

Radix64

- Base64

Visual Character 64					
i	1	2	3	4	5
	M	u	h	a	m
ASCII	77	117	104	97	109
Bit Pattern	01001101	01110101	01101000	01100001	01101101
	010011	01		011000	01
		0111	101000		0110
		0101	01		1101
Index	19	23	21	40	24
radix64	T	X	V	o	Y

Extended Euclidean Algorithm (EEA)

Extended Euclidean Algorithm

i	$b =$	a^*	q	$+$	r	u	v	w
0	100	7	14		2	0	1	-14
1	7	2	3		1	1	-14	43
2	2	1	2		0	-14	43	-100
					a^{-1}	43	a^*a^{-1}	$301 \equiv 1 \pmod{b}$

Irreducible Polynomials

Let an irreducible polynomial $m = 283_{10} = 256+16+8+2+1=100011011_2 = 11B_{16}$

In polynomial term, this irreducible polynomial $m(x) = x^8 + x^4 + x^3 + x + 1$.

Euclidean Algorithm				Extended		
$b =$	$a \cdot$	$q +$	r	u	v	$w=u-v \cdot q$
283	42	6	31	0	1	-6
42	31	1	11	1	-6	7
31	11	2	9	-6	7	-20
11	9	1	2	7	-20	27
9	2	4	1	-20	27	-128
2	1	2	0	27	-128	283

$$a^{-1} \bmod b = -128 + 283 = 155.$$

We always check $a \cdot a^{-1} \equiv 1 \pmod{b}$

$$42 \cdot 155 = 6510 = 23 \cdot 283 + 1 \equiv 1 \pmod{283}$$

AES S-Box

$$a^{-1} = D9_{16} = 11011001_2 \text{ (Inversekan urutan)}$$

$$b(x) = x^8 + x^4 + x^3 + x + 1 = 100011011_2 = 11B_{16}$$

$$\begin{bmatrix} b'_0 \\ b'_1 \\ b'_2 \\ b'_3 \\ b'_4 \\ b'_5 \\ b'_6 \\ b'_7 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 & 1 & 1 & 1 & 1 \\ 1 & 1 & 0 & 0 & 0 & 1 & 1 & 1 \\ 1 & 1 & 1 & 0 & 0 & 0 & 1 & 1 \\ 1 & 1 & 1 & 1 & 0 & 0 & 0 & 1 \\ 0 & 1 & 1 & 1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 1 & 1 & 1 & 1 \end{bmatrix} \cdot \begin{bmatrix} 1 \\ 0 \\ 0 \\ 1 \\ 0 \\ 1 \\ 1 \\ 1 \end{bmatrix} + \begin{bmatrix} 1 \\ 1 \\ 0 \\ 0 \\ 0 \\ 1 \\ 1 \\ 0 \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \\ 1 \\ 1 \\ 1 \\ 0 \\ 1 \\ 0 \end{bmatrix} + \begin{bmatrix} 1 \\ 1 \\ 0 \\ 0 \\ 1 \\ 1 \\ 1 \\ 0 \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \\ 1 \\ 1 \\ 1 \\ 1 \\ 0 \\ 0 \end{bmatrix}$$

xor-kan nombor yang highlighted

$$= 00111101 = 3D_{16}$$