

# CS5340 Lab 1: Belief Propagation and Maximal Probability

Name: Niharika Shrivastava  
Email: niharika.shrivastava@u.nus.edu  
Student ID: A0254355A

## 1. `factor_product()` and `factor_sum()`

Result is the element-wise multiplication (or addition in case of `factor_sum()`) of values at `A.val[idxA]` and `B.val[idxB]`.

## 2. `factor_marginalize()` and `factor_max_marginalize()`

Marginalize every variable from the factor one-by-one. Remove the variable and its cardinality from the original factor to get the final factor variable and cardinality.

Sum (or take maximum in case of `factor_max_marginalize()`) values of all the rows in the original factor which equals one row in the final factor (without the marginalized variable value). E.g., `X0` to be marginalized:

Original factor:			Marg assignment:		Final factor(sum):		Final factor(max):	
<code>X0</code>	<code>X1</code>	<code>P(X0, X1)</code>	<code>X1</code>	<code>P(X0, X1)</code>	<code>X1</code>	<code>P(X1)</code>	<code>X1</code>	<code>P(X1)</code>
0	0	0.2	0	0.2	0	0.5	0	0.3 ( <code>argmax={X2=0, X0=1}</code> )
1	0	0.3 ( <code>argmax={X2=0}</code> )	0	0.3	1	0.9	1	0.5 ( <code>argmax={X0=0}</code> )
0	1	0.5	1	0.5				
1	1	0.4 ( <code>argmax=None</code> )	1	0.4				

## 3. `observe_evidence()`

Loop through every factor and select the ones where the evidence variable is present. Set probability of all its assignments to 0 if it doesn't contain the evidence.

## 4. `compute_joint_distribution()`

Do a `factor_product` of all factors in the list sequentially.

## 5. `compute_marginals_naive()`

Observe evidence for all factors. Compute its joint probability. Marginalize over all the variables minus the given variable. Normalize the probabilities.

## 6. `compute_marginals_bp()` Do a DFS on the graph and store messages such that:

`messages[a][b] ==>` message from node a to node b, followed by inference on node b

Collect all messages from leaf to root nodes. Distribute all messages from root to the leaf nodes. Do an inference for all variables in `V`.

## 7. `map_eliminate()`

- Observe evidence for all factors. Convert all probabilities into its log values.
- Generate graph from the factors. Select `root=Node(0)`.
- Collect all messages from leaf to root nodes. Perform inference on the root node. These steps are enough to give us the:
  - Max probability of the entire graph as maximum probability remains the same no matter what the query node is.
  - Max probability configuration as `val_argmax` is populated while computing the marginals every time.
- Remove the evidence from the max decoding configuration and add for the root node.