

A person is shown from the side, wearing 3D glasses and looking at a computer monitor. The monitor displays a yellow sports car. The person's hands are on a keyboard. The background is a light blue and white grid pattern.

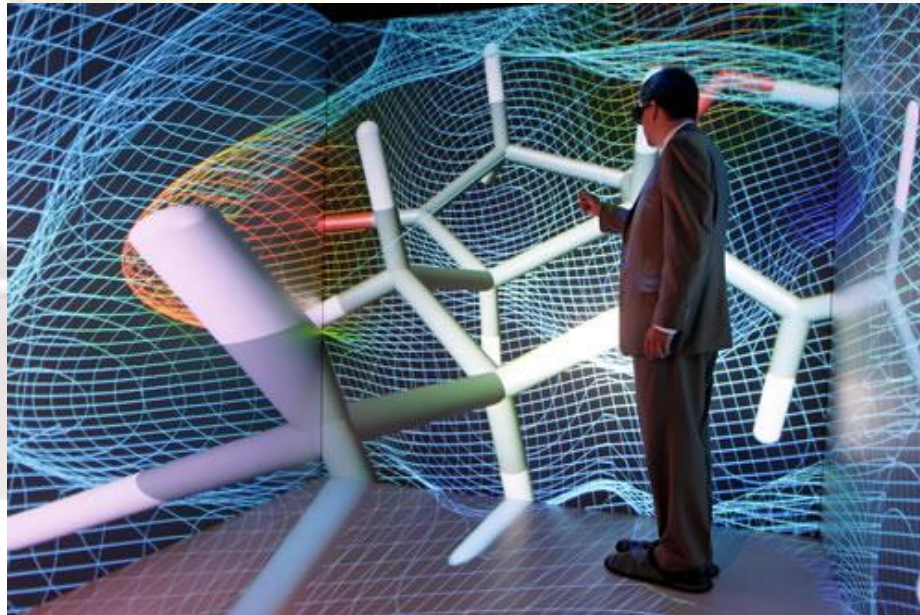
# ***STEREOSCOPY***

**Course 2024/2025**

# Motivation

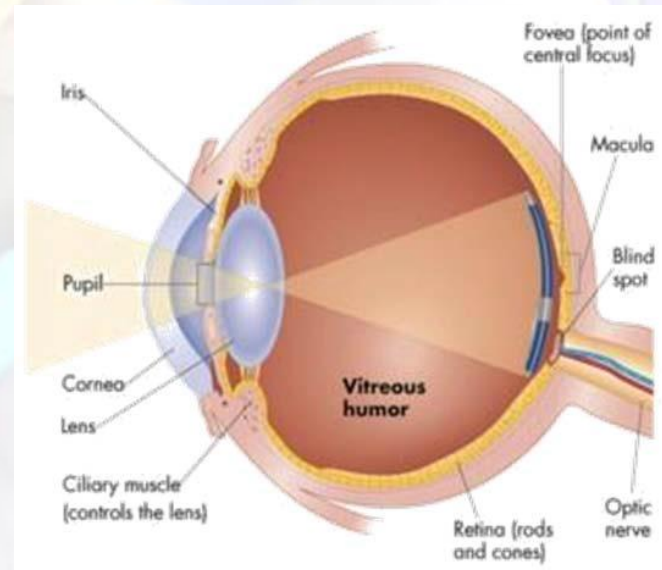
About stereoscopy

- One of the most important depth cues
- Key in all VR applications
- Influences both software and hardware
- Closely related to Human Visual System (HVS)



# Depth perception

- Our retinas only capture **planar images**
- But the HVS is able to recover depth information by combining multiple **depth cues**.
- Depth cues = image features that help the HVS obtain depth information.

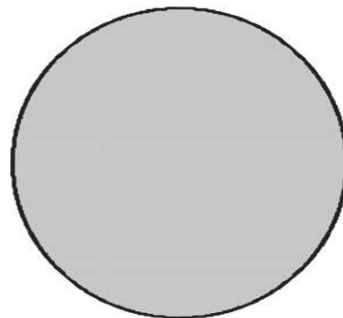
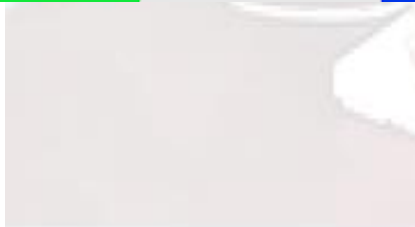
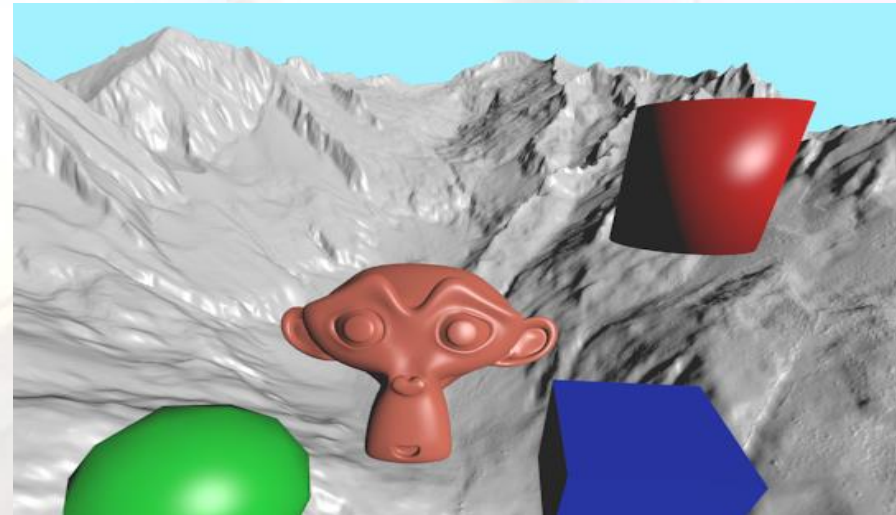
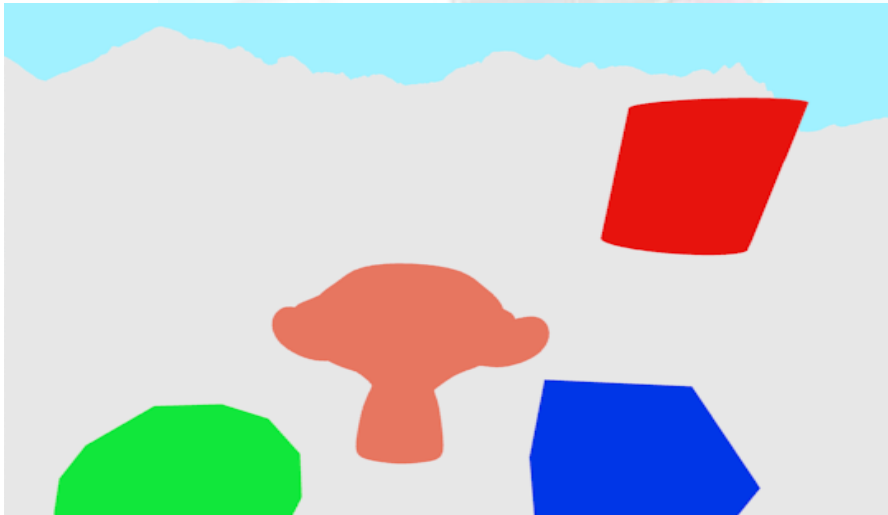


# Depth cues

- In the real-world, all depth cues agree.
- In VR, some depth cues might disagree!
- Depth cue classification
  - Monocular
    - Shading, Shadows, Relative size, Perspective, Texture gradient, Atmospheric perspective, Motion parallax, Occlusion, Accommodation
  - Binocular
    - Convergence, retinal disparity

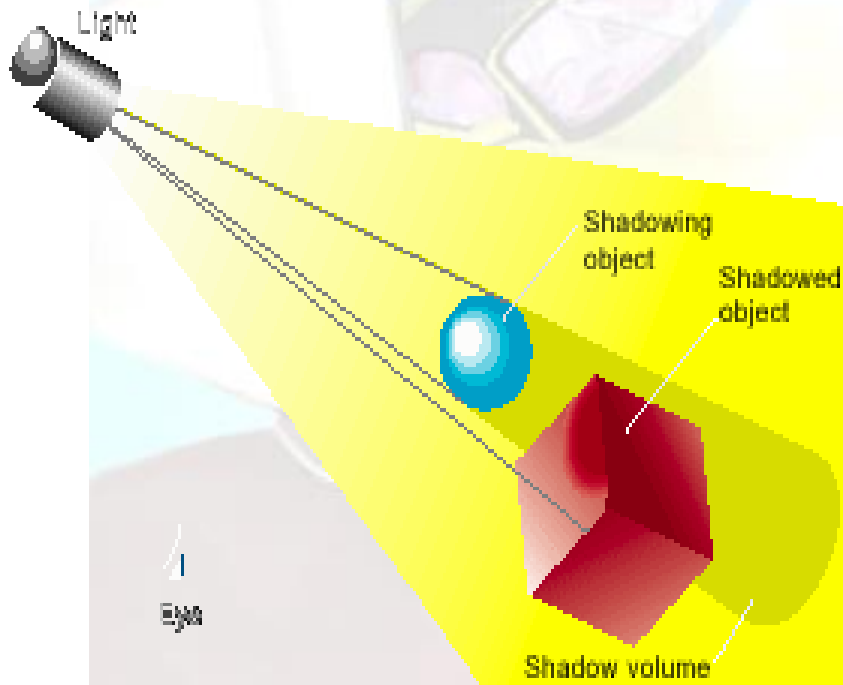
# Shading / lighting

Shading provides shape and depth information because it largely depends on the surface orientation



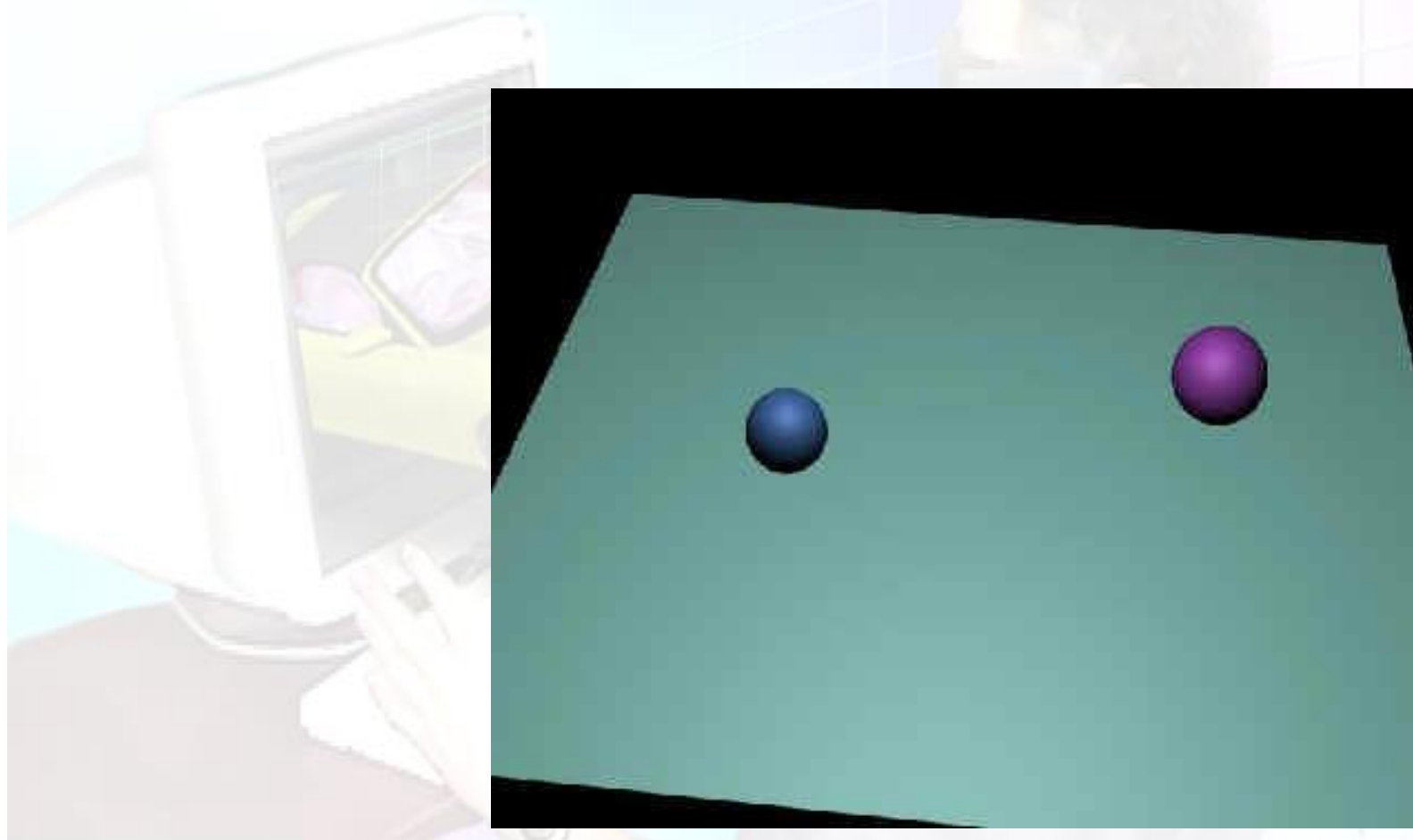
# Shadows

Shadows cast by objects play an important role in depth perception

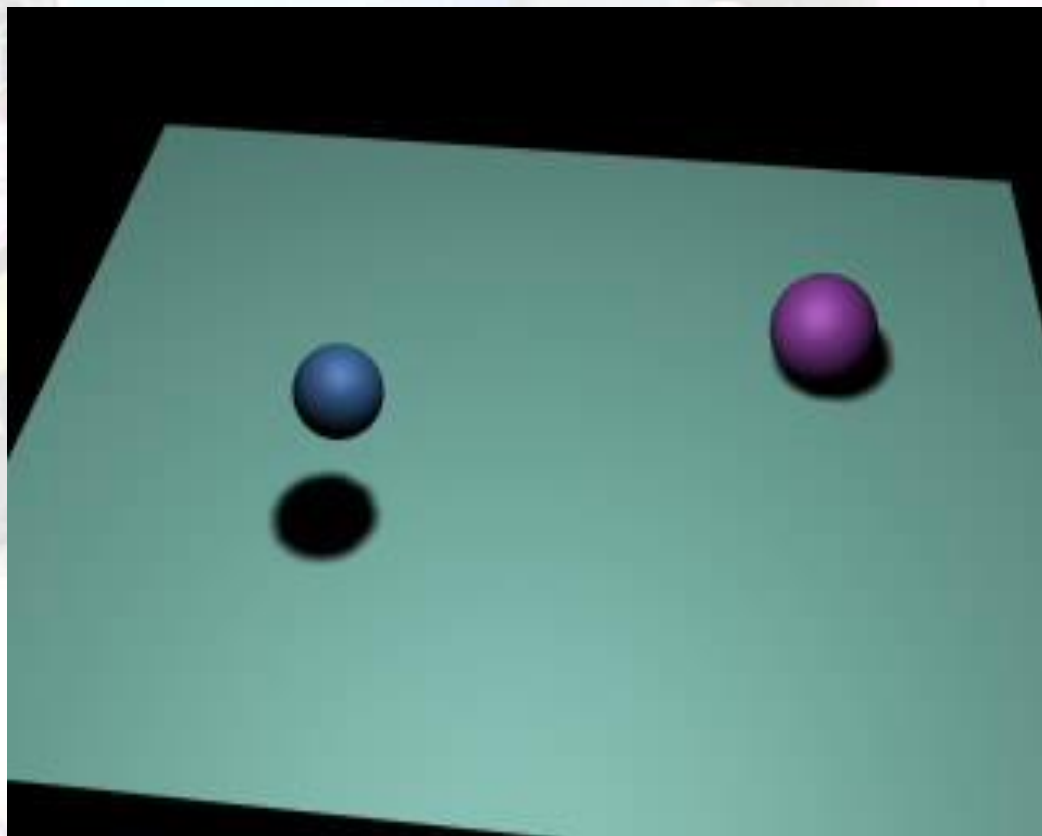




# Shadows



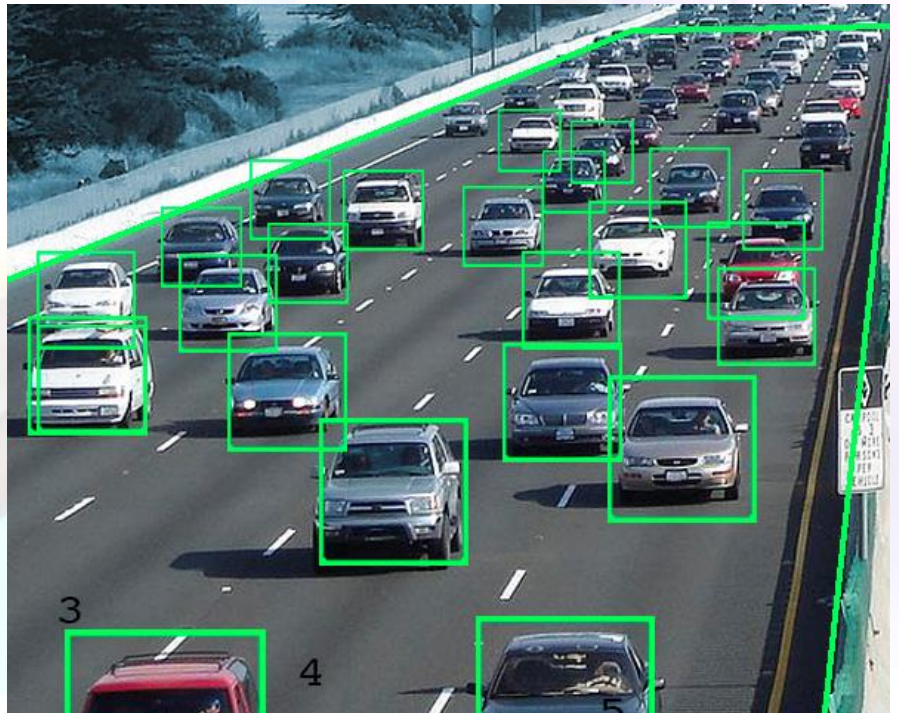
# Shadows





# Retinal image size

The visual system exploits the relative size of familiar objects to judge distance.



# Perspective (linear perspective)

- As objects become more distant, they appear smaller because their visual angle decreases.
- Parallel lines appear to be meeting at a distant point (the vanishing point) on the horizon.





# Texture gradient

The further apart an object, the higher the spatial frequency of its texture



# Atmospheric perspective (fog)

Objects that are a great distance away look hazier due to light scattering by the atmosphere

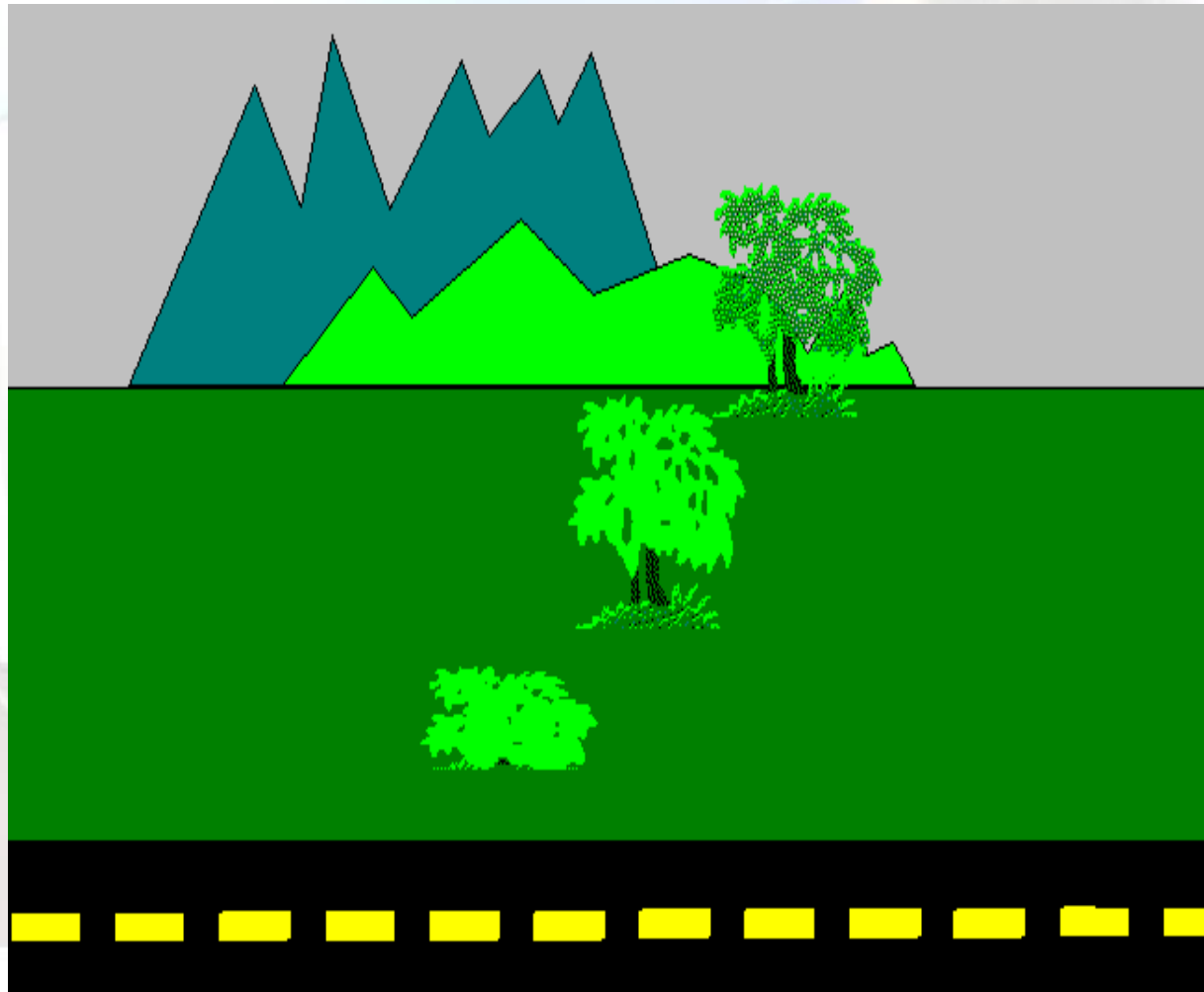




# Atmospheric perspective (fog)



# Motion parallax



# Occlusion (interposition)

Objects that block other objects appear to be closer.





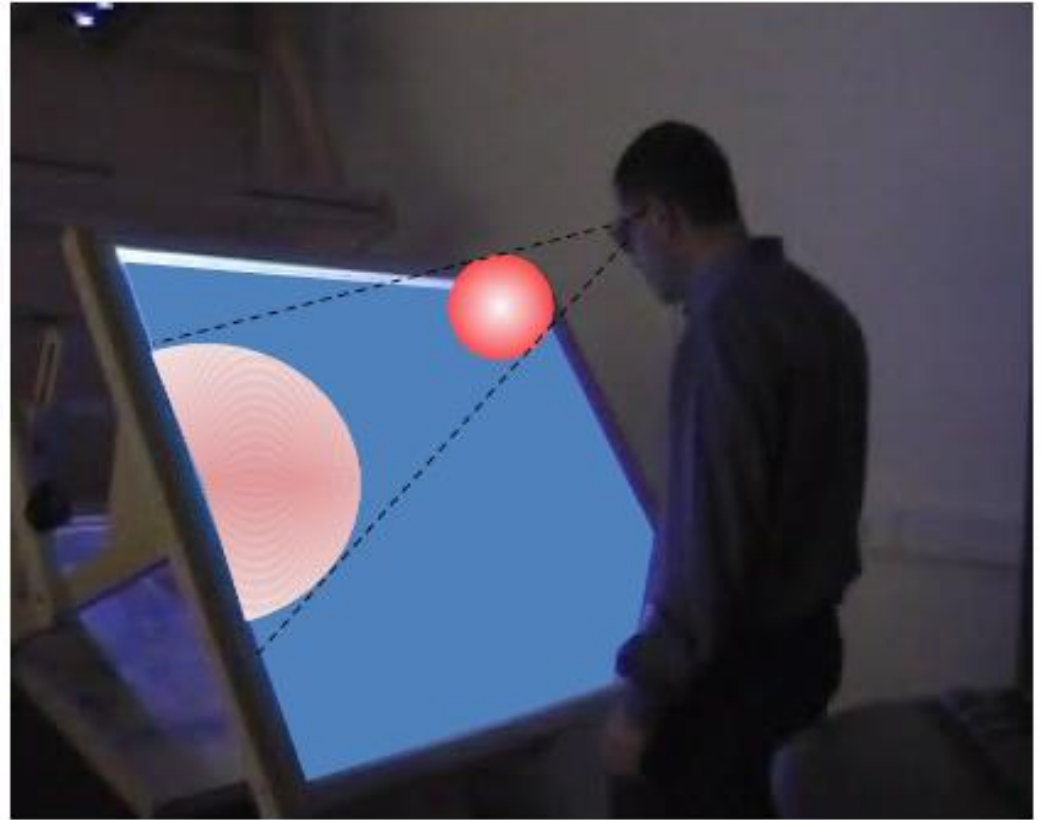
# Occlusion – screen surround



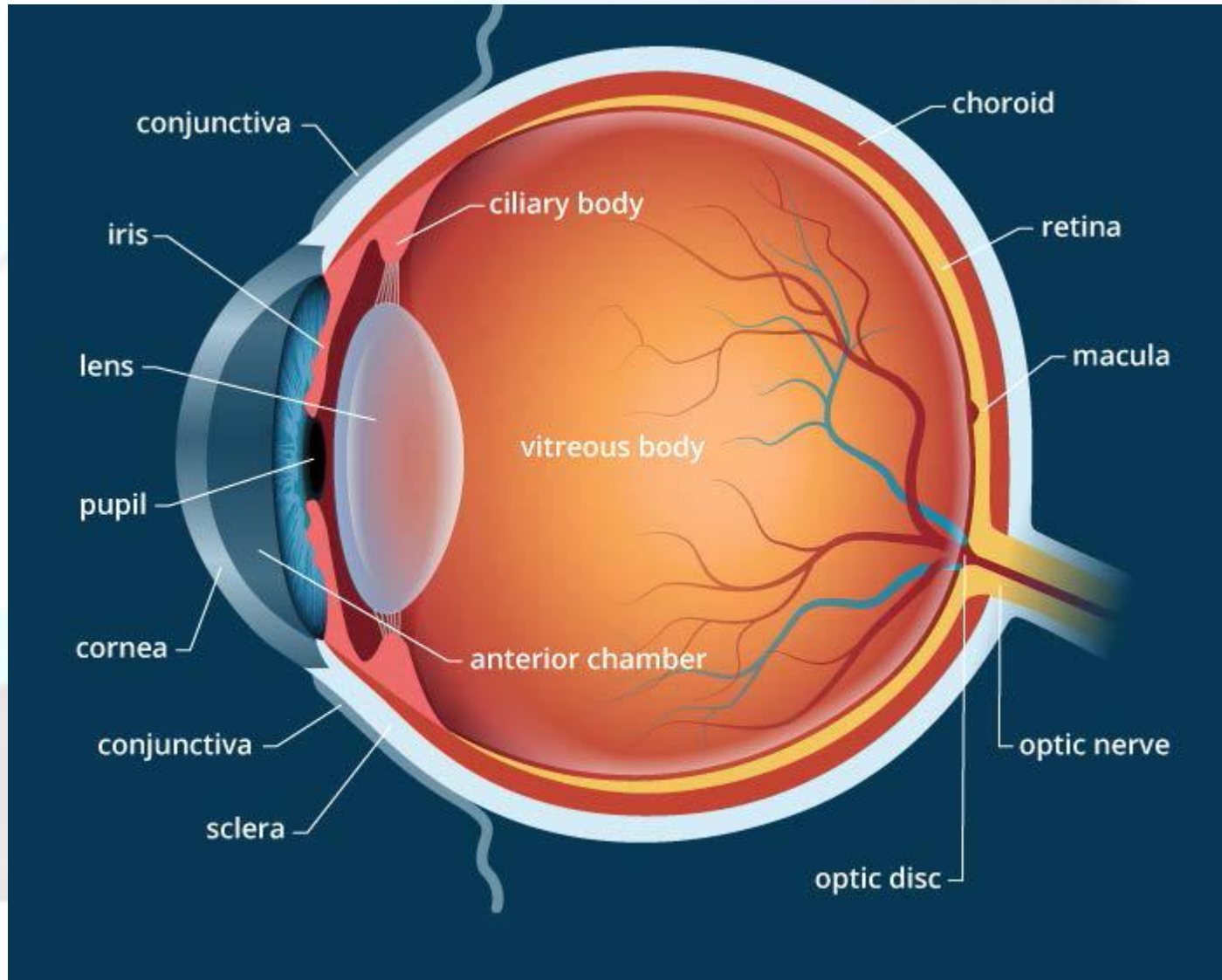
# Occlusion – screen surround



# Occlusion – screen surround

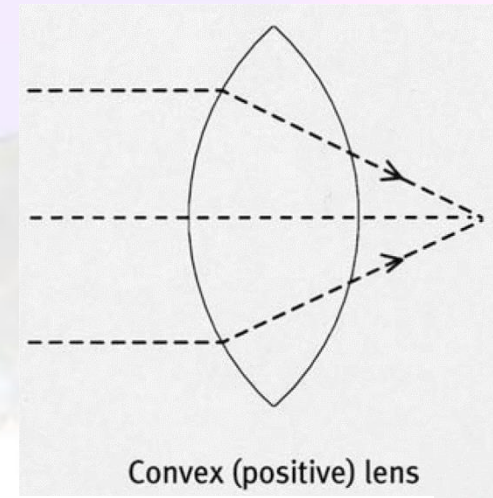


# Human eye

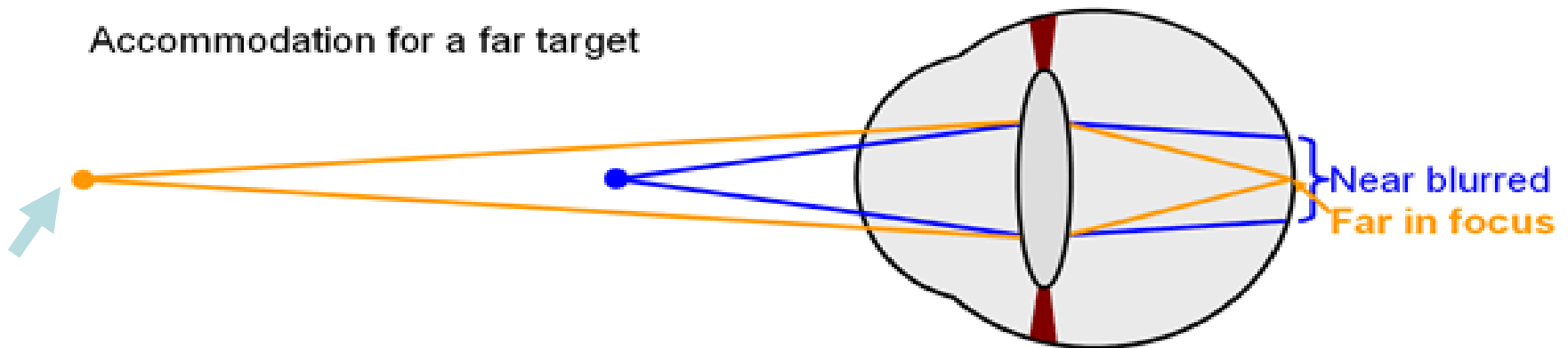


# Accommodation

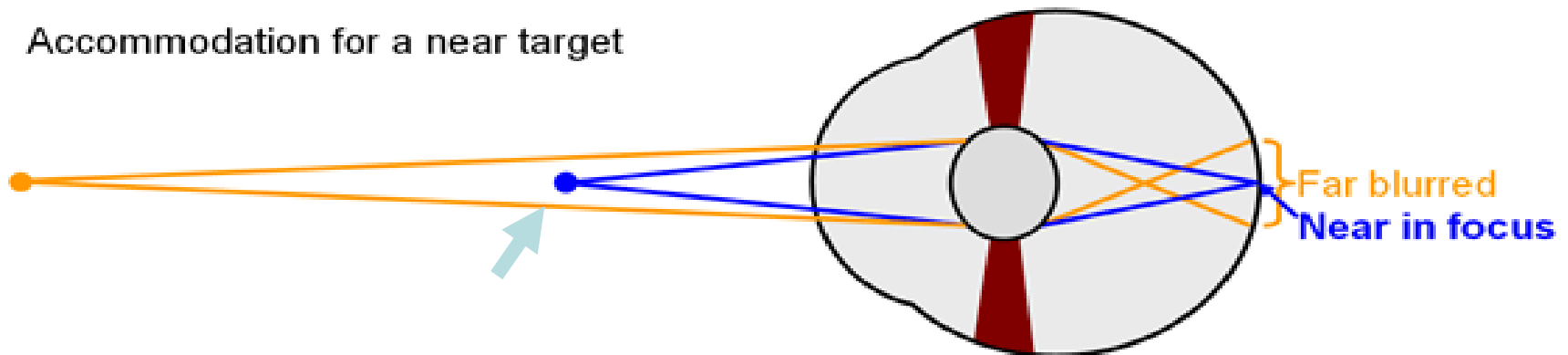
- **Deformation of the eye lens (*cristalino*)**
- Allows to **focus objects** at some distance



Accommodation for a far target

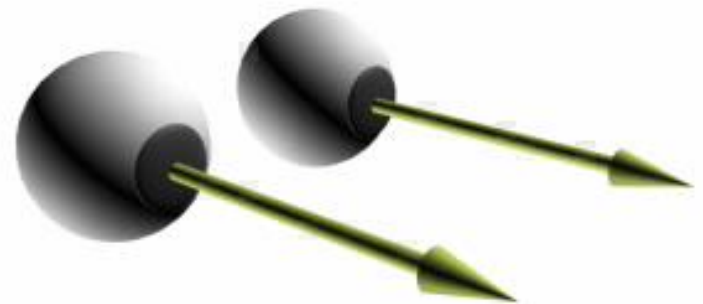
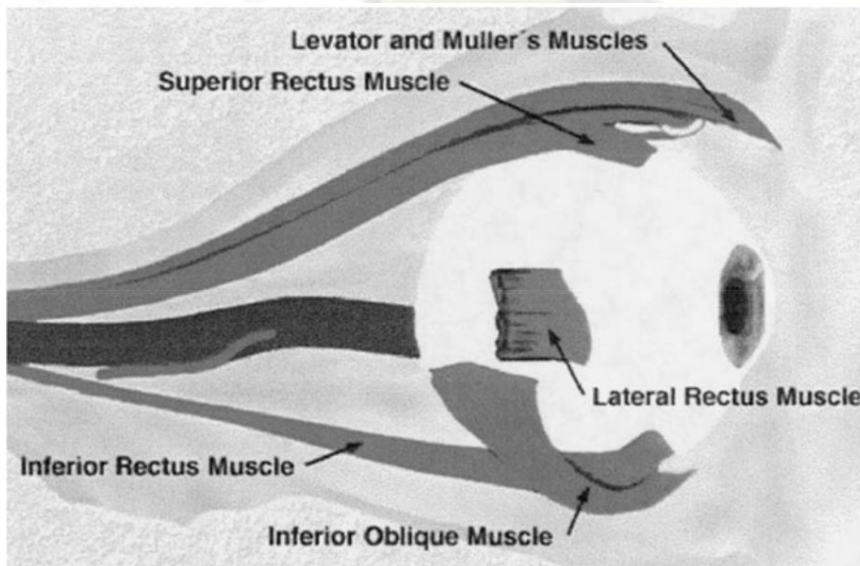
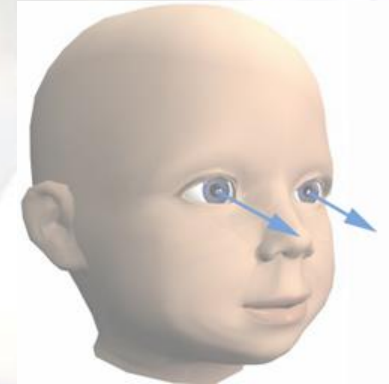


Accommodation for a near target



# Convergence

- **Rotation of the eye balls**
- Allows to **center the object we are looking at on the fovea.**

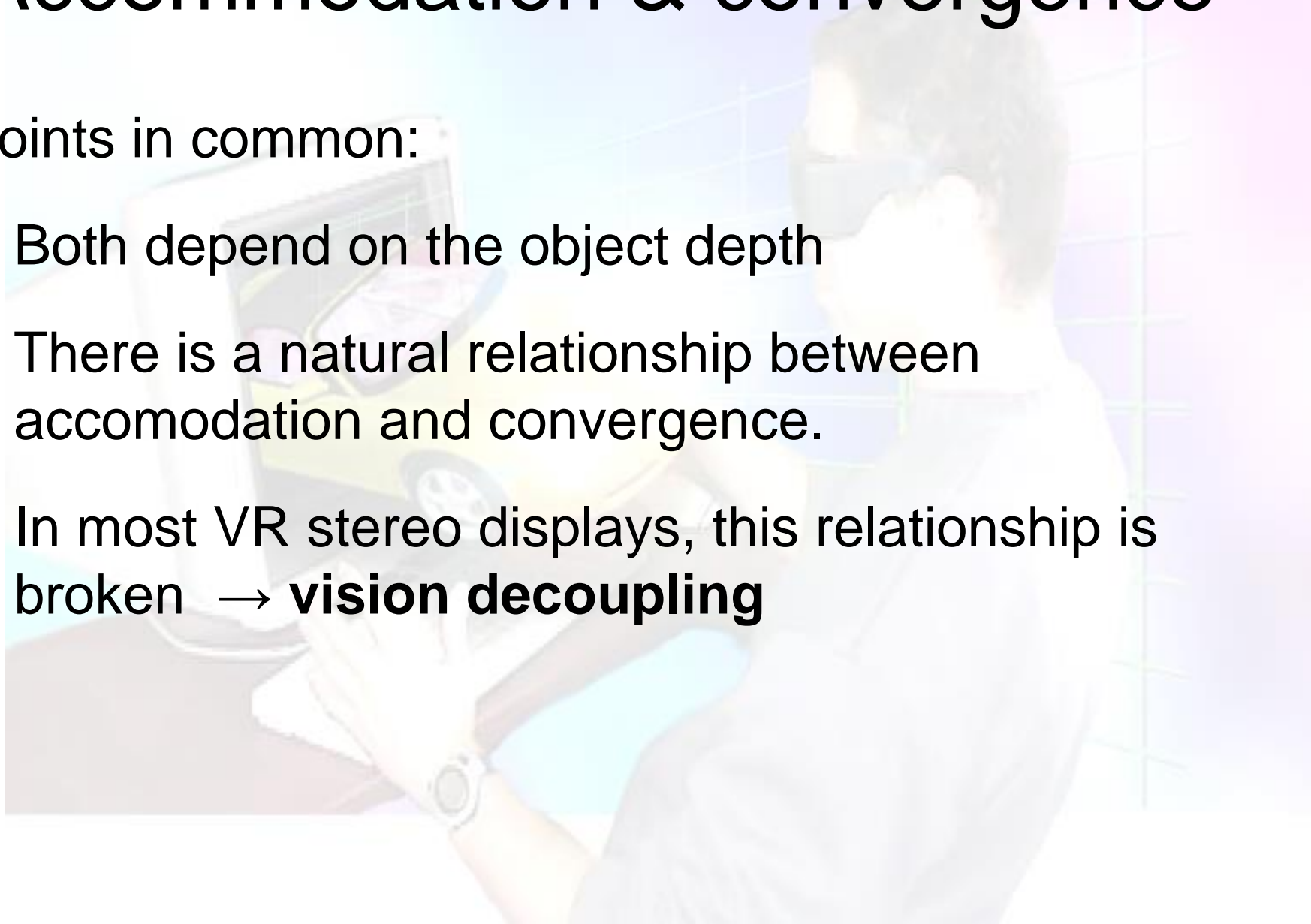




# Accommodation & convergence

Points in common:

- Both depend on the object depth
- There is a natural relationship between accommodation and convergence.
- In most VR stereo displays, this relationship is broken → **vision decoupling**



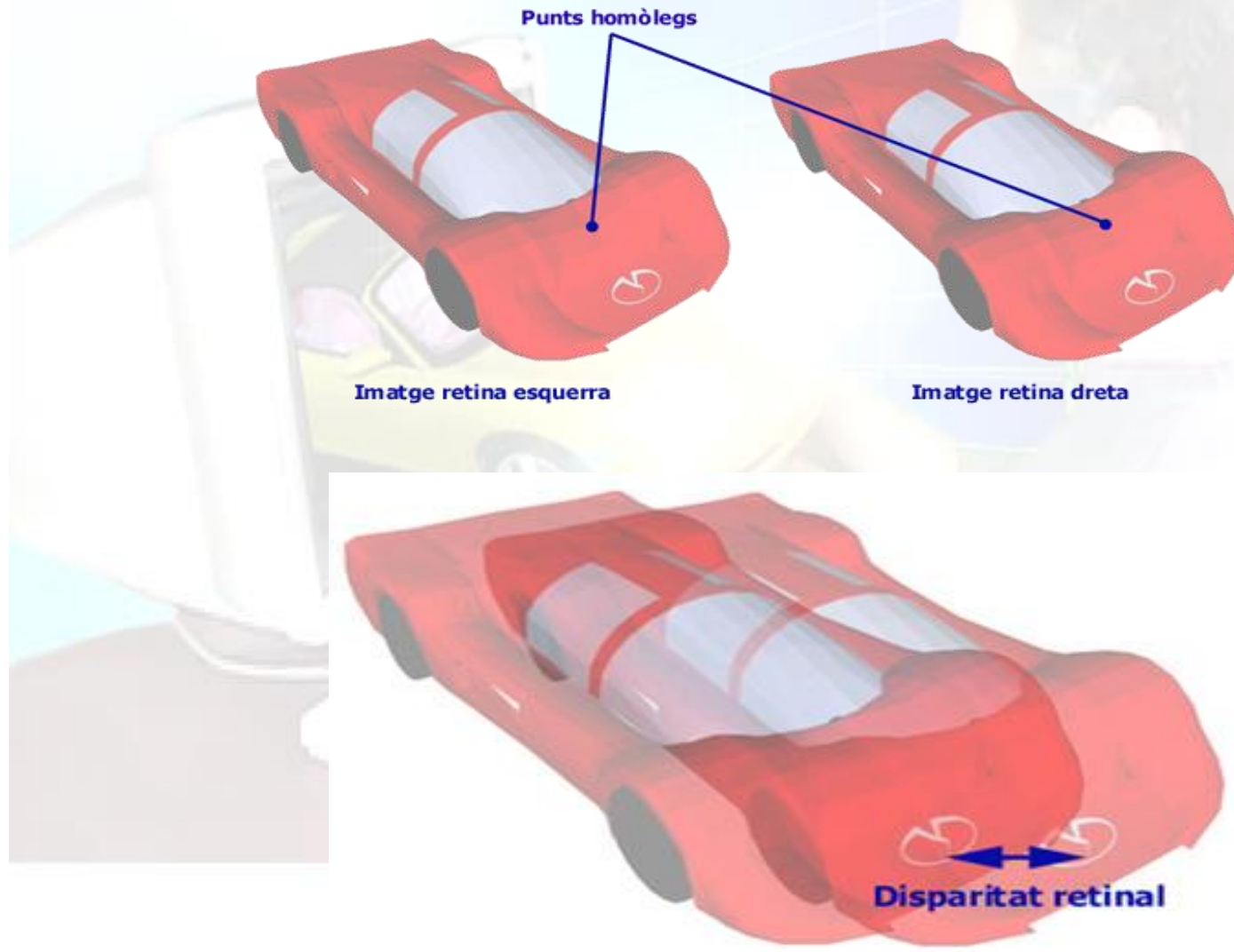


# Retinal disparity

Difference in the L/R images of an object due to the eyes' horizontal separation



# Retinal disparity (informally)



# Fusion and stereopsis

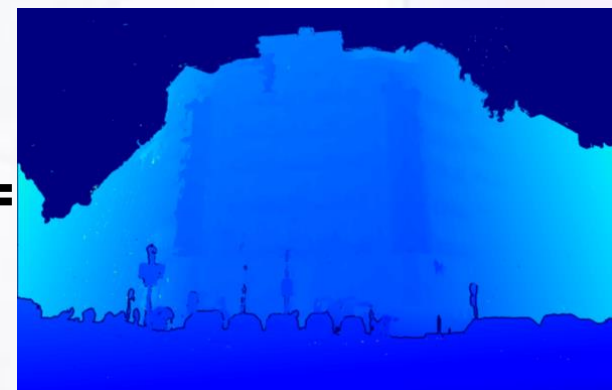
- The human brain is able to **combine two images with disparity into a single image with depth.**
- This ability is called **fusion** and the resulting sense is called **stereopsis.**



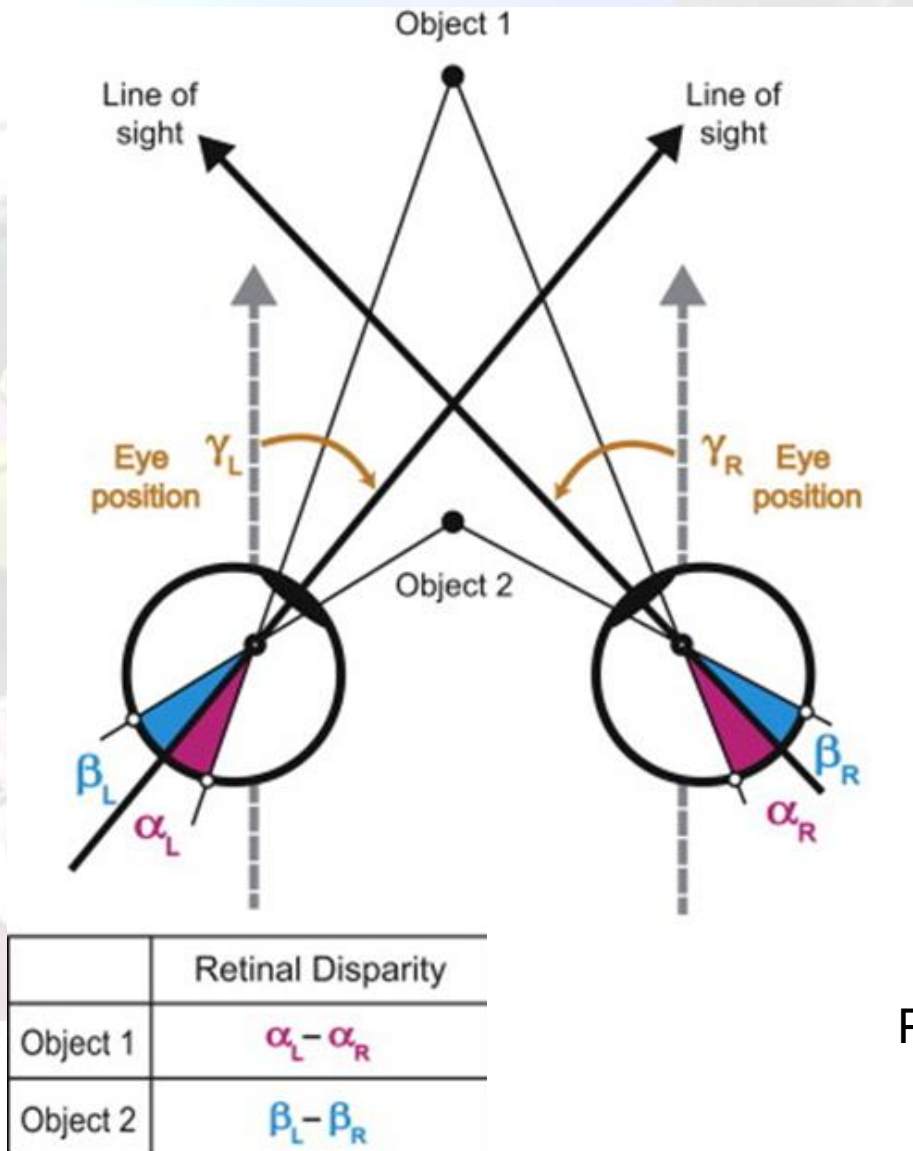
+



=



# Retinal disparity (more formally)

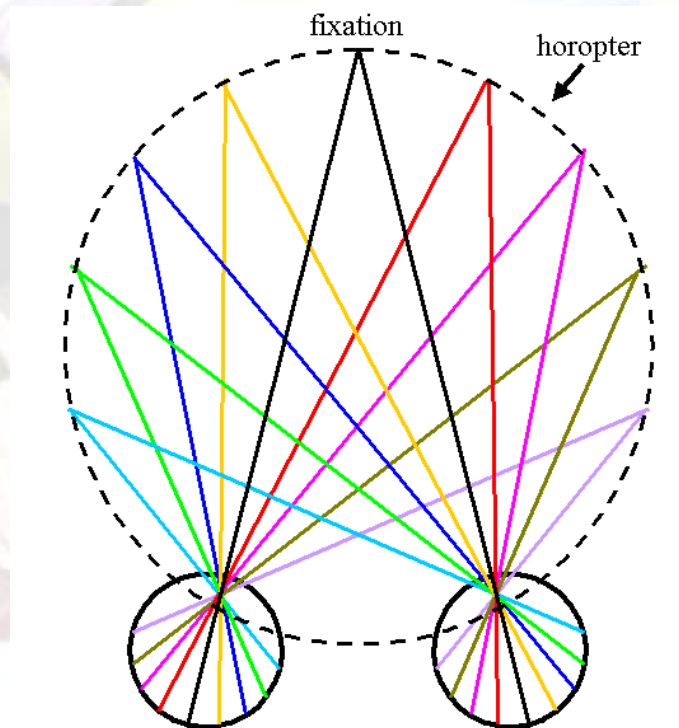


Positive angles



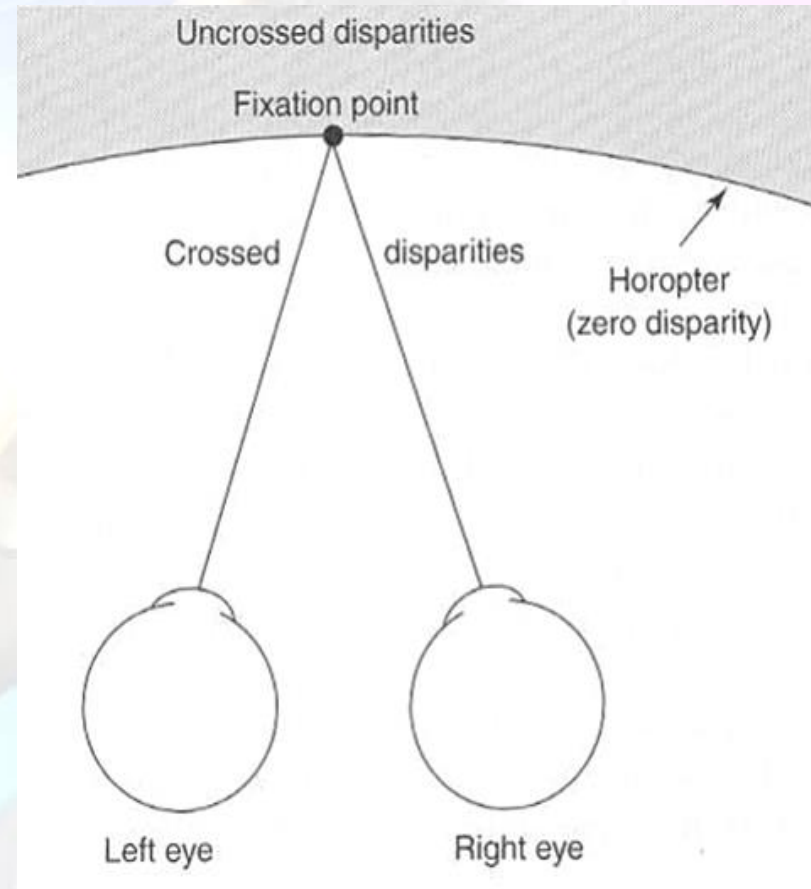
# Retinal disparity (more formally)

**Horopter:** surface of points in space that, for a given convergence, are projected onto points with **no disparity**



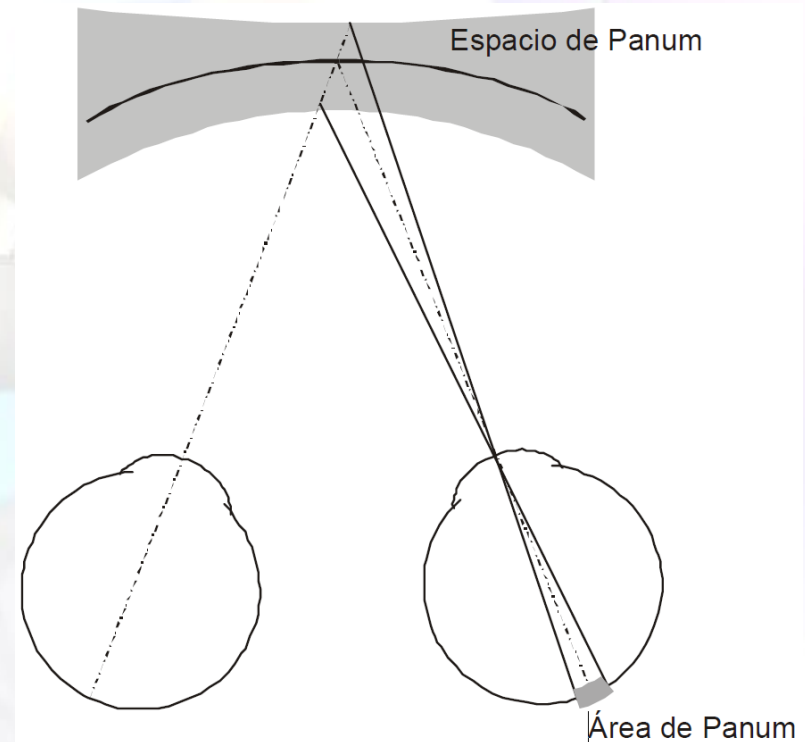
# Retinal disparity (more formally)

- **Points closer** than the Horopter have **crossed disparity** (negative disparity)
- **Points farther** than the Horopter have **uncrossed disparity** (positive disparity)



# Retinal disparity (more formally)

- **Panum's fusion area:** Space surrounding the horopter where fusion is feasible.
- **Within Panum's fusion area** points might have **non-zero disparity** but they can be fused (resulting in a single image with depth).
- **Outside Panum's fusion area** points have a **large disparity** and fusion fails, producing double images (diplopia).
- Near the fovea, the maximum binocular disparity resulting in fusion corresponds to a visual angle of about 10 minutes of arc (**1/6 of one degree**).





# Retinal disparity

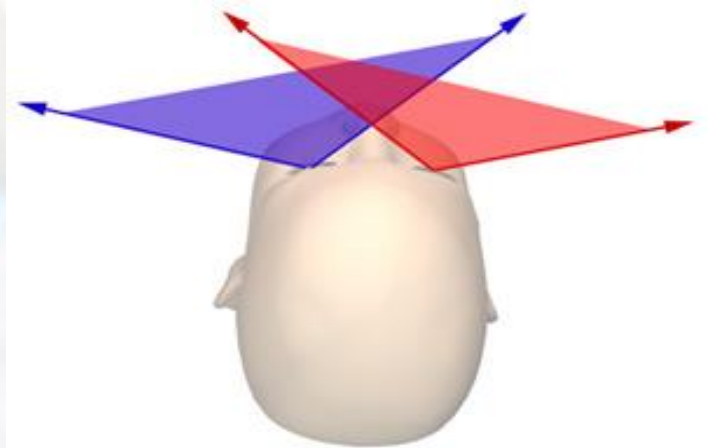
Remember:

- Every scene point has its own retinal disparity.
- If we change fixation point, we change retinal disparity!



# Human eye fact sheet

- IOD (interocular or interpupillary distance): 5 - 7.5 cm
- Average IOD: 6.3 – 6.6 cm
- Eye field-of-view:  $160^{\circ}$ - $180^{\circ}$  hor x  $130^{\circ}$  vert
- Horizontal overlap:  $140^{\circ}$



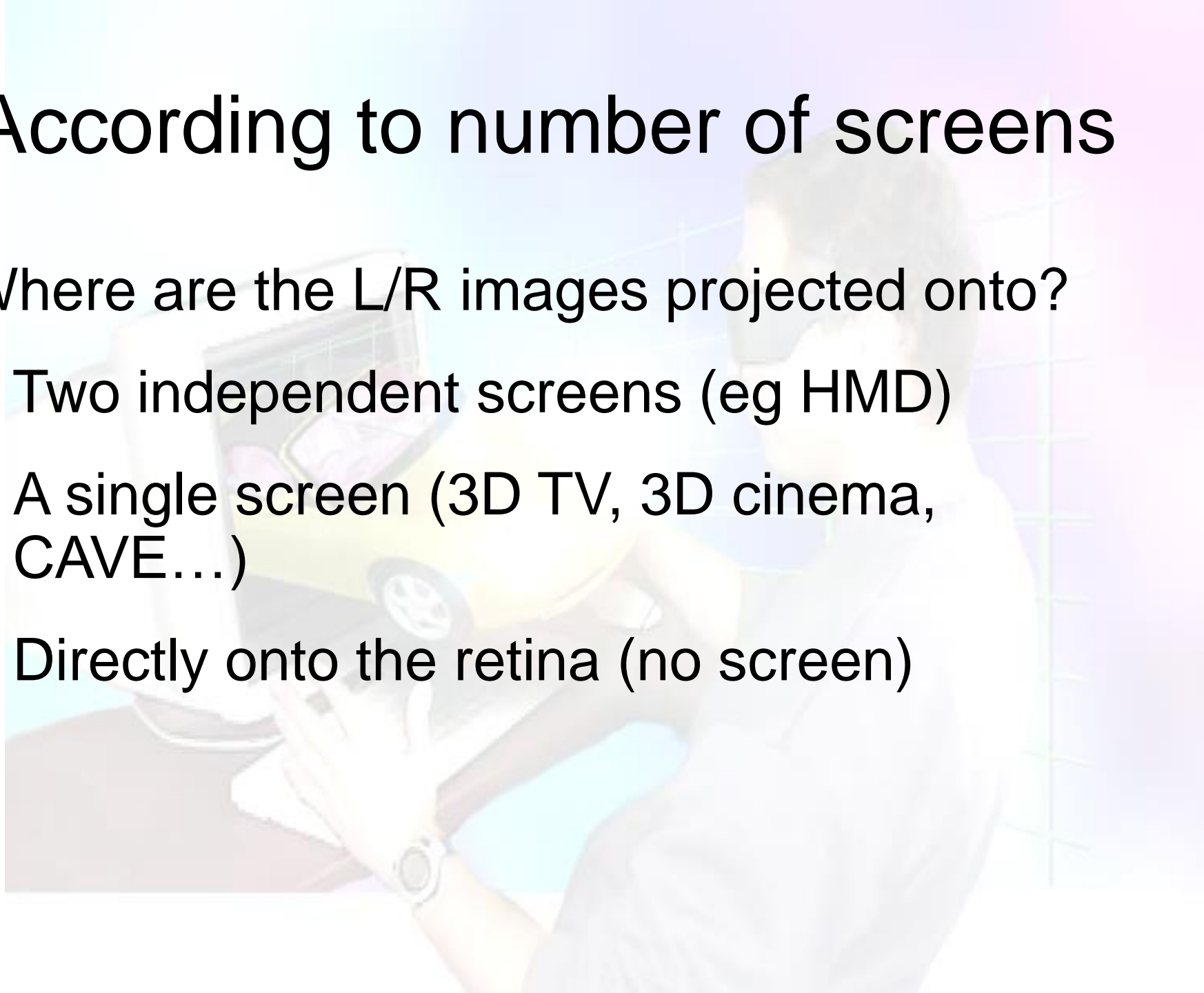
A person wearing VR goggles is shown from the side, interacting with a 3D model of a yellow sports car displayed on a computer monitor. The person's hand is reaching towards the car model. The background is a soft, colorful gradient. The text "TAXONOMY of 3D displays" is overlaid in the center.

# **TAXONOMY of 3D displays**

# According to number of screens

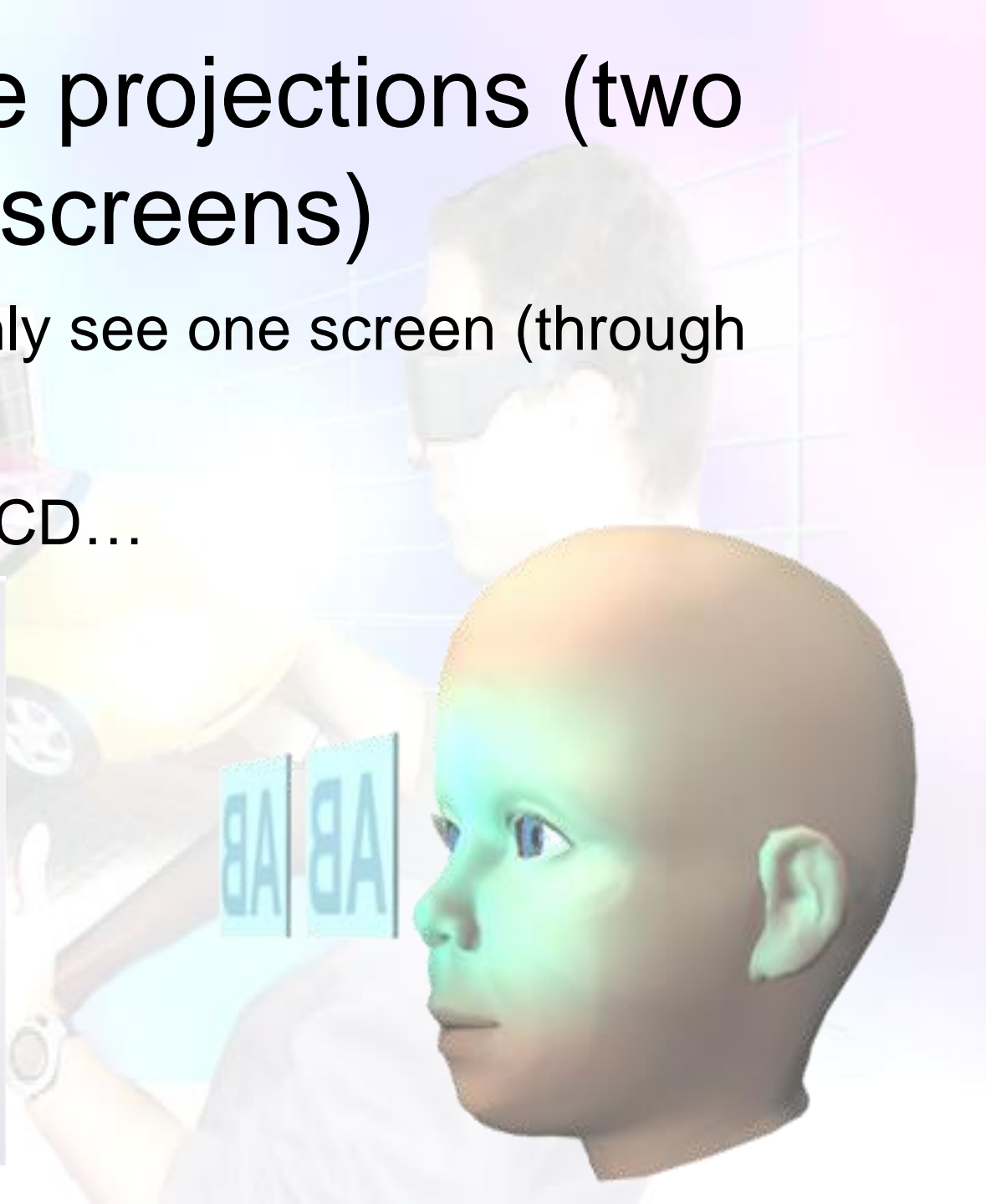
Where are the L/R images projected onto?

- Two independent screens (eg HMD)
- A single screen (3D TV, 3D cinema, CAVE...)
- Directly onto the retina (no screen)



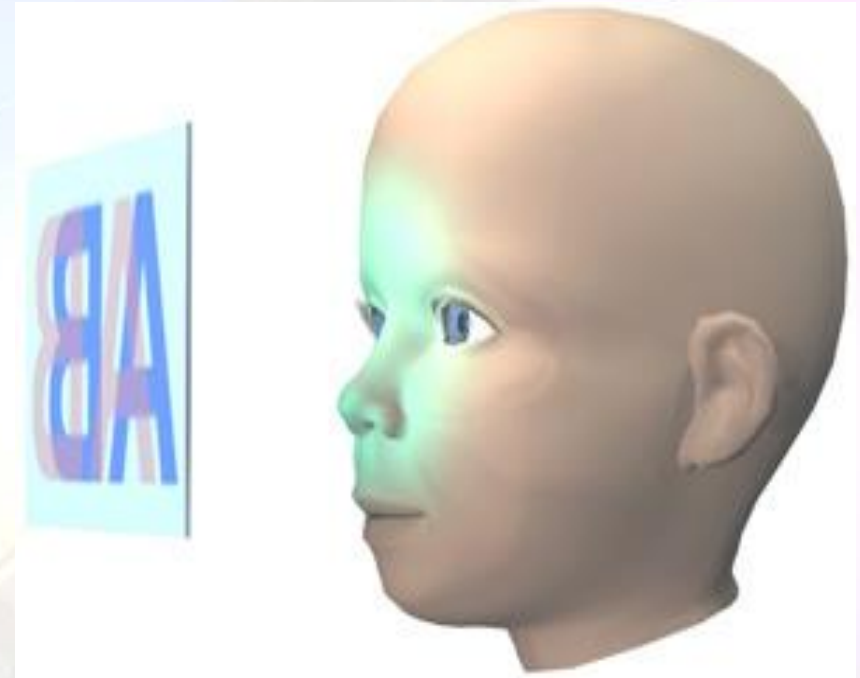
# Separate projections (two screens)

- Each eye can only see one screen (through optics)
- Used in HMD, HCD...



# Superimposed projections

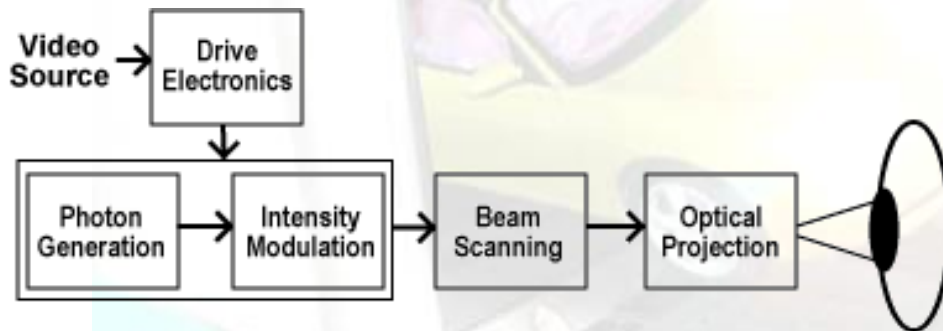
- Both eyes can see the screen
- Requires some **image separation technique** (eg polarization glasses, anaglyph...)
- Used in most projection-based equipment (CAVEs...)



# Direct projection into retinas

- Laser emitters
- Virtual Retinal Display, VRD

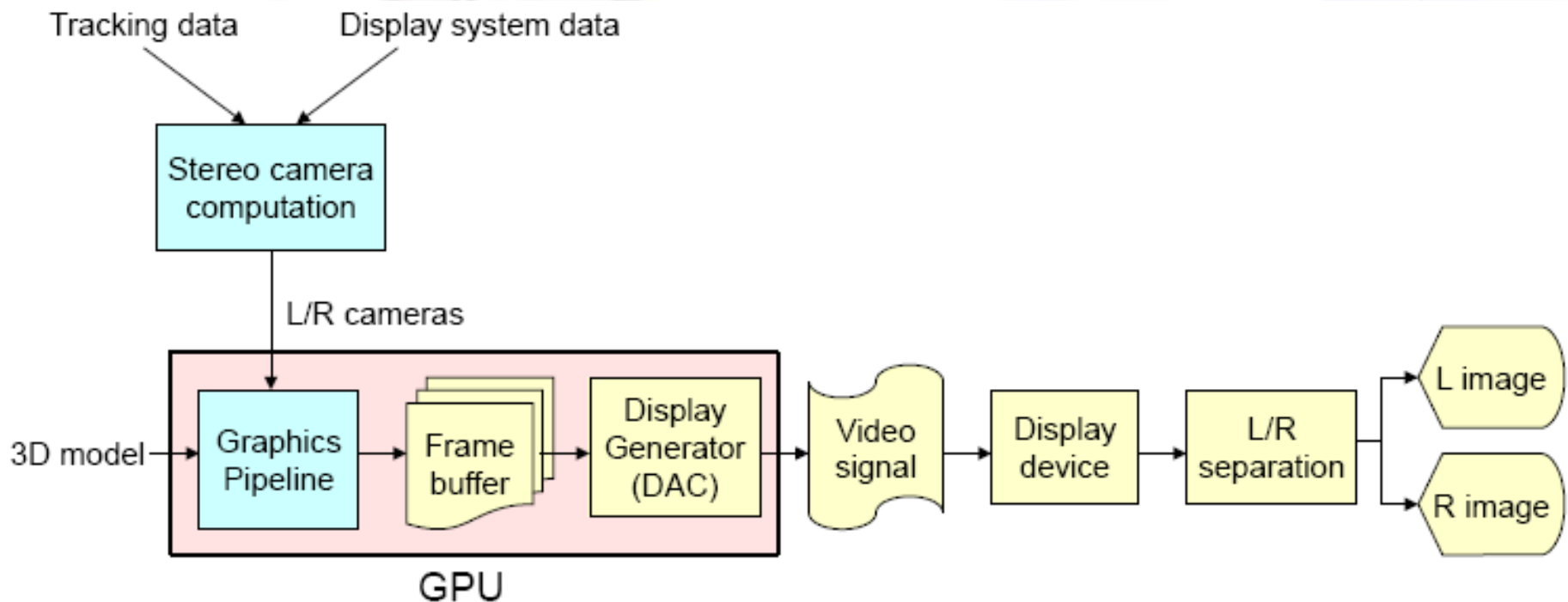
<http://www.hitl.washington.edu/projects/vrd/project.html>





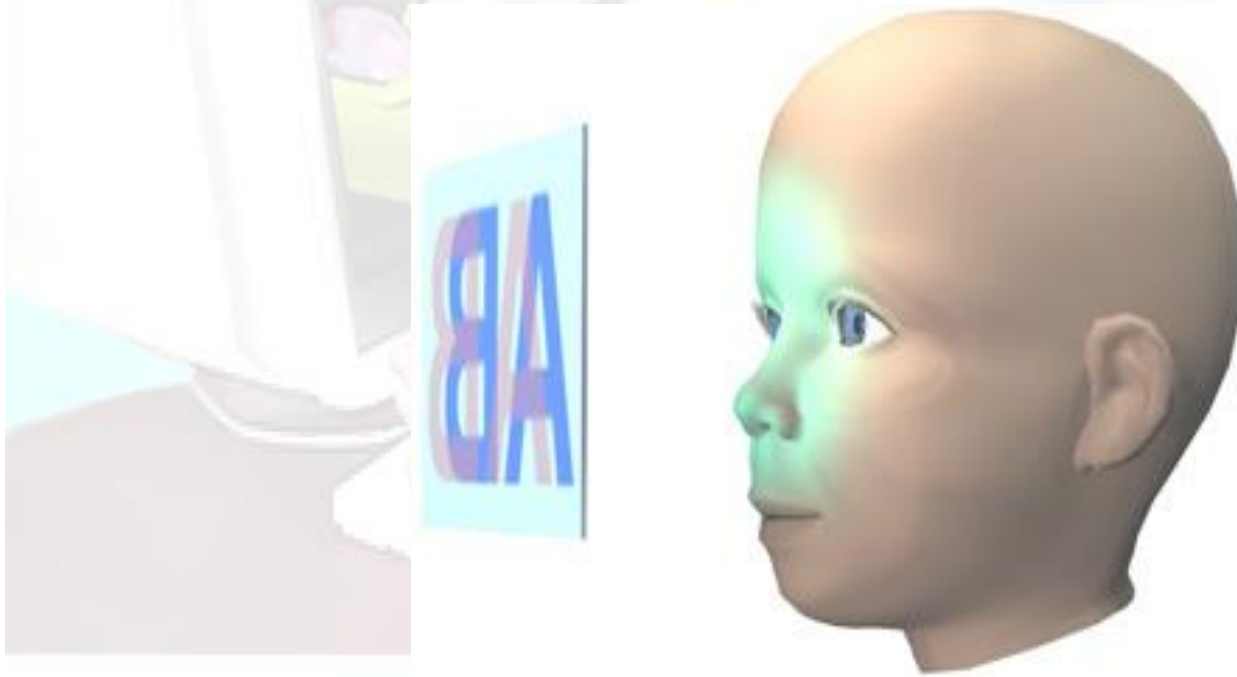
# Synthesis of stereo images

- Input: 3D model, tracking data, display system data
- Output: images with retinal disparity



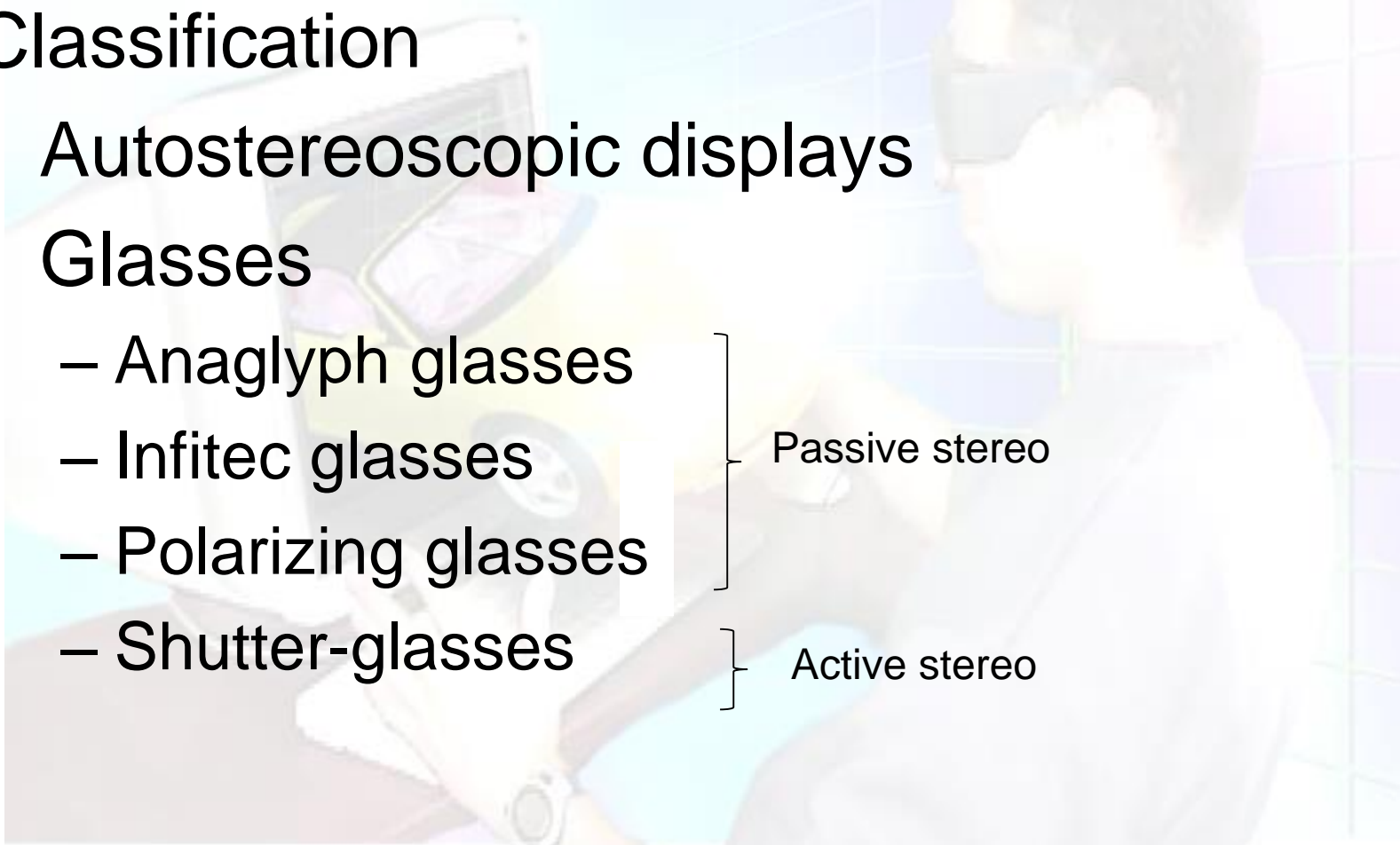
# Image separation

- Separation ~ means for providing each eye with its needed image (and rejecting the unnecessary image).
- Required when a single screen contains both images.

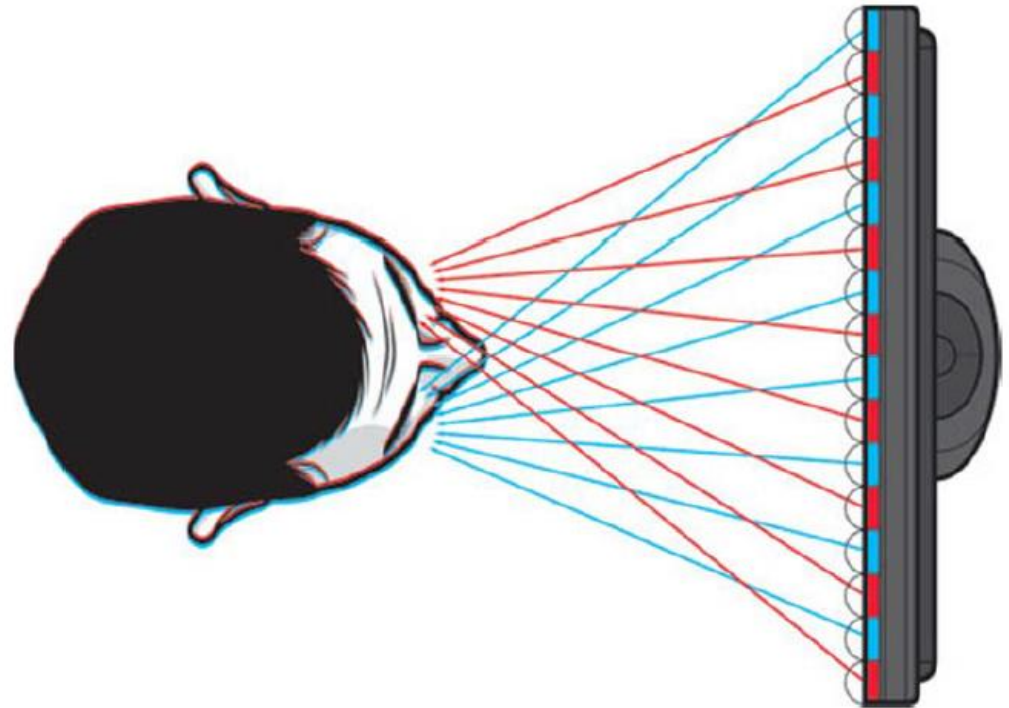


# Image separation

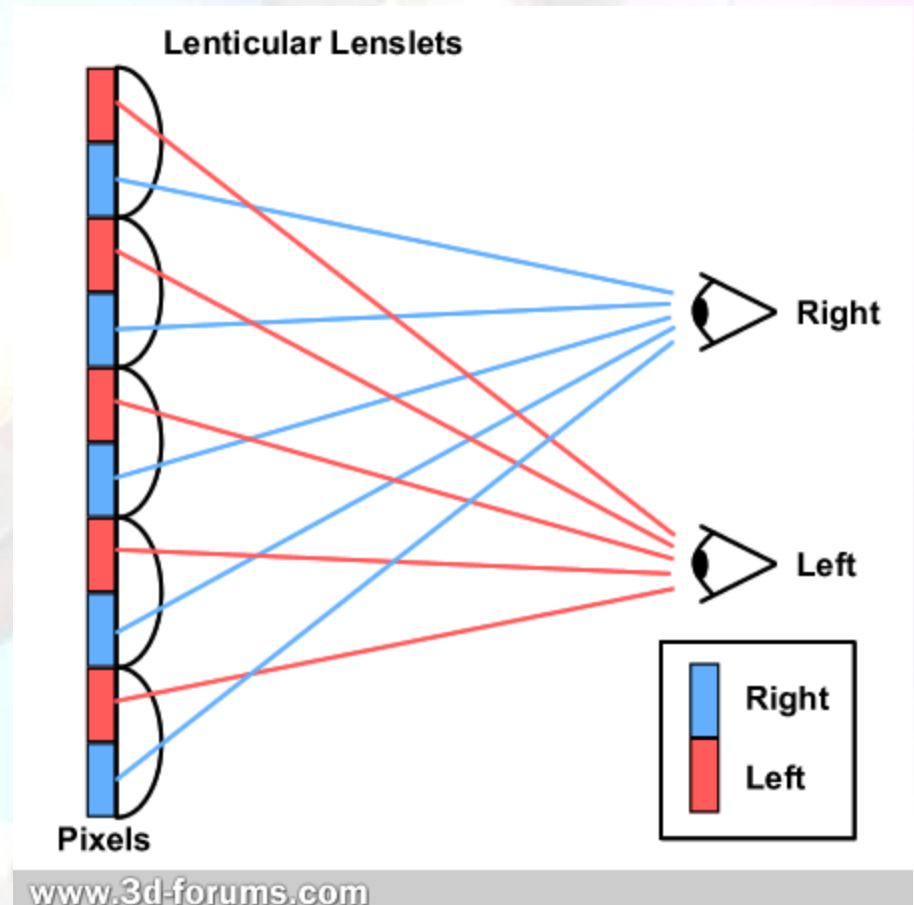
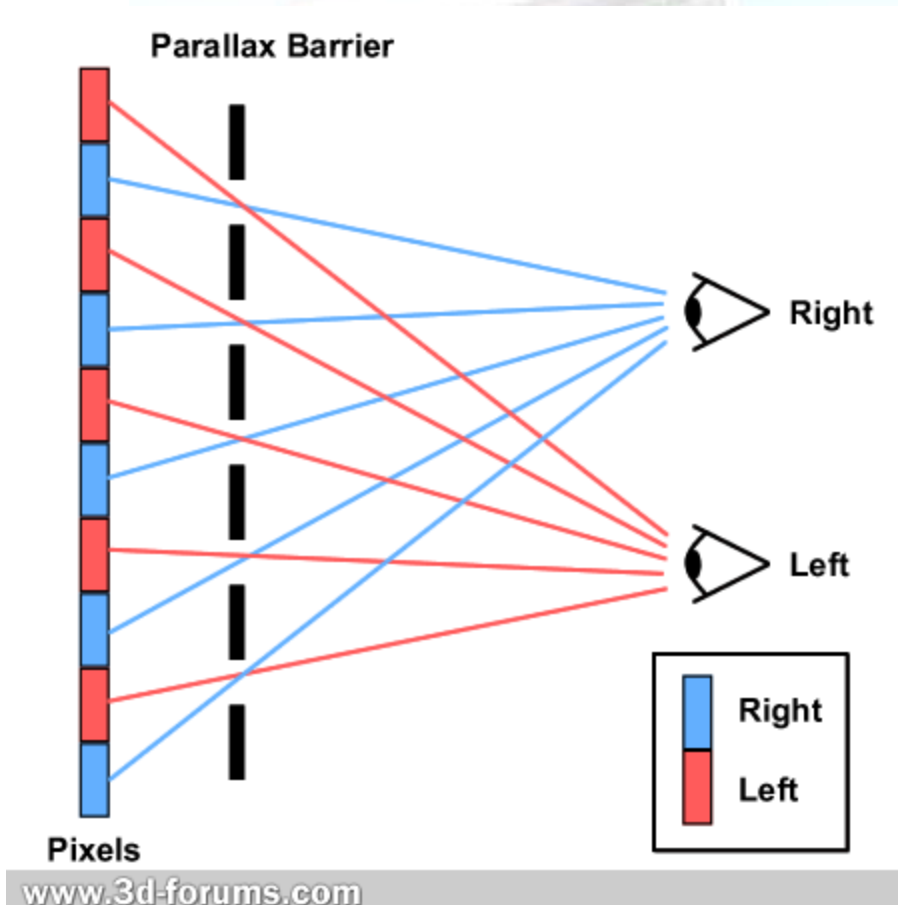
## Classification

- Autostereoscopic displays
  - Glasses
    - Anaglyph glasses
    - Infitec glasses
    - Polarizing glasses
    - Shutter-glasses
- Passive stereo
- Active stereo
- 
- A person is shown from the chest up, wearing dark 3D glasses. They are looking at a screen that displays a 3D image of a car. The background is a light blue grid pattern. The person is wearing a watch on their left wrist.

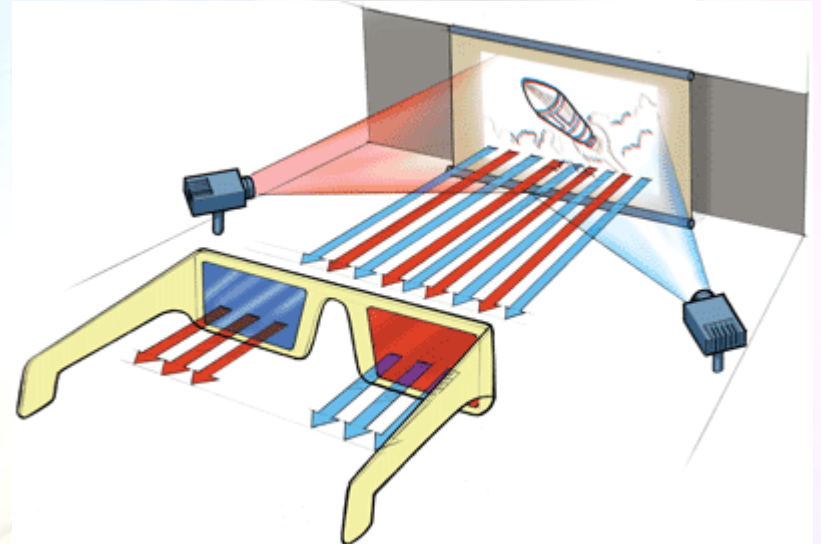
# Autostereoscopic displays



# Autostereoscopic displays



# Anaglyph filters





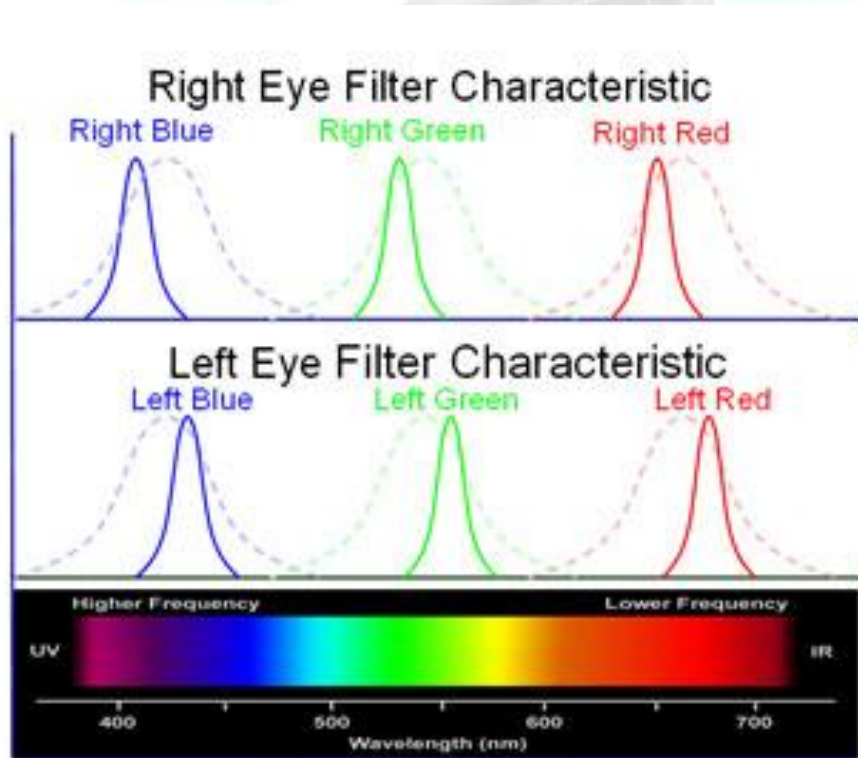
# Anaglyph filters

- Based on complementary colors:
  - R-GB, G-RB, B-RG
- Example: red-cyan, left filter blocks G and B; leaves R.
- Cheap
- Obvious color problems

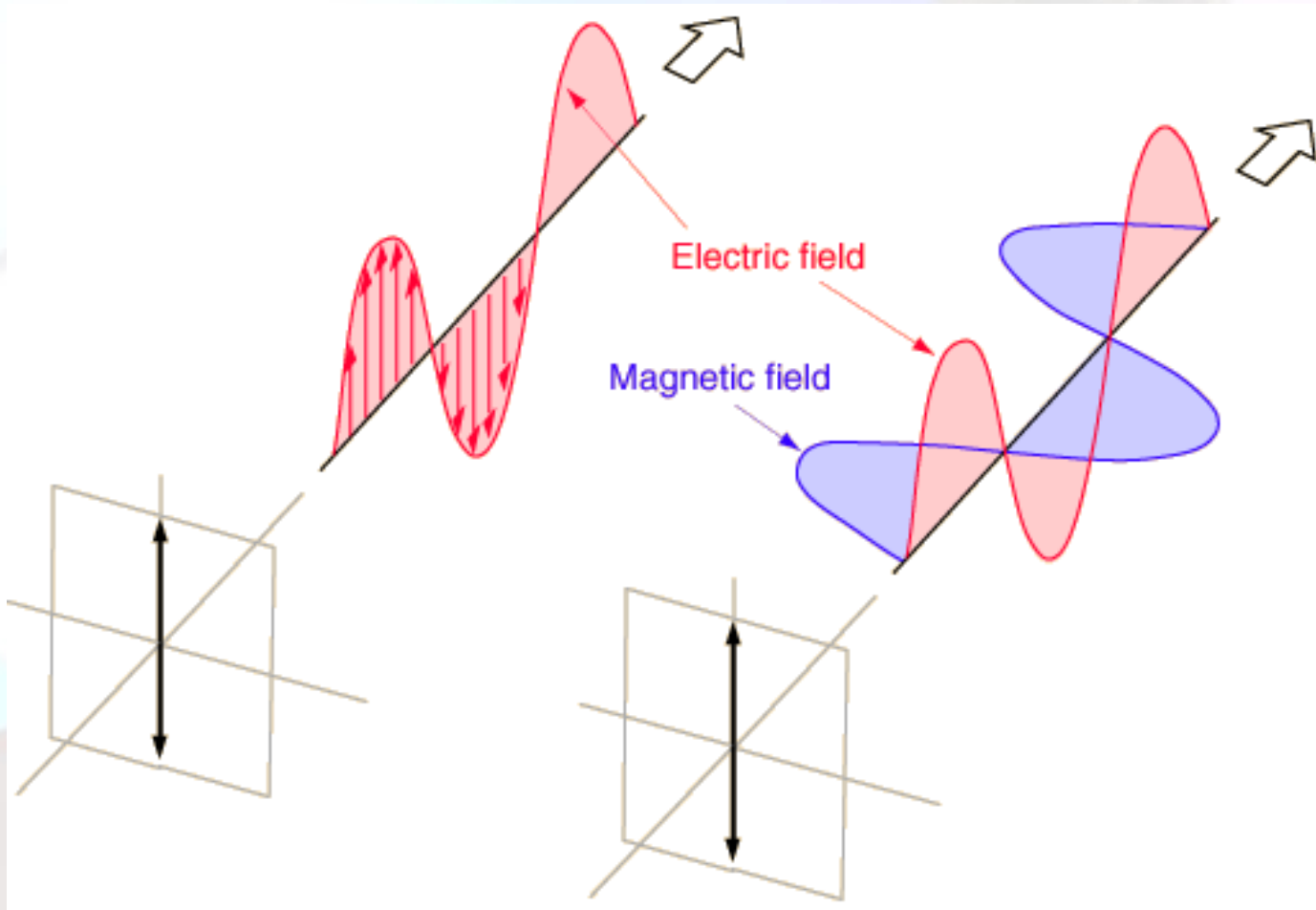


# Infitec glasses (Dolby 3D digital cinema)

- Improved version of anaglyph glasses



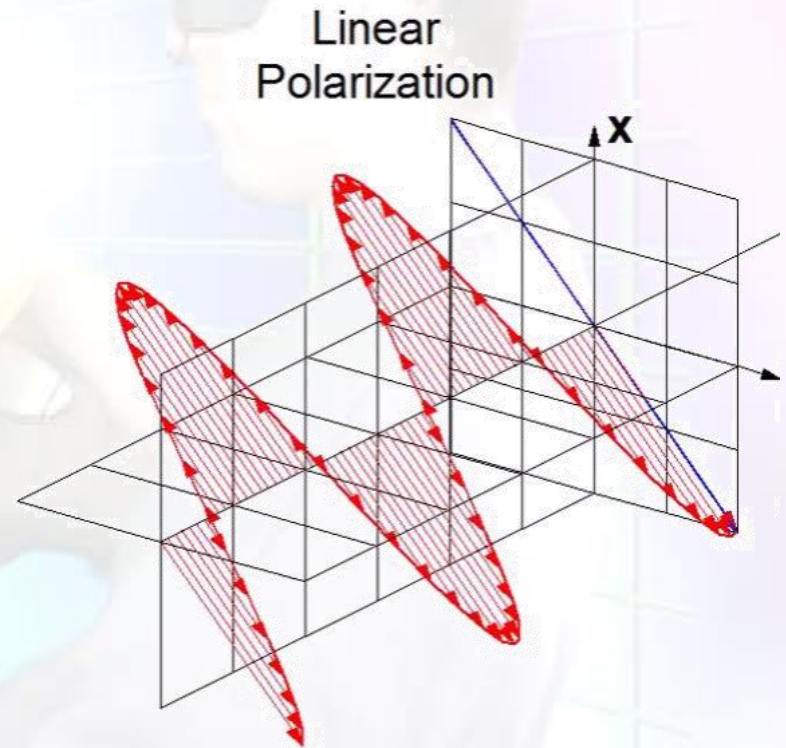
# Polarization



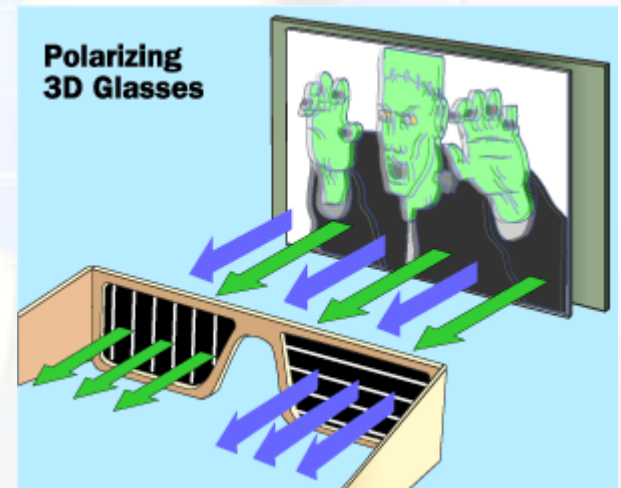
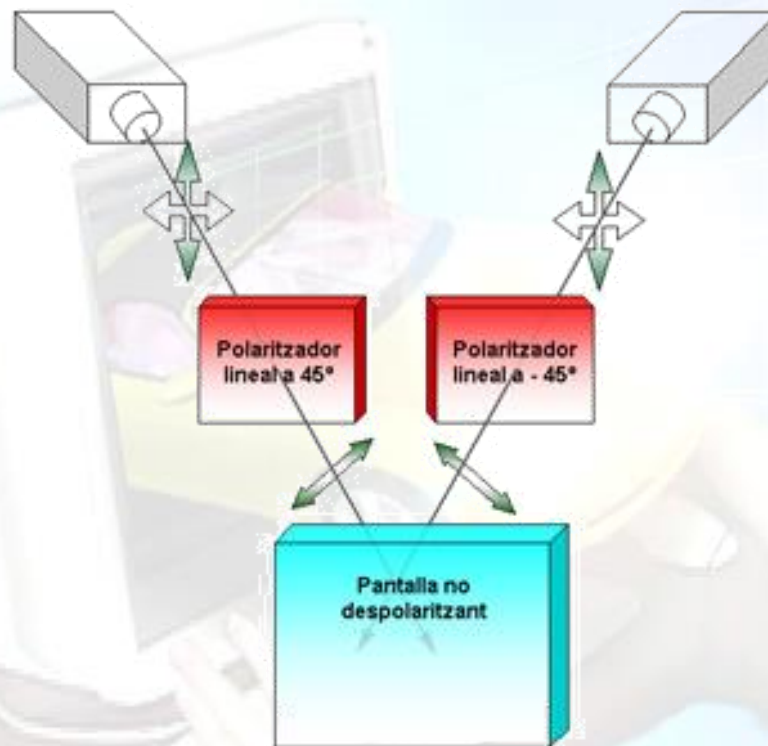
See this video: <https://www.youtube.com/watch?v=8YkfEft4p-w>

# Linear polarizing glasses

- Based on linear polarization filters
  - In the projectors
  - In the glasses
- Oriented at  $90^\circ$
- Cheap
- Sensible to head tilt



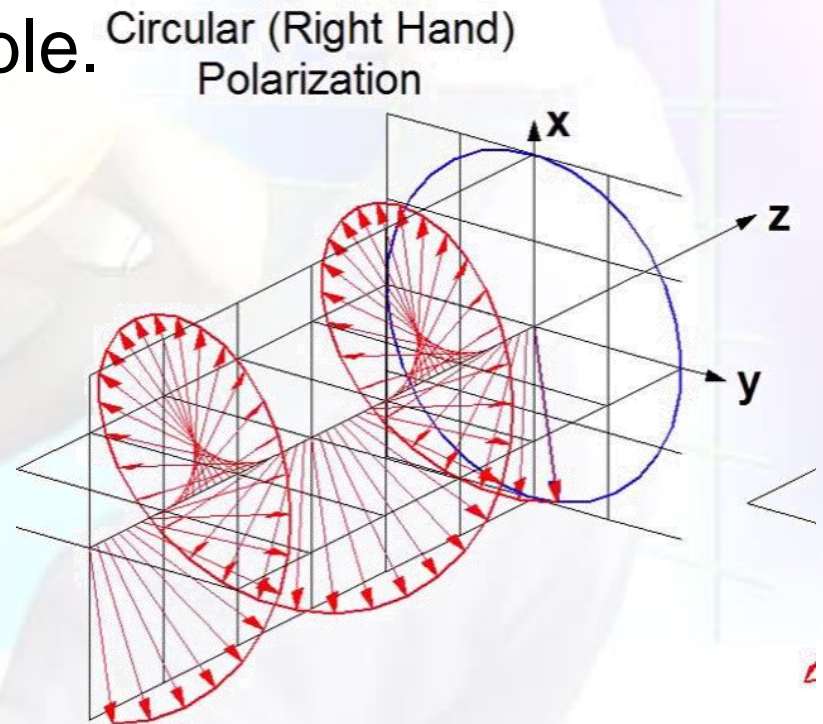
# Linear polarizing glasses





# Circular polarizing glasses

- Based on circular polarization filters (projectors & glasses)
- Cheap
- Almost head-tilt insensible.





# Shutter glasses

- A LC shutter avoids light from going through each eye, synchronized with the video signal.
- In any given time, one filter is in a *transparent state* and the other is in an *opaque state*.
- Requires a display device running at  $>100$  Hz
- Synchronization between graphics card and glasses:
  - Infrared signal
  - Wired



# Shutter glasses

Sync source:

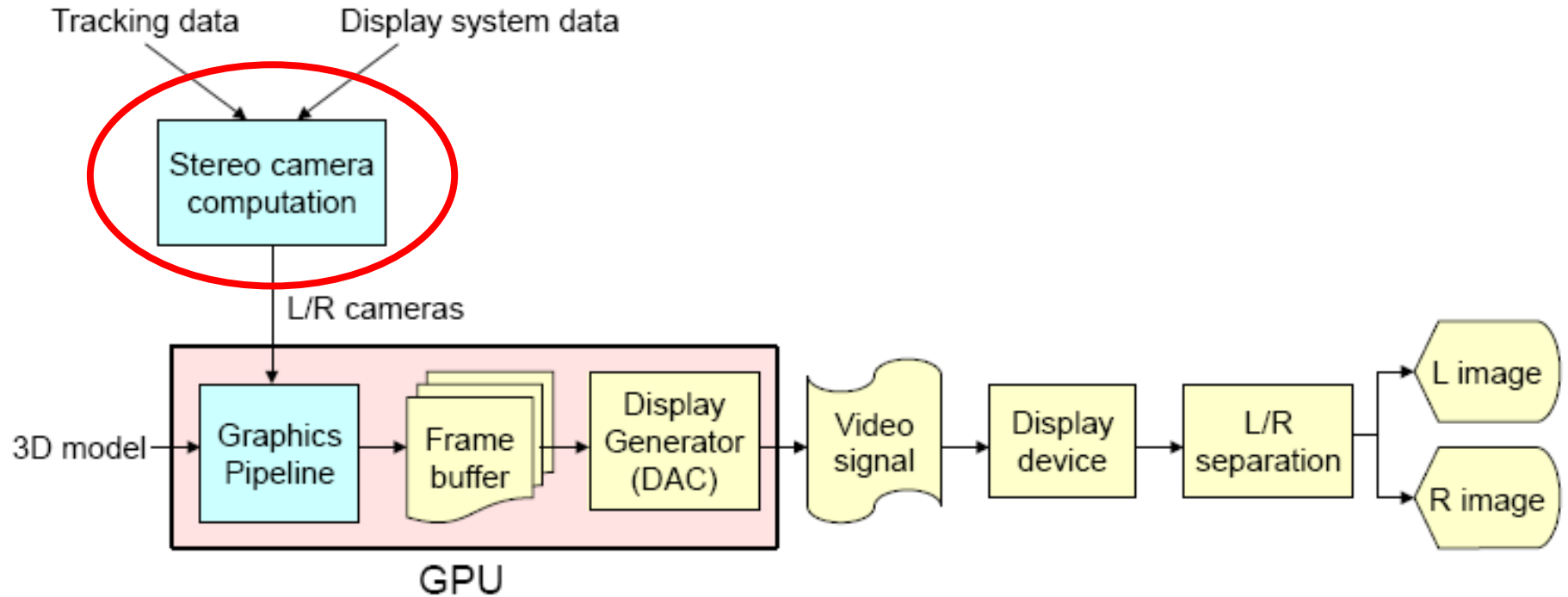
- Stereo-ready cards
  - Dedicated signal (eg VESA mini DIN-3)
- Non-stereo-ready cards:
  - VGA connector (pass-through)



# Comparison

Technology	Glasses	Head Pos	Head Tilt	Glasses Cost	Suitable for
Lenticular	No glasses	Y	Y	-	VR, TV
Anaglyph	Red/Cyan	N	N	Low	Press
Infitec	Infitec	N	N	High	VR, cinema
Passive stereo	Polarizing glasses	N	Y	Mid	VR, TV, cinema
Active stereo	Shutter glasses	N	N	High	VR, TV, cinema

# Synthesis of stereo images



# Stereo camera computation

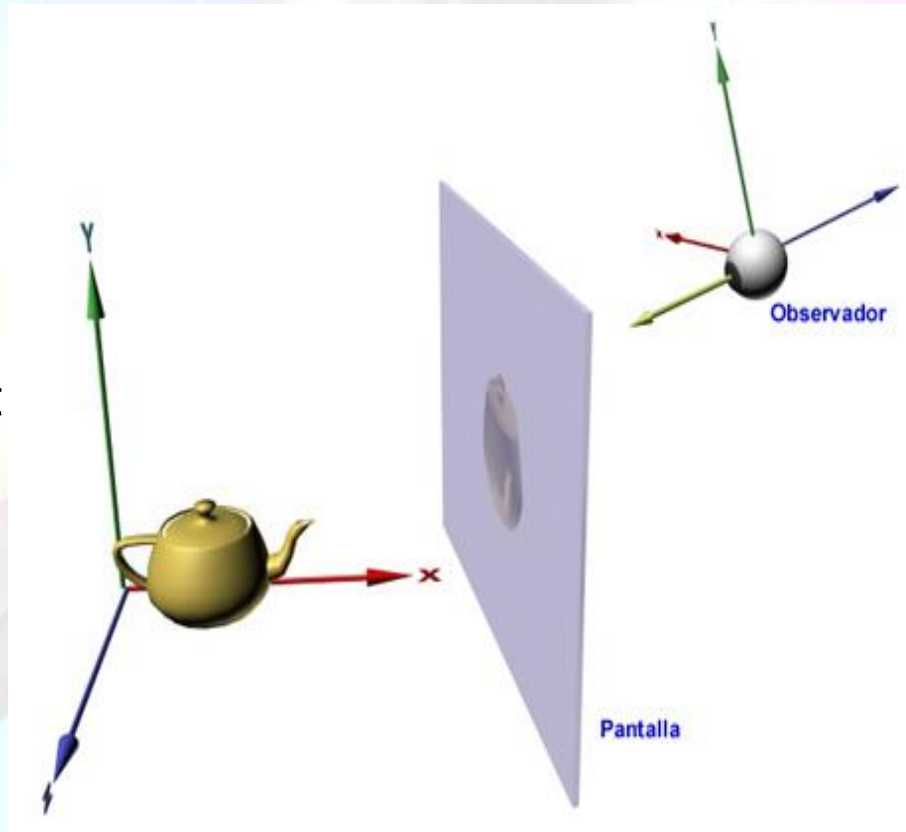
Output: Left and Right cameras:

- Extrinsic parameters: Eye (OBS), target (VRP), up (VUV)  $\rightarrow$  lookAt (eye.x, eye.y, eye.z, target.x, target.y, target.z, up.x, up.y, up.z);
- Intrinsic parameters: view frustum geometry  
 $\rightarrow$  frustum (left, right, bottom, top, near, far);



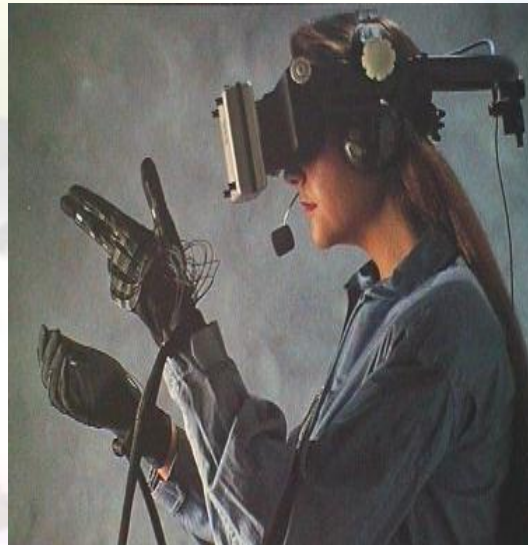
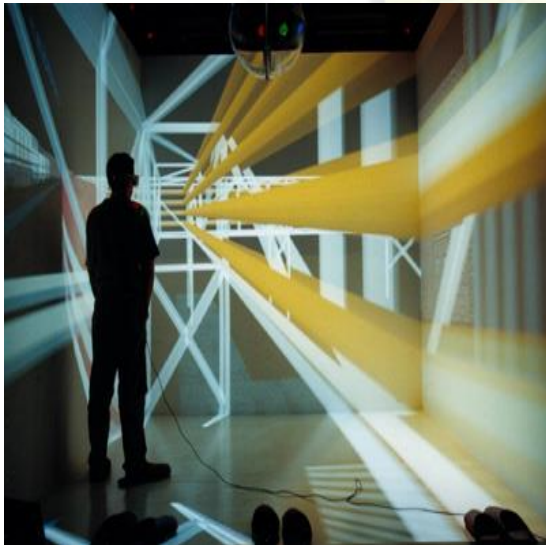
# Stereo rendering

- The virtual camera must be computed taking into account:
  - Screen geometry (size, position, orientation)
  - The eye position with respect to the screen.
- This is absolutely required:
  - On tiled-displays
  - On multi-screen displays
  - On head-tracked displays



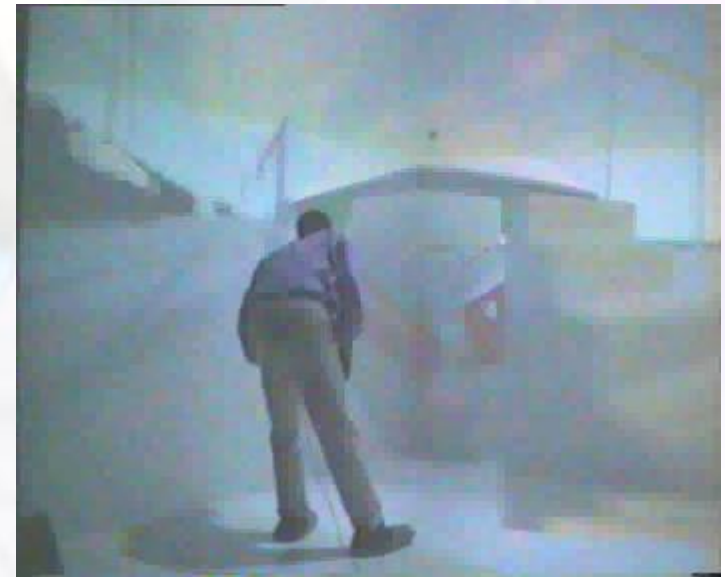
# Configurations

- Static screen + head-tracking (projection-based)
- Dynamic screen + head-tracking (HMDs)
- Desktop system without tracking



# Static screen

- This is the configuration of projection-based systems (CAVEs, Videowalls, workbenches...)
- Parameters:
  - Tracking data: L/R eye position
    - Two position trackers (3DOF each)
    - One 6DOF tracker (head, glasses...)
  - Display system data
    - Screen geometry



# Static screen

```
// View Matrix
```

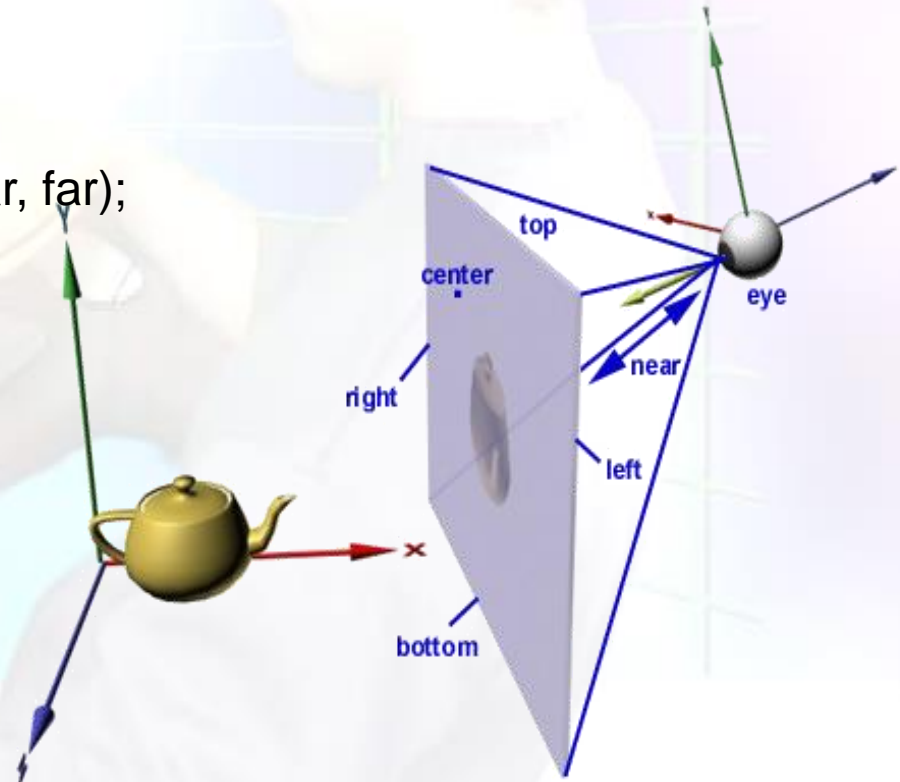
```
VM = lookAt(eye.x, eye.y, eye.z, center.x, center.y, center.z, up.x, up.y, up.z);
```

```
sendViewMatrix (VM);
```

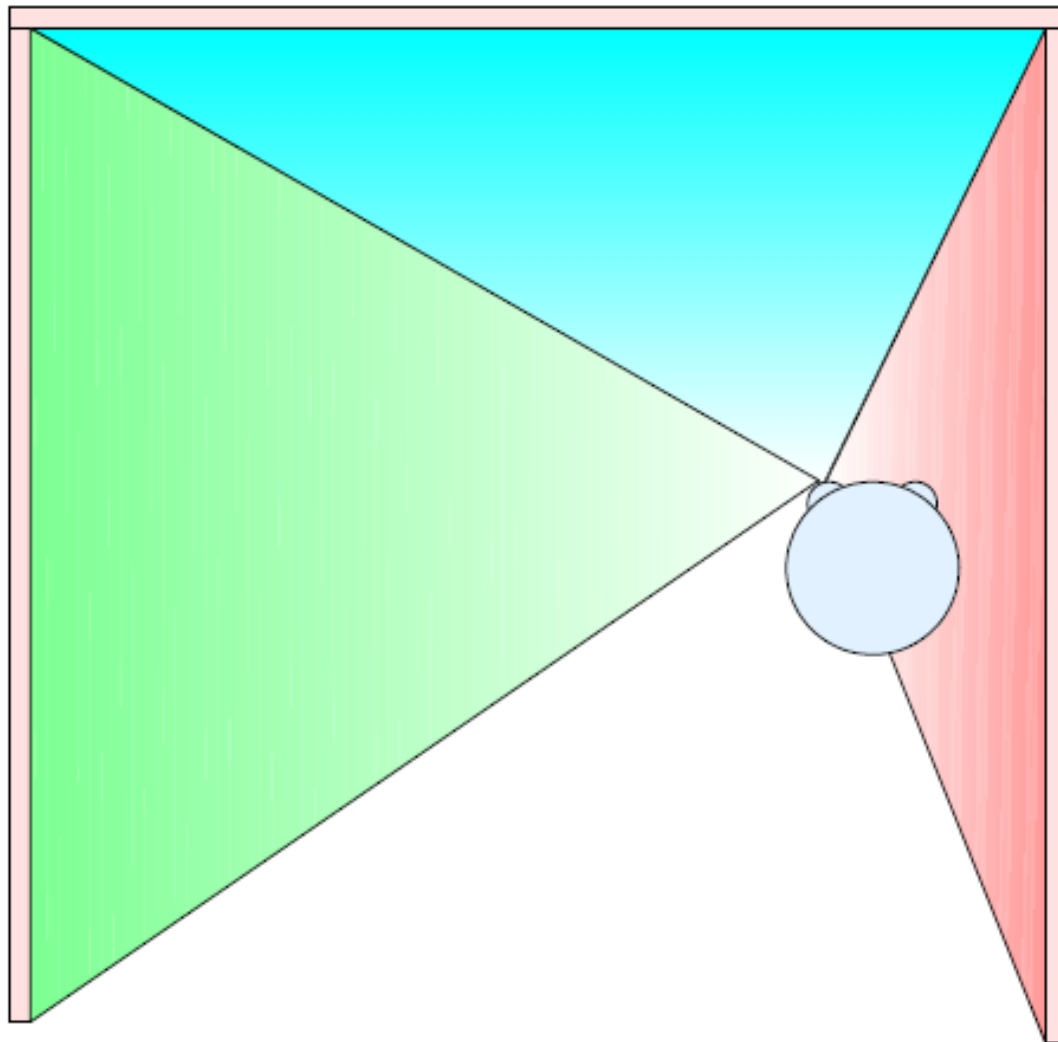
```
// Projection Matrix
```

```
PM = frustum (left, right, bottom, top, near, far);
```

```
sendProjectionMatrix (PM);
```

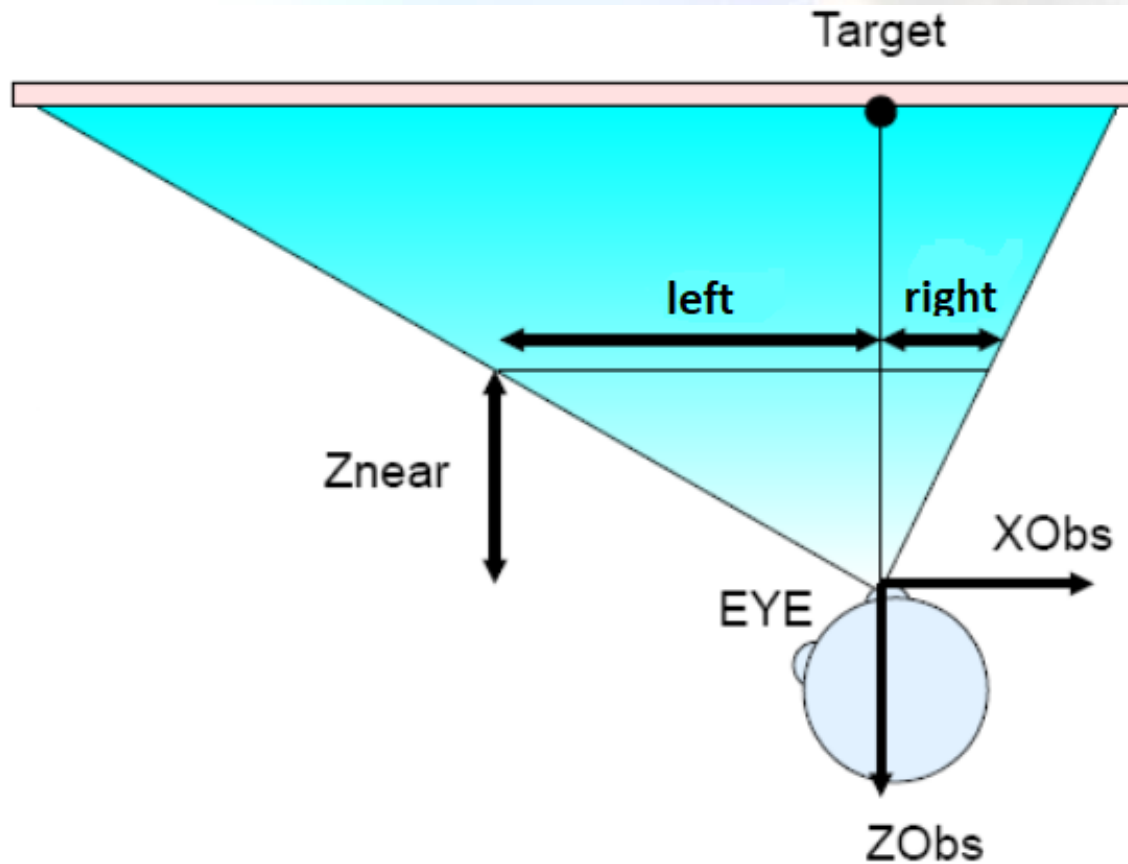


# Static screen

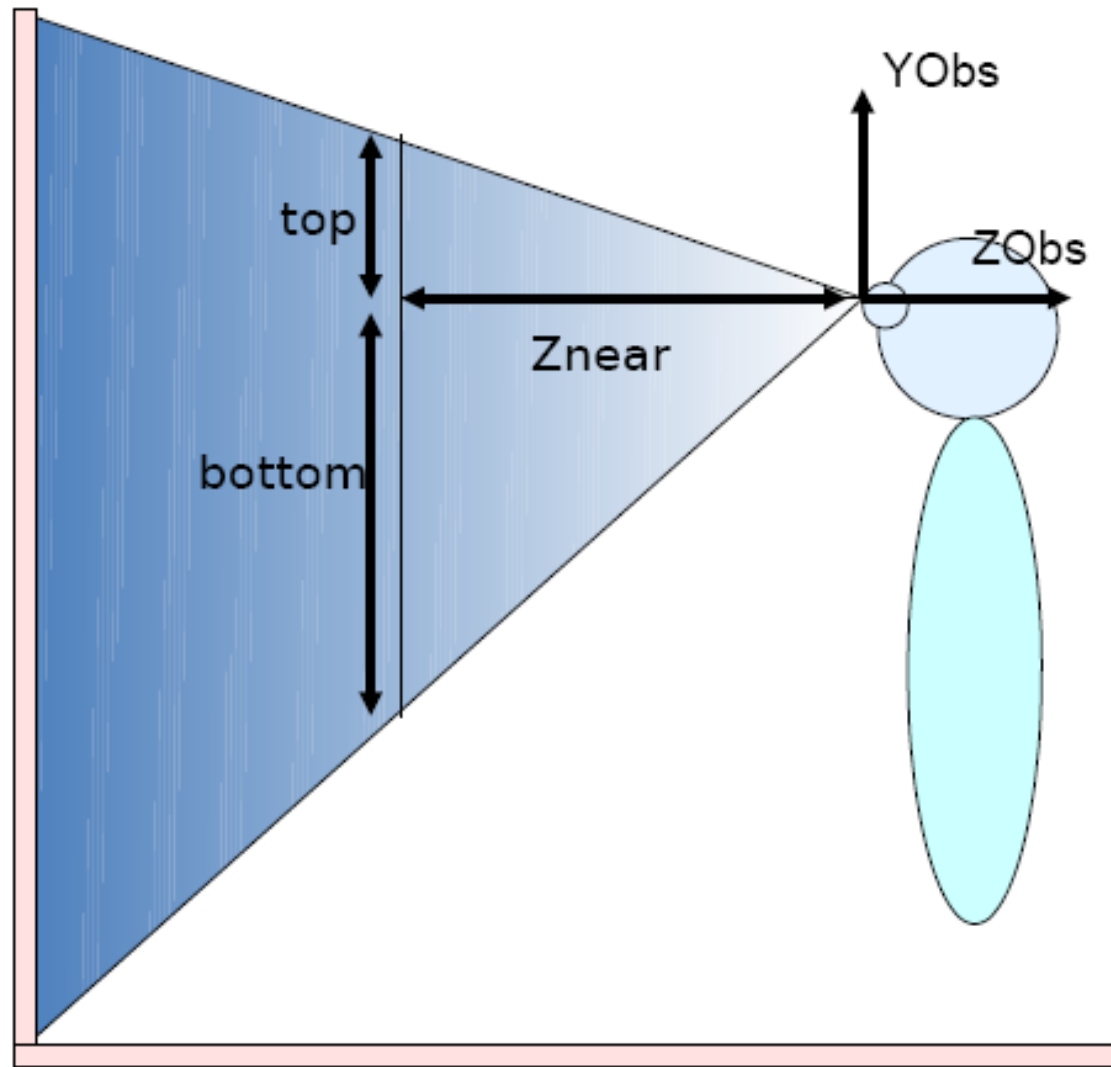




# Static screen

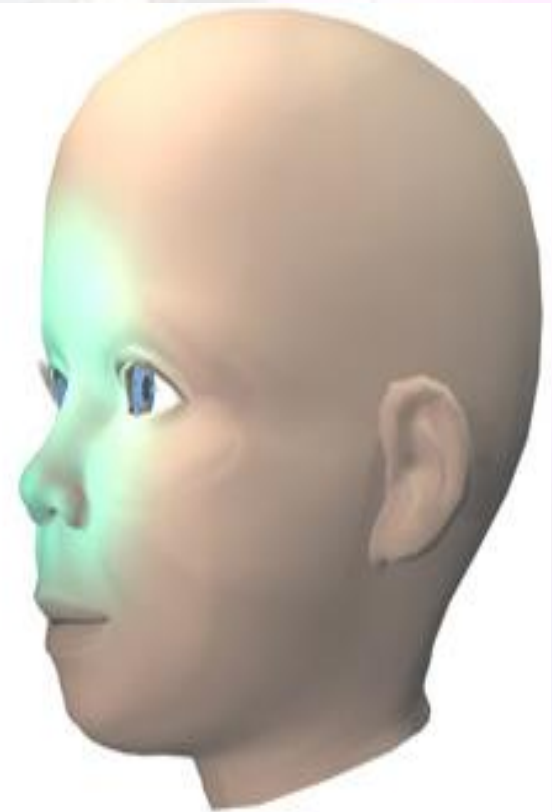


# Static screen



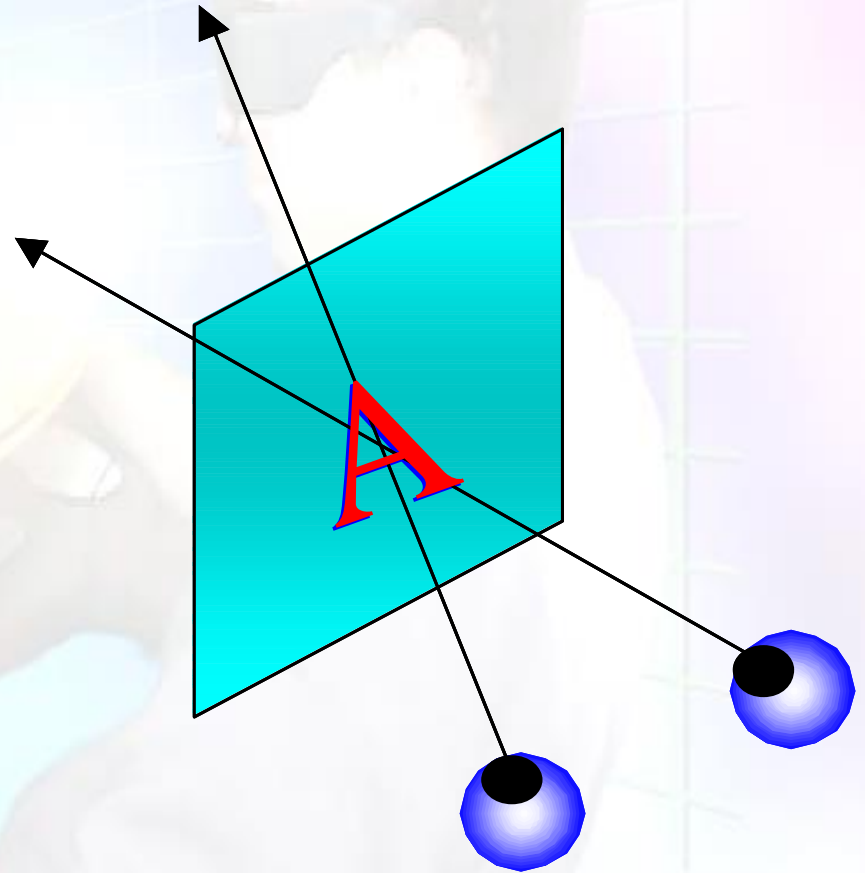
# Parallax

- **Parallax** is a 3D stereo concept.
- Related to (but distinct from!) **retinal disparity**.
- **Parallax**: distance between L/R points **measured on the screen**.
- Unlike retinal disparity, **parallax does not depend on eye convergence**.



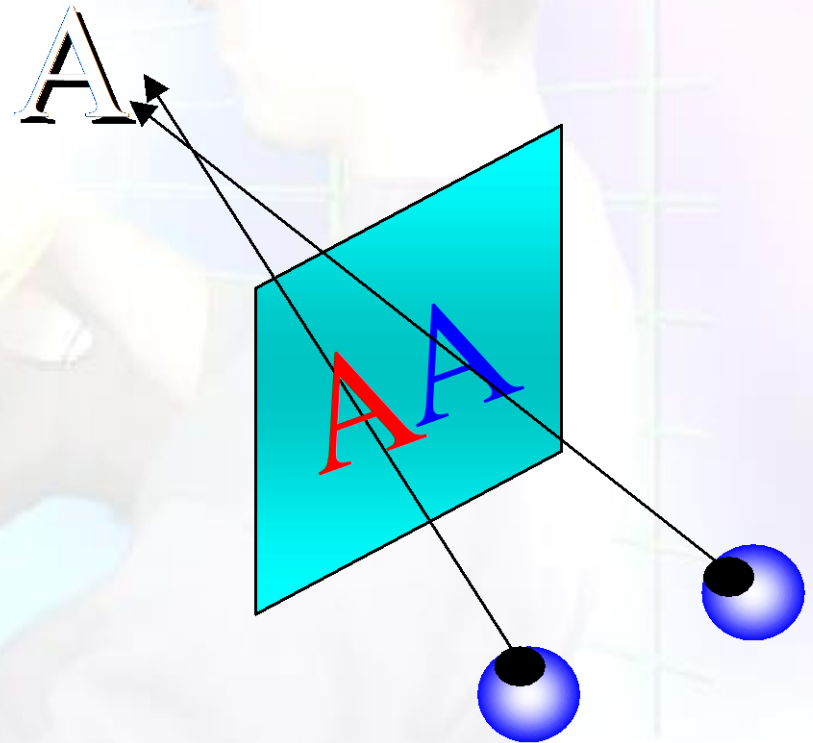
# Zero parallax

- An object has zero parallax when the corresponding L/R points overlap.
- When looking at the object, the eyes converge in the screen plane.
- The object appears to be **on the screen plane**.



# Positive parallax

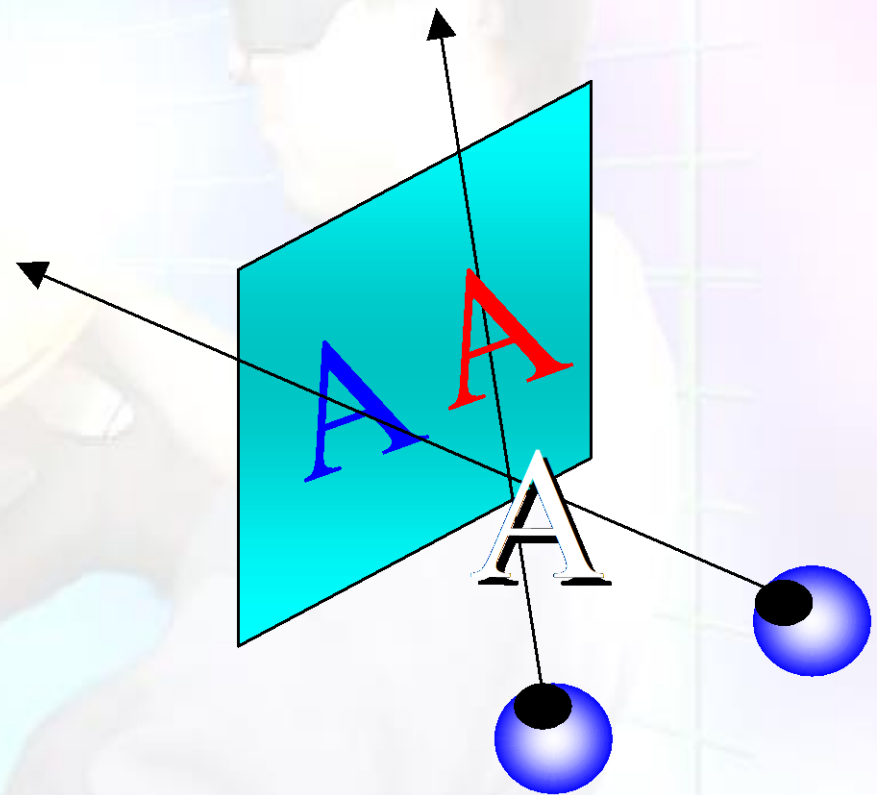
- An object has **positive parallax** when the corresponding L/R points have positive distance (**L point is to the left** of the R point).
- When looking at the object, the eyes converge at a point **behind the screen plane**.
- The object appears to be behind the screen.
- It should be in  $[0, 6.3\text{cm}]$
- If stereo cameras are computed correctly using actual eye positions, it will never be greater than the IOD.





# Negative parallax

- An object has **negative parallax** when the corresponding L/R points have negative distance (**L point is to the right** of the R point).
- When looking at the object, the eyes converge at a point **in front of the screen plane**.
- The object appears to be **in front of the screen**.
- Some studies recommend not to exceed 1.5 degrees (object is too close).



# Desktop system

- Used in low-cost systems (fish-tank VR)
- As in projection-based systems but guessing user's location.



# Dynamic screen

- Used in HMDs
- The screens follow the head movements, so they are fixed with respect to the eyes.
- Parameters:
  - Head orientation
  - Head position (optional)
  - HMD frustum + distortion



# Dynamic screen

If we could neglect lens distortion:

// View Matrix

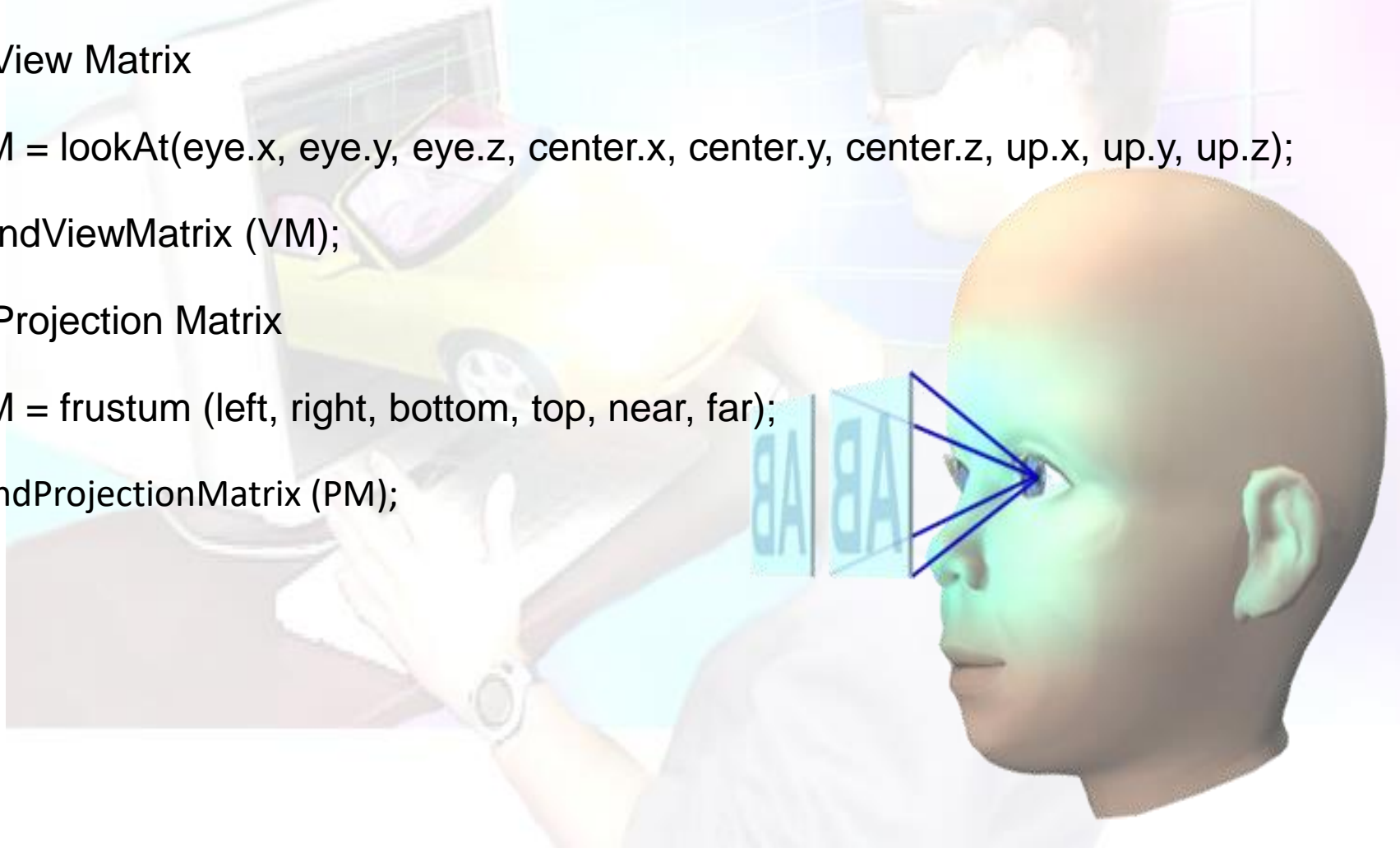
```
VM = lookAt(eye.x, eye.y, eye.z, center.x, center.y, center.z, up.x, up.y, up.z);
```

```
sendViewMatrix (VM);
```

// Projection Matrix

```
PM = frustum (left, right, bottom, top, near, far);
```

```
sendProjectionMatrix (PM);
```





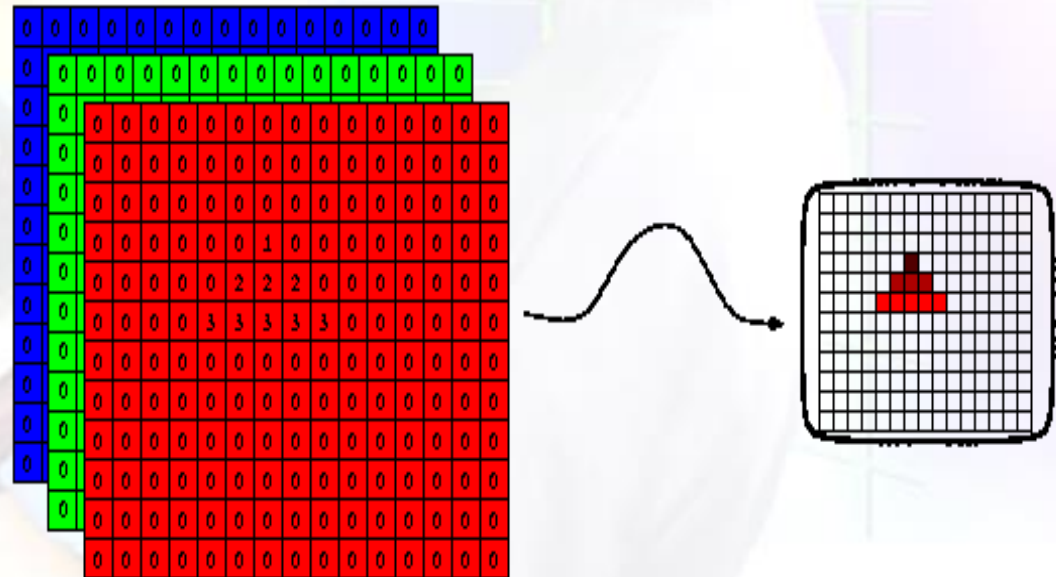
# Dynamic screen





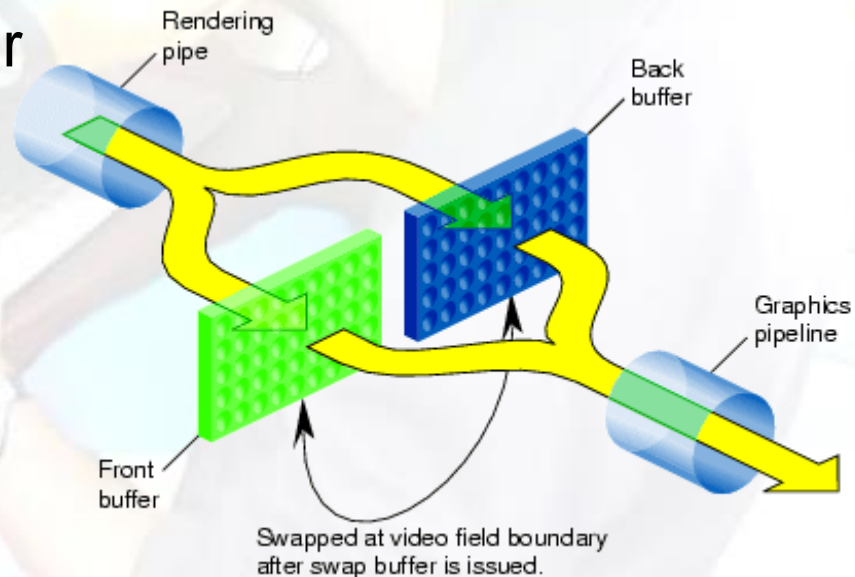
# Frame buffer: review

- Frame buffer
  - Color buffer(s)
  - Depth buffer
  - Stencil buffer
  - Accumulation buffer



# Frame buffer: review

- Double buffering
  - Two color buffers: GL\_FRONT, GL\_BACK
  - Depth buffer
  - Stencil buffer
  - Accumulation buffer



# Frame buffer formats

- How to encode a stereo pair in the color buffer.
- Required when a single frame buffer has to hold both L/R images
- Not required when each image is generated by a different PC.
- Must work together with *image separation*
- Classification:
  - Color based
    - Anaglyph stereo
  - Frame-based:
    - Above-and-below, or Side-by-side
    - Quad buffering
  - Line-based and column-based
    - Line-interlived (line sequential), column-interlived

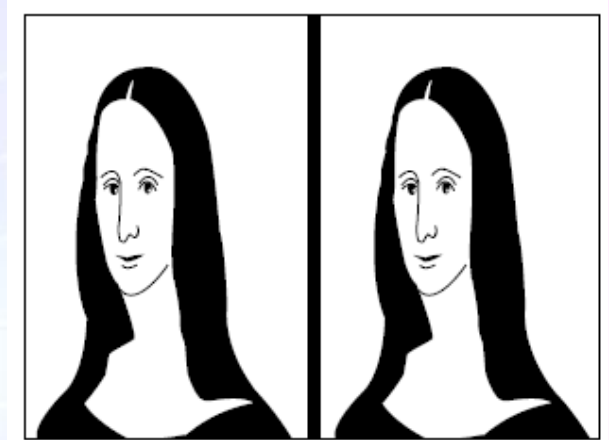
# Anaglyph stereo

- One color channel (eg Red) → left image
- The other two color channels (eg Green, Blue) → right image



# Side-by-side

- Left half → left image
- Right half → right image
- Typical configuration:
  - The graphics card has two outputs → two projectors





# Quad buffering

- Frame buffer
  - Four color buffers: GL\_FRONT\_LEFT, GL\_FRONT\_RIGHT  
GL\_BACK\_LEFT, GL\_BACK\_RIGHT
  - Depth buffer
  - Stencil buffer
- Quad buffering is used in *active stereo*
  - *Why two front buffers?* We need to provide both images during the time the application takes to draw the next frame.
  - *Why two back buffers?* Both L/R buffers are swapped simultaneously!
  - Supported by *stereo-ready* graphics cards (eg Nvidia Quadro)
  - Preferred format when using a single monitor/projector.

# Quad buffering: sample code

Setup a stereo format (Qt sample code):

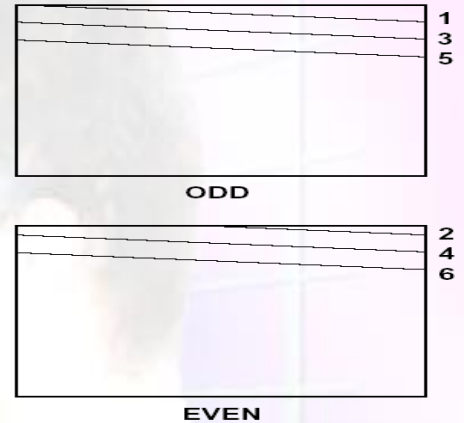
```
QGLFormat f;  
f.setStereo(true); // more flags...  
QGLFormat::setDefaultFormat(f);
```

Draw left/right images (OpenGL sample code):

```
Glboolean isStereo;  
glGetBooleanv (GL_STEREO, &isStereo);  
  
void paintGL() {  
    glDrawBuffer(GL_BACK_LEFT);  
    setupCamera(left);  
    drawScene();  
    glDrawBuffer(GL_BACK_RIGHT);  
    setupCamera(right);  
    drawScene();  
}
```

# Line/column-interlived

- Line interlived:
  - Odd lines encode the left image
  - Even lines encode the right image
- Column-interlived
  - Odd columns encode the left image
  - Even columns encode the right image
- Limitation: each eye sees half the number of lines (or columns).



# Display generator

- Converts the contents of the (FRONT) color buffer(s) into a video signal.
- Multiple configurations:
  - **Stereo-ready cards: one video signal**, encoding sequentially left and right images.
  - **Dual-head PCs** (most current graphics cards): two independent video signals (often DVI+VGA or DVI+DVI connectors)
  - **Quad-head PCs** (high-end graphics cards, eg Matrox QID)



# Display generator

## Dual-head PCs

- Most current graphics cards support two monitors.
- Simplest solution:
  - Configure a virtual desktop two times wide (eg  $2 \times 1024 \times 768 = 2048 \times 768$  desktop)
  - Graphics card will automatically output one half to each video signal.
  - Solution adopted in many display devices.



# Display generator

## Dual-head PCs

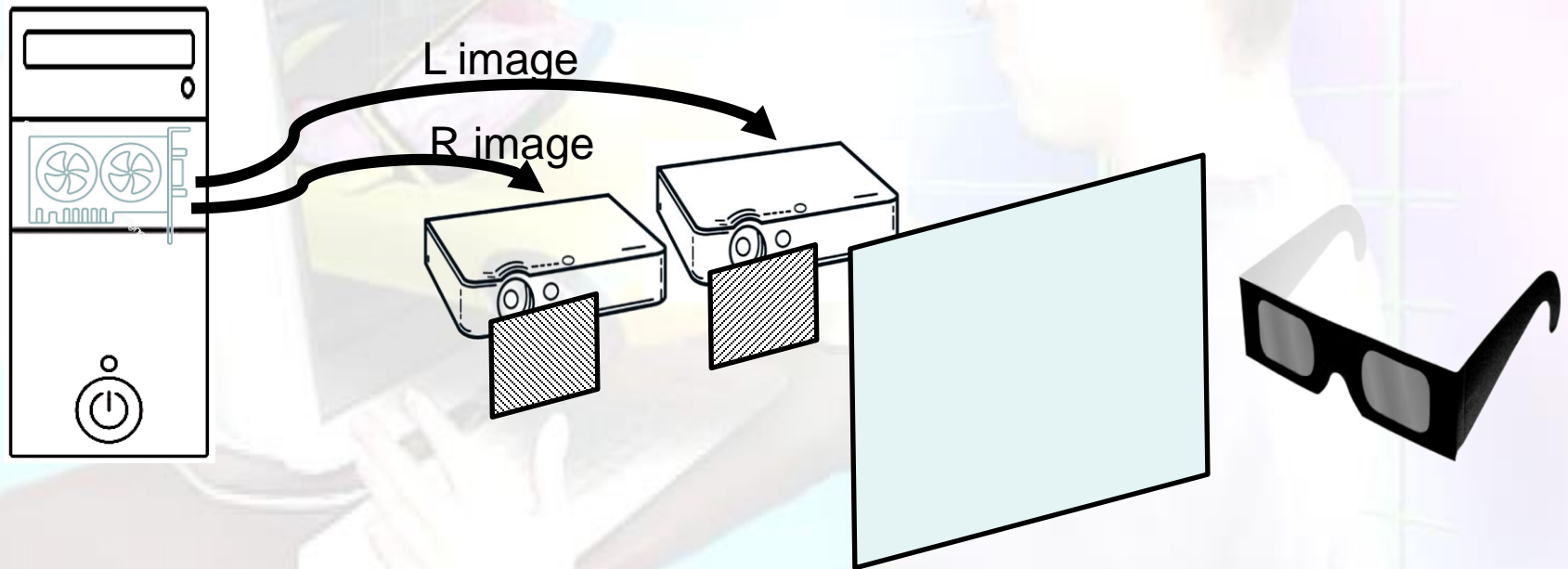
- OpenGL sample code (assuming a 2048x768 desktop)

```
void paintGL() {  
    glViewport(0,0,1024,768);  
    setupCamera(left);  
    drawScene();  
    glViewport(1024,0,1024,768);  
    setupCamera(right);  
    drawScene();  
}
```

# Sample configurations

- Passive stereo – 1 PC
- Passive stereo – 2 synced PCs
- Active stereo – 1 PC
- Active stereo – 4 PCs

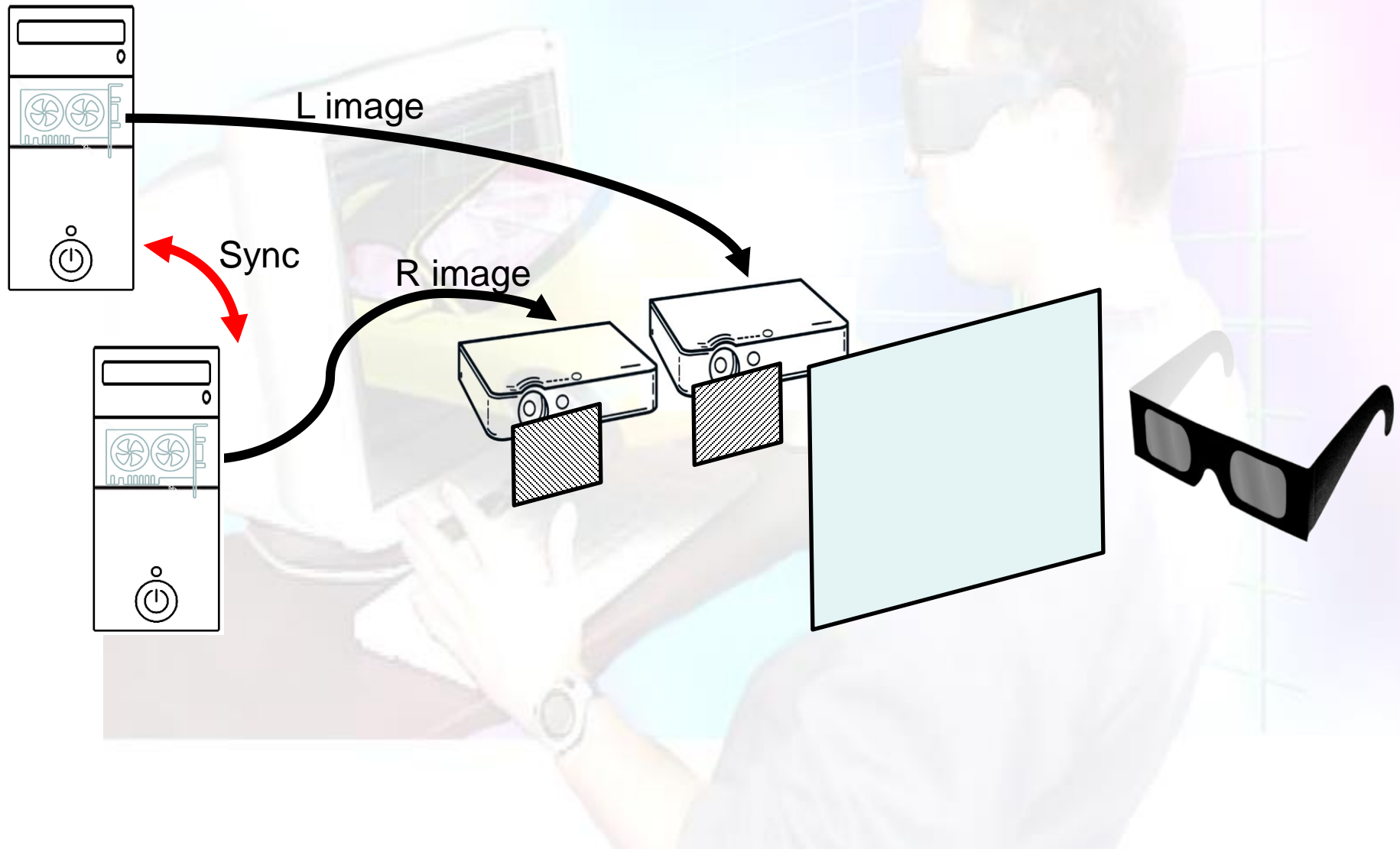
# Passive stereo, 1 PC



# Sample configurations

# PC	# Gfx cards	FB format	# Projectors	Filter	# Screens	Glasses	Comment
1	1 (dual-head)	Side-by-side	2 (passive, 60 Hz)	Polarizing filter	1	Polarizing glasses	Passive stereo
2	2	Normal	2 (passive, 60 Hz)	Polarizing filter	1	Polarizing glasses	Passive stereo; Needs PC sync
1	1	Quad buffering	1 (active, 120Hz)	-	1	Shutter glasses	Active stereo
4	4	Quad buffering	4 (active, 120 Hz)	-	4	Shutter glasses	Active CAVE Needs gfx sync!

# Passive stereo, 2 synced PCs

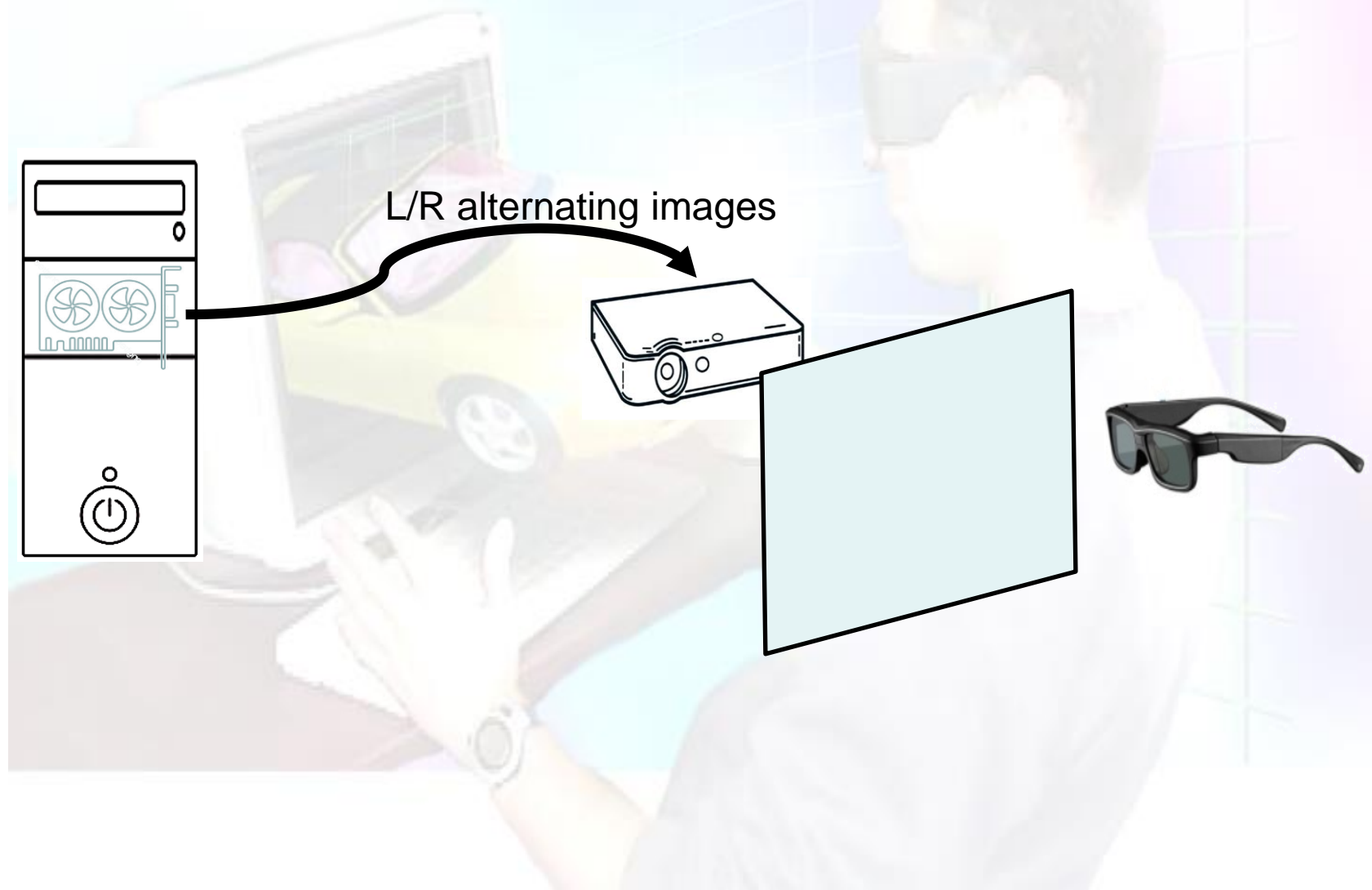


# Sample configurations

# PC	# Gfx cards	FB format	# Projectors	Filter	# Screens	Glasses	Comment
1	1 (dual-head)	Side-by-side	2 (passive, 60 Hz)	Polarizing filter	1	Polarizing glasses	Passive stereo
2	2	<b>Normal</b>	<b>2 (passive, 60 Hz)</b>	<b>Polarizing filter</b>	1	<b>Polarizing glasses</b>	<b>Passive stereo; Needs PC sync</b>
1	1	Quad buffering	1 (active, 120Hz)	-	1	Shutter glasses	Active stereo
4	4	Quad buffering	4 (active, 120 Hz)	-	4	Shutter glasses	Active CAVE Needs gfx sync!



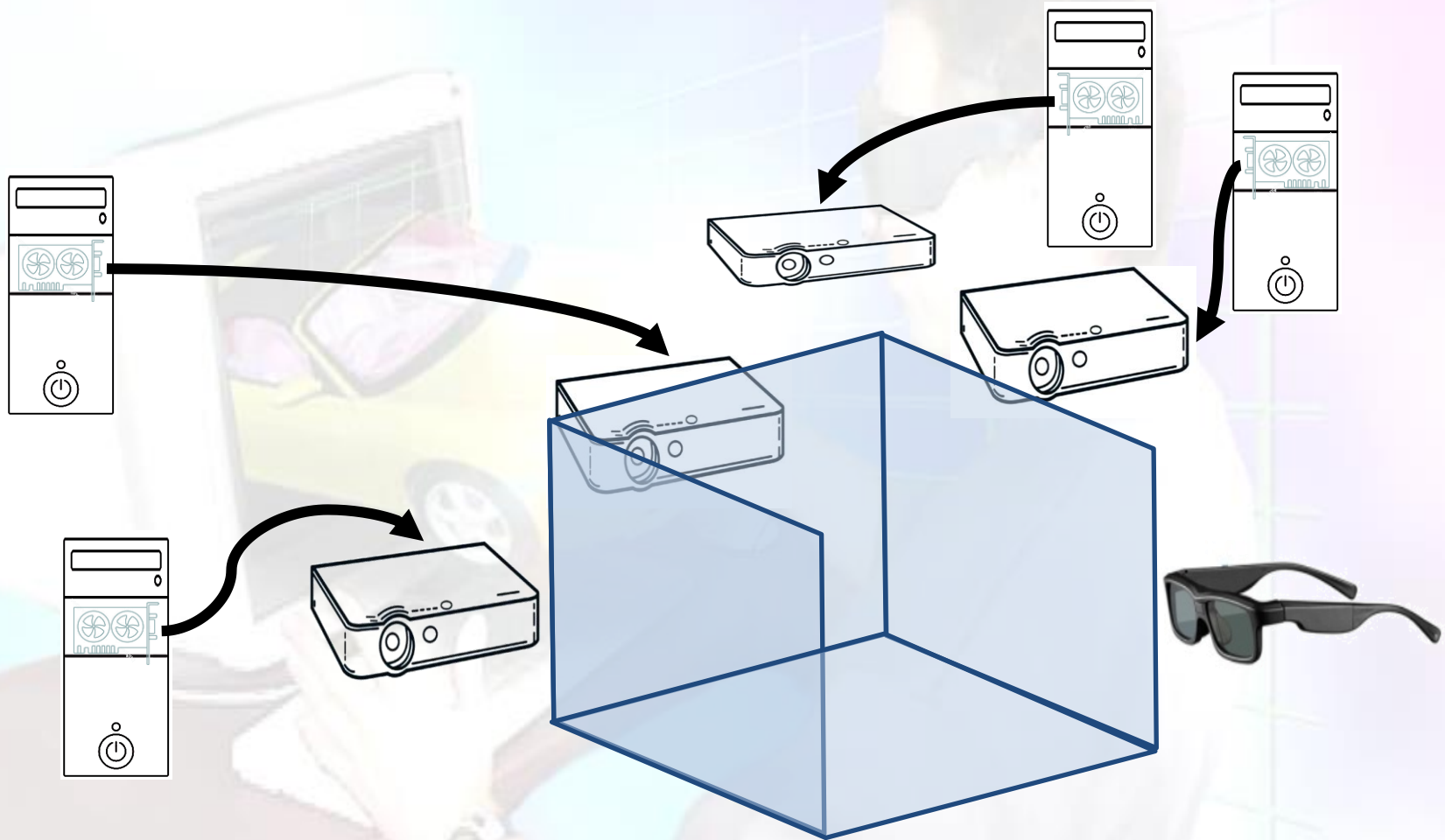
# Active stereo, 1 PC



# Sample configurations

# PC	# Gfx cards	FB format	# Projectors	Filter	# Screens	Glasses	Comment
1	1 (dual-head)	Side-by-side	2 (passive, 60 Hz)	Polarizing filter	1	Polarizing glasses	Passive stereo
2	2	Normal	2 (passive, 60 Hz)	Polarizing filter	1	Polarizing glasses	Passive stereo; Needs PC sync
<b>1</b>	<b>1</b>	<b>Quad buffering</b>	<b>1 (active, 120Hz)</b>	-	<b>1</b>	<b>Shutter glasses</b>	<b>Active stereo</b>
4	4	Quad buffering	4 (active, 120 Hz)	-	4	Shutter glasses	Active CAVE Needs gfx sync!

# Active stereo, 4 PCs



# Sample configurations

# PC	# Gfx cards	FB format	# Projectors	Filter	# Screens	Glasses	Comment
1	1 (dual-head)	Side-by-side	2 (passive, 60 Hz)	Polarizing filter	1	Polarizing glasses	Passive stereo
2	2	Normal	2 (passive, 60 Hz)	Polarizing filter	1	Polarizing glasses	Passive stereo; Needs PC sync
1	1	Quad buffering	1 (active, 120Hz)	-	1	Shutter glasses	Active stereo
4	4	<b>Quad buffering</b>	<b>4 (active, 120 Hz)</b>	-	4	<b>Shutter glasses</b>	<b>Active CAVE Needs gfx sync!</b>

A person is shown from the side, wearing 3D glasses and looking at a computer monitor. The monitor displays a yellow sports car. The person's hands are on a keyboard. The background is a light blue and white grid pattern.

# ***STEREOSCOPY***

**Course 2024/2025**