

# A Guide to NOI for Beginners (Draft)

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Reference Book: <http://www.ituring.com.cn/book/1044>

Practice Solutions: <https://github.com/yogykwan/acm-challenge-workbook/tree/master/src>

## Foreword

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This guide is designed specifically for those who already learned the basics of programming. I assume that you already know how to code in C++ and understand the concept of time complexity, as well as some other basic data structures like linked list, stack, queue, BST. (If not, there are lots of great tutorials/MOOCs online.)

We understand that it is hard to teach oneself competitive programming. So I made this guide and recorded a series of videos explaining it. This guide is meant for you to quickly get started on solving NOI problems and get familiar with some important algorithms. There is no guarantee that you can get a medal at NOI after reading this. But I am sure you can improve your knowledge and problem solving skills if you read this guide carefully and do lots of practice for every topic. Feel free to contact me if you find any mistakes or have doubts, I am always happy to discuss with you.

## 1. Time Complexity

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One important thing in NOI is time complexity. There is always a time limit for the problems and if your algorithm is too slow, you will get Time Limit Exceeded (TLE).

Usually the time limit is 1 second. You can substitute the maximum possible number of data within the given range to your algorithm's time complexity to get an estimated number of operations needed. For example, if your algorithm is  $O(n^2)$  and the data range is  $n \leq 1000$ , then the max operations needed is around  $10^6$ . You can check whether you will get TLE by checking the estimated number of operations according to:

- $10^6$ : no problem
- $10^7$ : should be ok
- $10^8$ : may not work

Now we will use a simple example to see how this works in practice.

### E.g.1 Pick Numbers

You are given  $n$  different integers  $k_1, \dots, k_n$ . You need to pick 4 numbers from them. You can pick the same number any times. If the sum of the 4 numbers you pick is  $m$ , you output YES, otherwise output NO.

$$1 \leq n \leq 1000, 1 \leq m \leq 10^8, 1 \leq k_i \leq 10^8$$

Solution 1: Brute Force

```
1  #include <stdio>
2  using namespace std;
3
4  const int MAX_N = 1002;
5
6  int main(){
7      int n, m, k[MAX_N];
8
9      scanf("%d %d", &n, &m);
10     for(int i=0; i<n; i++){
11         scanf("%d", &k[i]);
12     }
13
14     bool f = false;
15
16     // brute force all possibilities
17     for(int a=0; a<n; a++){
18         for(int b=0; b<n; b++){
19             for(int c=0; c<n; c++){
20                 for(int d=0; d<n; d++){
21                     if(k[a] + k[b] + k[c] + k[d] == m){
22                         f = true;
23                     }
24                 }
25             }
26         }
27     }
28
29     if(f) printf("YES");
30     else printf("NO");
31 }
```

The complexity for this solution is  $O(n^4)$ , so the estimated number of operations is  $10^{12}$ , which will definitely get you TLE.

One way to improve it: when you have chosen the first three numbers, you also know what the last number should be in order for the sum to be  $m$ . Hence you can use binary search to find the desired number.

Solution 2: Binary Search the last number

```
1  #include <stdio>
2  #include <algorithm>
3  using namespace std;
4
5  const int MAX_N = 1002;
6
7  int n, m, k[MAX_N];
8
9  bool binary_search(int x){
10     int l=0, r=n;
11
12     while(r-l>=1){
13         int i = (l+r)/2;
14         if(k[i]==x) return true;
15         else if(k[i]<x) l = i+1;
16         else r = i;
17     }
18
19     return false;
20 }
21
22 void solve(){
23     //must sort before BS
24     sort(k, k+n);
25
26     bool f = false;
27
28     for(int a=0; a<n; a++){
29         for(int b=0; b<n; b++){
30             for(int c=0; c<n; c++){
31                 if(binary_search(m-k[a]-k[b]-k[c])){
32                     f = true;
33                 }
34             }
35         }
36     }
37
38     if(f) printf("YES");
39     else printf("NO");
40 }
```

The complexity is now improved to  $O(n^3 \log n)$ . But this is still too slow.

One way to improve: when we have chosen the first two numbers, we also know the sum of the other two numbers in order to get a total sum of  $m$ . Hence, we can binary search among all possible sums of two given numbers to find if the desired sum is present.

Solution 3: Binary Search the sum of the last two numbers

```
1  #include <stdio>
2  #include <algorithm>
3  using namespace std;
4
5  const int MAX_N = 1002;
6
7  int n, m, k[MAX_N];
8
9  // sum of two numbers
10 int kk[MAX_N * MAX_N];
11
12 void solve(){
13     for(int c=0; c<n; c++){
14         for(int d=0; d<n; d++){
15             kk[c*n + d] = k[c] + k[d];
16         }
17     }
18
19     sort(kk, kk+n*n);
20
21     bool f = false;
22     for(int a=0; a<n; a++){
23         for(int b=0; b<n; b++){
24             // use STL BS
25             if(binary_search(kk, kk+n*n, (m-k[a]-k[b]))){
26                 f = true;
27             }
28         }
29     }
30
31     if(f) printf("YES");
32     else printf("NO");
33 }
```

Complexity: sorting  $n^2$  numbers:  $O(n^2 \log n)$ , nested loop with binary search:  $O(n^2 \log n)$

So overall complexity is:  $O(n^2 \log n)$ , which is acceptable.

## 2. Search

### 2.1 Recursion with Memoization

Naive recursion is often slow because it computes the same elements many times, which is a waste of time. For example, when calculating the fibonacci number, we compute fib(8) and fib(9) to get fib(10). However, while computing fib(9), we need to compute fib(8) again.

One way to avoid this is to store all computed values in a table for future use. This technique is called memoization.

Example: Fibonacci number

```
1  int memo[MAX_N + 1] = {0};
2
3  int fib(int n){
4      if(n<=1) return n;
5      if(memo[n]!=0) return memo[n];
6      return memo[n] = fib(n-1) + fib(n-2);
7  }
```

### 2.2 Stack

Stack is already implemented in STL.

To use Stack in STL:

```
1  #include <stack>
2  #include <cstdio>
3  using namespace std;
4
5  int main(){
6      stack<int> s;
7      s.push(2);
8      s.push(3);
9      printf("%d\n", s.top()); //3
10     s.pop();
11     printf("%d\n", s.top()); //2
12 }
```

### 2.3 Queue

To use Queue in STL:

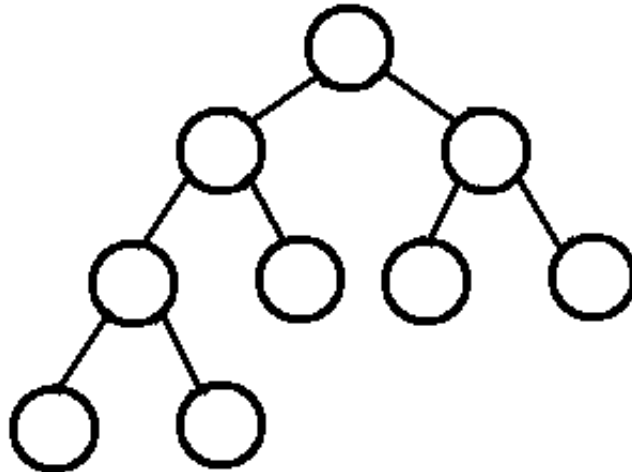
```

1  #include <queue>
2  #include <cstdio>
3  using namespace std;
4
5  int main(){
6      queue<int> que;
7      que.push(1);
8      que.push(2);
9      printf("%d\n", que.front()); //1
10     que.pop();
11     printf("%d\n", que.front()); //2
12 }

```

## 2.4 Depth-first Search (DFS)

We use a binary tree to illustrate DFS.



DFS starts from the root and goes all the way down to the leftmost leaf node, then returns back to the previous layer, travels through the second leaf node, then returns back to the previous layer, and so on.

DFS is usually implemented by recursion.

### E.g.1 Sum

You are given  $n$  integers  $a_1, \dots, a_n$ , determine if it is possible to choose some of them (each number can only be used once) so that their sum is  $k$ .

$$1 \leq n \leq 20, -10^8 \leq a_i \leq 10^8, -10^8 \leq k \leq 10^8$$

Since for each given number, we can choose to either take or not take, this is essentially searching through a binary tree.

```

1  const int MAX_N = 21;
2  int a[MAX_N];
3  int n, k;
4
5  bool dfs(int i, int sum){
6      // leaf node, note n not (n-1)
7      if(i==n) return sum == k;
8
9      // not take a[i]
10     if(dfs(i+1, sum)) return true;
11
12     // take a[i]
13     if(dfs(i+1, sum+a[i])) return true;
14
15     return false;
16 }
17
18 void solve(){
19     if(dfs(0, 0)) printf("YES");
20     else printf("NO");
21 }

```

Total possible cases (number of leaf nodes) is  $2^{n+1}$ , so complexity  $O(2^n)$ .

### **E.g.2 Lake Counting (POJ 2386)**

Given a  $N * M$  field, some areas some water after a rain ('W' : water, '.' : normal land). Connected areas with water (including diagonally adjacent) are counted as one puddle. Output the number of puddles in the field.

$N, M \leq 100$

Starting from one area with water, we can use DFS to find all areas with water connected with this area. We count the number such connected puddles while setting already counted areas to normal to avoid repetition.

```

1  const int MAX_N = 101;
2  int N, M;
3  char field[MAX_N][MAX_N];
4
5  void dfs(int x, int y){
6      // change this area to normal
7      field[x][y] = '.';
8
9      // check all 8 adjacent areas
10     for(int dx=-1; dx<=1; dx++){
11         for(int dy=-1; dy<=1; dy++){
12             int nx = x + dx, ny = y + dy;
13             if(nx>=0 && nx<N && ny>=0 && ny<M && field[nx][ny]=='W')
14                 dfs(nx, ny);
15         }
16     }
17 }
18
19 void solve(){
20     int res = 0;
21     for(int i=0; i<N; i++){
22         for(int j=0; j<M; j++){
23             if(field[i][j] == 'W'){
24                 dfs(i, j);
25                 res++;
26             }
27         }
28     }
29
30     printf("%d\n", res);
31 }

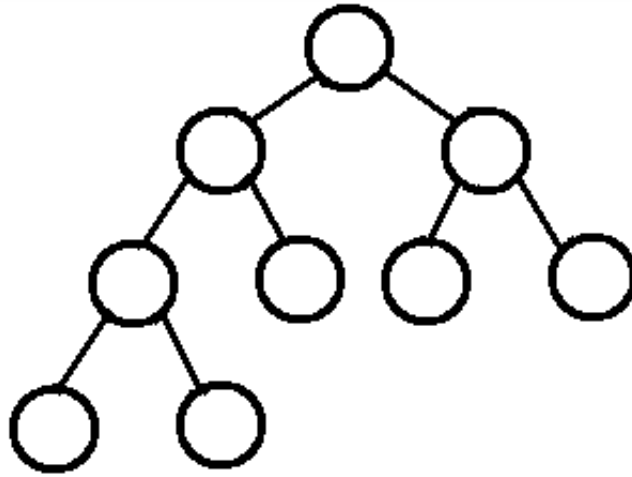
```

Since every area is only searched once (after once water is set to normal and won't be searched again), time complexity is  $O(N * M)$ .

## 2.5 Breadth-first Search (BFS)

We use a binary tree to illustrate BFS.





BFS searches from the nearest nodes to the farthest nodes. In the binary tree example, starting from the root, BFS first goes to the two nodes on the next layer which are the closest to it. Then it goes to the nodes on the third layer, and so on. BFS is usually implemented by queue.

### **E.g.1 Maze Runner**

You are given a  $N * M$  maze consisting of obstacles and normal lands. ('#' : obstacle, '.' : land, 'S': starting point, 'G': goal ). Each step you can move left, right, up or down. Find the minimum number of steps needed from starting point to the goal.

$N, M \leq 100$

```

1  const int MAX_N = 101;
2  const int INF = 9999999;
3
4  typedef pair<int, int> P;
5
6  char maze[MAX_N][MAX_N];
7  int N, M;
8  int sx, sy; //start pt
9  int gx, gy; //goal pt
10
11 int d[MAX_N][MAX_N];
12
13 int dx[4] = {1, 0, -1, 0}, dy[4] = {0, 1, 0, -1};
14
15 int bfs(){
16     queue<P> que;
17
18     for(int i=0; i<N; i++){
19         for(int j=0; j<M; j++){
20             d[i][j] = INF;
21         }
22     }
23

```

```

24     que.push(P(sx, sy));
25     d[sx][sy] = 0;
26
27     while(que.size()){
28         P cur = que.front();
29         que.pop();
30
31         if(cur.first==gx && cur.second==gy) break;
32
33         for(int i=0; i<4; i++){
34             int nx = cur.first + dx[i], ny = cur.second + dy[i];
35
36             // available and not visited
37             if(nx>=0 && nx<N && ny>=0 && ny<M && maze[nx][ny]!='#' && d[nx]
[nx][ny]==INF){
38                 que.push(P(nx, ny));
39                 d[nx][ny] = d[cur.first][cur.second] + 1;
40             }
41         }
42     }
43
44     return d[gx][gy];
45 }
46
47
48 void solve(){
49     int res = bfs();
50     printf("%d\n", res);
51 }

```

Each point in the maze has entered the queue **at most** once. Hence complexity is  $O(N * M)$ .

## 2.6 Pruning and Backtracking

In DFS, if at a certain state we realize that this state will definitely not generate a correct answer, then we do not need to continue with this state any more, we can just search the next possible state instead. This is called pruning.

Usually DFS is used to search for solution over a tree structure. Generally, this algorithm can be used to search over any problem space and it is called backtracking.

Example: Find all permutations of N numbers

```

1  int total = 0;  //#permutations
2  const int N = 4;  //use 4 as an example
3  int numbers[N], used[N], res[N];
4
5  void permutate(int ith){
6      if(ith==N){
7          for(int i=0; i<N; i++){
8              cout<<res[i];
9          }
10         cout<<endl;
11         total++;
12         return;
13     }
14
15     // find availble numbers
16     for(int i=0; i<N; i++){
17         if(!used[i]){
18             res[ith] = nums[i];
19             used[i] = 1;
20             permutate(ith+1);
21             //set free for future use
22             used[i]=0;
23         }
24     }
25 }
26
27 int main(){
28     for(int i=0; i<N; i++){
29         cin>>nums[i];
30     }
31     memset(used, 0, sizeof(used));
32     permutate(0);
33     cout<<total;
34 }

```

For permutation, it might be easier to directly use next\_permutation function. Note that you should use do while in this case, otherwise you will miss the original array case.

Example: next\_permutation

```

1  #include <algorithm>
2  #include <iostream>
3  using namespace std;
4
5  const int N = 4;
6  int nums[N] = {1, 2, 3, 4}, total=0;
7
8  int main(){
9      do{
10         total++;
11         for(int i=0; i<N; i++){
12             cout<<nums[i];
13         }
14         cout<<endl;
15     }while(next_permutation(nums, nums+N));
16     cout<<total; //24
17 }

```

(Practice list: refer to the recommended repo)

### 3. Greedy Algorithm

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In greedy algorithm, we choose the current best solution at each step.

#### E.g.1 Job Arrangement

There are  $n$  jobs, each job starts from time  $s_i$  and ends at time  $t_i$ . If you choose a job, you must not do any other jobs during its full period (including  $s_i$  and  $t_i$ ). Find the maximum number of jobs you can do.

$$1 \leq N \leq 10^5, 1 \leq s_i \leq t_i \leq 10^9$$

Intuition: we want to finish the current job as early as possible so that we have more time for other jobs. Every time we choose the job with the earliest ending time and not clashing with previously chosen jobs.

```

1  const int MAX_N = 100002;
2
3  int N, S[MAX_N], T[MAX_N];
4
5  pair<int, int> jobs[MAX_N];
6
7  void solve(){
8      // sorts the first element in pair by default
9      // should sort by end time
10     for(int i=0; i<N; i++){
11         jobs[i].first = T[i];
12         jobs[i].second = S[i];
13     }
14
15     sort(jobs, jobs+N);
16
17     // t: end time of prev chosen job
18     int ans=0, t=0;
19     for(int i=0; i<N; i++){
20         if(t < jobs[i].second){
21             ans++;
22             t = jobs[i].first;
23         }
24     }
25
26     printf("%d\n", ans);
27 }

```

Rigorous proofs of the correctness of the algorithm are possible but will not be covered here.

### **E.g.2 Smallest String (POJ 3617)**

Given a string  $S$  with length  $N$  (all characters are uppercase), and an empty string  $T$ . Everytime you can either remove the first or last character from  $S$  and append to the end of  $T$ . Construct the  $T$  with the minimum alphabetic order.

$$1 \leq N \leq 2000$$

Intuition: everytime choose the smaller character from the first and last character of  $S$ . If they are the same, compare the next character, do so until there is a difference (if all equal then doesn't matter).

```

1  const int MAX_N = 2002;
2  int N;
3  char S[MAX_N + 1];
4
5  void solve(){
6      int count = 0;
7      int a = 0, b = N - 1;
8
9      while(a<=b){
10         bool left = false;
11
12         for(int i=0; a+i<=b-i; i++){
13             if(S[a+i] < S[b-i]){
14                 left = true;
15                 break;
16             }
17             else if(S[a+i] > S[b-i]){
18                 left = false;
19                 break;
20             }
21         }
22
23         if(left) putchar(S[a++]);
24         else putchar(S[b--]);
25         count++;
26         if(count%80==0) putchar('\n');
27     }
28 }

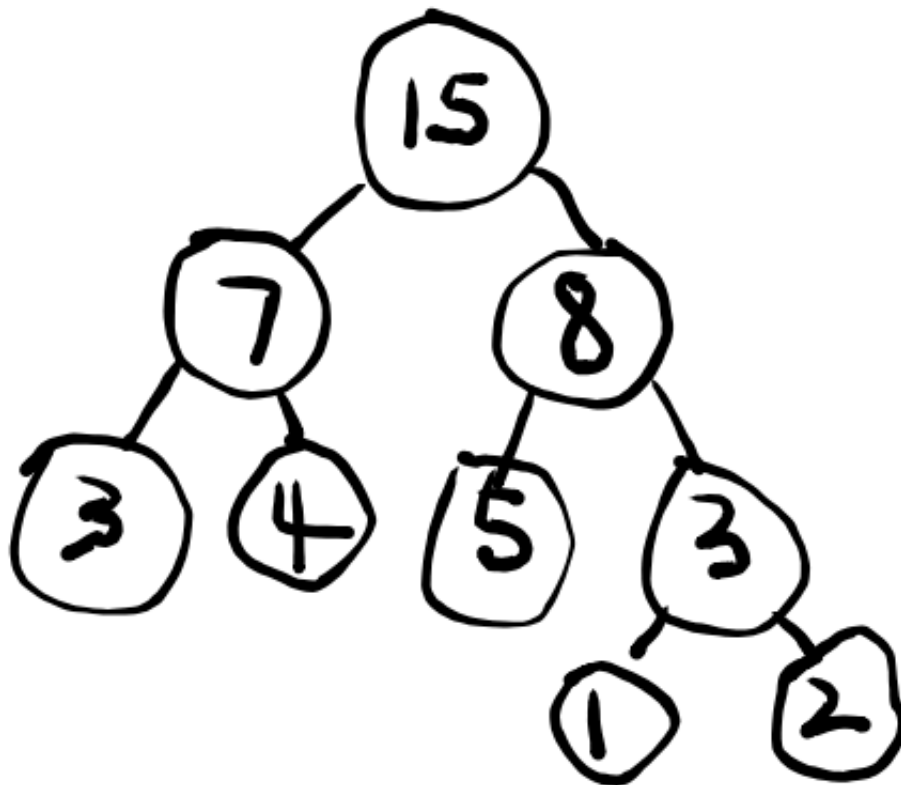
```

### **E.g.3 Fence Repair (POJ 3253)**

You need to cut a board into  $N$  pieces, with lengths  $L_1, \dots, L_N$ . The sum of all the cut boards should be the same of the original board. The cost of cutting a board into 2 pieces equals to the length of the board. For example, if you want to cut a board with length 21 into boards with lengths 5, 8, 8, you can first cut it into 13 and 8 (cost: 21), then cut 12 into 5 and 8 (cost: 13).

Find the minimum cost of cutting the board.

$$1 \leq N \leq 2 * 10^4, 0 \leq L_i \leq 5 * 10^4$$



Intuition: Cutting the board is like splitting the node into two child nodes. The total cost is the sum of all non-leaf nodes, which also equals to the sum of (leaf node value)\*(leaf node depth). Therefore, to get minimum total cost, we want the least value leaf nodes to have the largest depth.

Suppose we already have the cut boards  $L_1, \dots, L_N$ , then the shortest and second shortest board (suppose they are  $L_1, L_2$ ) should be brothers (note it is impossible for a node to have only one child node) and from the same parent node. Then we replace them with  $(L_1 + L_2)$  and continue the process until there is only one board left.

```

1  typedef long long ll;
2
3  int N, L[MAX_N];
4
5  void solve(){
6      ll ans = 0;
7
8      while(N > 1){
9          int min1=0, min2=1;
10         // min1: shortest, min2: second shortest
11         if(L[min1] > L[min2]) swap(min1, min2);
12
13         for(int i=2; i<N; i++){
14             if(L[i] < L[min1]){
15                 min2 = min1;
16                 min1 = i;
17             }
18             else if(L[i] < L[min2]){
19                 min2 = i;
20             }
21         }
22
23         int t = L[min1] + L[min2];
24         ans += t;
25
26         // replace min1 with t
27         // swap min2 with last ele and del it
28         if(min1 == N-1) swap(min1, min2);
29         L[min1] = t;
30         L[min2] = L[N-1];
31         N--;
32     }
33
34     printf("%lld\n", ans);
35 }

```

This can be further improved with priority queue (every time pop two front, push their sum).

(TODO: more examples from POJ)

## 4. Dynamic Programming

---



There are two approaches, top-down (recursion), bottom-up (iteration). I find it best to explain DP with examples. Most examples I list here are must-know for NOI.

### **E.g.1 0-1 Knapsack**

You have  $n$  items each with weight  $w_i$  and value  $v_i$ . Your bag has max weight capacity  $W$ . Find the max value of items that can be put in the bag.

$$1 \leq n \leq 100, 1 \leq w_i, v_i \leq 100, 1 \leq W \leq 10^4$$

Let  $dp(i, j)$  denote the max value the bag can have using only the first  $i$  items and with capacity  $j$ .

For each item, we either take or do not take (if capacity). So we can just choose the max from those two options.

Top-down: recursion with memoisation

```
1  const int MAX_N = 102;
2  const int MAX_W = 10002;
3
4  int dp[MAX_N][MAX_W];
5
6  int rec(int i, int j){
7      if(dp[i][j]>=0){
8          return dp[i][j];
9      }
10
11     int res;
12     // end case
13     if(i==0){
14         res = 0;
15     }
16     // can't take w[i]
17     else if(j < w[i]){
18         res = rec(i-1, j);
19     }
20     // j>=w[i]
21     else{
22         res = max(rec(i-1, j), rec(i-1, j-w[i])+v[i]);
23     }
24
25     return dp[i][j]=res;
26 }
27
28 void solve(){
29     memset(dp, -1, sizeof(dp));
30     printf("%d\n", rec(N, W));
31 }
```

In the bottom-up approach, we fill up the dp table in order.

(Note: sometimes I start from index 1 when inputting data.)

```
1  int dp[MAX_N][MAX_W];
2
3  void solve(){
4      // no item or no capacity: 0
5      memset(dp, 0, sizeof(dp));
6
7      for(int i=1; i<=N; i++){
8          for(int j=1; j<=W; j++){
9              if(j < W[i]){
10                 dp[i][j] = dp[i-1][j];
11             }
12             else{
13                 dp[i][j] = max(dp[i-1][j], dp[i-1][j-w[i]]+v[i]);
14             }
15         }
16     }
17 }
```

Complexity:  $O(nW)$

We can see that the most important part of DP is to identify the subproblem states and update equations.

In this problem, the subproblem state is the range of items available and the capacity. The update equations can then be deduced easily.

We can save some space by using a rolling array.

```
1  int dp[MAX+W + 1];
2
3  void solve(){
4      for(int i=1; i<=n; i++){
5          for(int j=W; j>=w[i]; j--){
6              dp[j] = max(dp[j], dp[j-w[i]]+v[i]);
7          }
8      }
9      printf("%d\n", dp[W]);
10 }
```

Note that we need to go from right to left in the inner loop in order to use the values from previous  $i$ .

### E.g.2 Longest Common Subsequence (LCS)

Find the length of the longest common subsequence of two string. For example, the LCS of 'abcd' and 'beed' is 'bcd'.

String length:  $1 \leq n, m \leq 1000$

Let  $dp(i, j)$  denote the length of LCS of substrings  $s_1 \dots s_i$  and  $t_1 \dots t_j$ .

If  $s_i = t_j$ :  $dp(i, j) = \max(dp(i-1, j-1)+1, dp(i-1, j), dp(i, j-1))$

Else:  $dp(i, j) = \max(dp(i-1, j), dp(i, j-1))$

```
1  int n, m;
2  char s[MAX_N], t[MAX_M];
3
4  int dp[MAX_N+1][MAX_M+1];
5
6  void solve(){
7      memset(dp, 0, sizeof(dp));
8      for(int i=1; i<=n; i++){
9          cin>>s[i];
10     }
11     for(int i=1; i<=m; i++){
12         cin>>t[i];
13     }
14
15     for(int i=1; i<=MAX_N; i++){
16         for(int j=1; j<=MAX_M; j++){
17             dp[i][j] = max(dp[i-1][j], dp[i][j-1]);
18             if(s[i]==t[j]){
19                 dp[i][j] = max(dp[i][j], dp[i-1][j], dp[i][j-1]);
20             }
21         }
22     }
23
24     cout<<dp[n][m];
25 }
```

### E.g.3 Unbounded Knapsack

You have  $n$  types of items each with weight  $w_i$  and value  $v_i$ . Your bag has max wieght capacity  $W$ . Find the max value of items that can be put in the bag. Note that you can take unlimited number of copies of each type of item.

$1 \leq n \leq 100, 1 \leq w_i, v_i \leq 100, 1 \leq W \leq 10^4$

In this case, we need to add another inner loop to find the best number of copies to take within the capacity.

```

1  int dp[MAX_N + 1][MAX_W + 1];
2
3  void solve(){
4      memset(dp, 0, sizeof(dp));
5
6      for(int i=1; i<=n; i++){
7          for(int j=1; j<=W; j++){
8              for(int k=0; k*w[i]<=j; k++){
9                  dp[i][j] = max(dp[i][j], dp[i-1][j - k*w[i]] + k*v[i]);
10             }
11         }
12     }
13     printf("%d\n", dp[n][W]);
14 }

```

Complexity:  $O(nW^2)$

We can further improve this algorithm. Note that choosing  $k$  in  $dp[i][j]$  is the same as choosing  $(k - 1)$  in  $dp[i][j - w[i]]$  (take one copy of  $i$ th item). Hence we can use this to reduce repeated calculation.

$dp[i][j]$

$= \max\{dp[i - 1][j - k * w[i]] + k * v[i] | k \geq 0\}$

$= \max(dp[i][j], \max\{dp[i - 1][j - k * w[i]] + k * v[i] | k \geq 1\})$  (either not take or take at least one)

$= \max(dp[i][j], \max\{dp[i - 1][(j - w[i]) - k * w[i]] + k * v[i] | k \geq 0\})$  (take out one from  $k$ )

$= \max(dp[i][j], dp[i][j - w[i]] + v[i])$

(This can come from observation and intuition as well.)

```

1 void solve(){
2     memset(dp, 0, sizeof(dp));
3
4     for(int i=1; i<=n; i++){
5         for(int j=1; j<=W; j++){
6             if(j<w[i]){
7                 dp[i][j] = dp[i-1][j];
8             }
9             else{
10                dp[i][j] = max(dp[i-1][j], dp[i][j-w[i]]+v[i]);
11            }
12        }
13    }
14    printf("%d\n", dp[n][W]);
15 }

```

This can also be improved by using a rolling array.

```

1 int dp[MAX_W + 1];
2
3 void solve(){
4     memset(dp, 0, sizeof(dp));
5
6     for(int i=1; i<=n; i++){
7         for(int j=w[i]; j<=W; j++){
8             dp[j] = max(dp[j], dp[j-w[i]]+v[i]);
9         }
10    }
11
12    printf("%d\n", dp[W]);
13 }

```

Note that in the inner loop we go from left to right to use the computed values at this  $i$  iteration.

### **E.g.4 0-1 Knapsack 2**

You have  $n$  items each with weight  $w_i$  and value  $v_i$ . Your bag has max wieght capacity  $W$ . Find the max value of items that can be put in the bag.

$$1 \leq n \leq 100, 1 \leq w_i \leq 10^7, 1 \leq v_i \leq 100, 1 \leq W \leq 10^9$$

The difference of this problem with the first 0-1 knapsack is that the range for  $w_i$  and  $W$  become much larger and  $O(nW)$  will get TLE.

