



# Real World Planning and Acting

CS4246/CS5446

AI Planning and Decision Making



# Hierarchical Planning and Acting

Manage complexity

# Examples

- Example 1:

How to go to CSxx46 lecture from home?

- Solution: Go to i3 from home, find lecture hall
- Solution: take MRT, change to internal bus, get off, find i3-AUD.

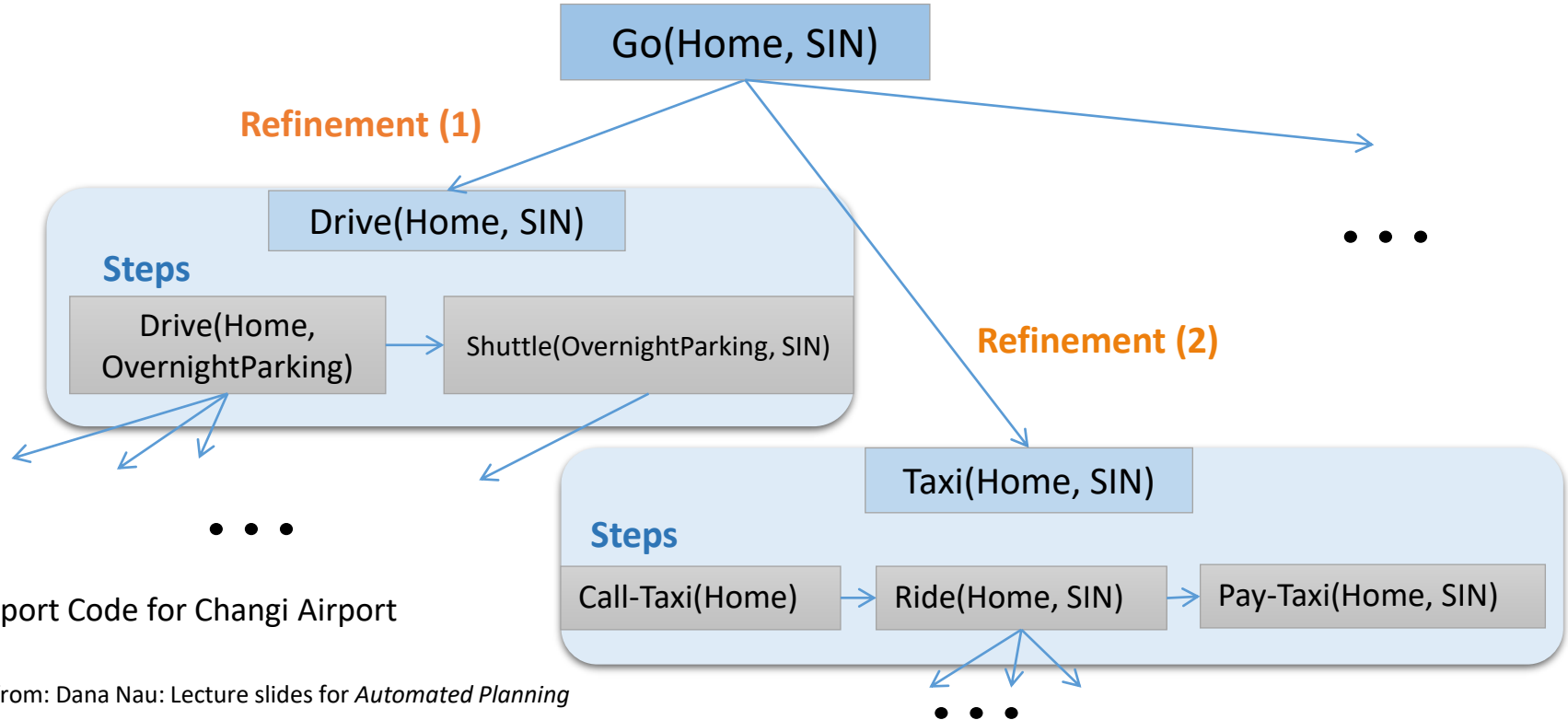
- Example 2:

How to land on the Jezero Crater of Mars from X space station?

- Example 3:

How to get from home to Changi airport?

# Example: Going to Changi Airport



SIN: Airport Code for Changi Airport

Adapted from: Dana Nau: Lecture slides for *Automated Planning*



# Managing Complexity in Planning

- Hierarchical decomposition
  - Division of **tasks** into different **subtasks** at next level
  - At each level focus only a small number of tasks
- Deferred planning
  - Planning can occur before and during plan execution
  - Particular action can remain at an abstract level prior to the execution phase



# Hierarchical Decomposition

- Key benefits

- At each level of hierarchy, a **task** is reduced to a small number of **subtasks** or **activities** at the next lower level
- Computational cost of finding the correct way to arrange activities for current problem is small

- Examples

- Software components, subroutines
- Military, government, and corporations

# Hierarchical Task Networks

- Hierarchical task networks (HTNs)
  - A formalism to help understand hierarchical decomposition
  - A planning model that manages complexity through task abstractions
- Key concept
  - High-level actions (HLAs)
- Assumptions
  - Full observability
  - Deterministic
  - Availability of primitive actions with standard precondition-effect schemas
  - Main ideas are general in problem solving and planning and decision making

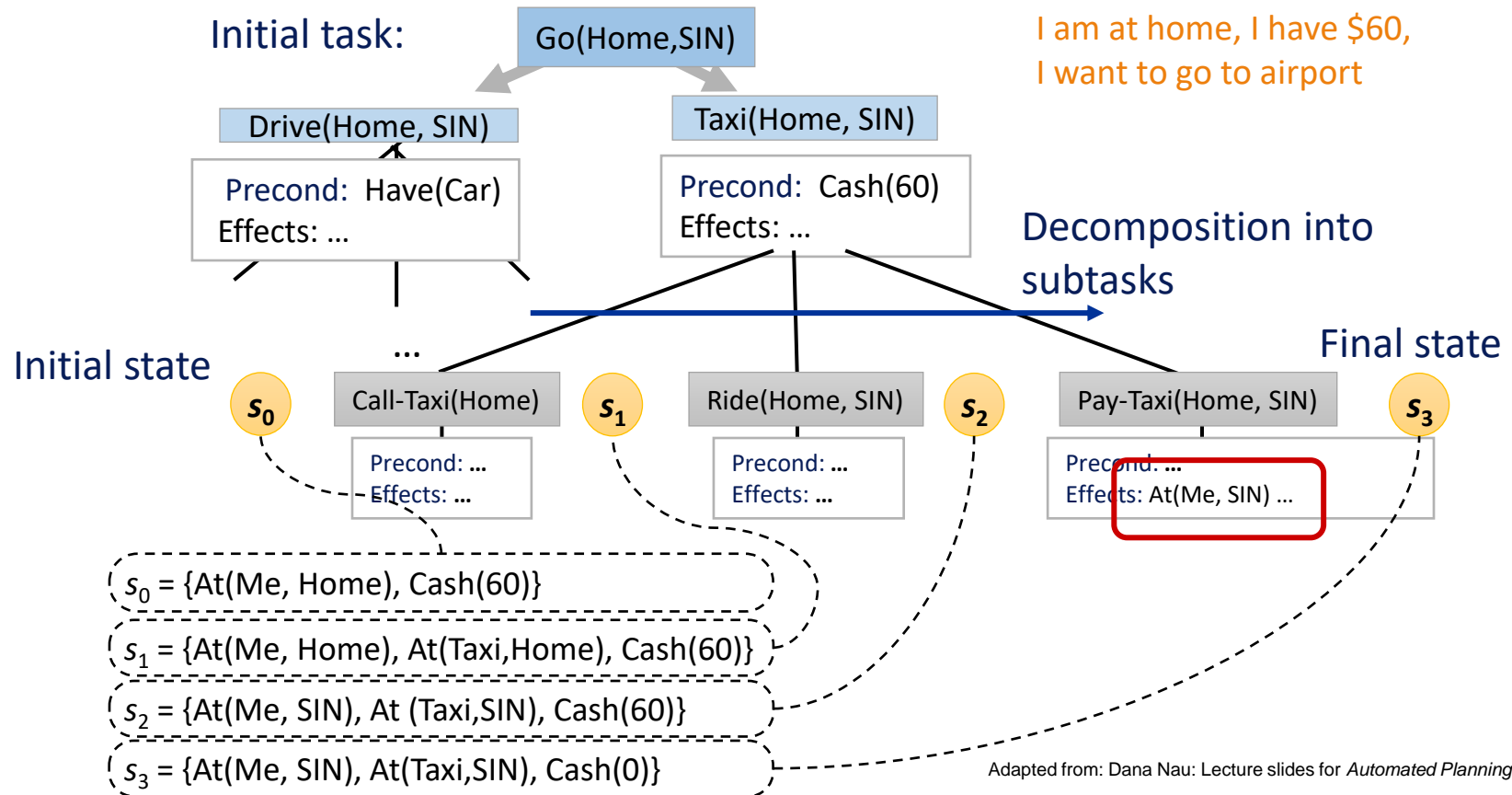


# HTN Planning

- Planning Problem or Model
  - HLAs, action schemas, initial state, goal state, task list
- Planning Algorithm
  - Input: a problem
  - Output: a solution in the form of an action sequence
- Planning Solution
  - Any executable plan generated by recursively applying:
    - HLA to nonprimitive tasks
    - Actions to primitive tasks
  - A goal state that satisfies certain properties



# Example: Going to Changi Airport



# High-Level Actions (HLAs)

- Definition

- Each HLA has one or more **refinements** into a sequence of actions
- Each (refined) action can be an HLA or a primitive action
- Recursive refinement may be needed

- Meaning

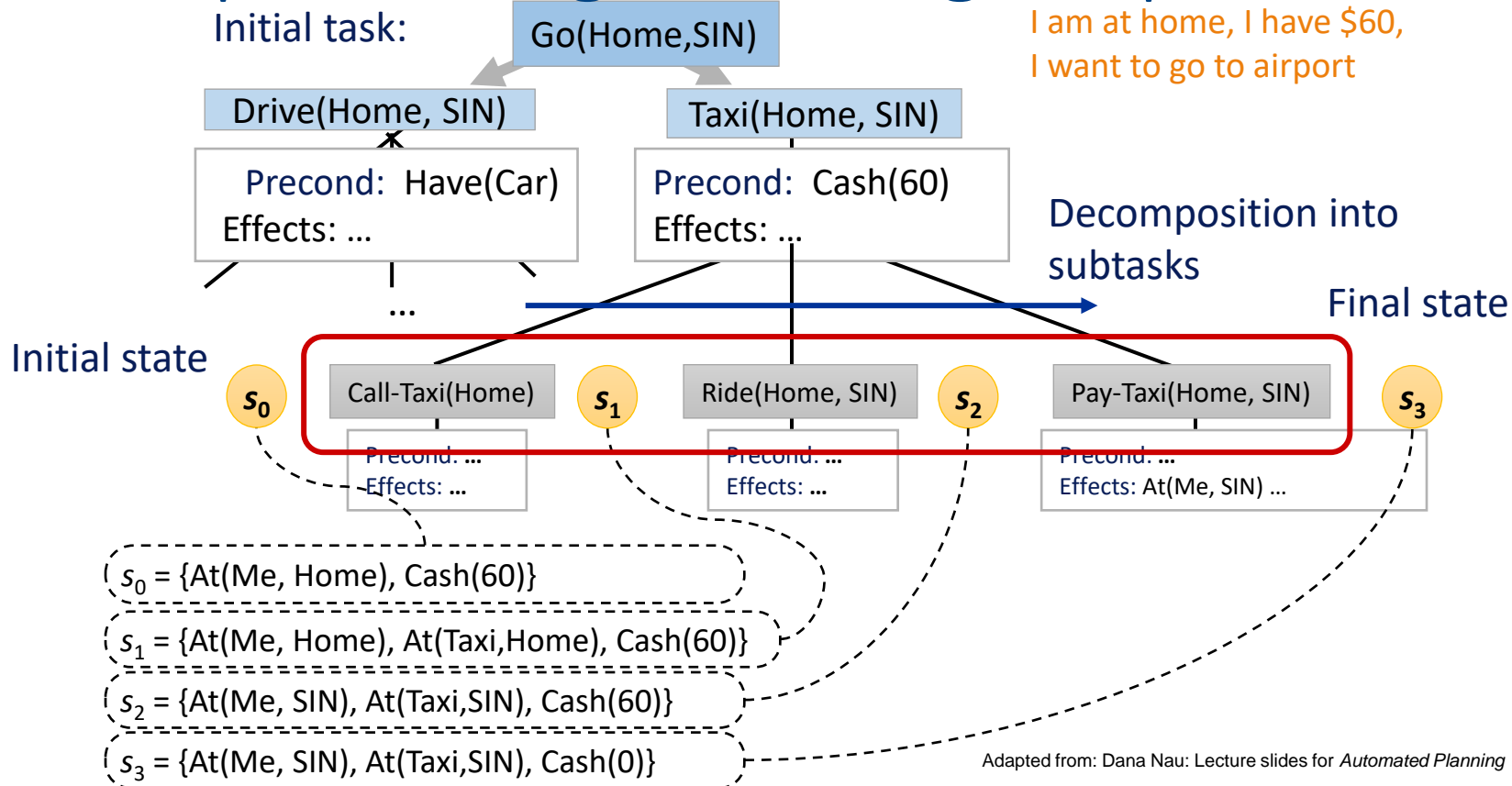
- HLAs and their refinements embody knowledge about **how to do things**  
e.g., Go(Home, SIN) – drive or take a taxi



# Implementation

- HLA implementation
  - An HLA refinement that contains only primitive actions
- High-level plan implementation
  - High-level plan – a sequence of HLAs
  - Concatenate implementations of each HLA in the sequence
- Observation
  - Given the precondition-effect definitions of each primitive action, can directly determine whether any given implementation of a high-level plan achieves the goal.

# Example: Going to Changi Airport



# Planning with HLAs

- Definition

- Achieves the goal from a given state if at least one of its implementations achieves the goal from that state

- Note

- Not all implementations need to achieve the goal
- The agent **decides** which implementation to execute

- Question:

- How is this different from **nondeterministic** planning?

# Planning with HLAs

- With one HLA implementation

- Compute preconditions and effects of HLA from those of the implementation
- Treat HLA exactly as if it were a primitive action

- Observation

- Right collection of HLAs can reduce time complexity of (blind) search from exponential to linear in solution depth
- Devising an appropriate collection of HLAs is **HARD!**

- With multiple HLA implementations

- Search among implementations for one that works; **OR**
- Reason directly about the HLAs - enables derivation of provably correct abstract plans, without having to consider their implementations



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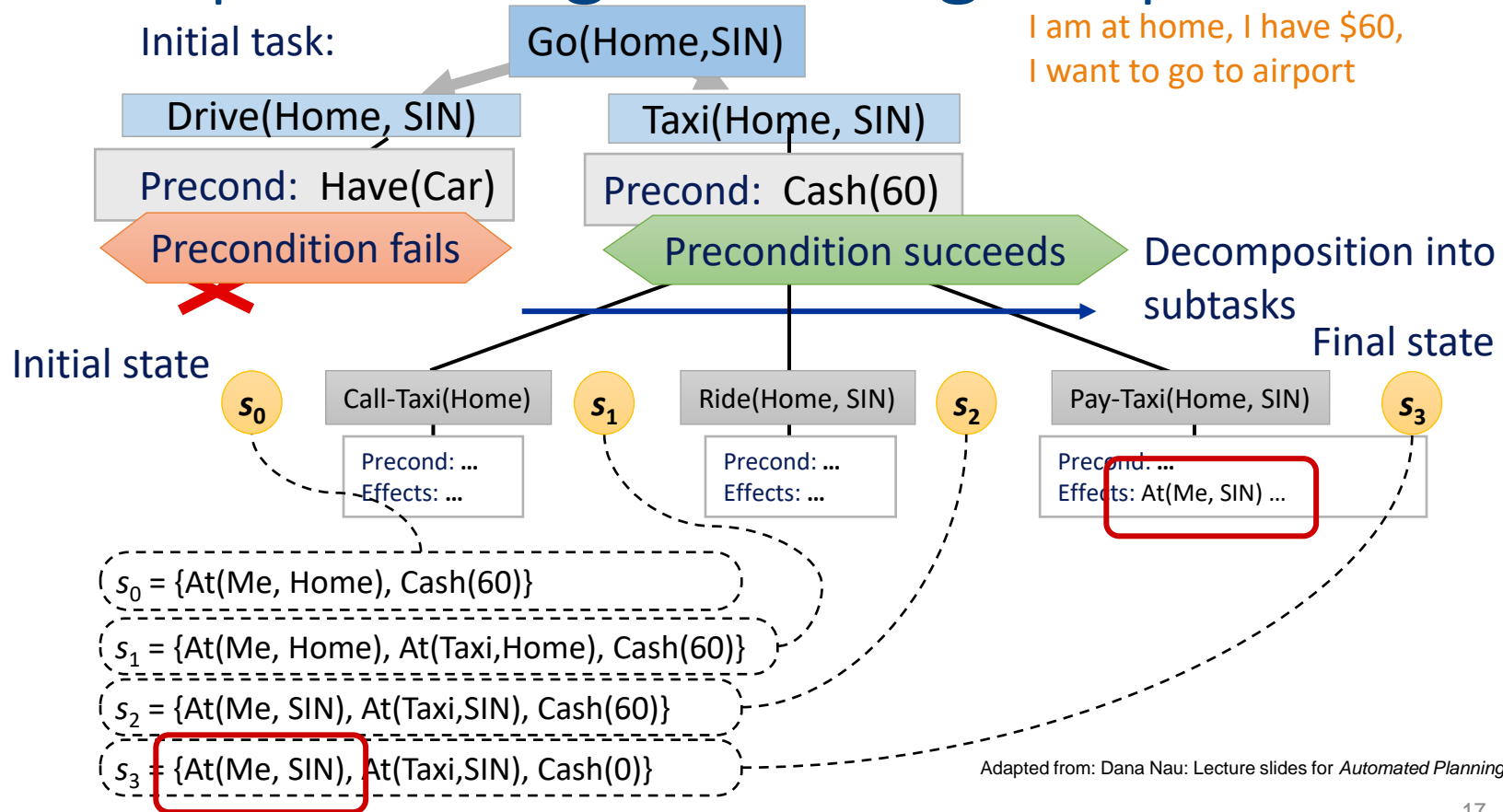


# Hierarchical Planning as Search

Searching for Primitive Solutions



# Example: Going to Changi Airport



# Searching for Primitive Solutions

- HTN Planning
  - Start with top level action *Act*
  - Find an implementation of *Act* that achieves the goal
- Hierarchical planning algorithm
  - Repeatedly choose an HLA in current plan and replace with refinement
  - Until the plan achieves the goal
- Example:
  - Breadth-first search tree
  - Plans are considered in order of depth of nesting of the refinements, rather than number of primitive steps
  - Can use graph-search, depth-first, and iterative deepening

# Generic Planning Framework

- Classical planning definition:
  - For each primitive action  $a_i$ :
  - Provide one refinement of  $Act$  with steps –  $[a_i, Act]$
  - Create recursive definition of  $Act$  to add actions
  - Final refinement:
    - steps – empty, precondition – goal, effect – null
- Algorithm:
  - Repeatedly choose an HLA in the current plan
  - Replace it with one of its refinements
  - Until the plan achieves the goal

# Hierarchical Search

**function** HIERARCHICAL-SEARCH(*problem, hierarchy*) **returns** a solution or *failure*

*frontier*  $\leftarrow$  a FIFO queue with [*Act*] as the only element

**while true do**

**if** IS-EMPTY(*frontier*) **then return** *failure*

*plan*  $\leftarrow$  POP(*frontier*)      // chooses the shallowest plan in frontier

*hla*  $\leftarrow$  the first HLA in *plan*, or null if none

*prefix, suffix*  $\leftarrow$  the action subsequences before and after *hla* in *plan*

*outcome*  $\leftarrow$  RESULT(*problem*.INITIAL, *prefix*)

**if** *hla* is null **then**      // so plan is primitive and outcome is its result

**if** *problem*.IS-GOAL(*outcome*) **then return** *plan*

**else for each** *sequence* **in** REFINEMENTS(*hla, outcome, hierarchy*) **do**

        add APPEND(*prefix, sequence, suffix*) to *frontier*

Source: RN Figure 11.8

# Hierarchical Search

- Main idea:
  - Explore space of sequences that conform to knowledge in the HLA library about how things are to be done
  - Knowledge about the problem is encoded in action sequences in each refinement and in the preconditions of the refinements
- Practical impact:
  - Can generate huge plans with little search
    - e.g., O-PLAN to develop production plans for HITACHI (Bell and Tate 1995)
  - Hierarchically structured – easier for human to understand
  - Find out more about recent applications in use!

# Complexity Analysis

- Assumption

- A planning problem has a solution with  $d$  primitive actions.

- For non-hierarchical, forward state-space planner

- With  $b$  allowable actions at each state, cost is  $O(b^d)$

- For HTN planner

- Suppose each nonprimitive action has  $r$  possible refinements, each into  $k$  actions at the next lower level
- So  $r^{(d-1)(k-1)}$  possible regular decomposition trees could be constructed (see details in RN 11.4.2)

- Observation

- Small  $r$  and large  $k$  - library of HLAs with small number of refinements each yielding a long action sequence - May be hard to construct!



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# Proving Plan Properties

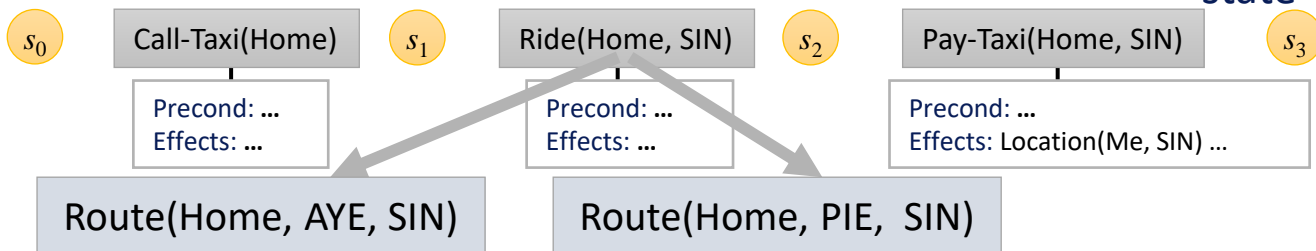
Searching for Abstract Solutions



# Motivation

- Example:
  - We should determine if a high-level plan can get one to the airport, without going through all the specific details like precise route or alighting terminal  
[Call-Taxi(Home), Ride(Home, SIN), Pay-Taxi(SIN)]

Initial  
state





# Searching for Abstract Solutions

- Approach

- Write precondition-effect description of the HLAs
- Prove that the high-level plan achieves the goal
- Work in small search space of high-level actions
- Refine committed plan to achieve exponential reduction

# Searching for Abstract Solutions

- Downward refinement property (of HLA descriptions)
  - Through description of the steps:
    - Every high-level plan that “claims” to achieve the goal achieves the goal
    - At least one implementation achieves the goal
- Main challenges
  - How to write HLAs with downward refinement property?
  - How to write HLAs with multiple implementations?
  - How to describe effects of an action that can be implemented in many different ways?
- Key idea
  - Determine if **reachable sets** of a sequence of HLAs in the plan overlap with goals

# Reachable Set

- Reachable set of an HLA

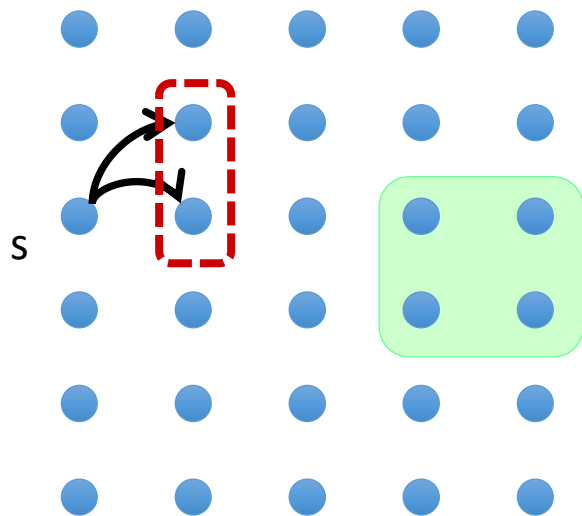
- Given a state  $s$  and an HLA  $h$ :  $REACH(s, h)$  is the set of states **reachable by** any of the HLA's implementations

- Reachable set of a sequence of HLAs

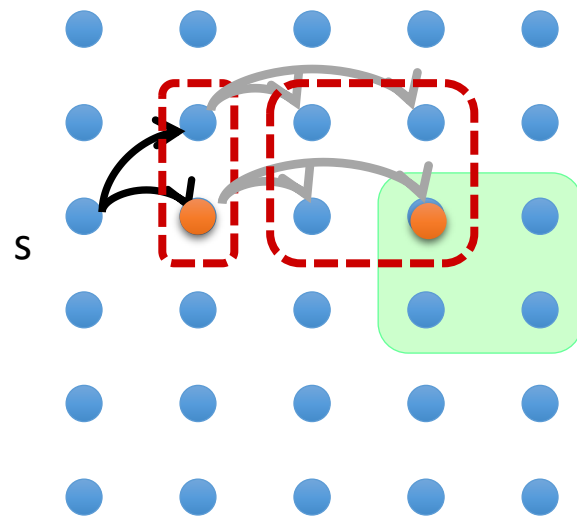
- Reachable set of a sequence of HLAs  $[h_1, h_2]$  is the union of all the reachable sets obtained by applying  $h_2$  in each state in the reachable set of  $h_1$ :

$$REACH(s, [h_1, h_2]) = \cup_{s' \in REACH(s, h_1)} REACH(s', h_2)$$

# Example



$REACH(s, [h_1])$



$REACH(s, [h_1, h_2])$

Source: RN: Fig 11.9



# High-Level Planning

- Practical implications
  - Agent can choose element of the reachable set it ends up in when it executes the HLA
  - HLA with multiple refinements is more “powerful” than the same with fewer refinements
- High-level plan
  - A sequence of HLAs
  - Achieves goal if its reachable set intersects set of goal states
  - Otherwise, the plan does not work
- Search algorithm
  - Search among high-level plans
  - Look for one whose reachable set intersects goal
  - Once that happens, commit to that abstract plan
  - Focus on refining the plan further

# Representing HLA Effects

- Effects as reachable sets
  - As reachable set for each possible initial state
  - Represent changes made to each fluent or state variable
- Recall: Primitive action
  - Can add or delete a fluent or variable or leave it unchanged
- HLA
  - Can also control variable value, depending on implementation chosen
  - Description derivable, in principle, from descriptions of its refinements, such that the downward refinement property holds

# Representing Reachable Set

- Notations:

- $\sim$  means possibly, if the agent chooses
- E.g.,  $\tilde{+}A$  means “possibly add  $A$ ”, i.e., either leave  $A$  unchanged or make it True

- Questions:

- What do  $\simeq A$  and  $\tilde{\pm}A$  mean?

- Example

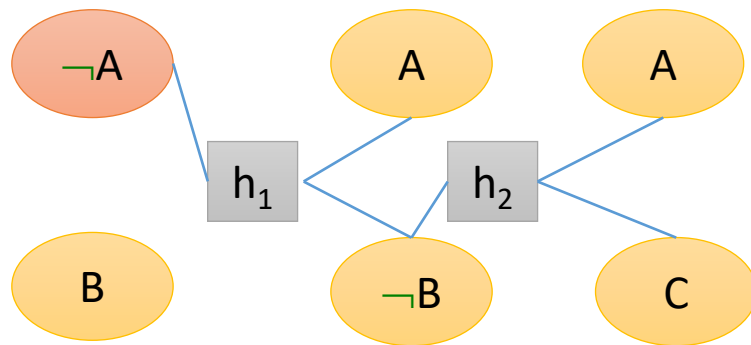
*Go(Home, SIN)* with two refinements

- *Drive(Home, SIN)* and *Taxi(Home, SIN)*
- Possibly delete *Cash* (if agent decides to take a taxi)
- So should have effect  $\simeq \text{Cash}$



# Example

- Consider:
  - Schemas for HLAs  $h_1$  and  $h_2$ :
  - Action ( $h_1$ , Precond:  $\neg A$ , Effect:  $A \wedge \simeq B$ )
  - Action ( $h_2$ , Precond:  $\neg B$ , Effect:  $\tilde{+}A \wedge \tilde{\pm}C$ )
- Meaning:
  - $h_1$  adds A and possibly delete B
  - $h_2$  possibly adds A and has full control over C
- Exercise:
  - If only B is true in the initial state and goal is  $A \wedge C$
  - Q: What sequence of HLAs will achieve the goal?



# HTN Planning Today

- Key idea
  - Construct plan library (knowledge base) of known methods for implementing complex, HLAs
- Approach
  - Learn planning methods from problem-solving experience
  - Save used plan in library as a method for task-specific HLA implementation
  - Accumulate knowledge over time
  - Generalize methods, eliminating problem-specific details, keeping key elements of the plan
- In practice:
  - Many real-world applications; ideas adopted in modern day planning and reinforcement learning
  - Old HTN planners: Noah, Nonlin, O-Plan, SIPE, SIPE-2, SHOP, SHOP2
  - Fast Downward (Helmert 2006) won 2004 IPC; uses hierarchical decomposition of planning tasks to derive heuristics with delayed evaluation in best first search
  - New research trends in hierarchical planning and hierarchical reinforcement learning

# Example: PANDA

- The PANDA framework for hierarchical planning
  - <https://rdcu.be/cn6Ra>
  - Höller, D., et al., *The PANDA Framework for Hierarchical Planning*. KI - Künstliche Intelligenz, 2021.
  - Höller, D., et al., *HDDL: An Extension to PDDL for Expressing Hierarchical Planning Problems*. Proceedings of the AAAI Conference on Artificial Intelligence, 2020. **34**(06): p. 9883-9891.



# Summary

- Hierarchical planning
  - Using abstraction to manage complexity
  - Planning as refinements
  - Planning in abstract space
- HTN Planning
  - Focus on tasks instead of goals
  - Use hierarchical decomposition and delayed planning ideas to manage complexity
- Searching for primitive actions
  - Recursive refinement
- Search for abstract actions
  - Downward refinement property
  - Check if reachable set intersects with goals