

ROC & AUC

Precision or Recall?

| Data | Accuracy | Precision | Recall |
|---------------------|----------|-----------|--------|
| 1 1 1 1 1 0 1 0 1 1 | | | |
| 1 1 1 1 1 0 1 0 1 1 | 80% | 0% | 0% |
| 1 1 0 1 1 1 1 0 1 1 | 80% | 50% | 50% |
| 1 1 0 0 1 0 1 0 1 0 | 70% | 40% | 100% |

1: Not fraud
0: Fraud

Accuracy = correctly classified/total data

Precision = Actually positive among predicted positive / totally positive prediction

Recall = Correctly predicted positive among actually positive /Actually positive

ROC

| X | Y | Y(T0) | Y(T3) | Y(T5) | Y(T6.5) | Y(T9.5) |
|---|---|-------|-------|-------|---------|---------|
| 1 | 0 | 1 | 0 | 0 | 0 | 0 |
| 4 | 0 | 1 | 1 | 0 | 0 | 0 |
| 5 | 0 | 1 | 1 | 0 | 0 | 0 |
| 6 | 1 | 1 | 1 | 1 | 0 | 0 |
| 7 | 1 | 1 | 1 | 1 | 1 | 0 |
| 9 | 1 | 1 | 1 | 1 | 1 | 0 |

| P/A (T0) | 1 | 0 |
|----------|---|---|
| 1 | 3 | 0 |
| 0 | 3 | 0 |

$$\text{TPR} = \text{TP} / (\text{TP} + \text{FN}) = 3 / (3 + 0) = 1$$

$$\text{FPR} = \text{FP} / (\text{FP} + \text{TN}) = 3 / (3 + 0) = 1$$

ROC

| X | Y | Y(T0) | Y(T3) | Y(T5) | Y(T6.5) | Y(T9.5) |
|---|---|-------|-------|-------|---------|---------|
| 1 | 0 | 1 | 0 | 0 | 0 | 0 |
| 4 | 0 | 1 | 1 | 0 | 0 | 0 |
| 5 | 0 | 1 | 1 | 0 | 0 | 0 |
| 6 | 1 | 1 | 1 | 1 | 0 | 0 |
| 7 | 1 | 1 | 1 | 1 | 1 | 0 |
| 9 | 1 | 1 | 1 | 1 | 1 | 0 |

| P/A (T3) | 1 | 0 |
|----------|---|---|
| 1 | 3 | 0 |
| 0 | 2 | 1 |

$$\text{TPR} = \text{TP} / (\text{TP} + \text{FN}) = 3 / (3 + 0) = 1$$

$$\text{FPR} = \text{FP} / (\text{FP} + \text{TN}) = 2 / (2 + 1) = 0.67$$

ROC

| X | Y | Y(T0) | Y(T4.5) | Y(T5) | Y(T6.5) | Y(T9.5) |
|---|---|-------|---------|-------|---------|---------|
| 1 | 0 | 1 | 0 | 0 | 0 | 0 |
| 4 | 0 | 1 | 0 | 0 | 0 | 0 |
| 5 | 0 | 1 | 1 | 0 | 0 | 0 |
| 6 | 1 | 1 | 1 | 1 | 0 | 0 |
| 7 | 1 | 1 | 1 | 1 | 1 | 0 |
| 9 | 1 | 1 | 1 | 1 | 1 | 0 |

| P/A (T4.5) | 1 | 0 |
|------------|---|---|
| 1 | 3 | 0 |
| 0 | 1 | 2 |

$$\text{TPR} = \text{TP} / (\text{TP} + \text{FN}) = 3 / (3 + 0) = 1$$

$$\text{FPR} = \text{FP} / (\text{FP} + \text{TN}) = 1 / (2 + 1) = 0.33$$

ROC

| X | Y | Y(T0) | Y(T3) | Y(T5) | Y(T6.5) | Y(T9.5) |
|---|---|-------|-------|-------|---------|---------|
| 1 | 0 | 1 | 0 | 0 | 0 | 0 |
| 4 | 0 | 1 | 1 | 0 | 0 | 0 |
| 5 | 0 | 1 | 1 | 0 | 0 | 0 |
| 6 | 1 | 1 | 1 | 1 | 0 | 0 |
| 7 | 1 | 1 | 1 | 1 | 1 | 0 |
| 9 | 1 | 1 | 1 | 1 | 1 | 0 |

| P/A (T5) | 1 | 0 |
|----------|---|---|
| 1 | 3 | 0 |
| 0 | 0 | 3 |

$$\text{TPR} = \text{TP} / (\text{TP} + \text{FN}) = 3 / (3 + 0) = 1$$

$$\text{FPR} = \text{FP} / (\text{FP} + \text{TN}) = 0 / (0 + 3) = 0$$

ROC

| X | Y | Y(T0) | Y(T3) | Y(T5) | Y(T6.5) | Y(T9.5) |
|---|---|-------|-------|-------|---------|---------|
| 1 | 0 | 1 | 0 | 0 | 0 | 0 |
| 4 | 0 | 1 | 1 | 0 | 0 | 0 |
| 5 | 0 | 1 | 1 | 0 | 0 | 0 |
| 6 | 1 | 1 | 1 | 1 | 0 | 0 |
| 7 | 1 | 1 | 1 | 1 | 1 | 0 |
| 9 | 1 | 1 | 1 | 1 | 1 | 0 |

| P/A (T6.5) | 1 | 0 |
|------------|---|---|
| 1 | 2 | 1 |
| 0 | 0 | 3 |

$$\text{TPR} = \text{TP} / (\text{TP} + \text{FN}) = 2 / (2 + 1) = 0.67$$

$$\text{FPR} = \text{FP} / (\text{FP} + \text{TN}) = 0 / (0 + 3) = 0$$

ROC

| X | Y | Y(T0) | Y(T3) | Y(T5) | Y(T6.5) | Y(T9.5) |
|---|---|-------|-------|-------|---------|---------|
| 1 | 0 | 1 | 0 | 0 | 0 | 0 |
| 4 | 0 | 1 | 1 | 0 | 0 | 0 |
| 5 | 0 | 1 | 1 | 0 | 0 | 0 |
| 6 | 1 | 1 | 1 | 1 | 0 | 0 |
| 7 | 1 | 1 | 1 | 1 | 1 | 0 |
| 9 | 1 | 1 | 1 | 1 | 1 | 0 |

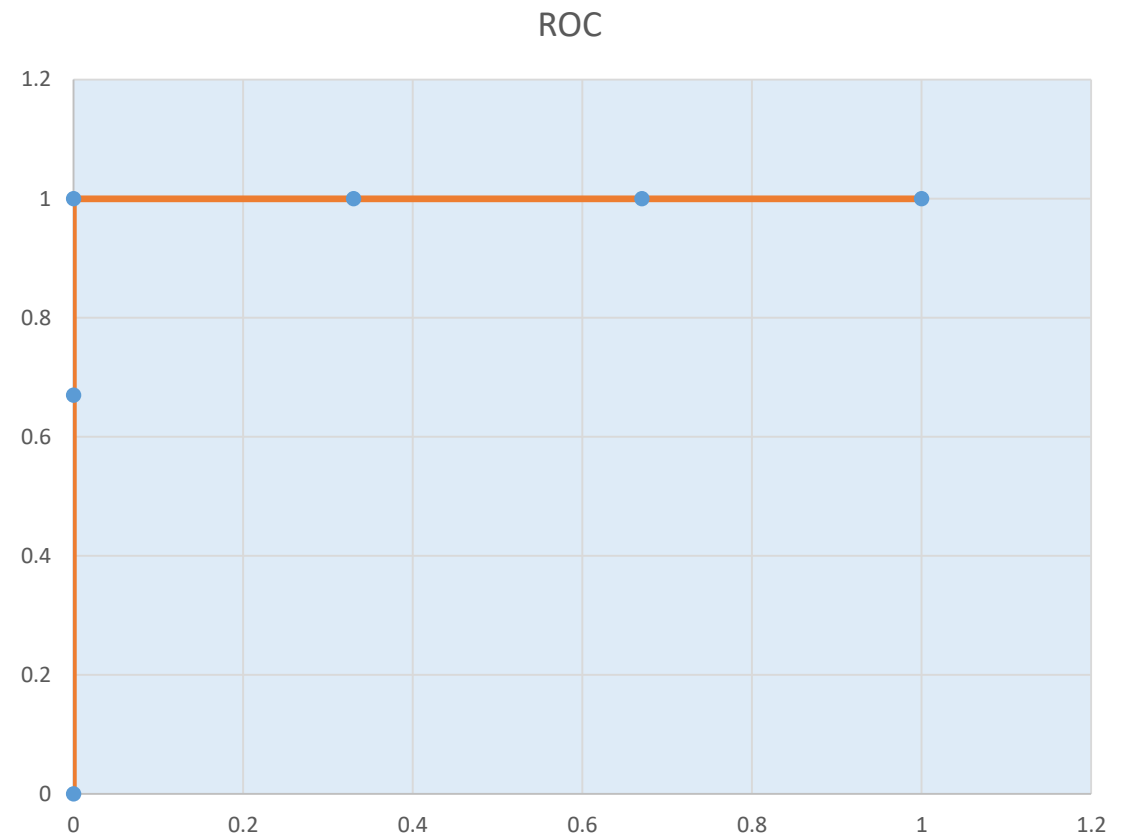
| P/A (T9.5) | 1 | 0 |
|------------|---|---|
| 1 | 0 | 3 |
| 0 | 0 | 3 |

$$\text{TPR} = \text{TP} / (\text{TP} + \text{FN}) = 0 / (0 + 3) = 0$$

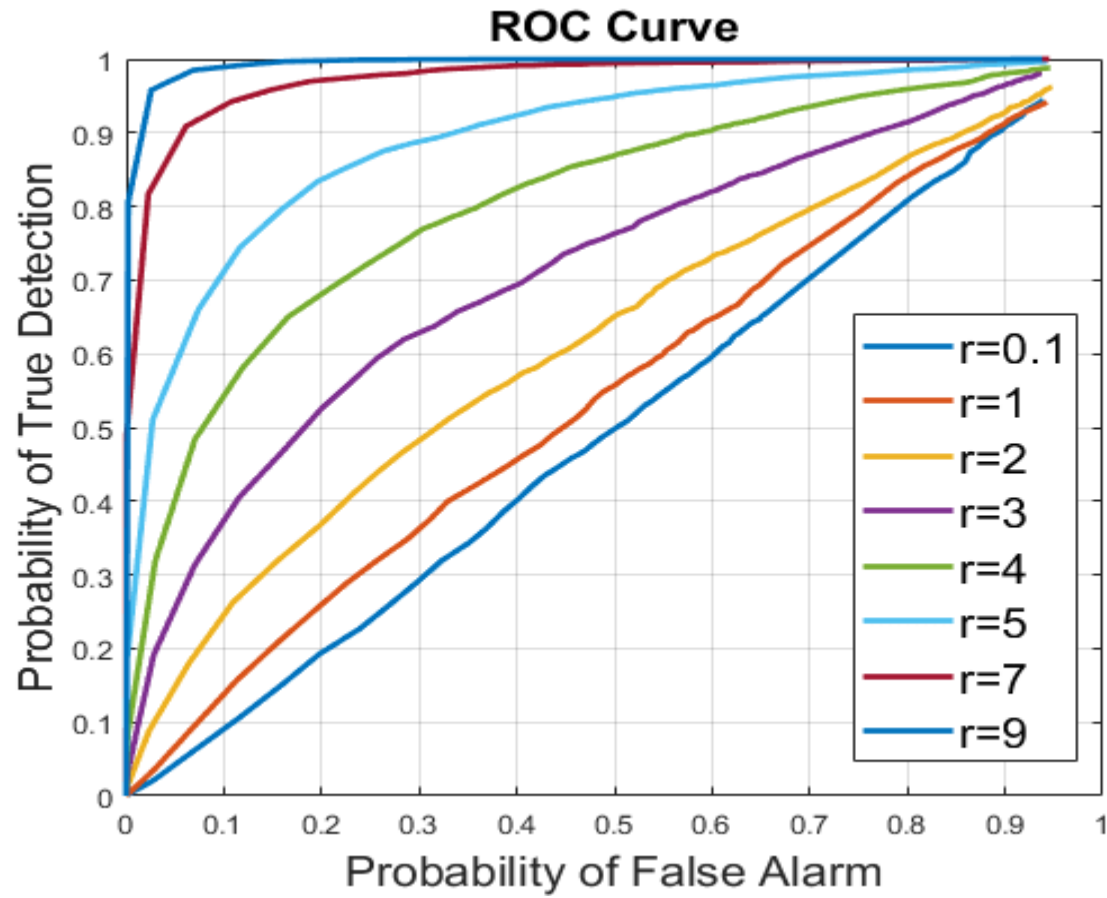
$$\text{FPR} = \text{FP} / (\text{FP} + \text{TN}) = 0 / (0 + 3) = 0$$

ROC

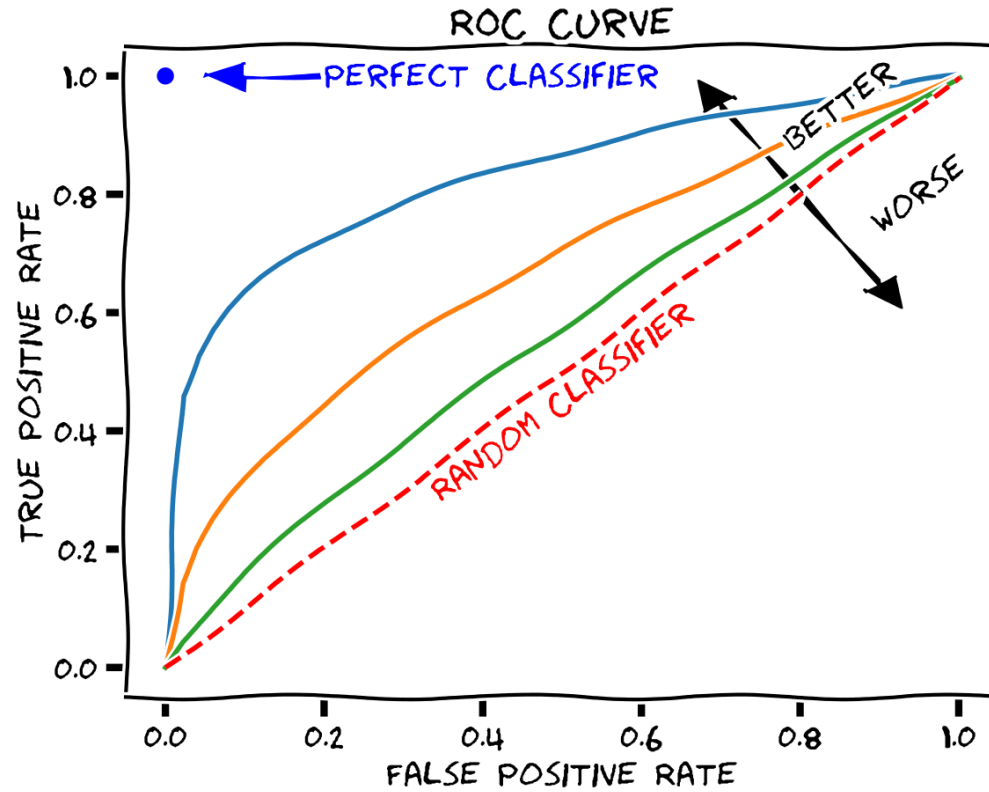
| Threshold | FPR | TPR |
|-----------|------|------|
| 0 | 1 | 1 |
| 3 | 0.67 | 1 |
| 4.5 | 0.33 | 1 |
| 5 | 0 | 1 |
| 6.5 | 0 | 0.67 |
| 9.5 | 0 | 0 |



Analysis of ROC



Analysis of ROC



AUC

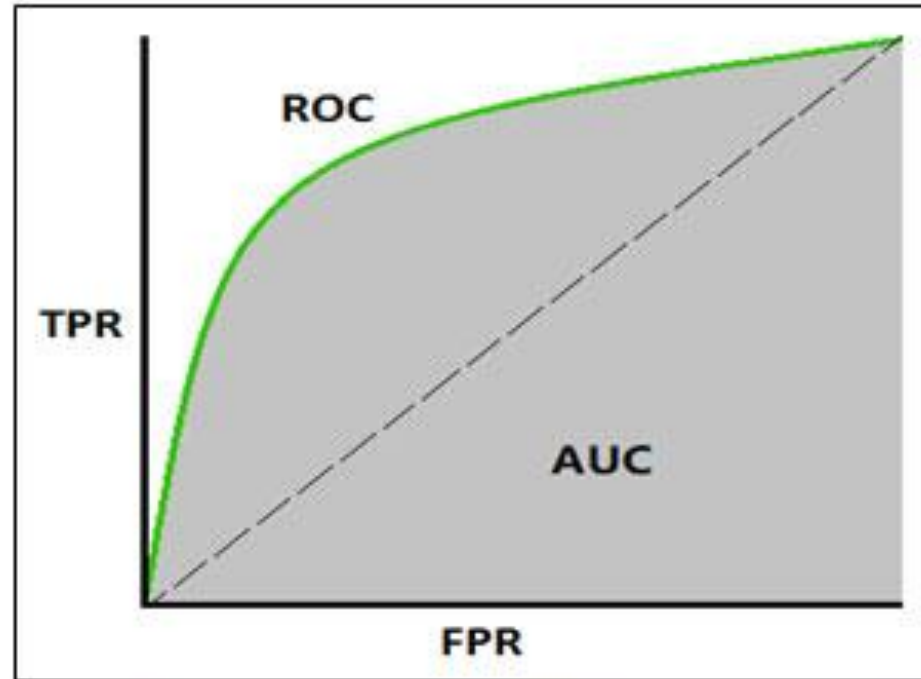


Figure 1: Indicating ROC Curve and AUC