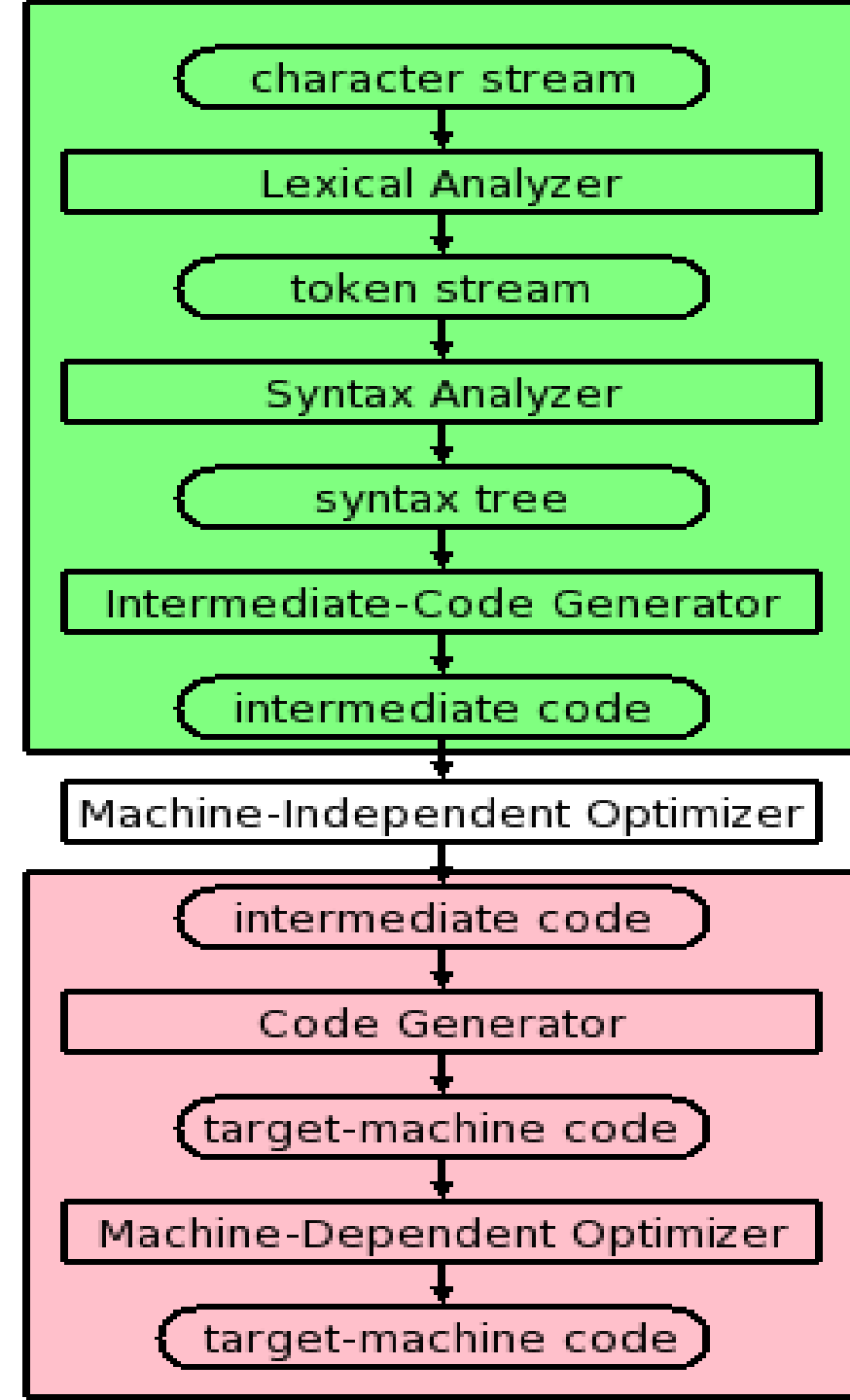


CS 420 - Compilers

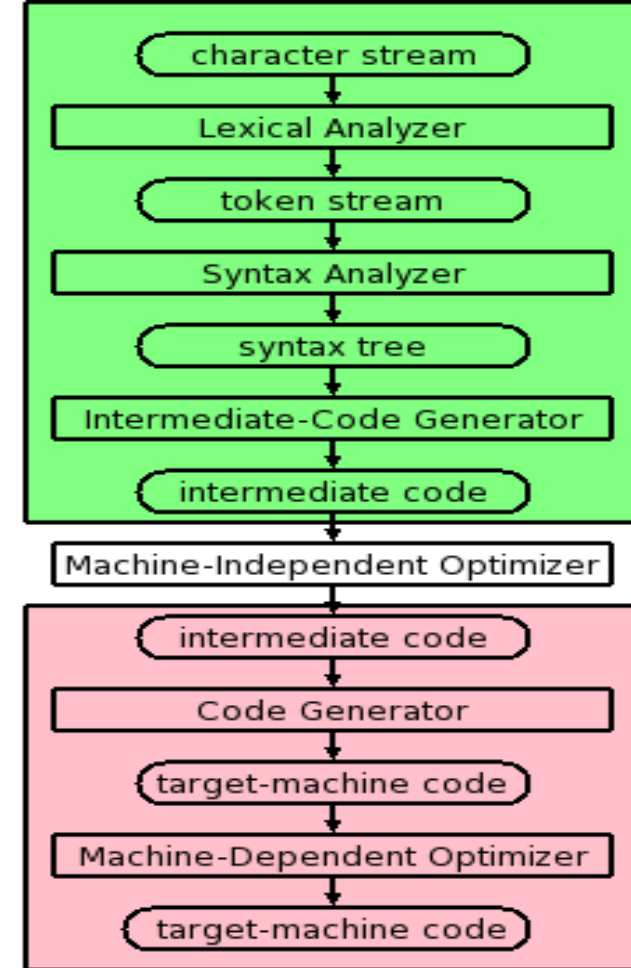
Dr. Chen-Yeou (Charles) Yu

- The goal of this chapter is to know the idea of a very simple compiler.
- Really we are just going as far as the intermediate end. (i.e. front end)
- Nonetheless, the output, i.e. the intermediate code, does look somewhat like assembly language.



- The Structure of a Compiler

- Lexical Analysis (or Scanning)
- Syntax analysis (parsing)
- Semantic Analysis
- Intermediate code generation
- Code optimization
- Code generation
- Symbol-Table Management (not specifically pointed in book)
- Error Handling Routing (not specifically pointed out in book)



- In this chapter, there is:
 - A simple source language.
 - A target close to the source.
 - No optimization.
 - No machine-dependent back end.
 - No tools.
 - Little theory.
- A quick review:
 - What is the job of Lexical Analysis ? Scanning or Tokenizing
 - What is the job of Syntax Analysis ? Parsing
 - This is Ch.2.
 - Ch.3 is the Lexical Analysis and Ch.4 is the Syntax Analysis
 - We are pretty much on the warm-up stage for Ch.4 in this chapter

Introduction

- The *syntax* describes the *form* of a program in a given language.
- The *semantics* describes the *meaning* of that program.

(They are different!)

- We will learn the standard *representation* for the *syntax*
 - *Context-free grammars* also called BNF (Backus-Naur Form).

Syntax Definition

- **Definition of Grammars**

- A *context-free grammar* (CFG) consists of
 - A set of *terminals*
 - A set of *non-terminals*.
 - A set of *productions* (**rules** for **transforming** non-terminals). This is written as LHS \rightarrow RHS, where LHS is a single non-terminal
 - The RHS is a **string** containing **non-terminals** and/or **terminals**.
 - A specific nonterminal designated as **start symbol**

Syntax Definition

- **Definition of Grammars (Cont.)**

Example:

Terminals: 0 1 2 3 4 5 6 7 8 9 + -

Nonterminals: list digit

Productions:

list \rightarrow list + digit

list \rightarrow list - digit

list \rightarrow digit

digit \rightarrow 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

Start symbol: list

$A \rightarrow B \mid C$

is simply shorthand for

$A \rightarrow B$

$A \rightarrow C$

Syntax Definition

- If no start symbol is specifically designated, the **LHS** of the first production is the start symbol.
- **Derivations**
 - This is the **process** of applying **productions**, starting with the start symbol and ending when only terminals are present is **called** a ***derivation***
 - The final string has been *derived* from the initial string (in this case the start symbol).
 - See how we generate $7+4-5$
 - It begins with the start symbol, applying productions, and **stopping** when **no productions** can be applied (because only **terminals remain**).
 - See the example in the next page

Syntax Definition

```
list → list - digit
      → list - 5
      → list + digit - 5
      → list + 4 - 5
      → digit + 4 - 5
      → 7 + 4 - 5
```

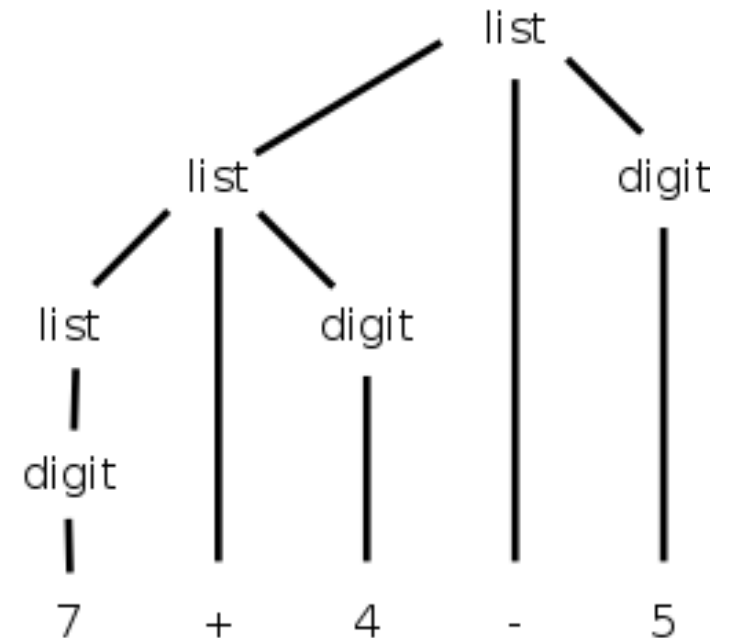
- The set of all strings derivable from the **start** symbol is the *language generated by the CFG* (Yes! This is my name!)
- The way you get different final expressions is that you make **different choices** of which production to apply. There are **3 productions you can apply to list** and **10 ways you can apply to digit**. (The derivation you had seen is ONLY one of the them!)
- The result cannot have blanks since blank is not a terminal.
- The empty string is not possible since, starting from list, we cannot get to the empty string. If we wanted to include the empty string, we would add the production, $\text{list} \rightarrow \epsilon$
- **Q&A: If there is a number, say 25, allowed as an operand in the process of derivation?**

Syntax Definition

- Given a grammar, *parsing* a string (of terminals) consists of determining if the string is in the language generated by the **grammar**.
 - If it is in the language, parsing produces a derivation.
 - If it is not, parsing reports an error.

- **Parse Trees**

- Our previous example, 7+4-5
- Parse Tree is constructed
- The leaves of the tree, read from left to right, is called the *yield* of the tree.
- We say that this string is *derived*, from the (nonterminal at the) root, or is *generated* by the root



Syntax Definition

- **Ambiguity**

- An *ambiguous* grammar may be used to **construct 2 or more parse trees**
- And these can **yield to the SAME final string**
- Avoid such grammars when designing a new programming language

Syntax Definition

- **Ambiguity (Cont.)** --- An example of erroneously prove of ambiguity

- Consider the grammar

$S \rightarrow A B$

$A \rightarrow x$

$B \rightarrow x$

- And if you say the grammar is ambiguous because we can derive the string: xx in **two** ways. It is WRONG! They have the **same** parse tree!

$S \rightarrow A B \rightarrow A x \rightarrow x x$

$S \rightarrow A B \rightarrow x B \rightarrow x x$

Syntax Definition

$$\begin{aligned} & \rightarrow l - l \\ & \rightarrow l - 8 \\ & \rightarrow l - l - 8 \\ & \rightarrow l - 8 - 8 \\ & \rightarrow l - 8 - 8 \\ & \rightarrow 8 - 8 - 8 \end{aligned}$$

- **Associativity of operators**

- Our grammar gives **left associativity**
- If you traverse the parse tree in post-order and perform the indicated arithmetic you will evaluate the string **left to right**.
- 8-8-8, this can be **correctly** derived using our grammar and is evaluated to -8
- What if, we **replace the first 2 productions**? New Grammar!

`list → digit + list`
`list → digit - list`

Terminals: 0 1 2 3 4 5 6 7 8 9 + -

Nonterminals: list digit

Productions:

→ `list → list + digit`

→ `list → list - digit`

`list → digit`

`digit → 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9`

Start symbol: list

- It will be **right** associative!

Syntax Definition

- **Precedence of operators**

- We normally want * to have higher precedence than +.
- We do this by introducing an **additional nonterminal** to indicate the items that have been multiplied. (in this grammar, it is “term”!)
- The example below gives the four basic arithmetic operations their normal precedence unless overridden by parentheses.

```
expr    → expr + term | expr - term | term
term     → term * factor | term / factor | factor
factor  → digit | ( expr )
digit   → 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

Syntax Definition

- In the quiz,
 - I might like to ask you to generate a parsing tree according to some grammar.
 - Or, I give you a string (i.e. $a-b+c$) and a grammar. Then, I ask you if this is possible?

Syntax-Directed Translation

- Postfix Notation

- This notation is called **postfix** because the rule is **operator after operand(s)**.
- The notation we normally use is called **infix** because the rule is **operator in between operands**
- For example, $E \text{ op } F$ becomes **$E' F' \text{ op}$** , where E' and F' are the postfix of E and F respectively.
- Our question is, given, say $1+2-3$, what are E , F and op ? Does $E=1+2$, $F=3$, and $\text{op}=-$? Or does $E=1$, $F=2-3$ and $\text{op}=+$? This is the issue of **precedence** and associativity mentioned above.
- To simplify the present discussion we will start with **fully parenthesized infix expressions**.

Syntax-Directed Translation

- Example1
 - $1+2/3-4*5$
 - Parenthesize (using standard precedence) to get $(1+(2/3))-(4*5)$
 - Apply the rule mentioned earlier (still remember “E’ F’ op” ?) to calculate $P\{(1+(2/3))-(4*5)\}$, where $P\{X\}$ means “the function” to convert the infix expression X to postfix
 - Step A~ F
 - A. $P\{(1+(2/3))-(4*5)\}$
 - B. $P\{(1+(2/3))\} P\{(4*5)\} -$
 - C. $P\{1+(2/3)\} P\{4*5\} -$
 - D. $P\{1\} P\{2/3\} + P\{4\} P\{5\} * -$
 - E. $1 P\{2\} P\{3\} / + 4 5 * -$
 - F. $1 2 3 / + 4 5 * -$

Syntax-Directed Translation

- Example2
 - $(1+2)/3-4*5$
 - Parenthesize to get $((1+2)/3)-(4*5)$
 - Calculate $P\{((1+2)/3)-(4*5)\}$
 - Step A~ F
 - A. $P\{((1+2)/3) P\{(4*5)\} -$
 - B. $P\{(1+2)/3\} P\{4*5\} -$
 - C. $P\{(1+2)\} P\{3\} / P\{4\} P\{5\} *$
 - D. $P\{1+2\} 3 / 4 5 * -$
 - E. $P\{1\} P\{2\} + 3 / 4 5 * -$
 - F. $1 2 + 3 / 4 5 * -$

Syntax-Directed Translation

- The example1 and example2 is a way to construct the tree in the bottom-up style!
- Bottom: infix
- Up: postfix
- This is the “translation”

Syntax-Directed Translation

- Synthesized Attributes

- We want to decorate the parse trees we construct with **annotations** that give the **value** of certain **attributes** of the corresponding **node** of the tree.
- For convenience, the grammar is repeated just below.
- This grammar supports parentheses, although our example $1+2/3-4*5$ does not use them

```
expr   → expr + term | expr - term | term
term   → term * factor | term / factor | factor
factor → digit | ( expr )
digit  → 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

Syntax-Directed Translation

- An attribute is said to be synthesized if its value at a parse-tree node N is determined from attribute values at the children of N and N itself.
- Synthesized attributes have the desirable property that they can be evaluated during a single bottom-up traversal of a parse tree.

Syntax-Directed Translation

- Here is a “movie” which a parse tree is built from the example:

- $1+2/3-4*5$

```
expr    → expr + term | expr - term | term
term     → term * factor | term / factor | factor
factor  → digit | ( expr )
digit   → 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```

Syntax-Directed Translation

- Step1:

digit
|
1 + 2 / 3 - 4 * 5

- Step2:

factor
|
digit
|
1 + 2 / 3 - 4 * 5

- Step3:

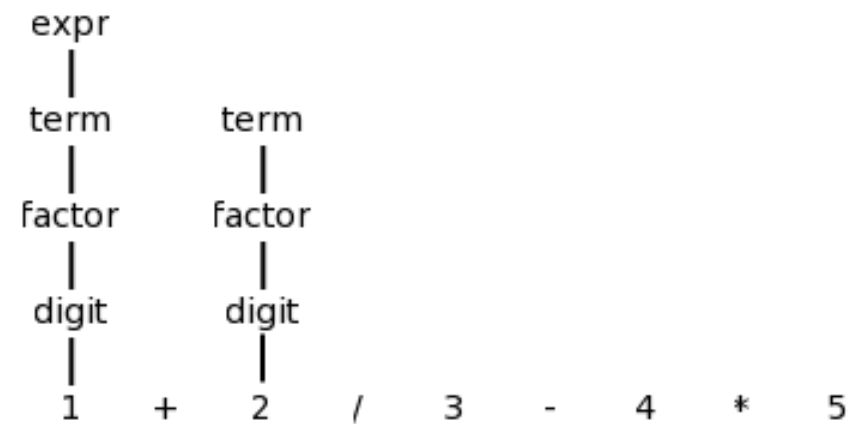
term
|
factor
|
digit
|
1 + 2 / 3 - 4 * 5

Syntax-Directed Translation

- Step4:

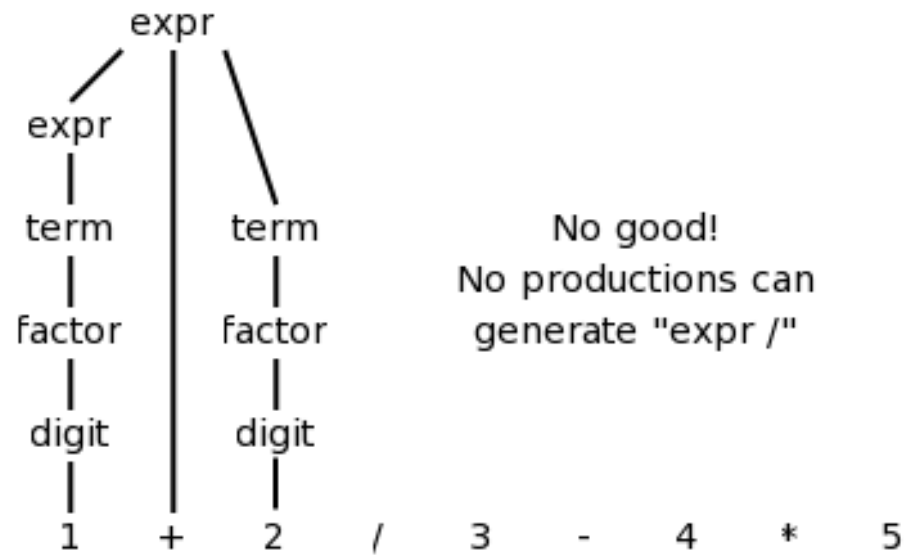


- Step5:



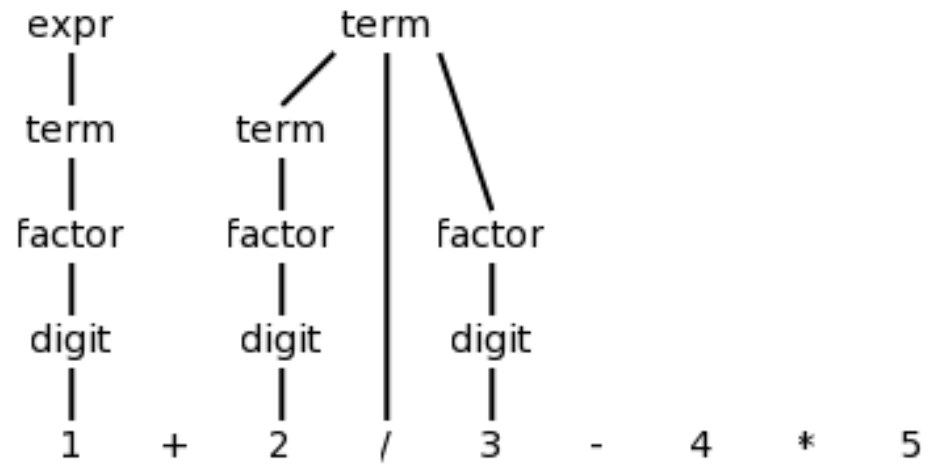
Syntax-Directed Translation

- Step6:



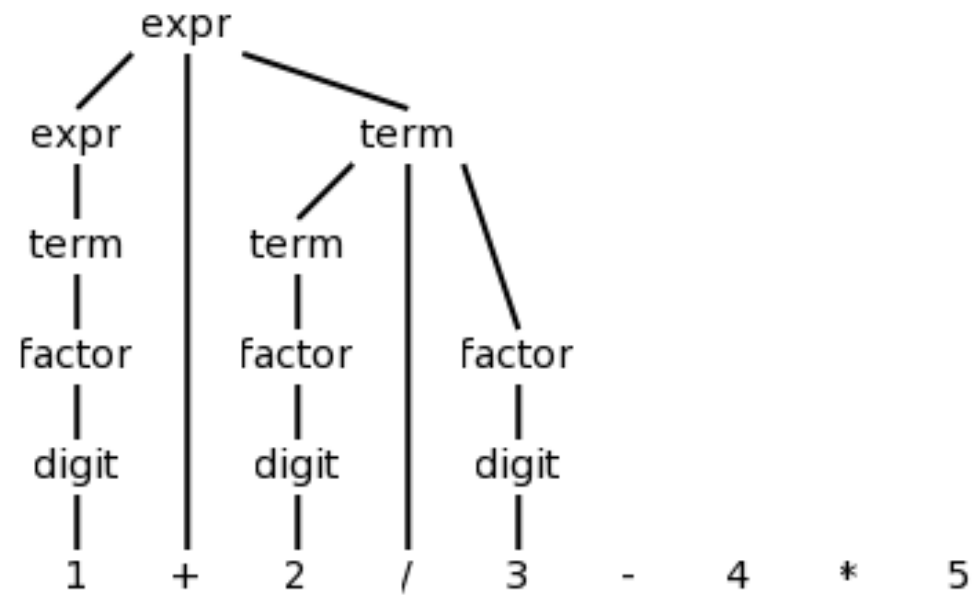
Syntax-Directed Translation

- Step7:



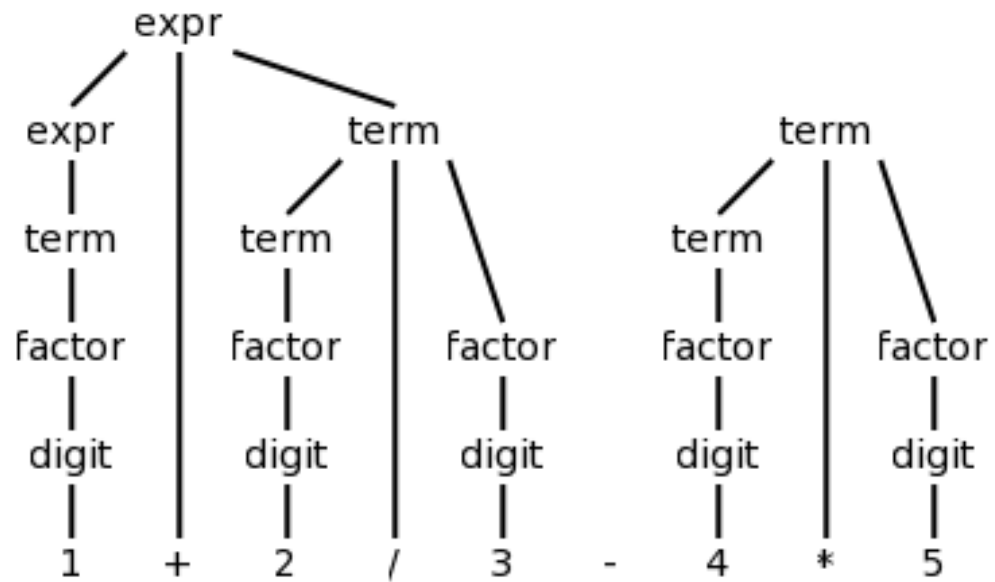
Syntax-Directed Translation

- Step8:



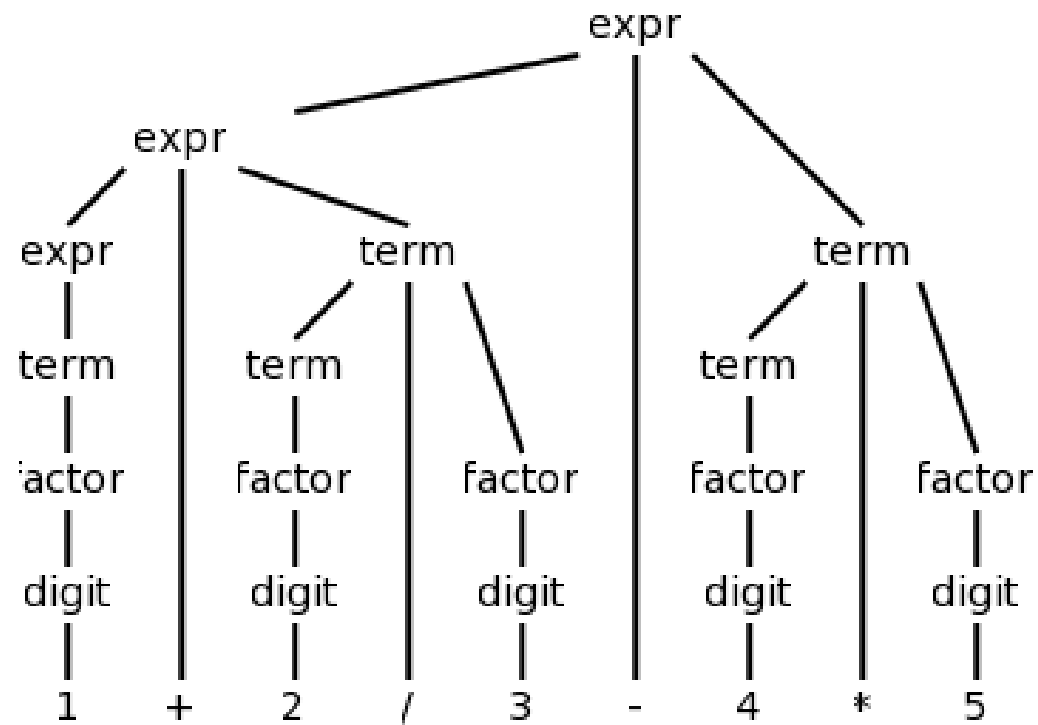
Syntax-Directed Translation

- Step9:



Syntax-Directed Translation

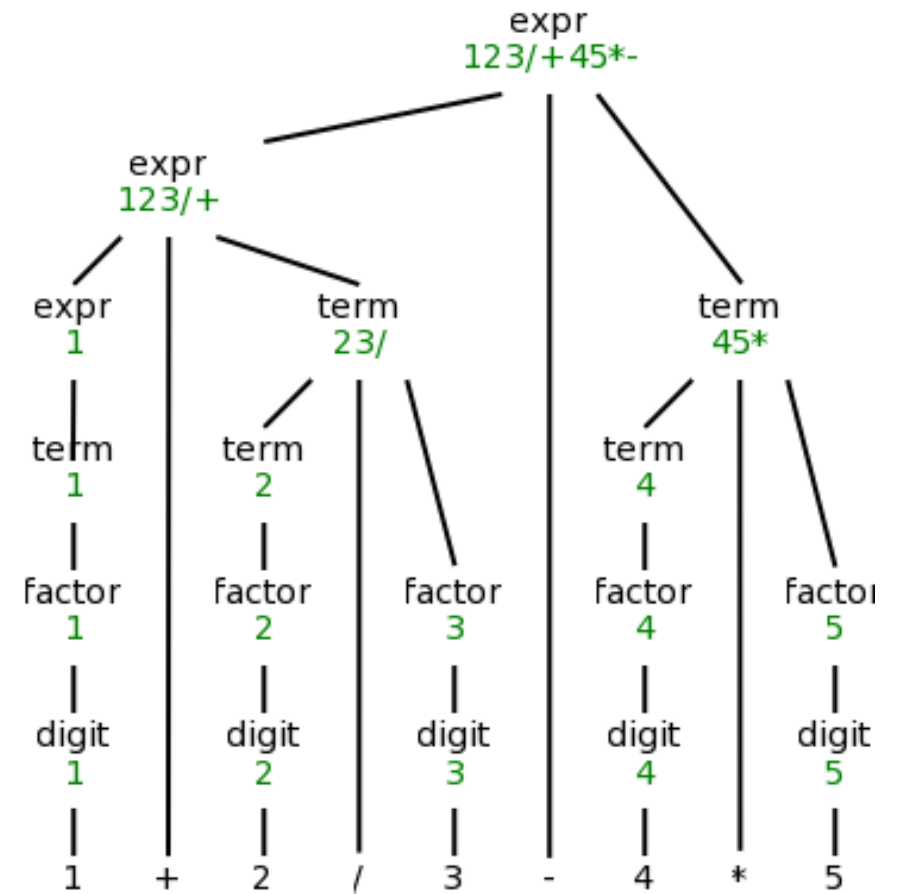
- Step10:



Syntax-Directed Translation

- Step11: (The last step, having all the internal nodes to associate the attributes)

```
expr  → expr + term | expr - term | term
term  → term * factor | term / factor | factor
factor → digit | ( expr )
digit  → 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
```



Syntax-Directed Translation

- Syntax-Directed Definitions (SDDs)
 - The attribute values at a node can depend on the values of attributes at the children of the node but not on attributes at the parent of the node.
 - We call such bottom-up attributes synthesized, since they are formed by synthesizing the attributes of the children.

Syntax-Directed Translation

- Simple Syntax-Directed Definitions
 - Book Chapter 2.3.3
 - TBD