dots, x_T)$ 

yt depends only on x0, ....., xt and not on any "future" inputs xt+1, ....., xT



# SEQUENCE MODELING (CONT.)

The goal of learning in the sequence modeling setting is to find a network f that minimizes some expected loss between the actual outputs and the predictions,

L(y0, ...., yT; f(x0, ...., xT)),

where the sequences and outputs are drawn according to some distribution.



#### BACKGROUND

#### **Convolutional Networks**

- Used prominently for speech recognition in the 80s and 90s
- Applied to NLP tasks such as part-of-speech tagging and semantic role labelling
- Applied to sentence and document classification
- More recently, applied to language modeling and machine translation

#### **Recurrent Networks**

Gained tremendous popularity due to prominent applications to language modeling and machine translation



Should Recurrent Networks be regarded as a natural starting point for sequence modeling tasks?



### RECURRENT NETWORK (RNN)

- RNN is a class of artificial neural networks where connections between nodes form a directed graph along a temporal sequence (Rumelhart, 1988).
- Unlike feedforward neural networks, RNNs contain cycles and use an internal state memory h to process sequences of inputs.
- \* A basic recurrent neural network is described by the propagation equations:

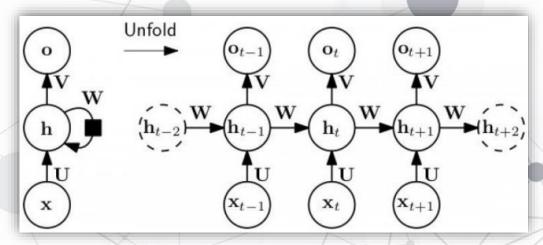
$$egin{aligned} \mathbf{h}_t &= \sigma(\mathbf{U} \cdot \mathbf{x}_t + \mathbf{W} \cdot \mathbf{h}_{t-1} + \mathbf{b}) \ \mathbf{o}_t &= \mathbf{V} \cdot \mathbf{h}_t + \mathbf{c} \end{aligned}$$

- ❖ Where the parameters are the bias vectors **b** and **c** along with the weight matrices:
- ❖ **U** input-to-hidden
- ❖ **V** hidden-to-output
- ❖ W hidden-to-hidden



# RNN (CONT.)

\* The computational graph and its unfolded version is shown in the following figure:



- Weight matrices:
- ❖ **U** input-to-hidden
- ❖ **V** hidden-to-output
- ❖ W hidden-to-hidden

- \*Computing the gradients involves performing a forward propagation pass through the unrolled graph followed by a backward propagation pass.
- The runtime is O(T) and cannot be reduced by parallelization because the forward propagation graph is inherently sequential, i.e., each time step may be computed only after the previous one.



# RNN (CONT.)

- Recurrent models construct very deep computational graphs by repeatedly applying the same operation at each time step of a long temporal sequence. This gives rise to the vanishing gradient problem and makes it notoriously difficult to train RNNs.
- To prevent these difficulties more elaborate recurrent architectures were developed, such as the long short-term memory (LSTM) (Hochreiter, 1997) and the gated recurrent unit (GRU) (Cho, 2014).



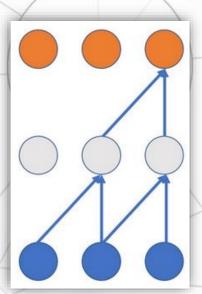
# TEMPORAL CONVOLUTIONAL NETWORK (TCN)

- TCN is inspired by recent convolutional architectures for sequential data and combines simplicity, <u>autoregressive prediction</u>, and very long memory.
- The distinguishing characteristics of TCNs are:
  - 1) The **convolutions in the architecture are causal,** meaning that there is no information "leakage" from future to past.
- 2) The architecture can take a sequence of any length and map it to an output sequence of the same length, just as with an RNN.



# TCN — CAUSAL CONVOLUTIONS

1) TCN uses **causal convolutions**, i.e., convolutions where an output at time t is convolved only with elements from time t and earlier in the previous layer.



2) TCN uses a 1D fully-convolutional network (FCN) architecture, where each hidden layer is the same length as the input layer.

TCN = 1D FCN + causal convolutions



### TCN (CONT.)

A major disadvantage of this basic design is that in order to achieve a long effective history size, we need an extremely deep network or very large filters.



### TCN — DILATED CONVOLUTIONS

A simple causal convolution is only able to look back at a history with size linear in the depth of the network.



To employ dilated convolutions that enable an exponentially large receptive field.

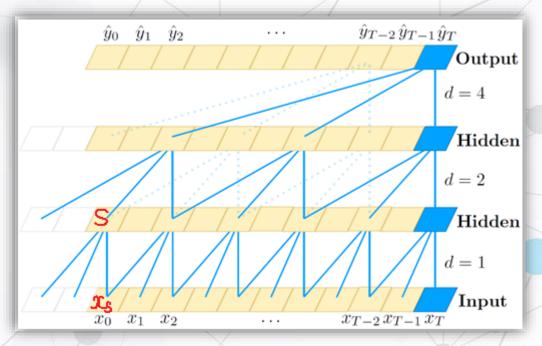




### TCN — DILATED CONVOLUTIONS

Given a 1-D sequence input  $x \in R^n$  and a filter  $f : \{f0, ...., k-1\} \rightarrow R$ , the dilated convolution

operation F on element s of the sequence is defined as:



$$F(s) = (\mathbf{x} *_d f)(s) = \sum_{i=0}^{\kappa-1} f(i) \cdot \mathbf{x}_{s-d \cdot i}$$

 $d = 2^{v}$  – dilation factor, with v the level of the network

k – filter size

(s - d\*i) - direction of the past

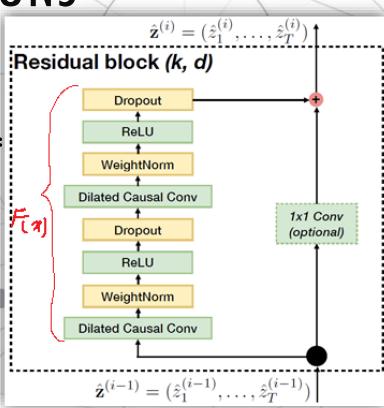


# TCN — RESIDUAL (BLOCKS) CONNECTIONS

A residual block contains a branch leading out to a series of transformations F, whose outputs are added to the input x of the block:

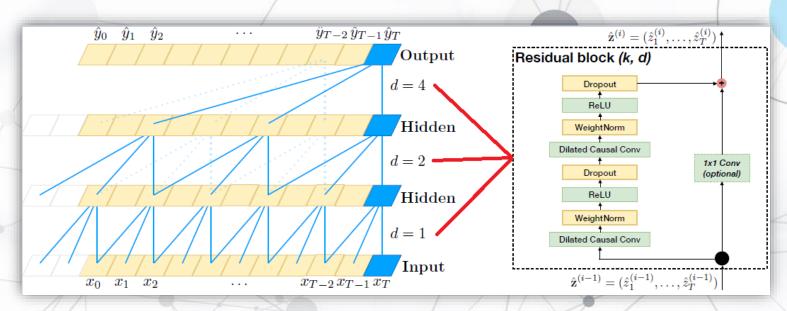
$$o = Activation(\mathbf{x} + \mathcal{F}(\mathbf{x}))$$

This effectively allows layers to learn modifications to the identity mapping x rather than the entire transformation F(x), which has repeatedly been shown to benefit very deep networks.





# TCN — RESIDUAL (BLOCKS) CONNECTIONS (CONT.)



- \* Normalization: applied weight normalization to the convolutional filters.
- \* Regularization: a spatial dropout was added after each dilated convolution and at each training step, a whole channel is zeroed out.
- An 1x1 convolution is added when residual input and output have different dimensions.



#### TCN — SUMMARY

A simple temporal convolutional network (TCN) that combines best practices such as dilations and residual connections with the causal convolutions needed for autoregressive prediction.



#### TCN HYPERPARAMETERS SETTING

	TCN SETTINGS						
Dataset/Task	Subtask	k	n	Hidden	Dropout	Grad Clip	Note
	T = 200	6	7	27			
The Adding Problem	T = 400	7	7	27	0.0	N/A	
	T = 600	8	8	24			
Seq. MNIST	_	7	8	25	0.0	N/A	
ocq. MINIST		6	8	20	0.0	IVA	
Permuted MNIST	_	7	8	25	0.0	N/A	
Termuted WINDT		6	8	20			
	T = 500	6	9	10		1.0	
Copy Memory Task	T = 1000	8	8	10	0.05		RMSprop 5e-4
	T = 2000	8	9	10			
Music JSB Chorales	-	3	2	150	0.5	0.4	
Music Nottingham	•	6	4	150	0.2	0.4	
	PTB	3	4	600	0.5		Embed. size 600
Word-level LM	Wiki-103	3	5	1000	0.4	0.4	Embed. size 400
	LAMBADA	4	5	500	0.4		Embed. size 500
Char-level LM	PTB	3	3	450	0.1	0.15	Embed, size 100
Chai level Elvi	text8	2	5	520	0.1	0.15	Ellibed, Size 100

- $\diamond$  The most important factor for picking parameters is to make sure that the TCN has a sufficiently large receptive field by choosing k and d that can cover the amount of context needed for the task.
- $\diamond$  There are two ways to increase the receptive field of a TCN: choosing lager filter sizes k and increasing the dilation factor d, since the effective history of one layer is (k-1)\*d.



### **RESULTS**

<sup>h</sup> means that higher is better.

<sup>l</sup> means that lower is better.

	Model Size (≈)	Models					
Sequence Modeling Task		LSTM	GRU	RNN	TCN		
Seq. MNIST (accuracy <sup>h</sup> )	70K	87.2	96.2	21.5	99.0		
Permuted MNIST (accuracy)	70K	85.7	87.3	25.3	97.2		
Adding problem $T$ =600 (loss $^{\ell}$ )	70K	0.164	5.3e-5	0.177	5.8e-5		
Copy memory $T=1000 \text{ (loss)}$	16K	0.0204	0.0197	0.0202	3.5e-5		
Music JSB Chorales (loss)	300K	8.45	8.43	8.91	8.10		
Music Nottingham (loss)	1M	3.29	3.46	4.05	3.07		
Word-level PTB (perplexity <sup>ℓ</sup> )	13M	78.93	92.48	114.50	88.68		
Word-level Wiki-103 (perplexity)	-	48.4	-	_	45.19		
Word-level LAMBADA (perplexity)	-	4186	_	14725	1279		
Char-level PTB (bpc <sup>ℓ</sup> )	3M	1.36	1.37	1.48	1.31		
Char-level text8 (bpc)	5M	1.50	1.53	1.69	1.45		



**NOTE:** the **number of hidden units** was chosen so that the model size is approximately at the same level as the recurrent models with which we are comparing.

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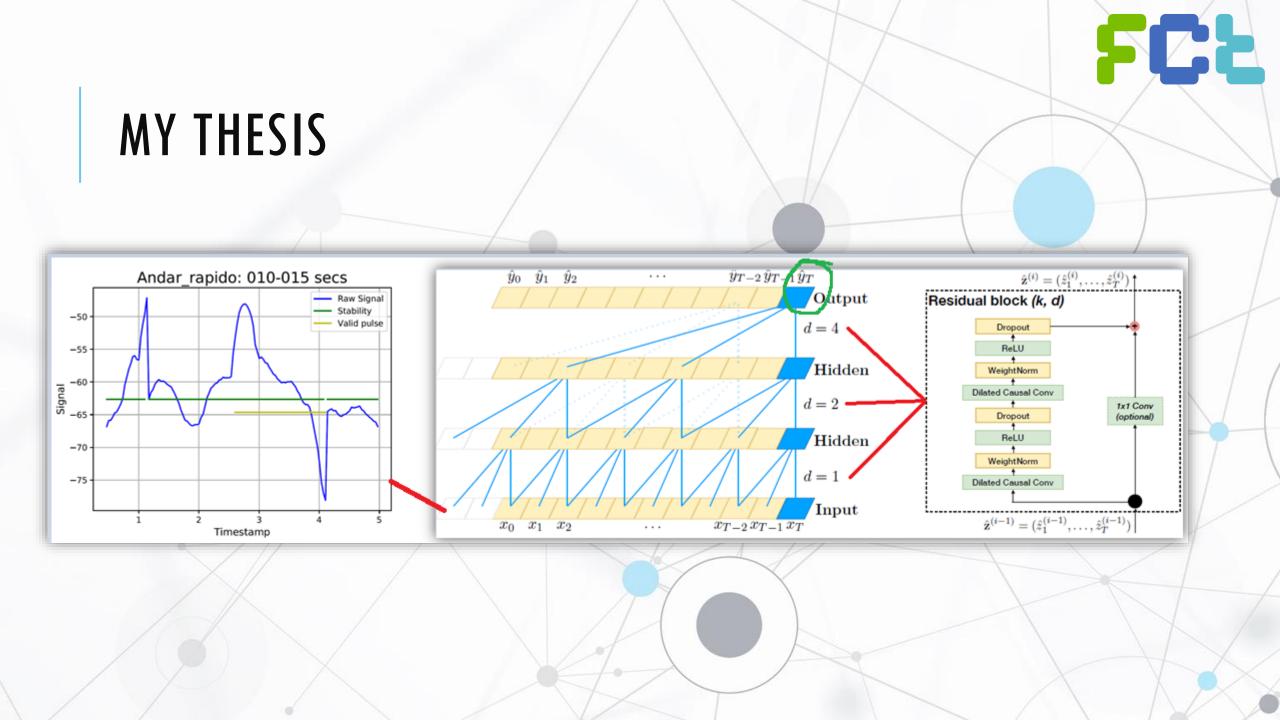
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					1		



- 1) "TCNs can be build to have very long effective history sizes, which means they have the ability to look very far into the past to make a prediction. To this end, a combination of very deep networks augmented with residual layers and dilated convolutions are deployed."
- 2) "Generic TCN architecture outperform canonical recurrent architectures across a broad variety of sequence modelling tasks that are commonly used to benchmark the performance of recurrent architectures."



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#### **Temporal Convolution Network - Liveness Detection**

