

# CS 420 - Compilers

Dr. Chen-Yeou (Charles) Yu

- **A Translator for Simple Expressions**
- **Lexical Analysis**

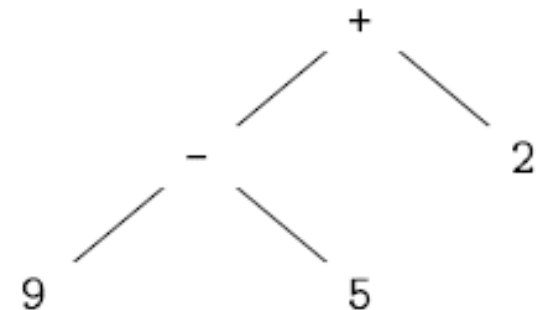
# A Translator for Simple Expressions

- Objective:
    - In this example, we need to do **infix to postfix** translation
    - We start with just **plus** and **minus**
    - Finding a grammar for the desired language is one problem
    - Given a grammar, constructing a translator for the language is another problem
    - We are tackling the second problem.
    - One problem we must **solve** is that, this grammar is left recursive.
- ```
expr → expr + term { print('+') }  
expr → expr - term { print('-') }  
expr → term  
term → 0           { print('0') }  
...  
term → 9           { print('9') }
```

# A Translator for Simple Expressions

- **Abstract and Concrete Syntax**

- If the **syntax tree** would just have the operators **+** and **-** and the 10 digits 0,1,...,9. That would be called the **abstract syntax tree**. (AST)
- A parse **tree** coming from a **grammar** is technically called a **concrete syntax tree**.
- An (AST) example: input is “9-5+2”.
- The root represents the operator +.



# A Translator for Simple Expressions

- **Adapting the Translation Scheme**

- From the last time of the class, we have this:
  - In general, **for any nonterminal A**, and **any strings  $\alpha$ , and  $\beta$**  ( $\alpha$  and  $\beta$  cannot start with A). we can replace the pair of productions in this way!

$$A \rightarrow A \alpha \mid \beta$$

with the triple

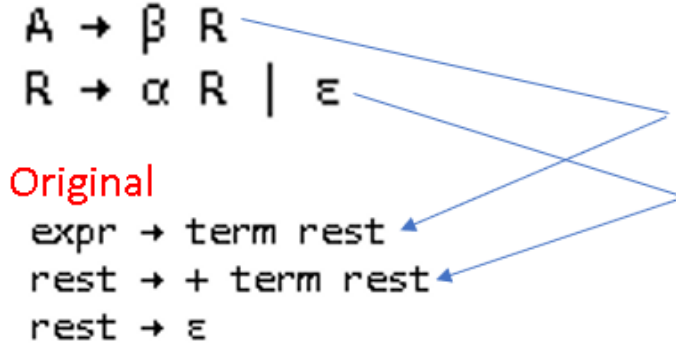
$$A \rightarrow \beta R$$
$$R \rightarrow \alpha R \mid \epsilon$$

- Where A is **expr**, **R is rest**,  **$\alpha$  is + term**, and  $\beta$  is **term**.
- And we find there is a **mapping** to our original production and **removed the left recursion!!**

**New Form**

$$A \rightarrow \beta R$$
$$R \rightarrow \alpha R \mid \epsilon$$

**Original**

$$\text{expr} \rightarrow \text{term rest}$$
$$\text{rest} \rightarrow + \text{term rest}$$
$$\text{rest} \rightarrow \epsilon$$


# A Translator for Simple Expressions

- **Adapting the Translation Scheme (Cont.)**

- This time there are two operators + and - so we replace the triple

- $A \rightarrow A \alpha \mid A \beta \mid \gamma$

with the quadruple

- $A \rightarrow \gamma R$
  - $R \rightarrow \alpha R \mid \beta R \mid \epsilon$

And this time we have “actions”, check this:

- Similarly,  $\alpha$  is + term { print('+') };  $\beta$  is - term { print('-') };  $\gamma$  is term; A is expr; and **R is rest**
- Eventually, the formulas still hold and we get
- It is said that the left recursion is removed!
- This is the translation scheme for Left-recursion elimination

```
expr → expr + term { print('+') }  
expr → expr - term { print('-') }  
expr → term  
term → 0           { print('0') }  
...  
term → 9           { print('9') }
```

```
expr → term rest  
rest → + term { print('+') } rest  
      | - term { print('-') } rest  
      |  $\epsilon$   
term → 0           { print('0') }  
...  
      | 9           { print('9') }
```

# A Translator for Simple Expressions

- **Adapting the Translation Scheme (Cont.)**
  - **Finally, we translate 9-5+2 to 95-2+**

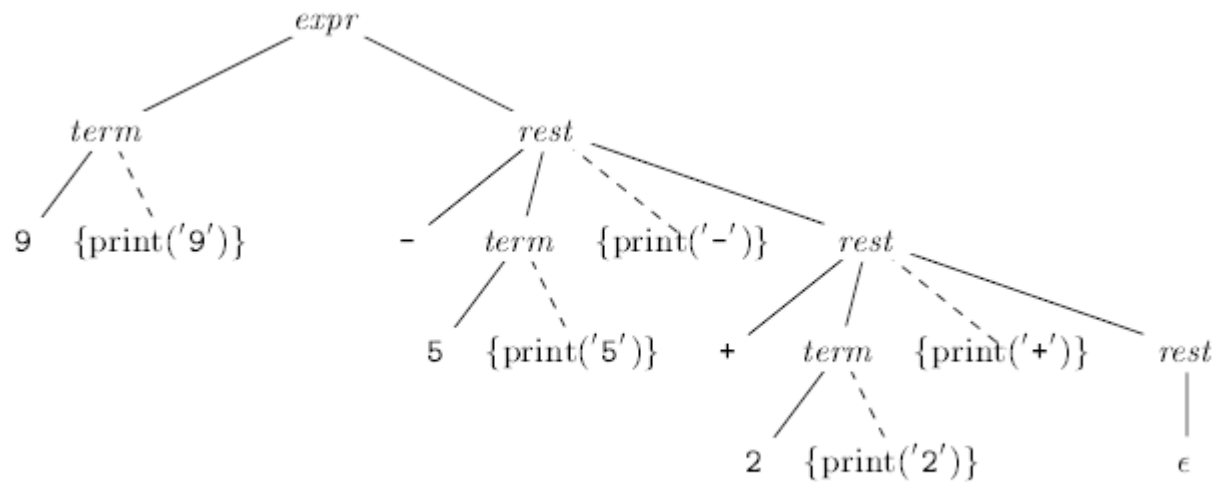


Figure 2.24: Translation of 9-5+2 to 95-2+

# A Translator for Simple Expressions

- **Procedures for the Non-terminals *expr*, *term*, and *rest***

- Fig. 2.25 implement the syntax-directed translation scheme in Fig. 2.23.
- These functions mimic the production bodies of the corresponding non-terminals.

- *expr* implements the production

*expr*  $\rightarrow$  *term* *rest*,  
by the calls *term*(),  
followed by *rest*().

- See the next page for  
Fig. 2.25 pseudo-code

$$\begin{array}{lll} \textit{expr} & \rightarrow & \textit{term} \textit{rest} \\ \\ \textit{rest} & \rightarrow & + \textit{term} \{ \text{print}(' + ') \} \textit{rest} \\ & | & - \textit{term} \{ \text{print}(' - ') \} \textit{rest} \\ & | & \epsilon \\ \\ \textit{term} & \rightarrow & 0 \{ \text{print}(' 0 ') \} \\ & | & 1 \{ \text{print}(' 1 ') \} \\ & & \dots \\ & | & 9 \{ \text{print}(' 9 ') \} \end{array}$$

Figure 2.23: Translation scheme after left-recursion elimination



# A Translator for Simple Expressions

```
void expr() {  
    term(); rest();  
}  
  
void rest() {  
    if ( lookahead == '+' ) {  
        match('+'); term(); print('+'); rest();  
    }  
    else if ( lookahead == '-' ) {  
        match(' - '); term(); print(' - '); rest();  
    }  
    else { } /* do nothing with the input */ ;  
}  
  
void term() {  
    if ( lookahead is a digit ) {  
        t = lookahead; match(lookahead); print(t);  
    }  
    else report("syntax error");  
}
```

- If the test succeeds, variable *t* saves the digit represented by lookahead so it can be written after the call to *match*.
- Note that *match* changes the lookahead symbol, so the digit needs to be saved for later printing

*rest* →  $\epsilon$

The epsilon production is only used when all others fail (that is why it is the else arm and not the other else if arms).

Figure 2.25: Pseudocode for nonterminals *expr*, *rest*, and *term*.

# A Translator for Simple Expressions

- **Simplifying the translator**

Our job is to eliminate the tail recursive. How to do it?

Next page is the solution!

Tail recursive!

```
void expr() {  
    term(); rest();  
}  
  
void rest() {  
    if ( lookahead == '+' ) {  
        match('+'); term(); print('+'); rest();  
    }  
    else if ( lookahead == '-' ) {  
        match(' '); term(); print(' '); rest();  
    }  
    else { } /* do nothing with the input */ ;  
}  
  
void term() {  
    if ( lookahead is a digit ) {  
        t = lookahead; match(lookahead); print(t);  
    }  
    else report("syntax error");  
}
```

Figure 2.25: Pseudocode for nonterminals *expr*, *rest*, and *term*.

# A Translator for Simple Expressions

```
void rest() {  
    while( true ) {  
        if( lookahead == '+' ) {  
            match('+'); term(); print('+'); continue;  
        }  
        else if ( lookahead == '-' ) {  
            match(''); term(); print('-'); continue;  
        }  
        break ;  
    }  
}
```

# A Translator for Simple Expressions

- **The complete program**

- The complete parser program which is written in Java
- Infix to postfix
- Very useful. In chapter 2.5.5

# Lexical Analysis

- The purpose of lexical analysis is to convert: a sequence of characters (the source) → a sequence of tokens
- How? Input characters are becoming “token objects” by the grouping
- In this section, a token is (a terminal + additional information)
- The lexical analyzer in this section allows numbers, identifiers, and “white space” (blanks, tabs, and newlines) to appear within expressions

# Lexical Analysis

- Now we extend the original little bit by incorporating \* and /

|               |   |                             |                               |
|---------------|---|-----------------------------|-------------------------------|
| <i>expr</i>   | → | <i>expr</i> + <i>term</i>   | { print('+' ) }               |
|               |   | <i>expr</i> - <i>term</i>   | { print('-' ) }               |
|               |   | <i>term</i>                 |                               |
| <i>term</i>   | → | <i>term</i> * <i>factor</i> | { print('*' ) }               |
|               |   | <i>term</i> / <i>factor</i> | { print('/' ) }               |
|               |   | <i>factor</i>               |                               |
| <i>factor</i> | → | ( <i>expr</i> )             |                               |
|               |   | <b>num</b>                  | { print( <b>num.value</b> ) } |
|               |   | <b>id</b>                   | { print( <b>id.lexeme</b> ) } |

Figure 2.28: Actions for translating into postfix notation

# Lexical Analysis

- The lexer operates on the **input** and the resulting token sequence, is the input to the **parser**.
  - Remember the 2 big boxes and several stages?
- The reason we were able to produce the translator in the previous section without a lexer is that, **all the tokens were just one character** (that is why we had just single digits).

# Lexical Analysis

- Removal of White Space and Comments
  - These do not become tokens so that the parser need not worry about them.
  - C-like pseudo code

```
for ( ; ; peek = next input character ) {  
    if ( peek is a blank or a tab ) do nothing;  
    else if ( peek is a newline ) line = line+1;  
    else break;  
}
```

Figure 2.29: Skipping white space



# Lexical Analysis

- Reading Ahead
  - Consider distinguishing  $x < y$  from  $x \leq y$ .
  - After reading the “<” we must read another character.
    - If it is y, we have found our token (<).
    - However, **we must unread the y** so that when asked for the next token, **we will start at y**. If it is never more than one extra character that must be examined, a single char variable would suffice. A more general solution is discussed in the next chapter (Lexical Analysis).
    - A lexical analyzer for C or Java must read ahead after it sees the character >. If the next character is =, then “>” is just “part” of the character sequence “>=”, the lexeme for “>=”
    - A general approach to reading ahead on the input, is to maintain an input buffer from which the lexical analyzer can read characters
    - For Input buffers, since fetching a block of characters is usually more efficient than fetching one character at a time

# Lexical Analysis

- **Constants**

- About the ways in dealing with constants in lexical analysis
- Integer constants can be allowed either by creating a terminal symbol, say num, for such constants or by incorporating the syntax of integer constants into the grammar
- In the book, there is a pseudo code:
  - Figure 2.30: Grouping digits into integers

# Lexical Analysis

- **Recognizing identifiers and keywords**
  - <Ch 2.6.4> TBD