

Lets consider (age)

{youth, middle-age}, {youth, senior}, {senior, middle-age}.

$$gini_{age \in \{youth, middle-age\}}(D) = \left(\frac{2}{14}\right) gini(D_1) + \frac{5}{14} gini(D_2)$$

$$= \frac{2}{14} \left(1 - \left(\frac{6}{7}\right)^2 - \left(\frac{3}{7}\right)^2\right) + \frac{5}{14} \left(1 - \left(\frac{3}{5}\right)^2 - \left(\frac{2}{5}\right)^2\right)$$

$$= 0.4571$$

$$= gini_{age \in \{senior\}}(D)$$

$$gini_{age \in \{youth, senior\}}(D) = \frac{10}{14} \left(1 - \left(\frac{5}{10}\right)^2 - \left(\frac{5}{10}\right)^2\right) + \frac{4}{14} \left(1 - \left(\frac{4}{4}\right)^2 - \left(\frac{0}{4}\right)^2\right)$$

$$= 0.3571$$

$$= gini_{age \in \{middle-aged\}}(D)$$

$$gini_{age \in \{middle-aged, senior\}}(D) = \frac{2}{14} \left(1 - \left(\frac{7}{9}\right)^2 - \left(\frac{2}{9}\right)^2\right) - \frac{5}{14} \left(1 - \left(\frac{2}{5}\right)^2 - \left(\frac{3}{5}\right)^2\right)$$

$$= 0.3236$$

$$= gini_{age \in \{youth\}}(D)$$

Let's consider {student}

binary attribute.

$$\text{gini}_{\text{student}}(D) = \frac{7}{14} \left(1 - \left(\frac{6}{7} \right)^2 - \left(\frac{1}{7} \right)^2 \right) + \frac{7}{14} \left(1 - \left(\frac{3}{7} \right)^2 - \left(\frac{4}{7} \right)^2 \right)$$

$$= .3673$$

Similarly, {~~age~~

$$\text{gini}_{\text{credit-rating}}(D) = .4285$$

Reduction of impurity

$$\text{age} \rightarrow .459 - .3571 = .1019$$

$$\text{income} \rightarrow .459 - .4428 = .0162$$

$$\text{student} \rightarrow .459 - .3673 = .0917$$

$$\text{credit-rating} \rightarrow .459 - .4285 = .0305$$