



Machine Learning

CSE - 465

Lecture - 10

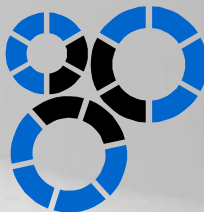


Lecture 10

Classifier Performance Evaluation

Outline

- Model evaluation & selection
- Evaluating classifier accuracy
- Metrics for evaluating classifier performance
 - Confusion matrix
- Plotting an ROC curve



◉ Model Evaluation & Selection

- How can we measure accuracy?
 - Use **test set** of class-labeled tuples instead of training set when assessing accuracy
- Methods for estimating a classifier's accuracy:
 - Holdout method, random sub-sampling
 - Cross-validation
 - Bootstrap
- Comparing classifiers:
 - Confidence intervals
 - Cost-benefit analysis and ROC Curves

◉ Evaluating Classifier Accuracy

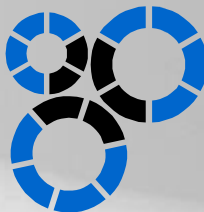
- **Holdout method**

- Given data is randomly partitioned into two independent sets
 - Training set (e.g., $2/3$) for model construction
 - Test set (e.g., $1/3$) for accuracy estimation
- **Random sampling:** a variation of holdout
 - Repeat holdout k times, accuracy = avg. of the accuracies obtained

◉ Evaluating Classifier Accuracy

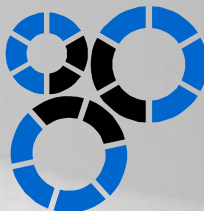
- **Cross-validation**

- In k-fold cross-validation, the initial data are randomly partitioned into k mutually exclusive subsets or “folds,” D_1, D_2, \dots, D_k , each of approximately equal size. Training and testing is performed k times. In iteration i , partition D_i is reserved as the test set, and the remaining partitions are collectively used to train the model. That is, in the first iteration, subsets D_2, \dots, D_k collectively serve as the training set to obtain a first model, which is tested on D_1 ; the second iteration is trained on subsets D_1, D_3, \dots, D_k and tested on D_2 ; and so on.



Metrics for Evaluating Classifier Performance

- True positives (TP)
 - These refer to the positive tuples that were correctly labeled by the classifier. Let TP be the number of true positives.
- True negatives(TN)
 - These are the negative tuples that were correctly labeled by the classifier. Let TN be the number of true negatives.





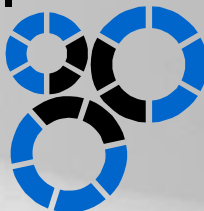
Metrics for Evaluating Classifier Performance

- False positives (FP)

- These are the negative tuples that were incorrectly labeled as positive (e.g., tuples of class buys computer = no for which the classifier predicted buys computer = yes). Let FP be the number of false positives.

- False negatives (FN)

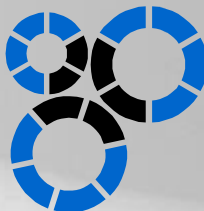
- These are the positive tuples that were mislabeled as negative (e.g., tuples of class buys computer = yes for which the classifier predicted buys computer = no). Let FN be the number of false negatives.



Metrics for Evaluating Classifier Performance

- Confusion Matrix

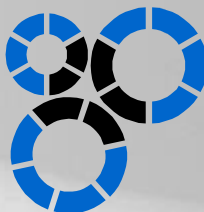
- A confusion matrix (also known as an error matrix) is a table that is often used to describe the performance of a classification model (or classifier) on a set of test data for which the true values are known. It allows the visualization of the performance of an algorithm
- A confusion matrix is a summary of prediction results on a classification problem. The number of correct and incorrect predictions are summarized with count values and broken down by each class. This is the key to the confusion matrix.



Metrics for Evaluating Classifier Performance

- Confusion Matrix

- The confusion matrix shows the ways in which your classification model is confused when it makes predictions
- It gives us insight not only into the errors being made by a classifier but more importantly the types of errors that are being made
- TP and TN tell us when the classifier is getting things right, while FP and FN tell us when the classifier is getting things wrong





Metrics for Evaluating Classifier Performance

Confusion Matrix

	Predicted class		Total
	<i>yes</i>	<i>no</i>	
Actual class	<i>yes</i>	<i>TP</i> <i>FN</i>	<i>P</i>
	<i>no</i>	<i>FP</i> <i>TN</i>	<i>N</i>
Total	<i>P'</i>	<i>N'</i>	<i>P + N</i>

<i>Classes</i>	<i>buys_computer = yes</i>	<i>buys_computer = no</i>	<i>Total</i>
<i>buys_computer = yes</i>	6954	46	7000
<i>buys_computer = no</i>	412	2588	3000
Total	7366	2634	10,000



Metrics for Evaluating Classifier Performance

<i>Measure</i>	<i>Formula</i>
accuracy, recognition rate	$\frac{TP + TN}{P + N}$
error rate, misclassification rate	$\frac{FP + FN}{P + N}$
sensitivity, true positive rate, recall	$\frac{TP}{P}$
specificity, true negative rate	$\frac{TN}{N}$
precision	$\frac{TP}{TP + FP}$
F , F_1 , F -score, harmonic mean of precision and recall	$\frac{2 \times \text{precision} \times \text{recall}}{\text{precision} + \text{recall}}$
F_β , where β is a non-negative real number	$\frac{(1 + \beta^2) \times \text{precision} \times \text{recall}}{\beta^2 \times \text{precision} + \text{recall}}$

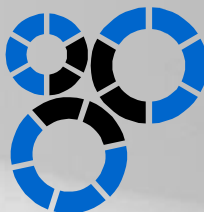


Plotting an ROC curve

<i>Tuple #</i>	<i>Class</i>	<i>Prob.</i>	<i>TP</i>	<i>FP</i>	<i>TN</i>	<i>FN</i>	<i>TPR</i>	<i>FPR</i>
1	<i>P</i>	0.90	1	0	5	4	0.2	0
2	<i>P</i>	0.80	2	0	5	3	0.4	0
3	<i>N</i>	0.70	2	1	4	3	0.4	0.2
4	<i>P</i>	0.60	3	1	4	2	0.6	0.2
5	<i>P</i>	0.55	4	1	4	1	0.8	0.2
6	<i>N</i>	0.54	4	2	3	1	0.8	0.4
7	<i>N</i>	0.53	4	3	2	1	0.8	0.6
8	<i>N</i>	0.51	4	4	1	1	0.8	0.8
9	<i>P</i>	0.50	5	4	0	1	1.0	0.8
10	<i>N</i>	0.40	5	5	0	0	1.0	1.0

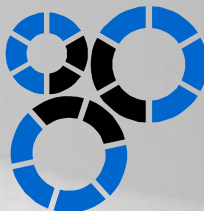
Plotting an ROC curve

- Receiver Operating Characteristics Curve
- The figure shows the probability value (column 3) returned by a probabilistic classifier for each of the 10 tuples in a test set, sorted by decreasing probability order. Column 1 is merely a tuple identification number, which aids in our explanation. Column 2 is the actual class label of the tuple. There are five positive tuples and five negative tuples, thus $P = 5$ and $N = 5$. As we examine the known class label of each tuple, we can determine the values of the remaining columns, TP, FP, TN, FN, TPR, and FPR.



Plotting an ROC curve

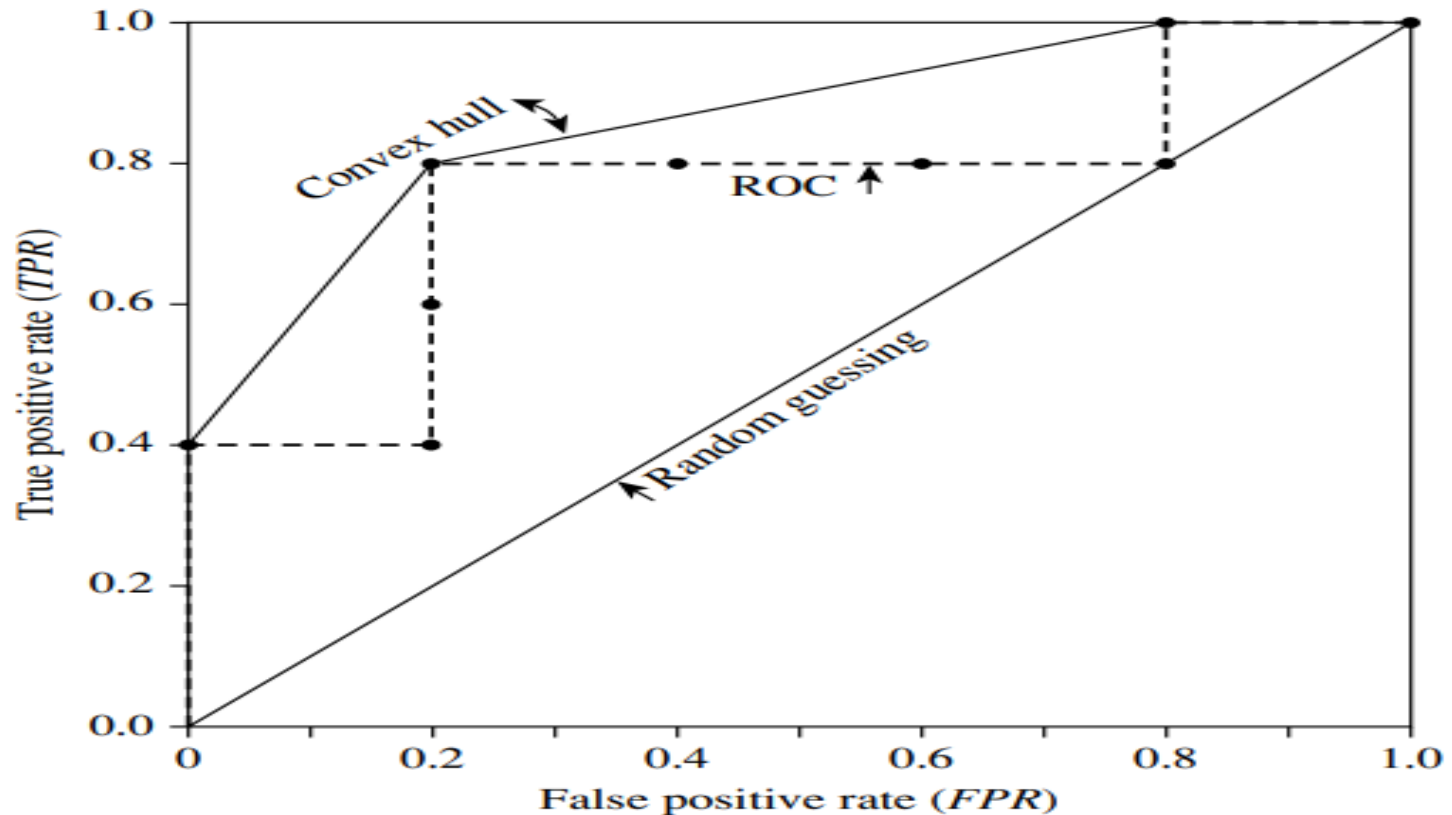
- We start with tuple 1, which has the highest probability score, and take that score as our threshold, that is, $t = 0.9$. Thus, the classifier considers tuple 1 to be positive, and all the other tuples are considered negative. Since the actual class label of tuple 1 is positive, we have a true positive, hence $TP = 1$ and $FP = 0$.
- Among the remaining nine tuples, which are all classified as negative, five actually are negative (thus, $TN = 5$). The remaining four are all actually positive, thus, $FN = 4$. We can therefore compute $TPR = TP/P = 1/5 = 0.2$, while $FPR = 0$. Thus, we have the point $(0.2, 0)$ for the ROC curve.



Plotting an ROC curve

- Next, threshold t is set to 0.8, the probability value for tuple 2, so this tuple is now also considered positive, while tuples 3 through 10 are considered negative. The actual class label of tuple 2 is positive, thus now $TP = 2$. The rest of the row can easily be computed, resulting in the point (0.4,0).
- Next, we examine the class label of tuple 3 and let t be 0.7, the probability value returned by the classifier for that tuple. Thus, tuple 3 is considered positive, yet its actual label is negative, and so it is a false positive. Thus, TP stays the same and FP increments so that $FP = 1$. The rest of the values in the row can also be easily computed, yielding the point (0.4,0.2).

Plotting an ROC curve





Thank You

