CSI 2300: Intro to Data Science

In-Class Exercise 23: Modeling – Clustering and Multidimensional Scaling

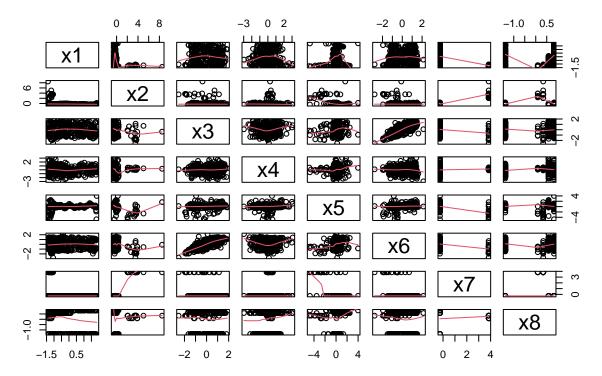
In this lecture, we're going to work with a mystery dataset and try to unlock some of the patterns it contains. The mystery dataset is from one of the mowater datasets, but it has been sub-sampled and some variables removed to protect its identity (and make it easier to work with). There's a lot to do, so get going!

1. Load and scale the dataset.

- Load in the dataset you were given in the rda file. The data frame contained has the mysterious name "lecture23".
- It's important to manage the scale of our variables in distance-based methods, otherwise variables that have a large range can dominate the distance calculations. Use as.data.frame(scale(lecture23)) command to change each variable to have 0 mean and standard deviation of 1. Replace your data (lecture23) with the output of that scaling.
- Check your work: run sapply(lecture23, mean) and sapply(lecture23, sd), and you should get values near zero and one.

```
load("lecture 23 inclass.rda")
lecture23 <- as.data.frame(scale(lecture23))</pre>
sapply(lecture23, mean)
                                          x3
                                                                       x5
             x1
                           x2
  4.810966e-17 -7.288152e-16 -1.708263e-15 -1.445198e-14 -1.398585e-14
#
             x6
                           x7
  7.651287e-17 3.098262e-15 -7.993606e-17
sapply(lecture23, sd)
# x1 x2 x3 x4 x5 x6 x7 x8
  1 1 1 1 1 1 1 1
pairs(
 lecture23,
 panel = panel.smooth,
 main = "Pairs Plot of Scaled Variables"
)
```

Pairs Plot of Scaled Variables



- 2. You've been given "original space" data. Explore this data by plotting some of its variables. You may find the pairs function useful. Do you notice any clusters? It may be hard to tell (because this data has more than two variables), but how many clusters do you think you see (just give an estimate)?
- 3. Construct the pairwise distance matrix, and then use it to construct a two-dimensional visualization using multidimensional scaling.
 - Construct the pairwise distance matrix, and save it in a variable called pairwise_dist.
 - Use multidimensional scaling to produce a 2-dimensional view of the pairwise_dist matrix you just created. Let's call this 2-dimensional version mds_2d.
 - Then plot mds_2d. Do you see clusters? How many clusters do you see?

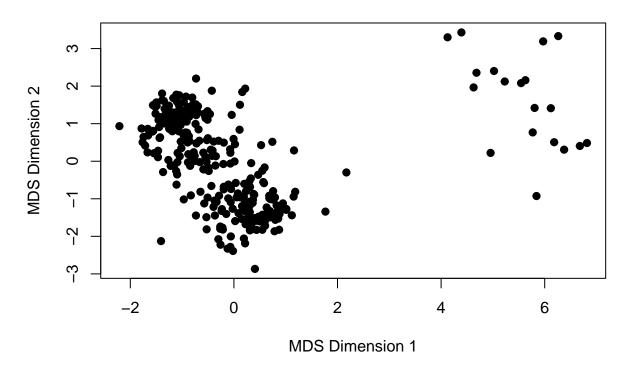
```
pairwise_dist <- dist(lecture23)

mds_2d <- cmdscale(pairwise_dist, k = 2, eig = TRUE)

mds_points <- as.data.frame(mds_2d$points)
colnames(mds_points) <- c("Dim1", "Dim2")</pre>
```

```
plot(
  mds_points$Dim1,
  mds_points$Dim2,
  xlab = "MDS Dimension 1",
  ylab = "MDS Dimension 2",
  main = "2D MDS of lecture23",
  pch = 19
)
```

2D MDS of lecture23



I see three main clusters with 2 having a large amount of dots and the two clusters are right next to eachother, and the 3rd being off to the side with the dots being more spread apart.

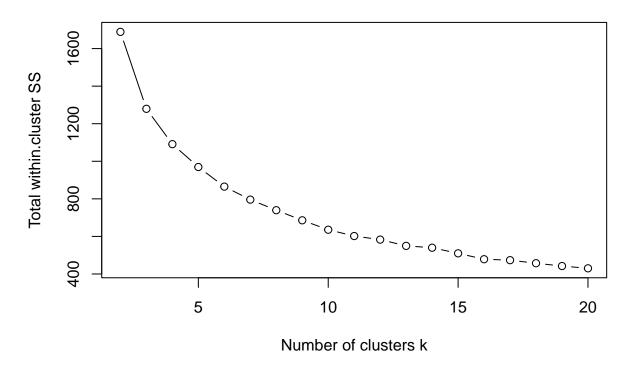
- 4. Cluster the original-space data using k-means.
 - Cluster lecture 23 with each value of k from 2 up to 20.
 - For each k, record the distortion (available as the field tot.withinss from the model).
 - Make a plot of the distortion as a function of k.
 - Based on this plot, how many clusters do you think there are in the data? Look for a low distortion, but good vertical separation between the distortion for your chosen k and the distortion for k-1.

```
ks <- 2:20
wss <- numeric(length(ks))

for (i in ks) {
   set.seed(123)
   km <- kmeans(lecture23, centers = i, nstart = 10)
   wss[i - 1] <- km$tot.withinss
}

plot(ks, wss, type = "b",
        xlab = "Number of clusters k",
        ylab = "Total within-cluster SS",
        main = "Elbow Plot: k-means Distortion")</pre>
```

Elbow Plot: k.means Distortion



I there is just one elbow at 3, and then it starts to go down more slowly. I would choose 3 clusters.

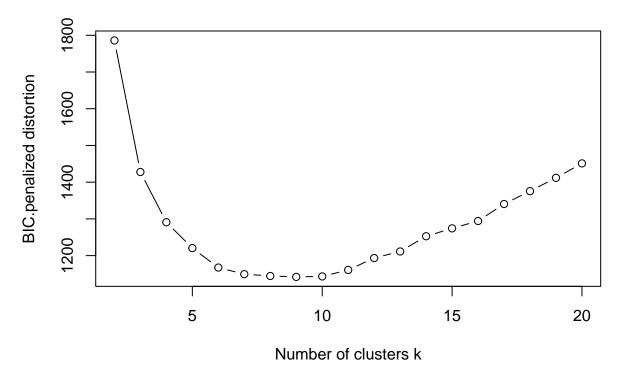
5. The distortion values tend to "just go down" as you add more clusters. We can use a penalized distortion with the BIC (Bayesian Information Criterion). The computation is:

$$BIC(k) = distortion(k) + (k - 1 + k \cdot d) \cdot log(n)$$

where k is the number of clusters, d is the number of dimensions (variables), and n is the number of observations. The penalty is based on the number of parameters estimated (k-1 "cluster priors" and $k \cdot d$ parameters for the cluster centers), and we multiply them by the BIC penalty $\log(n)$.

- Compute the BIC-penalized distortion according to the formula above and your distortion values from the previous question.
- Plot the BIC-penalized distortion as a function of k. What k would you choose based on that plot? Is it different than what you chose in the previous question?

BIC vs k for k.means



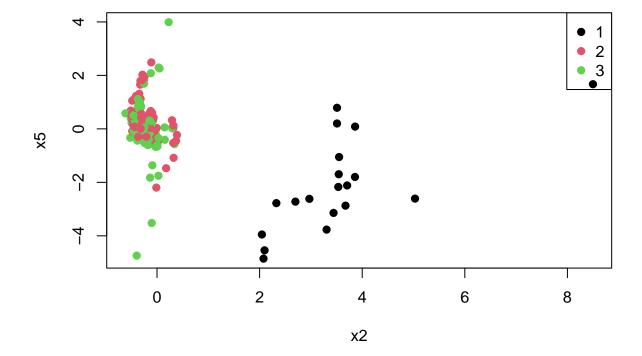
I would choose 3 clusters again. The BIC-penalized distortion is lower at 3 than at 4, and then it starts to go up again.

- 6. Let's visualize the k-means clustering. For ease of grading, we'll choose k = 3 (though you may have chosen a different k in the previous questions).
 - Cluster the lecture 23 data using k-means with k=3, and save the model in a variable.
 - Plot lecture23 variables x2 and x5, and color the points using the cluster labels.
 - Plot the mds 2d data, coloring the points using the cluster labels.
 - Do the clusters look reasonable? Keep in mind that we are clustering with 8 variables, but plotting in 2 dimensions, so some clusters may appear to overlap that's because we are not plotting all the dimensions (and the un-plotted dimensions get "collapsed" or "projected" down onto the two that we are plotting).

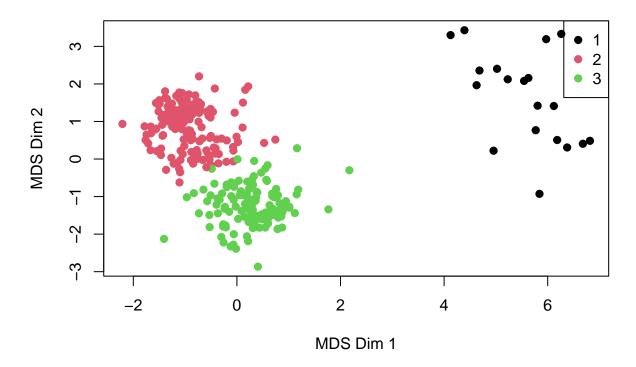
```
set.seed(123)
km3 <- kmeans(lecture23, centers = 3, nstart = 10)

plot(lecture23$x2, lecture23$x5,
        col = km3$cluster, pch = 19,
        xlab = "x2", ylab = "x5",
        main = "x2 vs x5 colored by k=3 clusters")
legend("topright", legend = 1:3, col = 1:3, pch = 19)</pre>
```

x2 vs x5 colored by k=3 clusters



MDS plot colored by k=3 clusters



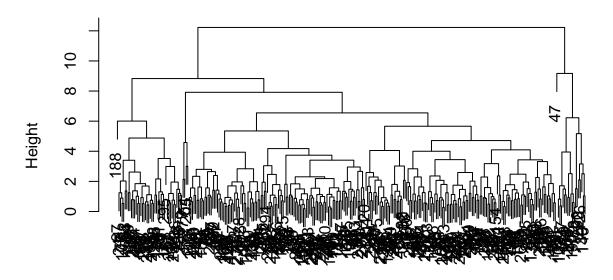
I think the clusters look reasonable. The points are all grouped together in the clusters, and the clusters are not overlapping too much.

- 7. Apply hierarchical clustering to the pairwise distance data.
 - Use hclust to cluster the pairwise_dist matrix, producing a model which we'll call hclust_model.
 - Plot the model to obtain the dendrogram.
 - How many clusters do you think there are based on this dendrogram? A good splitting point of the dendrogram is a place where there is a large vertical separation between joined clusters.
 - For your chosen number of clusters, extract the clustering membership labels (one for each observation) from the hierarchical clustering model. You may find cutree useful here.

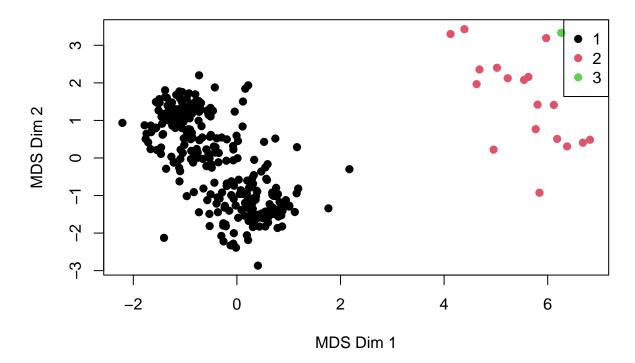
• Plot the multidimensional scaling data and color the observations with its cluster membership you just extracted.

```
hclust_model <- hclust(pairwise_dist, method = "complete")
plot(hclust_model,
    main = "Dendrogram of lecture23",
    xlab = "", sub = "")</pre>
```

Dendrogram of lecture23



MDS plot colored by hierarchical clusters

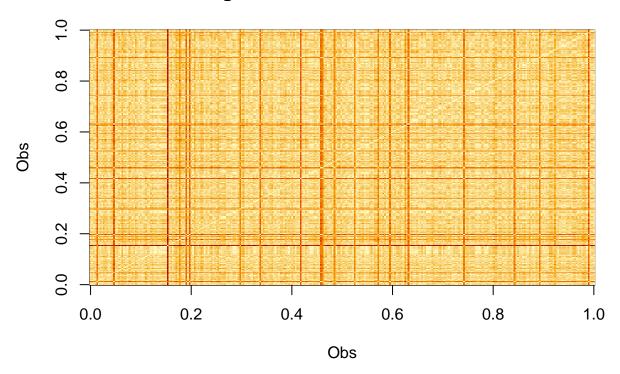


I see 3 clusters in the dendrogram, and I think the clusters look reasonable. The points are all grouped together in the clusters, and the clusters are not overlapping too much.

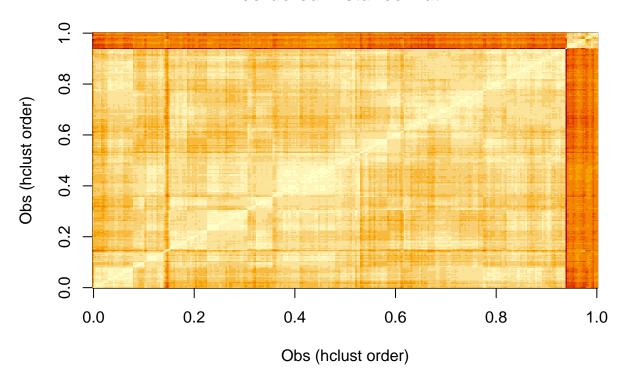
- 8. Extra Credit Let's look at the pairwise dist distance matrix.
 - Create an image of the pairwise_dist matrix we created in question 3. You may find as.matrix useful here.
 - The hierarchical clustering model (hclust_model) we created in question 6 has an \$order field, which is the order of the observations along the bottom of the dendrogram. Use this order to:
 - Reorder the lecture23 observations according to the order found by hclust.
 - Create a pairwise distance matrix of the reordered observations.
 - Create an image of this reordered distance matrix.

Does this second matrix appear to have more or less of a pattern than the first matrix? Do either of the matrices appear to show you clustering information?

Original Pairwise Distance Matrix



Reordered Distance Matrix



The first matrix appears to have more of a pattern than the second matrix. The first matrix has more of a block pattern, while the second matrix is more random. The first matrix shows some clustering information, while the second matrix does not.