

Separating double-beta decay events from solar neutrino interactions in kiloton-scale liquid scintillator detectors

Andrey Elagin¹, Henry Frisch¹, Lindley Winslow², *et al* (**opt-in**)

¹*Enrico Fermi Institute, University of Chicago*

²*Massachusetts Institute of Technology*

Abstract

We propose a technique for separating $0\nu\beta\beta$ -decay events from background due to 8B solar neutrino interactions in a liquid scintillator detector. The technique compares event topology of the signal and background events using spherical harmonics analysis of the early light emitted in $0\nu\beta\beta$ -decay and 8B events. Selection of early photons using fast photo-detectors allows for separation of directional Cherenkov from isotropic scintillation light and identification of two event topologies based on the spatial distribution of the early photons in the detector.

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1 Introduction

Introductory paragraphs saying that $0\nu\beta\beta$ -decay is important and we'd like to improve sensitivity of liquid scintillator detectors.

In a large liquid scintillator detector two dominant backgrounds to $0\nu\beta\beta$ -decay signal are $2\nu\beta\beta$ -decay and electron scattering (ES) of 8B solar neutrinos. As an example we show simulation of the energy spectrum for the $0\nu\beta\beta$ -decay signal and various backgrounds in SNO+ experiment in Fig. 1.

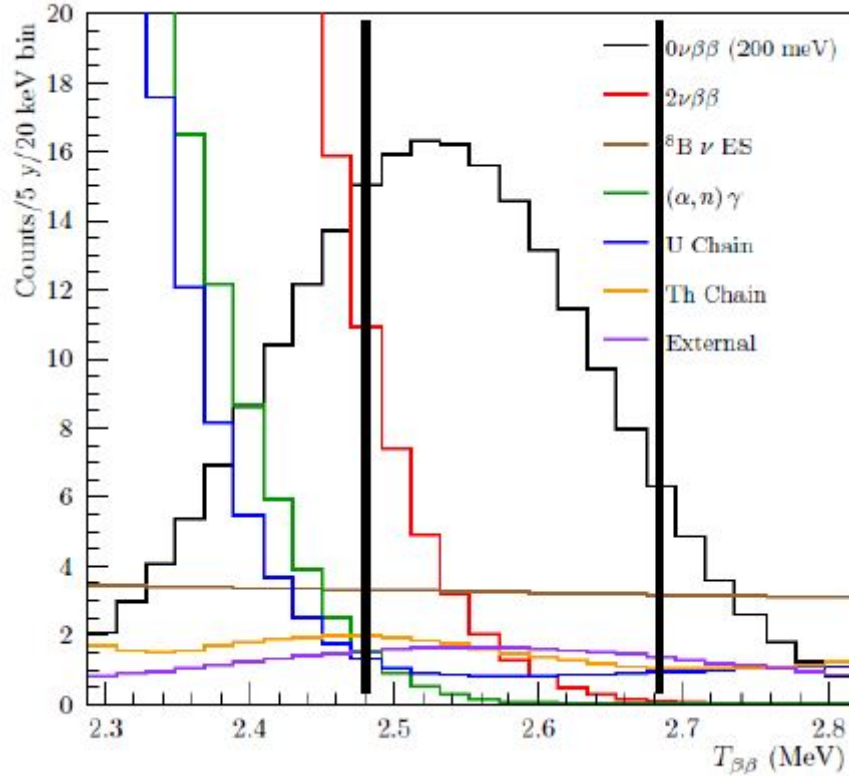


Figure 1: SNO+ Phase I signal and background energy spectrum (visible kinetic energy reconstructed under a $0\nu\beta\beta$ hypothesis). Plot taken from [2]

The event topology of $0\nu\beta\beta$ - and $2\nu\beta\beta$ -decays are very similar - both produce two electron tracks in the detector. As shown in Fig. 2, in the region of interest (ROI) where total kinetic energy of the electrons is close to the energy spectrum end point (Q-value), there is almost no difference in kinematic distributions between $0\nu\beta\beta$ - and

45 $2\nu\beta\beta$ -decays. Therefore the energy resolution is the key parameter for discrimination
 46 between these two processes in any detector searching for $0\nu\beta\beta$ -decay.

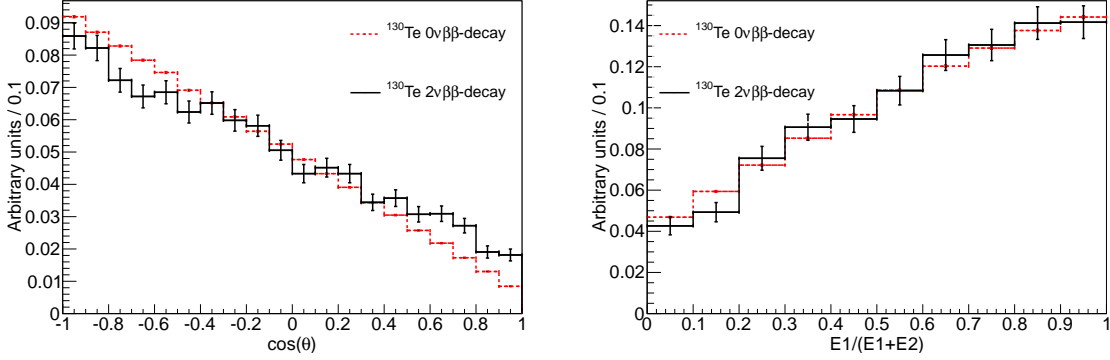


Figure 2: Comparison between kinematics of $0\nu\beta\beta$ - (dashed red lines) and $2\nu\beta\beta$ -decays (solid black lines) for events with the total kinetic energy of the electrons above 90% of the Q-value. (Left) Cosine of the angle between two electrons. (Right) Fraction of energy carried by one of the two electrons. Due to limited statistic around the energy spectrum end point for $2\nu\beta\beta$ -decay we show statistical errors for each bin.

47 While the event topology of $2\nu\beta\beta$ -decay is very similar to the $0\nu\beta\beta$ -decay, the topol-
 48 ogy of the next largest background coming from the ^8B solar neutrino is sufficiently
 49 different and can be used to suppress this type of background.

50 ^8B solar neutrino interactions produce only one electron. In a liquid scintillator de-
 51 tector the difference between two electrons and one electron will show up in the distri-
 52 bution of the Cherenkov photons. Abundant scintillation light makes it challenging to
 53 extract small Cherenkov light contribution from low energy electrons. However, as have
 54 been shown in our previous work, photo-detectors with time resolution of ~ 100 ps can
 55 allow for selection of photons that contain significant fraction of Cherenkov light pro-
 56 duced by 1-5 MeV electrons in a kilo-ton scale liquid scintillator detector. Cherenkov
 57 photons on average arrive to the detector surface earlier than scintillation light due to
 58 longer wavelength of the Cherenkov photons and a delay in the scintillation process.
 59 Thus early light primarily consist of Cherenkov photons.

60 In this paper we propose to use spherical harmonics to analyze distributions of the
 61 early photo-electrons (PE) for discrimination between ^8B background and $0\nu\beta\beta$ -decay

62 signal.

63 Section 2 describes our detector model. Section 3 introduces spherical harmonics
64 analysis. Performance and experimental challenges are discussed in Sec. 4

65 2 Detector Model

66 Copy info from [1].

67 Figures 3 and 4 show simulation output relevant for further discussion.

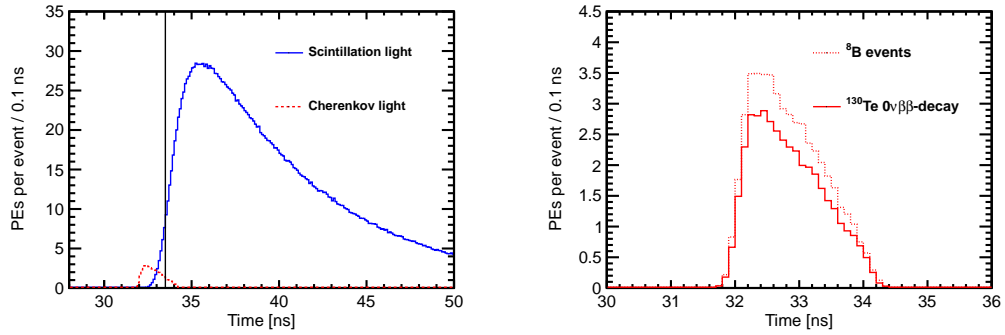


Figure 3: (Left) Photo-electron (PE) arrival times after application of the photo-detector transit time spread (TTS) of 100 ps for the simulation of 1000 $0\nu\beta\beta$ -decay events of ^{130}Te at the center of the detector. PEs from Cherenkov light (red, dash line) and scintillation light (blue, solid line) are compared. The black vertical line illustrates a time cut at 33.5 ns. (Right) Comparison between Cherenkov PE arrival time for ^{130}Te $0\nu\beta\beta$ -decay (solid line) and ^8B (dotted line) events. **Distributions of the scintillation PE arrival time are indistinguishable between ^{130}Te $0\nu\beta\beta$ -decay and ^8B due to identical total energy in the event, $Q(^{130}\text{Te})=2.529$ MeV.**

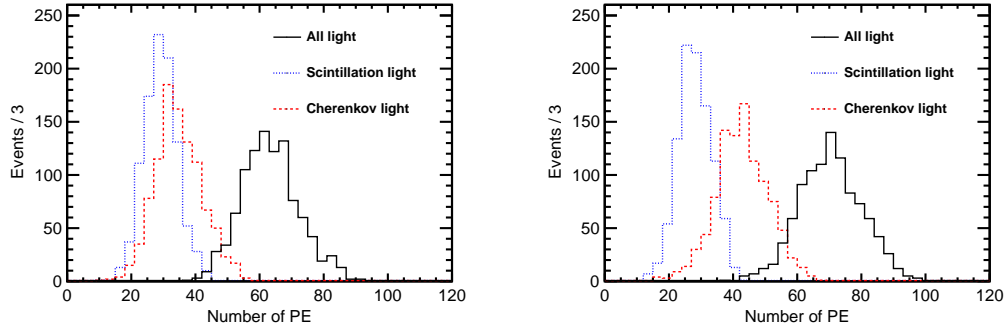


Figure 4: Number of Cherenkov (red dash line), scintillation (blue dotted line), and total (black solid line) PEs for the simulation of 1000 ^{130}Te $0\nu\beta\beta$ -decay (left panel) and ^8B (right panel) events.

3 Event Topology and Spherical Harmonics Analysis

3.1 Topology of $0\nu\beta\beta$ -decay and ^8B Events

Electrons in the energy range around Q-value of all isotopes considered for $0\nu\beta\beta$ -decay searches are above Cherenkov threshold in liquid scintillators. Each electron above the threshold will produce a fuzzy ring of Cherenkov light at the detector surface. The fuzziness of the ring depends on electron scattering. In most cases Cherenkov rings from low energy electrons degrade to randomly shaped clusters of Cherenkov photons around direction of the electron track.

Large fraction of $0\nu\beta\beta$ -decay events will have two Cherenkov clusters¹ as opposed to one cluster from ^8B events. Therefore separation of $0\nu\beta\beta$ -decay signal from ^8B background depends on ability to identify topology of the Cherenkov light on the detector sphere on top of uniformly distributed scintillation light. We show that analysis of spherical harmonics of the early photons allows to achieve noticeable separation between $0\nu\beta\beta$ -decay and ^8B events.

¹Only one Cherenkov cluster is produced when either the angle between the two $0\nu\beta\beta$ -decay electrons is too small or when the energy splits between the electrons in such a way that one electron falls below the Cherenkov threshold.

83 In order to illustrate differences between different event topologies we introduce
 84 three event topologies: two electrons produced back-to-back at 180° angle, two electrons
 85 at 90° angle, and a single electron. The two former are representative topologies of
 86 $0\nu\beta\beta$ -decay signal events and the latter represents 8B background events. Figure 5
 87 shows Cherenkov photon distributions of 5 MeV electrons for each of the three topology.
 88 Overlay of 100 events with no QE applied is shown in order to make Cherenkov rings
 89 visible.

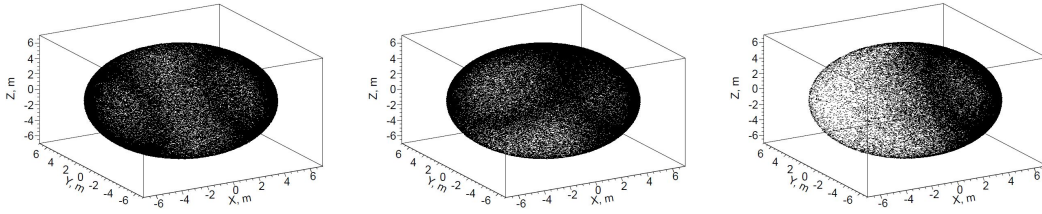


Figure 5: Cherenkov photons distributions on the detector sphere for the three representative event topologies: two back-to-back electrons (Left), two electrons at 90° angle (Middle), and a single electron (Center). All electrons are 5 MeV and originate at the center of the detector. 100 events overlayed for better visibility of the Cherenkov rings. 100% QE is assumed.

90 Cherenkov clusters that form at lower energies are shown in Fig. 6. All Cherenkov
 91 photons produced in a single event are shown for the three event topologies with total
 92 kinetic energy of 2.529 MeV that corresponds to Q-value of ^{130}Te . One can try to guess
 93 the event topology by comparing different segments of the detector sphere.

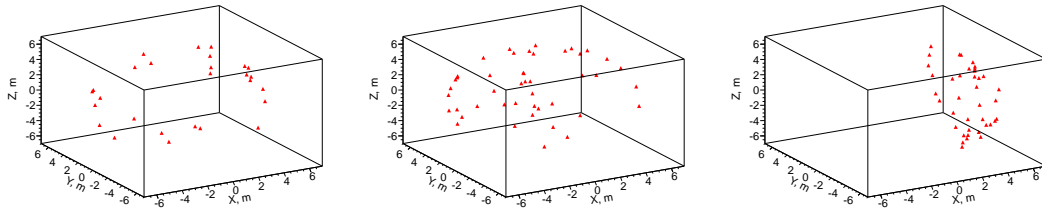


Figure 6: Cherenkov photons distributions on the detector sphere for the three representative event topologies: two back-to-back 1.26 MeV electrons (Left), two 1.26 MeV electrons at 90° angle (Middle), and a single 2.529 MeV electron (Center). All electrons originate at the center of the detector. One randomly selected event is chosen for each category. Default QE is applied.

94 More realistic examples of ^{130}Te $0\nu\beta\beta$ -decay and ^8B events simulated at the center
 95 of the detector are shown in Fig. 7. Early PEs from Cherenkov and scintillation light
 96 are shown. Default simulation QE is applied. Time cut of 33.5 ns on the photon arrival
 97 time is used to select early PEs. Uniformly distributed scintillation light make it more
 98 difficult to guess the event topology. Nevertheless we show that there is still sufficient
 99 difference in the spatial distribution of the early PEs to separate two track and single
 100 track events.

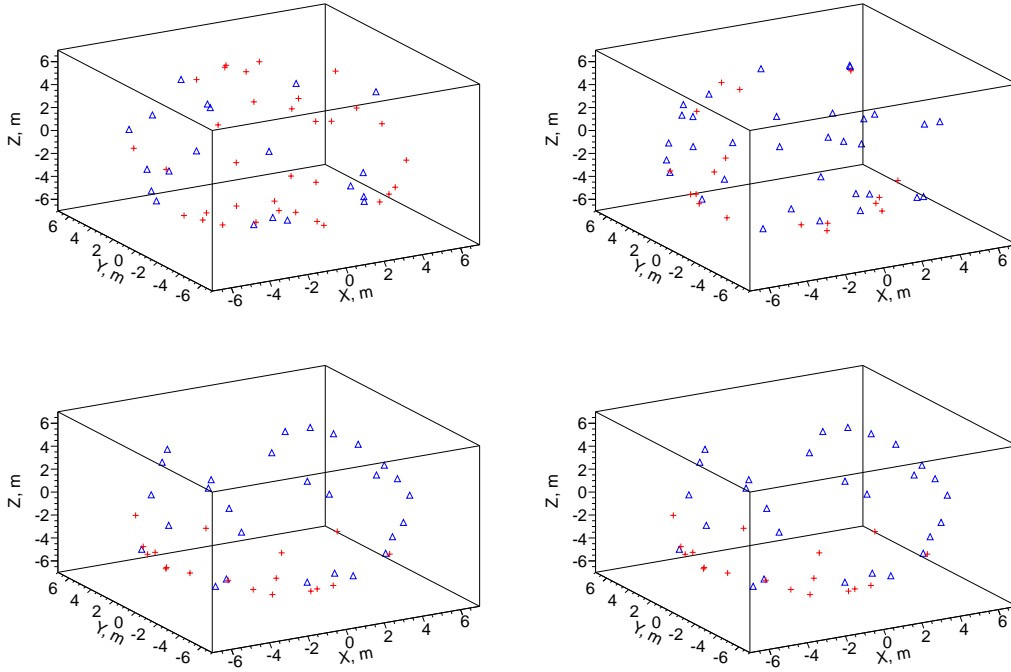


Figure 7: Examples of PEs position on the detector sphere after time cut of 33.5ns. PEs from Cherenkov (red) and scintillation light (blue) are compared. (Top left) ^{130}Te $0\nu\beta\beta$ -decay back-to-back electrons: $E_1=1.257$ MeV, $E_2=1.270$ MeV, $\cos(\theta)=-0.908$. (Top right) ^{130}Te $0\nu\beta\beta$ -decay electrons at $\sim 90^\circ$: $E_1=1.264$ MeV, $E_2=1.263$ MeV, $\cos(\theta)=-0.029$. (Bottom left) ^{130}Te $0\nu\beta\beta$ -decay electrons at $\sim 0^\circ$: $E_1=1.186$ MeV, $E_2=1.340$ MeV, $\cos(\theta)=0.888$. (Bottom right) 2.529 MeV single electron. Events are simulated at the center of the detector. Default QE is applied.

101 For quantitative description of the difference in the event topology we analyze
 102 spherical harmonics of the photon distributions on the detector sphere. We construct
 103 rotation invariant variables and compare them between signal and background events.

104 As it is shown in the bottom part of Fig. 7 $0\nu\beta\beta$ -decay become indistinguishable from
 105 single track topology when the angle between two electrons is small (two degenerate
 106 tracks). Event topologies of $0\nu\beta\beta$ -decay and 8B events are also very similar when only
 107 one electron from $0\nu\beta\beta$ -decay is above the Cherenkov threshold. Therefore spherical
 108 harmonics analysis is most efficient for events with large angular separation between
 109 the two electrons and when both electrons are above Cherenkov threshold.

110 In this paper we focus on topological difference between two tracks and single track
 111 events and do not make any attempt to use absolute directional information to suppress
 112 single track events where direction of the track is consistent with the direction of solar
 113 neutrinos. Once a single track topology is established one can use a centroid method
 114 (see Ref. [1]) to reconstruct directionality of the track (or two degenerate tracks) and
 115 suppress events that are aligned with the direction of 8B solar neutrinos.

116 3.2 Description of Spherical Harmonics Analysis

117 A function $f(\theta, \phi)$ can be decomposed to a sum of spherical harmonics:

$$f(\theta, \phi) = \sum_{l=0}^{\infty} \sum_{m=-l}^l f_{lm} Y_{lm}(\theta, \phi), \quad (1)$$

118 where Y_{lm} are Laplace's spherical harmonics defined in real-value basis using Leg-
 119 endre polynomials P_l :

$$Y_{lm} = \text{LONGformulaHERE}, \quad (2)$$

120 where coefficients f_{lm} are defined as

$$f_{lm} = \text{LONGformulaHERE}. \quad (3)$$

Equation 4 defines power spectrum of $f(\theta, \phi)$ in spherical harmonics representation, s_l , where l is a multiple moment. The power spectrum s_l is invariant under rotation. It is unique to each of the functions $f_i(\theta, \phi)$, $i = 1, 2, 3, \dots$, that can not be transformed into each other by rotation.

$$s_l = \sum_{m=-l}^{m=l} |f_{lm}|^2 \quad (4)$$

One can consider PEs distribution for each of $0\nu\beta\beta$ -decay signal or background event as a function $f_i(\theta, \phi)$. Events with similar power spectrum would correspond to PE distributions on the detector sphere that can be closely aligned by a rotation. Such PE distributions belong to events with similar topology.

Topology of $0\nu\beta\beta$ -decay signal or background in a spherical detector determines the distribution of the PE's on the detector sphere and therefore a set of s_l 's can serve as a quantitative figure of merit for different event topologies. Rotation invariance of s_l 's ensures that this figure of merit does not depend on the orientation of the event with respect to the chosen coordinate frame.

Sum of s_l 's over all multiple moments equals to L2 norm of the function $f(\theta, \phi)$:

$$\sum_{l=0}^{\infty} s_l = \int_{\Omega} |f(\theta, \phi)|^2 d\Omega. \quad (5)$$

Therefore normalized power spectrum

$$S_l = \frac{s_l}{\sum_{l=0}^{\infty} s_l} = \frac{s_l}{\int_{\Omega} |f(\theta, \phi)|^2 d\Omega} \quad (6)$$

can be used to compare shapes of various functions $f(\theta, \phi)$ with different normalization. The total number of PEs detected on the detector sphere fluctuates from event

138 to event, therefore in all of the following we use normalized power S_l .

139 Figure 8 compares normalized power spectrum for the three representative event
 140 topologies that have been already shown in Fig. 5. We note that most of the information
 141 contains in the power spectrum with $l < 6$. In most cases we found that there is no
 142 need to calculate S_l for $l > 3$ to achieve maximal separation between $0\nu\beta\beta$ -decay and
 143 8B events, because fluctuations in the PE distribution produce a lot of noise in the
 144 power spectrum for higher orders of multiple moments.

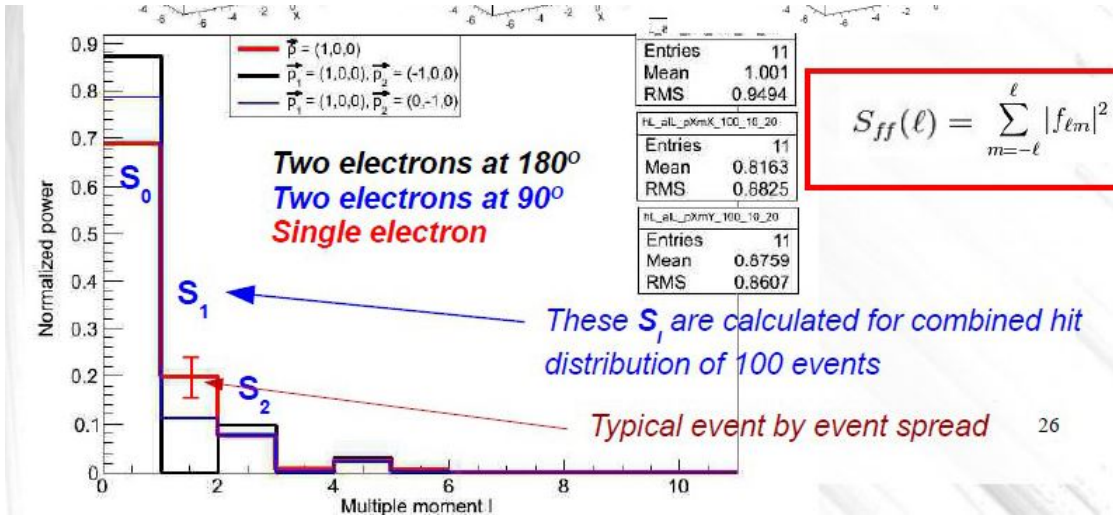


Figure 8: Average S_l values for two electrons at 180 degree (color1) and 90 degree (color2) 1.5 MeV each and a single electron (color3) with the energy of 3 MeV. Error bars are RMS values of each corresponding individual S_l distribution (each consists of 1000 events simulated at the center of the detector) indicating typical event-by-event variation.

145 3.3 Spherical Harmonics Analysis and Off-center Events

146 In order to compare spherical harmonics for events with vertices located off-center any-
 147 where inside the detector volume a coordinate transformation for each photon hit is
 148 needed. The necessary transformation applied for each PE within an event is illustrated
 149 in Fig. 9. Solid circle with radius R schematically shows actual detector boundaries.
 150 Dotted circle shows a new sphere with the same radius R , which now has the event
 151 vertex in its center. The radius vector of each PE is stretched or shortened to its inter-

152 section with this new sphere using transformation $\vec{r}_{PE} = \frac{\vec{a}}{|\vec{a}|} \cdot R$. Where \vec{r}_{PE} is a new
 153 radius vector of a PE and $\vec{a} = \vec{r}_{PE} - \vec{r}_{vtx}$ with \vec{r}_{PE} and \vec{r}_{vtx} being radius vectors of the
 154 PE and the vertex in the original coordinates respectively.

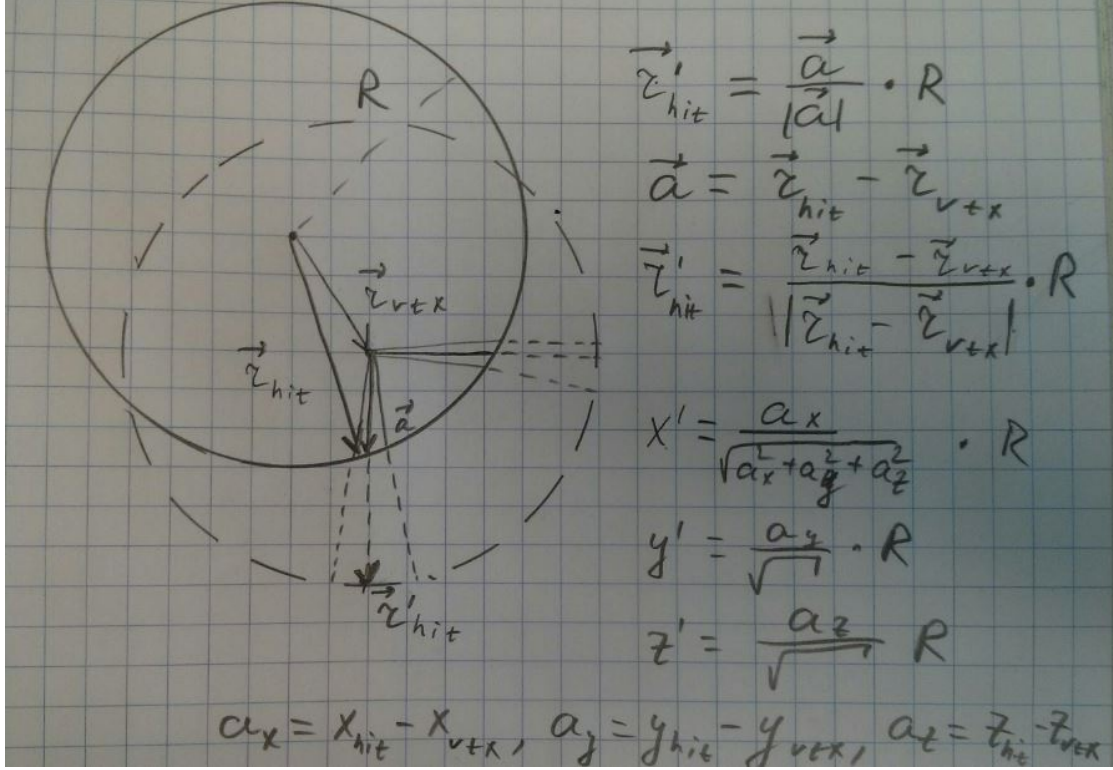


Figure 9: Coordinate transformation applied to events that are off-center. Solid circle with radius R schematically shows actual detector boundaries. Dotted circle shows a new sphere with the same radius R , which now has the event vertex in its center. The radius vector of each PE is stretched or shortened to its intersection with this new sphere using transformation $\vec{r}_{PE} = \frac{\vec{a}}{|\vec{a}|} \cdot R$. Where \vec{r}_{PE} is a new radius vector of a PE and $\vec{a} = \vec{r}_{PE} - \vec{r}_{vtx}$ with \vec{r}_{PE} and \vec{r}_{vtx} being radius vectors of the PE and the vertex in the original coordinates respectively.

155 3.4 Implementation of the spherical harmonics analysis

156 **A few words on the implementation.** Calculation of S_l 's requires numerical
 157 **integration that needs to be explained.**

158 To illustrate spherical harmonics analysis technique we compare distributions of S_0 ,
 159 S_1 , S_2 , and S_3 for the three representative event topologies described in Sec. 3.1. Almost

160 all the information about event topology is carried by Cherenkov light. Therefore we
161 first show spherical harmonics for back-to-back, 90° and single track topologies based
162 on Cherenkov PEs only (see Fig. 10).

163 Two top panels of Fig. 10 show 2-dimensional distributions, S_0 vs S_1 and S_2 vs S_3 ,
164 to demonstrate that all four S_l 's provide separation between event topologies. No QE
165 is applied in simulation of these events. We also introduce a 1-dimensional variable,
166 S_{01} (bottom panel of Fig. 10), that has the best separation power for majority of
167 event topologies considered in this paper. S_{01} is defined as a projection of S_1 vs S_2
168 distribution onto a linear fit of this 2-D distribution.

169 The effects due to presence of scintillation light and applying default QE are shown
170 in Fig. 11. Spherical harmonics of the same three representative event topologies are
171 now calculated using early light (photons with arrival time less than 33.5 ns) that
172 contains both directional Cherenkov light and uniform scintillation light. Default QE
173 is also applied. Higher order multiple moments, S_2 and S_3 , no longer provide noticeable
174 separation between different event topologies.

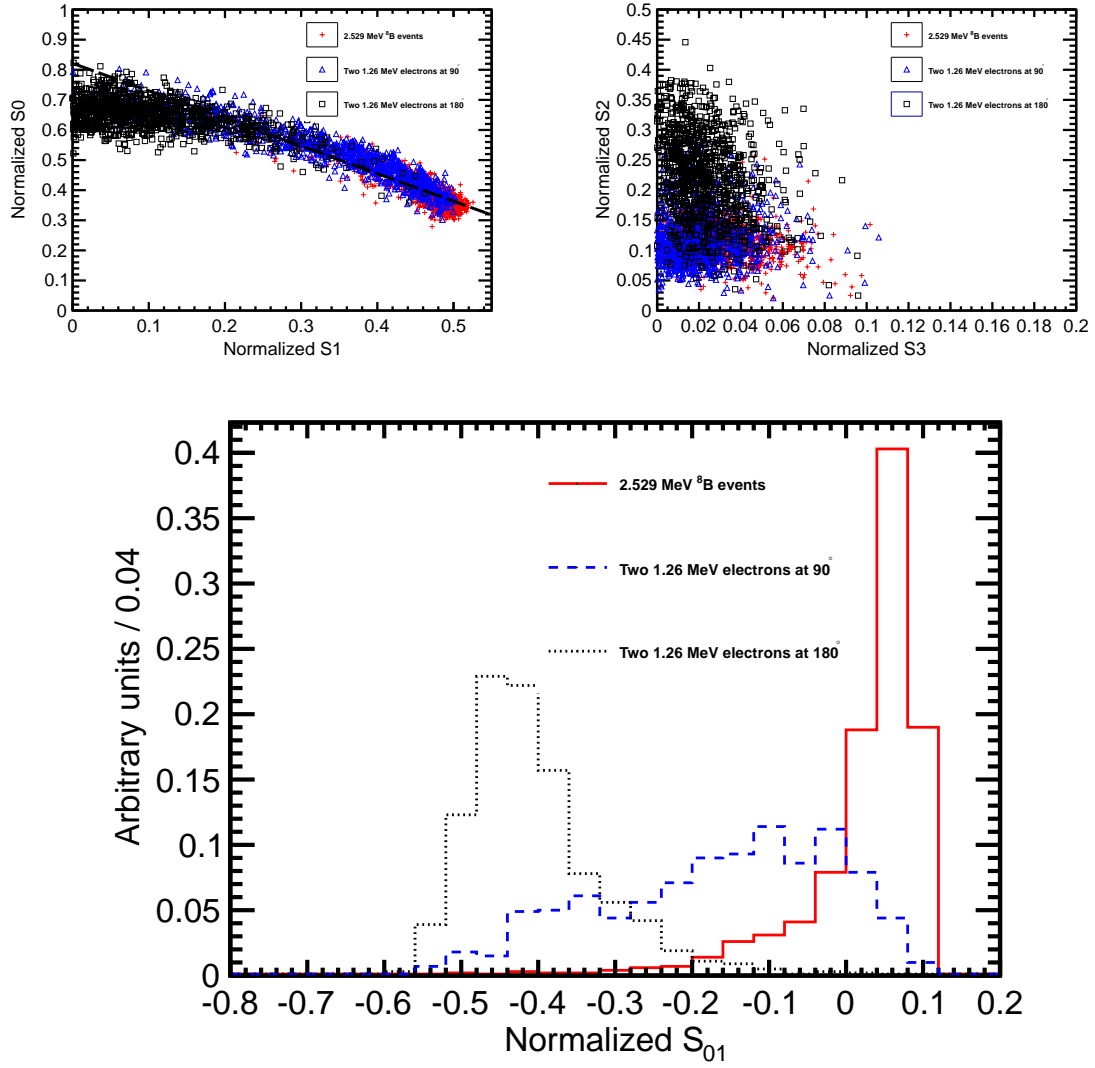


Figure 10: Spherical harmonics for three event topologies: two back-to-back 1.26 MeV electrons (black squares and black dotted line), two 1.26 MeV electrons at 90° angle (blue triangles and blue dashed line), and a single 2.529 MeV electron representing ^8B background (red crosses and red solid line). Simulation of 1000 events originated at the center of the sphere. Perfect separation between Cherenkov and scintillation light is implemented in this simulation by using only Cherenkov photons. (Top left) S_0 versus S_1 scatter plot. Black dotted line is a linear fit of the 90° topology and ^8B events. Variable S_{01} is defined as a projection of 2D distribution onto this linear fit. (Top right) S_2 versus S_3 scatter plot. (Bottom) S_{01} distributions for the three topologies. These distributions are normalized to unit area for shape comparison

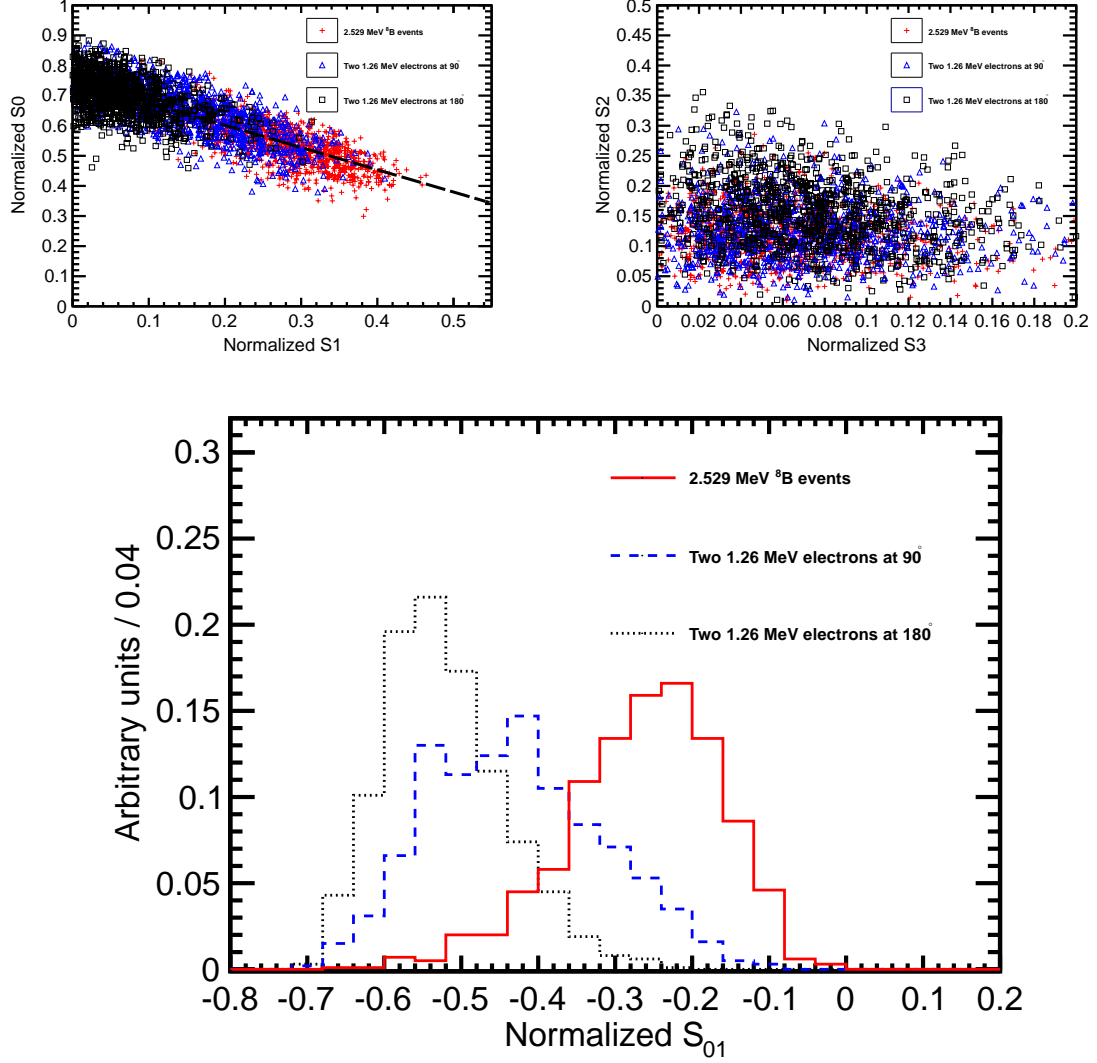


Figure 11: Spherical harmonics for three event topologies: two back-to-back 1.26 MeV electrons (black squares and black dotted line), two 1.26 MeV electrons at 90° angle (blue triangles and blue dashed line), and a single 2.529 MeV electron representing ${}^8\text{B}$ background (red crosses and red solid line). Simulation of 1000 events originated at the center of the sphere. Separation between Cherenkov and scintillation light is implemented 33.5 ns cut on the photon arrival time. Perfect vertex reconstruction - true vertex position is used. (Top left) S_0 versus S_1 scatter plot. Black dotted line is a linear fit of the 90° topology and ${}^8\text{B}$ events. Variable S_{01} is defined as a projection of 2D distribution onto this linear fit. (Top right) S_2 versus S_3 scatter plot. (Bottom) S_{01} distributions for the three topologies. These distributions are normalized to unit area for shape comparison

4 Performance and Experimental Challenges

4.1 Performance of the spherical harmonics analysis on $0\nu\beta\beta$ -decay and 8B events.

Comparison of S_0 and S_1 distributions between $0\nu\beta\beta$ -decay and 8B events is shown in Fig. 12. There is a noticeable separation between the signal and background. We also note that in the energy range of interest S_l 's do not have strong dependence on the energy deposited in the detector, which makes them reliable discriminators at the endpoint of the $0\nu\beta\beta$ -decay energy spectrum. The information about the event topology is complimentary to the energy measurements.

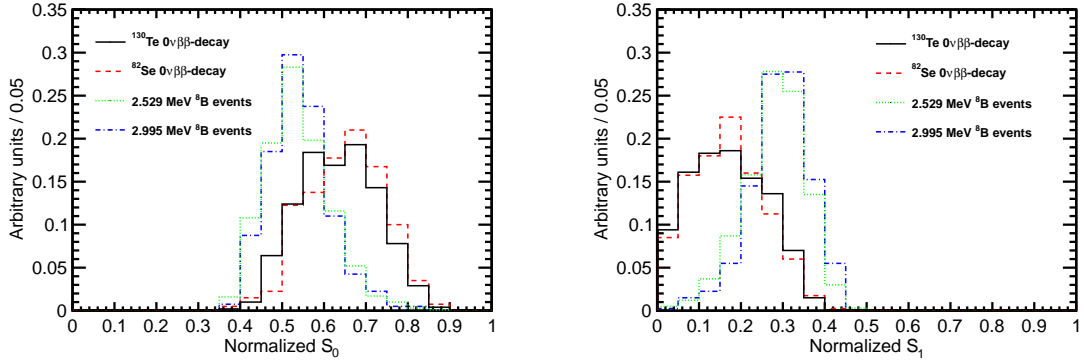


Figure 12: S_0 (left) and S_1 (right) distributions for events with two different event topologies and total kinetic energy. ${}^{130}\text{Te}$, ${}^{82}\text{Se}$ $0\nu\beta\beta$ -decay, 2.529 MeV and 2.995 MeV events are compared. The simulation is done for events with the vertex in the center of the detector. 8B events are implemented as 2.529 MeV or 2.995 MeV electrons with initial direction along x -axis. Perfect vertex reconstruction - true vertex position is used. Time cut of 33.5 ns on the photon arrival time is applied.

Figure 13 shows separation between ${}^{130}\text{Te}$ signal and 8B background events simulated at the center of the detector. True values of vertex position and time is used. Time cut of 33.5 ns on the photon arrival time is applied to separate Cherenkov and scintillation light. Most of the discrimination between signal and background comes from S_0 and S_1 . In the following S_2 and S_3 are not used to separate ${}^{130}\text{Te}$ and 8B

189 events². The scatter plot of S_2 vs S_3 is shown here for completeness.

190 In order to optimize separation between ^{130}Te signal and ^8B background a linear
191 combination of S_0 and S_1 , S_{01} , is used. A linear fit, $S_0 = A \times S_1 + B$, of 2-dimensional S_0
192 vs S_1 scatter plot is performed as shown in Fig. 13. Then this 2-dimensional distribution
193 is projected onto the fitted line. **A little bit of math here to quantitatively**
194 **describe S_{01} via S_0 and S_1 :** A new coordinate frame is obtained by rotation of the
195 original S_0 - S_1 frame at angle θ obtained from the fit: $\tan(\theta)=A$. A transformation,
196 $S_{01} = S_1 \cdot \cos(\theta) + S_0 \cdot \sin(\theta)$, defines the S_{01} variable.

197 Bottom plot in Fig. 13 shows performance of the S_{01} variable to separate ^{130}Te
198 signal and ^8B background. A fit to this distribution can be done to optimize the
199 discrimination power in a particular experimental settings. Here we refrain from quan-
200 titative estimates on the improvements in sensitivity to $0\nu\beta\beta$ -decay search using this
201 method of spherical harmonics as a reliable estimate would require a dedicated analysis
202 taking into account all the details of a particular experiment.

203 4.2 Experimental challenges

204 So far only events at the center of the detector have been considered. In this sec-
205 tion we discuss performance of the spherical harmonics analysis for events distributed
206 within the fiducial volume of the detector taking into account finite resolution on vertex
207 position reconstruction.

208 When the vertex is not at the center, a uniform time cut on the photon arrival
209 time is no longer effective in the selection of Cherenkov photons. In the case of off-
210 center vertex, even significantly delayed scintillation photons can reach the side of the
211 detector that is closer to the vertex much earlier than Cherenkov photons traveling to
212 the opposite side of the detector. Therefore, the time cut has to be position dependent
213 and take into account the total distance traveled by each individual photon.

214 We found that the time cut defined as $\Delta t = t_{measured}^{phot} - t_{predicted}^{phot} < 1$ ns selects pho-

² S_2 and S_3 are helpful for separation of ^{130}Te signal from ^{10}C background. See Appendix.

215 tons with sufficient fraction of Cherenkov photons. Predicted time, $t_{predicted}^{phot}=l/v^{phot}$,
 216 depends on total distance, l , traveled by the photon and proper assignment of the
 217 velocity for each photon, v^{phot} , that depends on index of refraction³. Therefore the
 218 relative Cherenkov/scintillation composition of the light selected with this Δt time cut
 219 depends on the vertex location and chromatic dispersions.

220 Due to chromatic dispersion, even with perfect vertex reconstruction one cannot
 221 achieve the same level of separation between Cherenkov and scintillation light com-
 222 pared to the central events considered above in Section 4. This in turn reduces the
 223 effectiveness of the spherical harmonics analysis in separating of $0\nu\beta\beta$ -decay and 8B
 224 events (see Fig. 14). However next generation detectors can recover losses due to chro-
 225 matic dispersion by choosing liquid scintillators with a more narrow emission spectrum.

226 Imprecise knowledge of the vertex position due to finite resolution is another factor
 227 affecting performance of the spherical harmonics analysis. Small deviations in vertex
 228 reconstruction cause large effect on S_0 and S_1 for single electron event topology. For
 229 the vertices shifted along the direction of the electron the Δt cut makes uniform
 230 scintillation light distribution less uniform. The Δt cut selects more forward emitted
 231 photons in the case when the reconstructed vertex is shifted to the direction opposite
 232 to the electron momentum (enhancing forward region populated by Cherenkov photons
 233 - more asymmetric photon distribution causing higher values of S_1). It selects more
 234 backward emitted photons in the case when the reconstructed vertex is shifted in the
 235 direction along the electron momentum (counter balancing forward region populated
 236 by Cherenkov photons - more symmetric photon distribution causing smaller values of
 237 S_1).

238 **Solution to this problem would be a better selection criteria of early**
 239 **light. It has to preserve high admixture of the Cherenkov photons, but**
 240 **needs to select scintillation photons in a more uniform manner. Working**
 241 **on it, but may not be simple so I don't want to include it in this paper.**

242 Good vertex resolution is essential for spherical harmonics analysis. Such strong

³We use average index of refraction of $n=1.53$

243 dependence on the vertex resolution can be addressed by choosing a different liquid
244 scintillator mixture with a more delayed emission of the scintillation light. Figure ??
245 shows spherical harmonics calculated for the time profile which has scintillation com-
246 ponent delayed by 0.5ns with respect to what is shown in Fig. 3

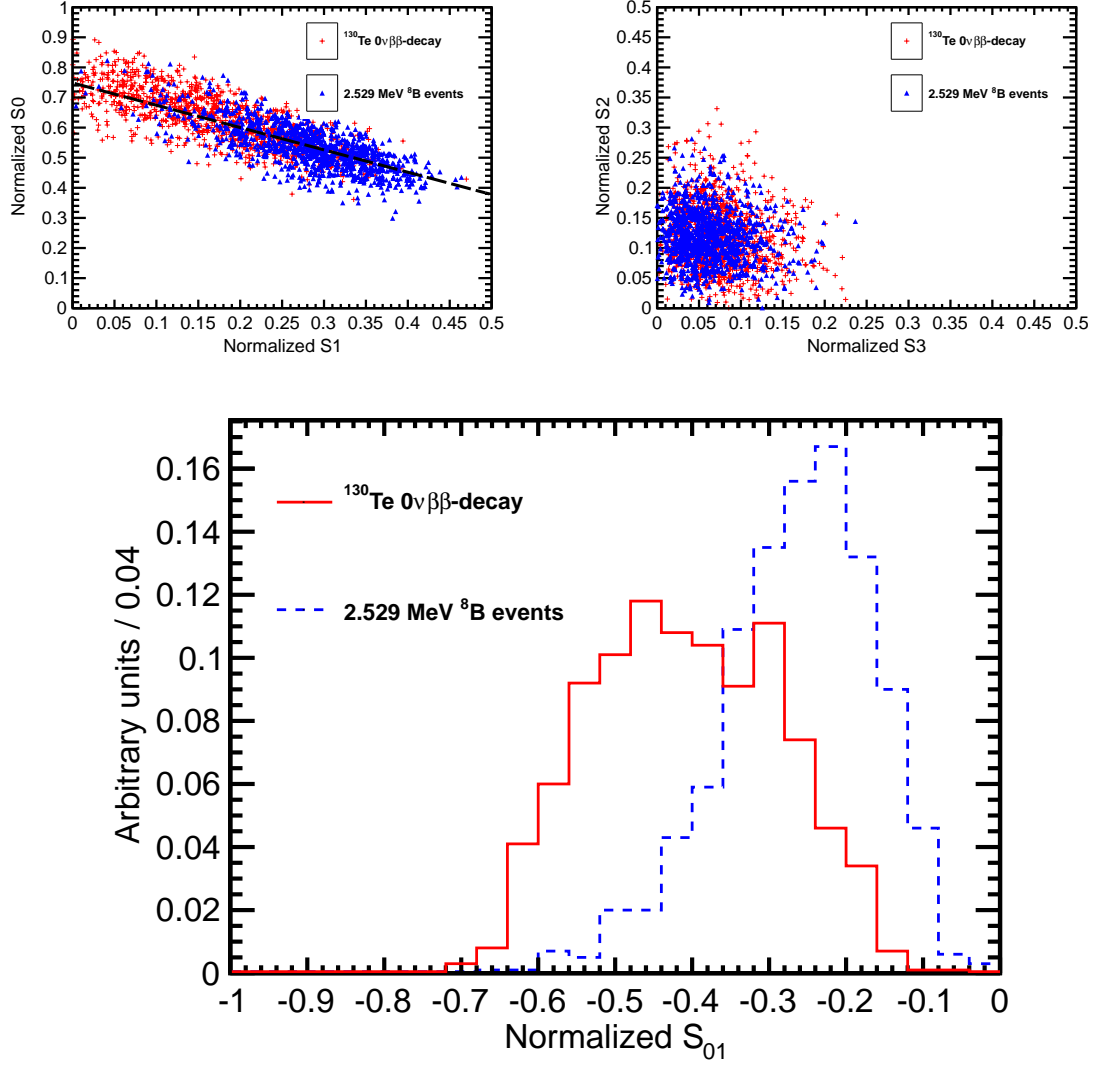


Figure 13: Spherical harmonics comparison between $^{130}\text{Te } 0\nu\beta\beta\text{-decay}$ signal ($Q=2.529$ MeV) (red) and ^8B solar neutrinos background (blue) for 1000 simulated events originated at the center of the sphere. ^8B events are implemented as 2.529 MeV electrons with initial direction along x -axis. Perfect vertex reconstruction - true vertex position is used. Time cut of 33.5 ns on the photon arrival time is applied. (Top left) S_0 versus S_1 scatter plot. Black dotted line is a linear fit of these 2D histograms. Variable S_{01} is defined as a projection of 2D distribution onto this linear fit. (Top right) S_2 versus S_3 scatter plot. (Bottom) S_{01} distribution for the signal and background.

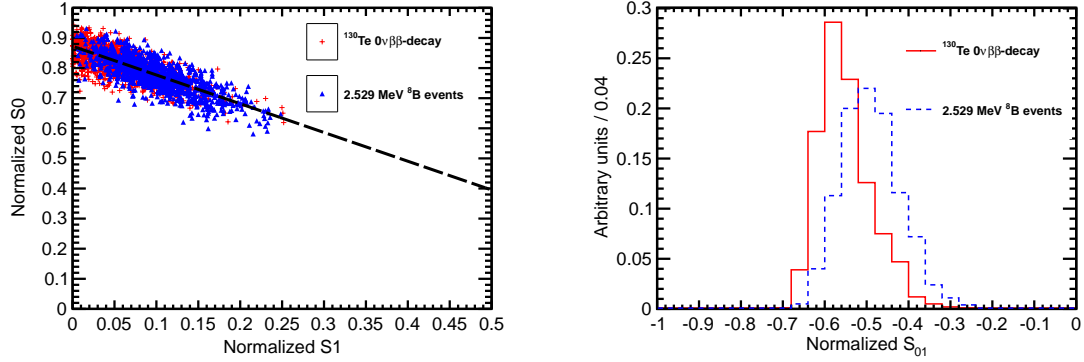


Figure 14: Spherical harmonics comparison between ^{130}Te $0\nu\beta\beta$ -decay signal ($Q=2.529$ MeV) (red) and ^8B solar neutrinos background (blue) for 1000 simulated events. Vertices are uniformly distributed within the fiducial volume, $R < 3$ m. ^8B events are implemented as 2.529 MeV electrons with the initial momentum direction uniformly distributed within 4π solid angle. Perfect vertex reconstruction - true vertex position is used. (Left) S_0 versus S_1 scatter plot. Black dotted line is a linear fit of these 2D histograms. Variable S_{01} is defined as a projection of 2D distribution onto this linear fit. (Right) S_{01}

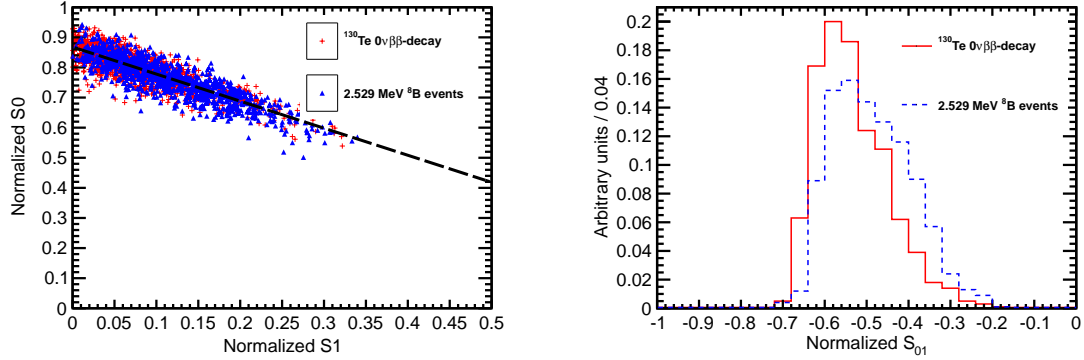


Figure 15: Spherical harmonics comparison between ^{130}Te $0\nu\beta\beta$ -decay signal ($Q=2.529$ MeV) (red) and ^8B solar neutrinos background (blue) for 1000 simulated events. Vertices are uniformly distributed within the fiducial volume, $R < 3$ m. ^8B events are implemented as 2.529 MeV electrons with the initial momentum direction uniformly distributed within 4π solid angle. Vertex is smeared with 3 cm resolution. (Left) S_0 versus S_1 scatter plot. Black dotted line is a linear fit of these 2D histograms. Variable S_{01} is defined as a projection of 2D distribution onto this linear fit. (Right) S_{01}

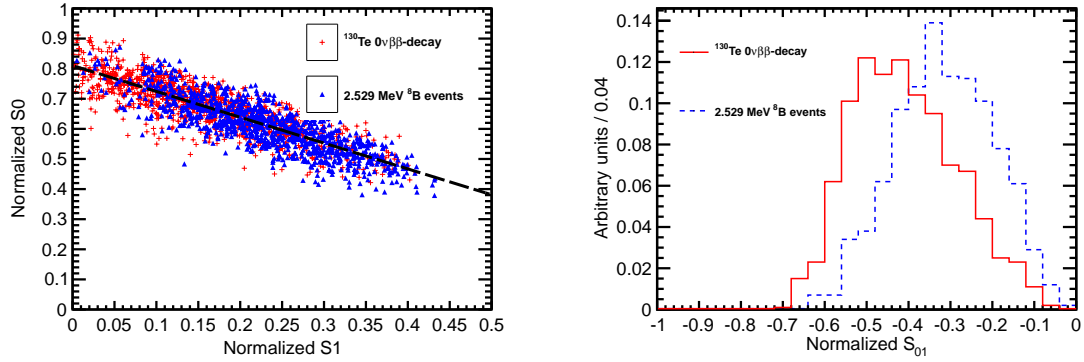


Figure 16: Spherical harmonics comparison between ^{130}Te $0\nu\beta\beta$ -decay signal ($Q=2.529$ MeV) (red) and ^8B solar neutrinos background (blue) for 1000 simulated events. Vertices are uniformly distributed within the fiducial volume, $R < 3$ m. ^8Be events are implemented as 2.529 MeV electrons with the initial momentum direction uniformly distributed within 4π solid angle. Vetrex is smeared with 3 cm resolution. **Scintillation light is delayed by additional 0.5 ns.** (Left) S_0 versus S_1 scatter plot. Black dotted line is a linear fit of these 2D histograms. Variable S_{01} is defined as a projection of 2D distribution onto this linear fit. (Right) S_{01}

5 Conclusions

A technique based on spherical harmonics analysis is discussed to separate $0\nu\beta\beta$ -decay from 8B solar neutrino interactions. The separation is based on distinct event topologies of signal and background. This event topology information is available in addition to the measurements of the energy deposited in the detector. This technique may be further developed and adopted by future large scale liquid scintillator detectors to suppress background coming from 8B solar neutrino interactions in the detector volume. The performance of the technique is mostly affected by chromatic dispersions, vertex reconstruction and time profile of the emission of the scintillation light. We show that a liquid scintillator detector with a ~ 1 ns total delay of the scintillation light with respect to the Cherenkov light allows for use of spherical harmonics analysis as an extra handle to extract $0\nu\beta\beta$ -decay signal.

6 Acknowledgments

To be finalized based on opt-in for the author list.

A $0\nu\beta\beta$ -decay vs ${}^{10}C$ background

Other common backgrounds to $0\nu\beta\beta$ -decay search include radioactive decays of nuclei excited by cosmic muons and decays of Th and U naturally present in the materials. In a liquid scintillator detectors most of events from Th and U decays are happening in the materials of the scintillator enclosure. Typically they enter the fiducial volume as 2.6 MeV gammas. These gammas either shower too late or have mis-reconstructed vertex. Both effects depend on details of a particular experiment and therefore in this paper we make no attempt to introduce a topology reconstruction for the backgrounds coming from Th and U lines. Cosmic induced backgrounds, to the contrary, are more generic and originate inside the fiducial volume. In this section we discuss

event topology of ^{10}C events that are most relevant in the energy of 2-3 MeV.

Typical energy deposition by ^{10}C events is shown in Fig. 17. We propose to use spherical harmonics analysis to separate $0\nu\beta\beta$ -decay events from ^{10}C events that within energy resolution overlap with the $0\nu\beta\beta$ -decay Q-value.

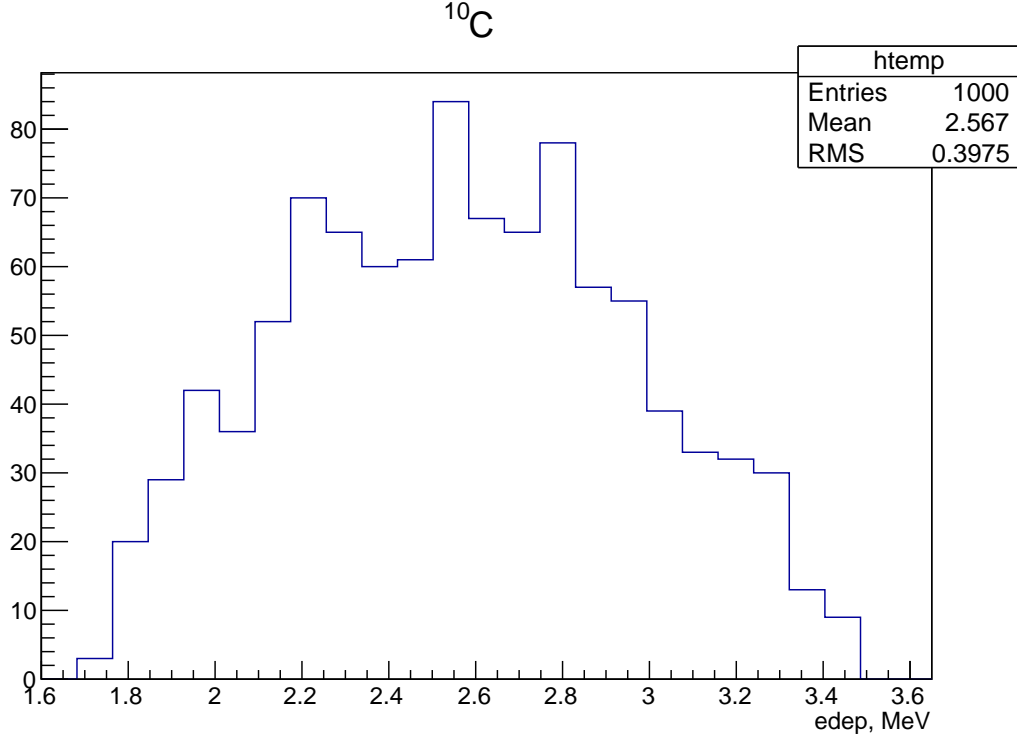


Figure 17: Energy deposition in ^{10}C events.

We note that 98% of ^{10}C decays through the excited state of $^{10}\text{B}(718)$ that has a half-life time of ~ 1 ns. Therefore majority of ^{10}C events have a prompt positron accompanied by a delayed 0.718 MeV gamma. This delayed gamma affects PEs arrival time distribution. Figure 18 shows shape comparison of PEs arrival time distribution between ^{130}Te $0\nu\beta\beta$ -decay and ^{10}C events. Time profile of the scintillation photons can be used to separate signal from ^{10}C events.

Comparison of spherical harmonics is shown in Fig. 19. ^{10}C events are generated at the center of the detector. True vertex position is used to apply a 33.5 ns time cut to select photons for the spherical harmonics analysis. The separation is seen in S0 vs S1

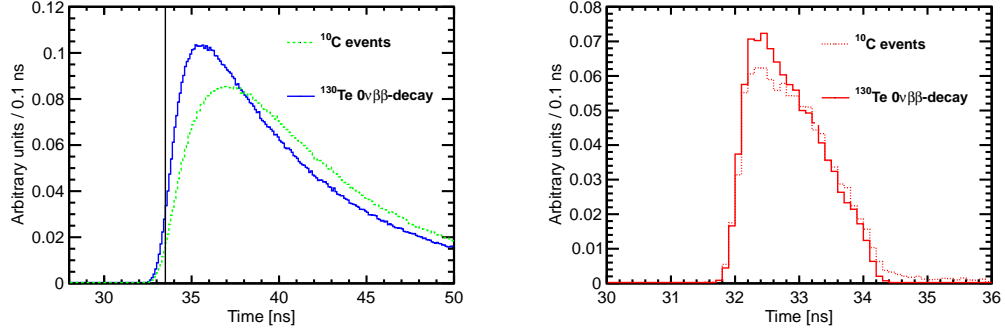


Figure 18: Photo-electron (PE) arrival times after application of the photo-detector transit time spread (TTS) of 100 ps for the simulation of 1000 $0\nu\beta\beta$ -decay events of ^{130}Te (solid lines) and ^{10}C (dotted lines) events at the center of the detector. All distributions are normalized for shape comparison. **Absolute number of PEs per event depends on the total energy deposited in the detector. Figure 17 shows energy deposited in the detector in ^{10}C events.** (Left) Scintillation PEs arrival time. The black vertical line illustrates a time cut at 33.5 ns. (Right) Cherenkov PEs arrival time.

284 and S2 vs S3 scatter plots. We project both scatter plots to a line that gives maximum
 285 separation (two bottom panels in Fig. 19).

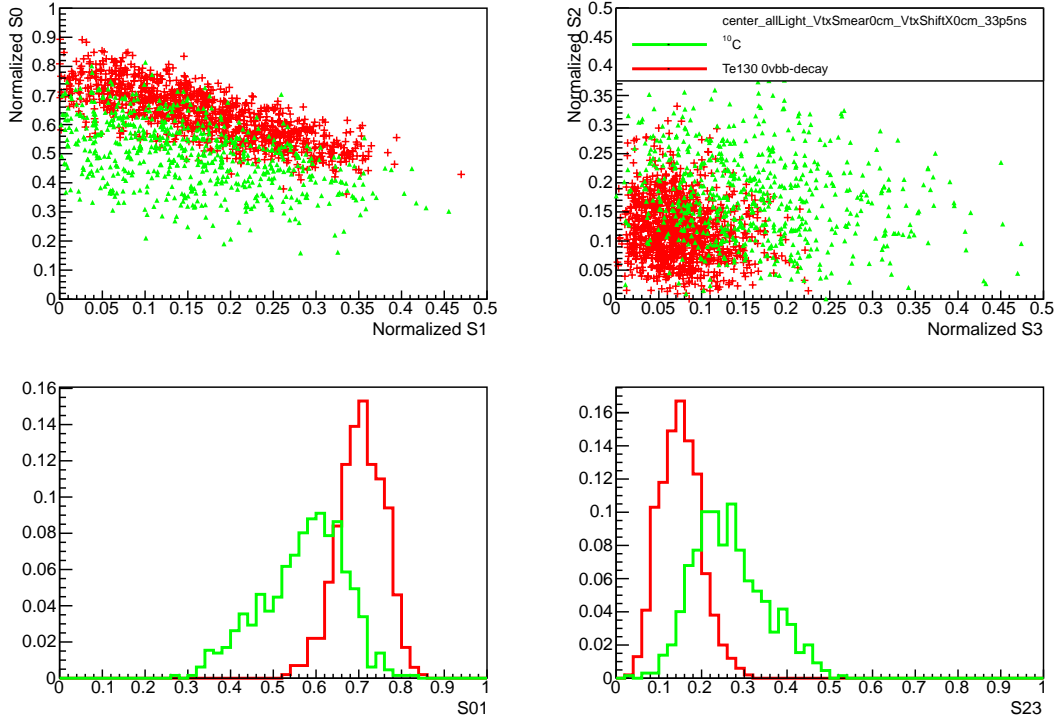


Figure 19: Spherical harmonics comparison between ^{130}Te $0\nu\beta\beta$ -decay signal ($Q=2.529$ MeV) (red) and ^{10}C solar neutrinos background (blue) for 1000 simulated events originated at the center of the sphere. ^{10}C with energy deposition between 2.1 MeV and 2.9 MeV are considered. Perfect vertex reconstruction - true vertex position is used. Time cut of 33.5 ns on the photon arrival time is applied. (Top left) S_0 versus S_1 scatter plot. (Top right) S_2 versus S_3 scatter plot. (Bottom left) Distribution of the S_{01}^{C10} variable calculated for signal (red) and background (green). (Bottom right) Distribution of the S_{23}^{C10} variable calculated for signal (red) and background (green).

References

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- [2] A good ref to SNO+ backgrounds description.