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WEEK 14

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# Relational Algebra and SQL

## (Set Operation)

# Objectives

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- ◆ Relational Algebra on Set Operation:  
(Union, Difference and Intersection)
- ◆ SQL on Union, Difference and Intersection
- ◆ Sub-query and Nested queries.

# Relational Algebra Operations

Selection

Projection

$P$ 
 $Q$ 
 $=$ 
 $P \times Q$

$a$
$b$

1
2
3

$a$	1
$a$	2
$a$	3
$b$	1
$b$	2
$b$	3

Cartesian product

$T$

$A$	$B$
$a$	1
$b$	2

$U$

$B$	$C$
1	$x$
1	$y$
3	$z$

$T \bowtie U$

$A$	$B$	$C$
$a$	1	$x$
$a$	1	$y$

Natural join

$T \bowtie_B U$

$A$	$B$
$a$	1

Semijoin

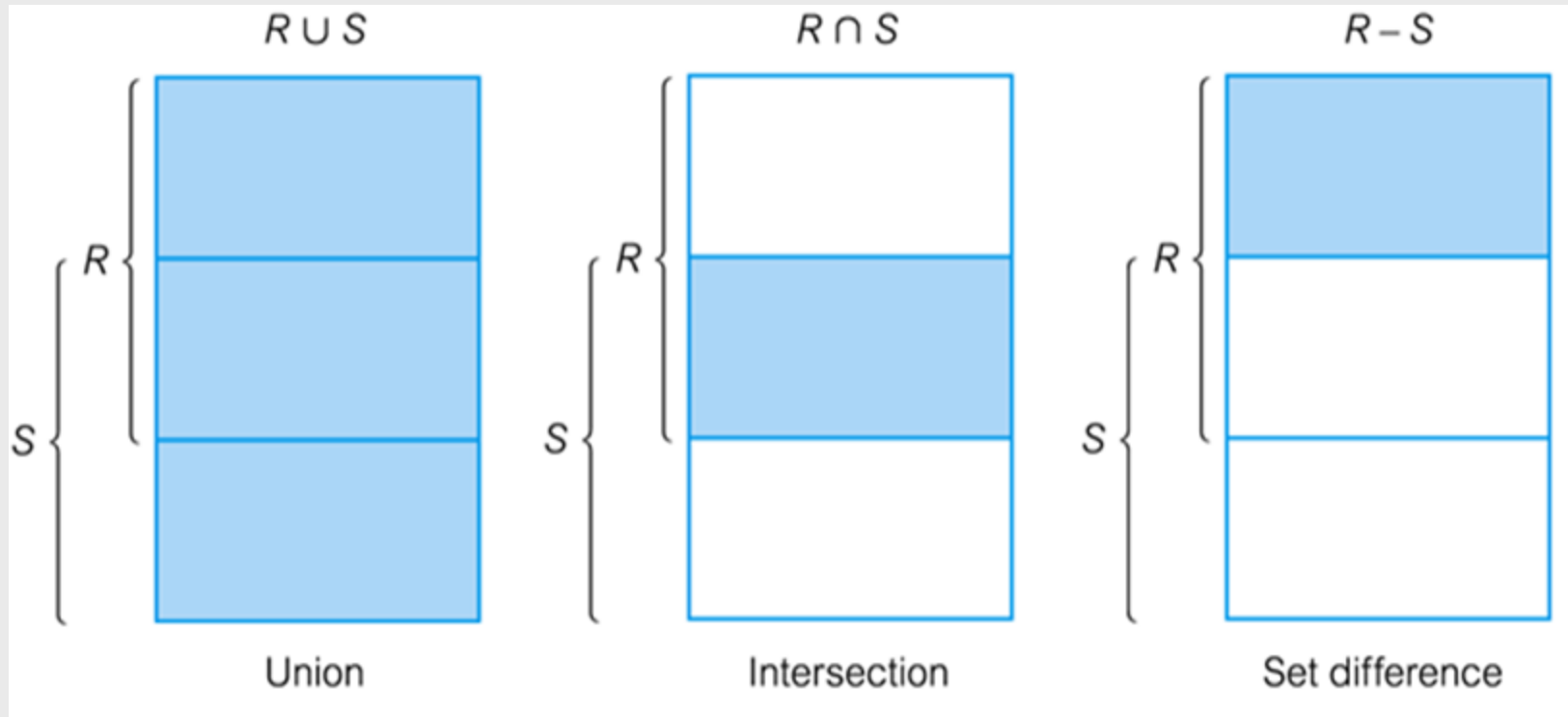
$T \bowtie_c U$

$A$	$B$	$C$
$a$	1	$x$
$a$	1	$y$
$b$	2	

Left Outer join

# Relational Algebra Operations

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# Union

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## ◆ $R \cup S$

- Union of two relations  $R$  and  $S$  defines a relation that contains all the tuples of  $R$ , or  $S$ , or both  $R$  and  $S$ , duplicate tuples being eliminated.
  - $R$  and  $S$  must be union-compatible.
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- ◆ If  $R$  and  $S$  have  $I$  and  $J$  tuples, respectively, union is obtained by concatenating them into one relation with a maximum of  $(I + J)$  tuples.

## Example - Union

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- ◆ List all cities where there is either a branch office or a property for rent.

$$\Pi_{\text{city}}(\text{Branch}) \cup \Pi_{\text{city}}(\text{PropertyForRent})$$

city
London
Aberdeen
Glasgow
Bristol

# Set Difference

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## ◆ $R - S$

- Defines a relation consisting of the tuples that are in relation  $R$ , but not in  $S$ .
- $R$  and  $S$  must be union-compatible.

## Example - Set Difference

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- ◆ List all cities where there is a branch office but no properties for rent.

$$\Pi_{\text{city}}(\text{Branch}) - \Pi_{\text{city}}(\text{PropertyForRent})$$

city
Bristol



# Intersection

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## ◆ $R \cap S$

- Defines a relation consisting of the set of all tuples that are in both  $R$  and  $S$ .
- $R$  and  $S$  must be union-compatible.

## ◆ Expressed using basic operations:

$$R \cap S = R - (R - S)$$

## Example - Intersection

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- ◆ List all cities where there is both a branch office and at least one property for rent.

$\Pi_{\text{city}}(\text{Branch}) \cap \Pi_{\text{city}}(\text{PropertyForRent})$

city
Aberdeen
London
Glasgow

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# SQL on Union, Intersection and Difference

## Example : SQL on UNION

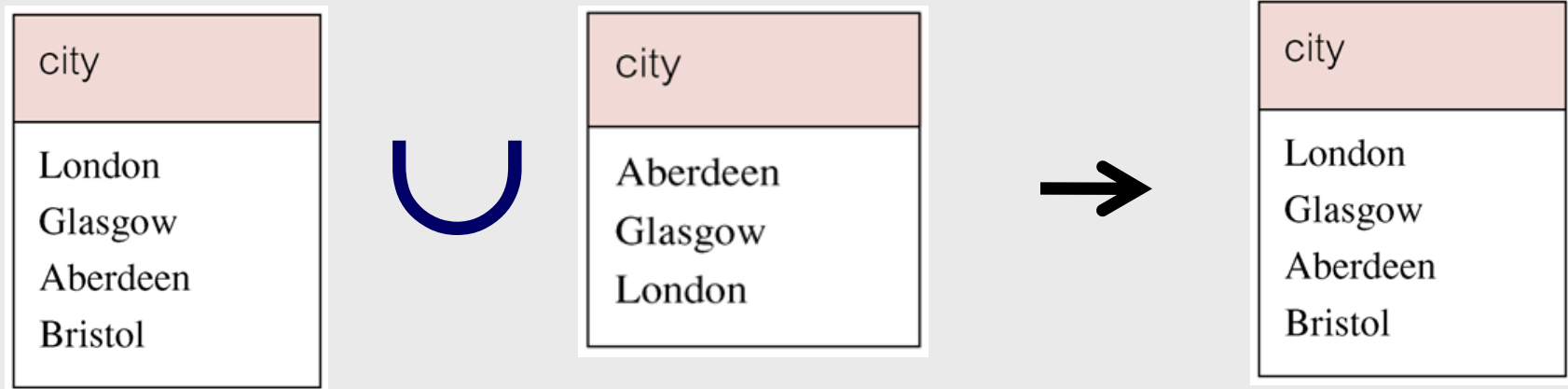
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List all cities where there is either a branch office or a property.

(SELECT city FROM Branch)

UNION

(SELECT city FROM PropertyForRent);



## Example : SQL on INTERSECTION

List all cities where there is both a branch office and a property.

(SELECT city FROM Branch)

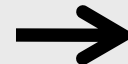
**INTERSECT**

(SELECT city FROM PropertyForRent);

city
London
Glasgow
Aberdeen
Bristol



city
Aberdeen
Glasgow
London



city
Aberdeen
Glasgow
London

## Example : SQL on **DIFFERENCE**

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List of all cities where there is a branch office but no properties.

(SELECT city FROM Branch)

**MINUS**

(SELECT city FROM PropertyForRent);

