

$$L^{[m \times m]} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & \ddots & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Strips bias terms from  $\Theta$

**Linear Regression:**

$$J(\theta) = \frac{1}{2m}(X\theta - y)^T(X\theta - y) + \frac{\lambda}{2m}[(L\theta)^T(L\theta)]$$

Cost Function

$$\nabla J = \frac{1}{m}(X^T(X\theta - y) + \lambda L\theta)$$

Cost Gradient

$$\theta := (1 - \frac{\alpha \lambda}{m}L\theta) - \frac{\alpha}{m}X^T(X\theta - y)$$

Paramater Update Rule

**Logistic Regression:**

$$\sigma(z) = \frac{1}{1+e^{-z}}$$

Logistic/Sigmoid Function

$$h = \sigma(X * \Theta')$$

Hypothesis/Prediction Function

$$J(\theta) = -\frac{1}{m}[y^T \log(h) + (1 - y)^T \log(1 - h)] + \frac{\lambda}{2m}[(L\theta)^T(L\theta)]$$

Cost Function

$$\nabla J = \frac{1}{m}(X^T(h - y) + \lambda L\theta)$$

Cost Gradient

$$\theta := (1 - \frac{\alpha \lambda}{m}L\theta) - \frac{\alpha}{m}X^T(h - y)$$

Paramater Update Function

**Neural Networks:**

$$\sigma'(z) = \sigma(z) * (1 - \sigma(z))$$

Sigmoid Derivative

$$a^l = \sigma(a^{l-1} * [\theta^{l-1}]^T)$$

Activation/Output of layer l

$$Y^{(i)} = \begin{bmatrix} 0 \\ 0 \\ \vdots \\ 1 \\ \vdots \\ 0 \end{bmatrix}, Y[k] = 1$$

One-Hot Form of Classification Result

$$J(\theta) = -\frac{1}{m} \sum_{i=1}^m \sum_{j=1}^{|L|} [Y * \log(a^{(L)}) + (1 - Y) * \log(1 - a^{(L)})] + \frac{\lambda}{2m} \sum_{l=1}^{L-1} \sum_{i=1}^{s_l} \sum_{j=1}^{s_{l+1}} (\theta_{i,j}^{(l)})^2$$

Cost function of NN used for Backpropogation, condensed down to a scalar

$$\delta^{(L)} = a^{(L)} - Y$$

Error of Neural Network Output

$$\delta^{(l)} = \delta^{(l+1)} \widehat{\Theta}^{(l)} \odot \sigma'(a^{(l)} \Theta^{(l)})$$

Error of layer l

$$\widehat{\Theta}^{(l)} = \Theta^{(l)}[i,j]; i \in [1,2,3...m], j \in [2,3,4,...n]$$

Reduced Paramater Matrix (No Bias Terms)

$$\Delta^{(l)} = \delta^{(l+1)T} * a^{(l)}$$

Cumulative Error of Layer l

$$\nabla_{\frac{\partial J}{\partial \Theta^{(l)}}} = \frac{1}{m} \Delta^{(l)} + \frac{\lambda}{m} \Theta^{(l)} L$$

Gradient of the Cost Function for Layer l