

**Swinburne University of Technology**  
*Faculty of Science, Engineering and Technology*

**ASSIGNMENT COVER SHEET**

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**Subject Code:** COS30008  
**Subject Title:** Data Structures and Patterns  
**Assignment number and title:** 4, Binary Search Trees & In-Order Traversal  
**Due date:** May 26, 2022, 14:30  
**Lecturer:** Dr. Markus Lumpe

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**Your name:** \_\_\_\_\_ **Your student id:** \_\_\_\_\_

Check Tutorial	Mon 10:30	Mon 14:30	Tues 08:30	Tues 10:30	Tues 12:30	Tues 14:30	Tues 16:30	Wed 08:30	Wed 10:30	Wed 12:30	Wed 14:30

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Marker's comments:

Problem	Marks	Obtained
1	94	
2	42	
3	8+86=94	
Total	230	

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**Extension certification:**

This assignment has been given an extension and is now due on \_\_\_\_\_

Signature of Convener: \_\_\_\_\_

**Problem 1: BinaryTreeNode.h**

```
// COS30008, Problem Set 4, Problem 1, 2022
```

```
#pragma once
```

```
#include <stdexcept>
```

```
#include <algorithm>
```

```
template<typename T>
```

```
struct BinaryTreeNode
```

```
{
```

```
    using BNode = BinaryTreeNode<T>;
```

```
    using BTreeNode = BNode*;
```

```
    T key;
```

```
    BTreeNode left;
```

```
    BTreeNode right;
```

```
    static BNode NIL;
```

```
    const T& findMax() const
```

```
{
```

```
    if ( empty() )
```

```
    {
```

```
        throw std::domain_error( "Empty tree encountered." );
```

```
    }
```

```
    return right->empty() ? key : right->findMax();
```

```
}
```

```
    const T& findMin() const
```

```
{
```

```
    if ( empty() )
```

```
    {
```

```
        throw std::domain_error( "Empty tree encountered." );
```

```
    }
```

```
    return left->empty() ? key : left->findMin();
```

```
}
```

```
bool remove( const T& aKey, BTreeNode aParent )
```

```
{
```

```
    BTreeNode x = this;
```

```
    BTreeNode y = aParent;
```

```
    while ( !x->empty() )
```

```
    {
```

```
        if ( aKey == x->key )
```

```
        {
```

```
            break;
```

```
        }
```

```
        y = x;
```

```
        // new parent
```

```
        x = aKey < x->key ? x->left : x->right;
```

```
    }
```

```

    if ( x->empty() )
    {
        return false;                // delete failed
    }

    if ( !x->left->empty() )
    {
        const T& lKey = x->left->findMax();    // find max to left
        x->key = lKey;
        x->left->remove( lKey, x );
    }
    else
    {
        if ( !x->right->empty() )
        {
            const T& lKey = x->right->findMin();    // find min to right
            x->key = lKey;
            x->right->remove( lKey, x );
        }
        else
        {
            if ( y != &NIL )                // y can be NIL
            {
                if ( y->left == x )
                {
                    y->left = &NIL;
                }
                else
                {
                    y->right = &NIL;
                }
            }

            delete x;                    // free deleted node
        }
    }

    return true;
}

// PS4 starts here

BinaryTreeNode() : key(T()), left(&NIL), right(&NIL) {}
BinaryTreeNode(const T& aKey) : key(aKey), left(&NIL), right(&NIL) {}
BinaryTreeNode(T&& aKey) : key(move(aKey)), left(&NIL), right(&NIL) {}
~BinaryTreeNode() {
    deleteSubtree(left);
    deleteSubtree(right);
}

// Checks if this node is empty
bool empty() const
{
    return this == &NIL;
}

// Checks if this node is a leaf node

```

```

bool leaf() const
{
    return left->empty() && right->empty();
}

// Returns the height of the tree rooted at this node
size_t height() const
{
    if (empty())
    {
        throw domain_error("Empty tree encountered");
    }
    if (leaf())
    {
        return 0;
    }
    const int left_height = left->empty() ? 1 : left->height() + 1;
    const int right_height = right->empty() ? 1 : right->height() + 1;
    return max(left_height, right_height);
}

// Inserts a new node with the given key into the tree rooted at this node
bool insert(const T& aKey) {
    if (empty()) {
        return false; // Cannot insert into an empty tree.
    }

    BNode* currentNode = this;

    while (true) {
        if (aKey > currentNode->key) {
            if (currentNode->right->empty()) {
                // If the right child is empty, insert a new node with the given
                key.
                currentNode->right = new BNode(aKey);
                return true; // Insertion successful.
            }
            else {
                // Move to the right subtree.
                currentNode = currentNode->right;
            }
        }
        else if (aKey < currentNode->key) {
            if (currentNode->left->empty()) {
                // If the left child is empty, insert a new node with the given
                key.
                currentNode->left = new BNode(aKey);
                return true; // Insertion successful.
            }
            else {
                // Move to the left subtree.
                currentNode = currentNode->left;
            }
        }
    }
}

```

```

        }
    }

    else {
        return false; // Duplicate key, insertion failed.
    }
}

private:
    void deleteSubtree(BinaryTreeNode<T>*& node) {
        if (!node->empty()) {
            delete node;
            node = &NIL;
        }
    }
};

template<typename T>
BinaryTreeNode<T> BinaryTreeNode<T>::NIL;

```

## Problem 2: BinarySearchTree.h

```

#pragma once
#include "BinaryTreeNode.h"
#include <stdexcept>
// Problem 3 requirement
template<typename T>
class BinarySearchTreeIterator;
template<typename T>
class BinarySearchTree
{
private:
    using BNode = BinaryTreeNode<T>;
    using BTreeNode = BNode*;
    BTreeNode fRoot;

public:
    BinarySearchTree() : fRoot((&BNode::NIL)) {}
    ~BinarySearchTree()
    {
        while (!fRoot->empty())
        {
            delete fRoot;
        }
    }

    // Checks if the binary search tree is empty
    bool empty() const
    {
        return fRoot->empty();
    }

    // Returns the height of the binary search tree

```

```
size_t height() const
{
    while (empty())
    {
        throw domain_error("Empty tree has no height.");
    }
    return fRoot->height();
}

// Inserts a new key into the binary search tree
bool insert(const T& aKey)
{
    if (empty())
    {
        fRoot = new BNode(aKey);
        return true;
    }

    BTreeNode currentNode = fRoot;
    while (true)
    {
        if (aKey < currentNode->key)
        {
            if (currentNode->left == &BNode::NIL)
            {
                currentNode->left = new BNode(aKey);
                return true;
            }
            currentNode = currentNode->left;
        }
        else if (aKey > currentNode->key)
        {
            if (currentNode->right == &BNode::NIL)
            {
                currentNode->right = new BNode(aKey);
                return true;
            }
            currentNode = currentNode->right;
        }
        else
        {
            return false; // Key already exists in the tree
        }
    }
}

// Removes a key from the binary search tree
bool remove(const T& aKey)
{
    if (empty())
    {
```

```

        throw domain_error("Unable to remove from an empty tree.");
    }

    if (fRoot->leaf())
    {
        if (fRoot->key == aKey)
        {
            fRoot = &BNode::NIL;
            return true;
        }
        return false;
    }

    return fRoot->remove(aKey, &BNode::NIL);
}

// Problem 3 methods

using Iterator = BinarySearchTreeIterator<T>;
// Allow iterator to access private member variables
friend class BinarySearchTreeIterator<T>;
Iterator begin() const
{
    return Iterator(*this).begin();
}
Iterator end() const
{
    return Iterator(*this).end();
}
};

```

### Problem 3: BinarySearchTreeIterator.h

```

// COS30008, Problem Set 4, Problem 3, 2022

#pragma once

#include "BinarySearchTree.h"

#include <stack>

template<typename T>
class BinarySearchTreeIterator
{
private:

    using BSTree = BinarySearchTree<T>;
    using BNode = BinaryTreeNode<T>;
    using BTreeNode = BNode*;
    using BTNStack = std::stack<BTreeNode>;
    const BSTree& fBSTree; // binary search tree
    BTNStack fStack; // DFS traversal stack

    void pushLeft(BTreeNode aNode)

```

```

        {
            while (!aNode->empty())
            {
                fStack.push(aNode);
                aNode = aNode->left;
            }
        }
    }

public:

    using Iterator = BinarySearchTreeIterator<T>;

    BinarySearchTreeIterator(const BSTree& aBSTree) : fBSTree(aBSTree), fStack()
    {
        pushLeft(aBSTree.fRoot);
    }

    // Dereference operator to get the value at the current position
    const T& operator*() const
    {
        return fStack.top()->key;
    }

    // Pre-increment operator (++iter)
    Iterator& operator++()
    {
        BTreeNode lPop = fStack.top();
        fStack.pop();
        pushLeft(lPop->right);
        return *this;
    }

    // Post-increment operator (iter++)
    Iterator operator++(int)
    {
        // Create a temporary iterator and move it to the end of the tree
        Iterator temp = *this;

        while (!temp.fStack.empty())
        {
            BTreeNode currentNode = temp.fStack.top();
            temp.fStack.pop();

            BTreeNode rightNode = currentNode->right;
            while (rightNode->nonEmpty())
            {
                temp.fStack.push(rightNode);
                rightNode = rightNode->left;
            }
        }

        return temp;
    }

    // Check if two iterators are equal or not
    bool isEqual(const Iterator& aOtherIter) const
    {
        return &fBSTree == &aOtherIter.fBSTree && fStack == aOtherIter.fStack;
    }

```



```
    }
    bool operator!=(const Iterator& aOtherIter) const
    {
        return !isEqual(aOtherIter);
    }

    // Return an iterator pointing to the beginning of the tree
    Iterator begin() const
    {
        Iterator temp = *this;
        temp.fStack = BTNStack();
        temp.pushLeft(temp.fBSTree.fRoot);
        return temp;
    }

    // Return an iterator pointing to the end of the tree
    Iterator end() const
    {
        Iterator temp = *this;
        temp.fStack = BTNStack();
        return temp;
    }
};
```