

CS 420 - Compilers

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- Chapter 1 touches on all the material.
- Chapter 2 constructs (the front end of) a simple compiler.
- Chapters 3-8 fill in the (considerable) gaps, as well as the presenting the beginnings of the compiler back end

Syntax-Directed Translation

- Syntax-Directed Definitions (SDDs)
 - In our previous example, we give the **syntax directed definition** as follows:
 - '||' means concatenate

Production	Semantic Rule
$\text{expr} \rightarrow \text{expr}_1 + \text{term}$	$\text{expr.t} := \text{expr}_1.\text{t} \text{term.t} '+'$
$\text{expr} \rightarrow \text{expr}_1 - \text{term}$	$\text{expr.t} := \text{expr}_1.\text{t} \text{term.t} '-'$
$\text{expr} \rightarrow \text{term}$	$\text{expr.t} := \text{term.t}$
$\text{term} \rightarrow \text{term}_1 * \text{factor}$	$\text{term.t} := \text{term}_1.\text{t} \text{factor.t} '*'$
$\text{term} \rightarrow \text{term}_1 / \text{factor}$	$\text{term.t} := \text{term}_1.\text{t} \text{factor.t} '/'$
$\text{term} \rightarrow \text{factor}$	$\text{term.t} := \text{factor.t}$
$\text{factor} \rightarrow \text{digit}$	$\text{factor.t} := \text{digit.t}$
$\text{factor} \rightarrow (\text{expr})$	$\text{factor.t} := \text{expr.t}$
$\text{digit} \rightarrow 0$	$\text{digit.t} := '0'$
$\text{digit} \rightarrow 1$	$\text{digit.t} := '1'$
$\text{digit} \rightarrow 2$	$\text{digit.t} := '2'$
$\text{digit} \rightarrow 3$	$\text{digit.t} := '3'$
$\text{digit} \rightarrow 4$	$\text{digit.t} := '4'$
$\text{digit} \rightarrow 5$	$\text{digit.t} := '5'$
$\text{digit} \rightarrow 6$	$\text{digit.t} := '6'$
$\text{digit} \rightarrow 7$	$\text{digit.t} := '7'$
$\text{digit} \rightarrow 8$	$\text{digit.t} := '8'$
$\text{digit} \rightarrow 9$	$\text{digit.t} := '9'$

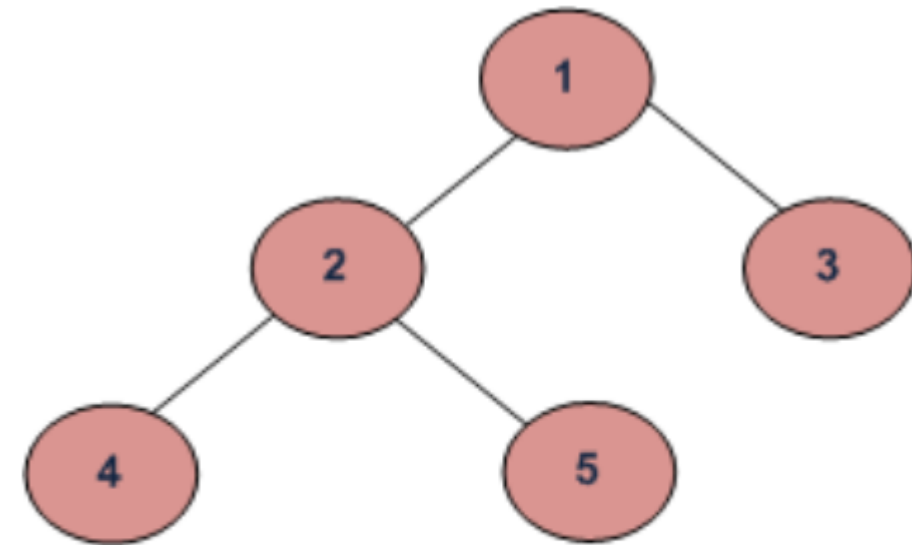
SDD for Infix to Postfix Translator

Syntax-Directed Translation

- Simple Syntax-Directed Definitions
 - Simple? Why it is called simple?
 - In the production (LHS) or in the semantic rule(RHS), if the left hand side (LHS) of the production is just the concatenation of the annotations for the non-terminals on the RHS **in the same order as the non-terminals appear in the production**, we call it simple
 - See the table of 1st one row
 - `expr`, `expr1` and `term`, no matter it is in LHS RHS. If they are showing up in the same order (no need to care about the '+' \leftarrow terminal), it is called simple.

Syntax-Directed Translation

- **(depth-first) Tree Traversals (left to right)**
 - The internal nodes (non-terminals, non-leaf) can be visited in on of the following approach
 - Before visiting any of its children.
 - Pre-order, roots gets highest priority
 - Between visiting its children.
 - Left kid \rightarrow root \rightarrow right kid
 - After visiting all of its children.
 - Post-order, roots gets lowest priority



Depth First Traversals:

(a) Inorder (Left, Root, Right) : 4 2 5 1 3

(b) Preorder (Root, Left, Right) : 1 2 4 5 3

(c) Postorder (Left, Right, Root) : 4 5 2 3 1

Breadth-First or Level Order Traversal: 1 2 3 4 5

Syntax-Directed Translation

- **(depth-first) Tree Traversals (left to right) (Cont.)**
 - I don't like the pseudocode in book in the chapter 2.3.4
 - Very ambiguous, just 3 lines of code which confuses us a lot
 - I like this one more!

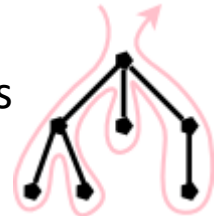
```
traverse (n : treeNode)
  if leaf(n)                                -- visit leaves once; base of recursion
    visit(n)
  else                                       -- interior node, at least 1 child
    -- visit(n)                             -- visit node PRE visiting any children
    traverse(first child)                   -- recursive call
    while (more children remain)           -- excluding first child
      -- visit(n)                           -- visit node IN-between visiting children
      traverse (next child)                 -- recursive call
    -- visit(n)                             -- visit node POST visiting all children
```

Syntax-Directed Translation

- **(depth-first) Tree Traversals (left to right) (Cont.)**

- Note the following properties

- Comments are introduced by -- and terminate at the end of the line
- If you uncomment just the **first** (interior node) visit, you get a **preorder traversal**, in which each node is visited before (i.e., pre) visiting any of its children.
- If you uncomment only the **middle** visit, you get an **inorder traversal**, in which the node is visited (in-) between visiting its children.
- If you uncomment just the **last** visit, you get a **postorder traversal**, in which each node is visited after (i.e., post) visiting all of its children.
- Inorder traversals are normally good for binary trees (exactly two children)
- If you uncomment all of the three visits, you get an *Euler-tour traversal*.
 - An *Eulerian tour* on a directed graph is one that traverses each **edge** once.
 - If we view the tree on the right as undirected and replace each edge with two arcs each direction, we see that the pink curve is indeed an Eulerian tour.



Syntax-Directed Translation

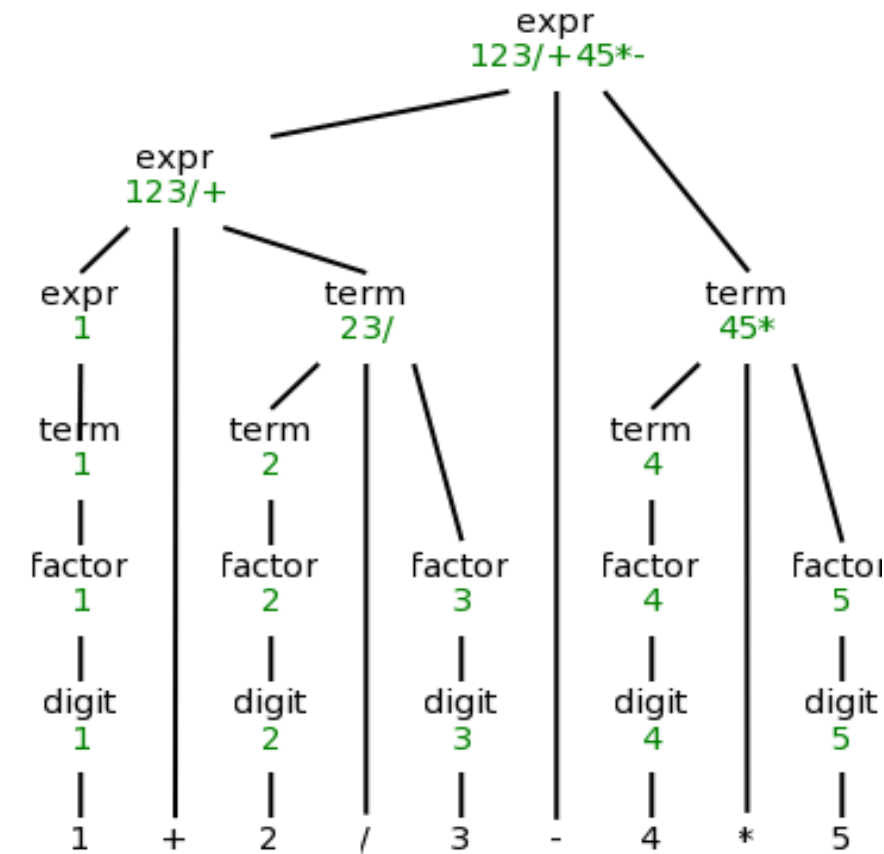
- **(depth-first) Tree Traversals (left to right) (Cont.)**

- At this point in the course, we are considering only synthesized attributes, a postorder traversal will always yield a correct evaluation order for the attributes.
- This is so since synthesized attributes depend only on attributes of child nodes and a postorder traversal visits a node only after all the children have been visited (and hence all the child node attributes have been evaluated).

Syntax-Directed Translation

- **Translation schemes**

- The bottom-up annotation scheme just described generates the final result as the annotation of the root. (remember this?)
- In our infix to postfix example, we get the result desired by printing the root annotation.
- There is another technique, that produces its results incrementally.
- There is a thing called “**semantic actions**”
- When it is drawn in diagrams (e.g., see the diagram below), the semantic action is connected to its node, with a distinctive, often dotted, line.



Syntax-Directed Translation

- **Translation schemes (Cont.)**

- **Definition:** A *syntax-directed translation scheme* is a context-free grammar with *embedded semantic actions*.
- An example, in the infix to postfix translation translator, the parent either
 - takes the attribute of its only child, or
 - concatenates the attributes, left to right of its several children, and adds something at the end.
- In practice, it is redundant to give both semantic actions and semantic rules. In this course we will emphasize semantic rules, i.e. syntax directed definitions (SDDs).
- I show both the rules and the actions in a table just so that we can see the correspondence.

Syntax-Directed Translation

- **Translation schemes (Cont.)**

- **Goal:** infix to postfix translation
- The diagram for input string $1+2/3-4*5$ with attached semantic **actions** is shown on the below.

Production with Semantic Action		Semantic Rule
$\text{expr} \rightarrow \text{expr1} + \text{term}$	{ print('+') }	$\text{expr.t} := \text{expr1.t} \parallel \text{term.t} \parallel '+'$
$\text{expr} \rightarrow \text{expr1} - \text{term}$	{ print('-') }	$\text{expr.t} := \text{expr1.t} \parallel \text{term.t} \parallel '-'$
$\text{term} \rightarrow \text{term1} / \text{factor}$	{ print('/') }	$\text{term.t} := \text{term1.t} \parallel \text{factor.t} \parallel '/'$
$\text{term} \rightarrow \text{factor}$	{ null }	$\text{term.t} := \text{factor.t}$
$\text{digit} \rightarrow 3$	{ print('3') }	$\text{digit.t} := '3'$

Semantic Actions and Rules for an Infix to Postfix Translator

- We just do a (left-to-right) depth first traversal of the corresponding diagram and perform the **semantic actions** as they occur.
- When these actions are print statements as above, we are said to be **emitting the translation**.

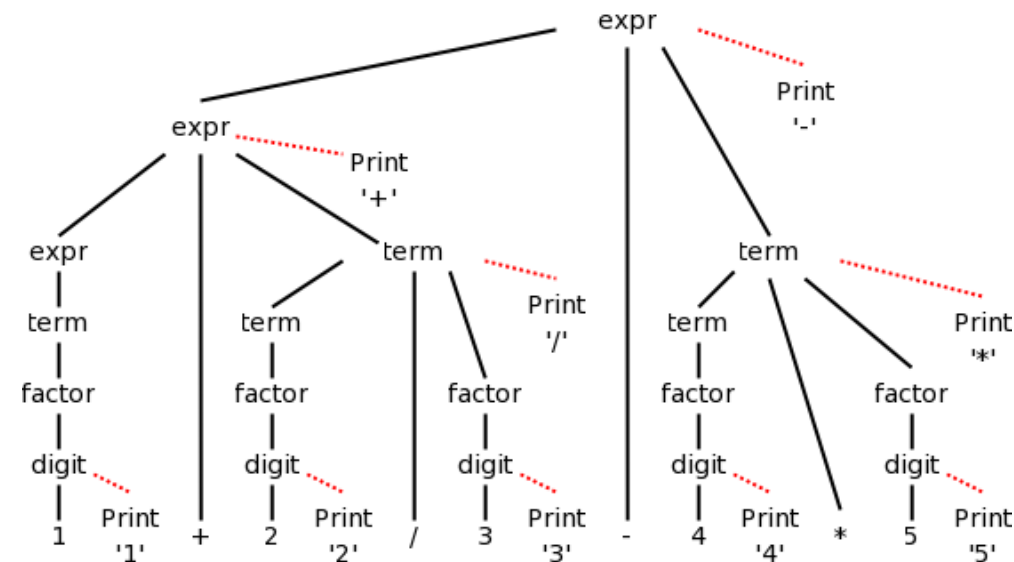
Syntax-Directed Translation

- **Translation schemes (Cont.)**

- Since the actions are all leaves of the tree, they occur in the same order for any depth-first (left-to-right) traversal
- Do on the board a depth first traversal of the diagram, performing the semantic actions as they occur, and confirm that the translation emitted is in fact **123/+45*-**, the postfix version of $1+2/3-4*5$

- **The way to traverse: left to right, all leaves!**

(produced by red-dotted line)



Syntax-Directed Translation

- **Translation schemes (Cont.)**

- **Goal:** prefix to infix translation
- In our previous example, we haven't talk about '(' and ')'
 - Precedence
 - In this example, we want to demonstrate this capability
 - Think about this grammar, which generates the simple language of prefix expressions consisting of addition and subtraction of digits between 1 and 3 without parentheses
 - $P \rightarrow + P P \mid - P P \mid 1 \mid 2 \mid 3$
 - Input string: +1-32
 - $P \rightarrow +PP \rightarrow +P-PP \rightarrow +P-32 \rightarrow +1-32$
 - We can do something in the translation table to add the function to support '(' and ')'

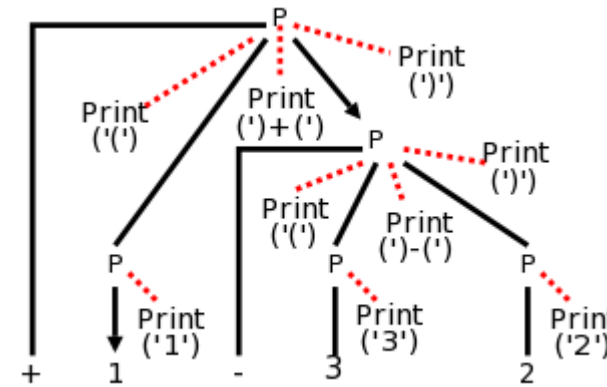
Syntax-Directed Translation

- **Translation schemes (Cont.)**
 - Here is the table (we are now working on the “action”)
 - And here is the tree by applying the red-dotted actions

See if you can get the
answer $(1)+((3)-(2))$???

Production with Semantic Action	Semantic Rule
$P \rightarrow + \{ \text{print('(')} \} P_1 \{ \text{print(')+(')} \} P_2 \{ \text{print(')')} \}$	$P.t := '(\parallel P_1.t \parallel ')+(\parallel P.t \parallel ')''$
$P \rightarrow - \{ \text{print('(')} \} P_1 \{ \text{print(')-(')} \} P_2 \{ \text{print(')')} \}$	$P.t := '(\parallel P_1.t \parallel ')-(\parallel P.t \parallel ')''$
$P \rightarrow 1 \{ \text{print('1')} \}$	$P.t := '1'$
$P \rightarrow 2 \{ \text{print('2')} \}$	$P.t := '2'$
$P \rightarrow 3 \{ \text{print('3')} \}$	$P.t := '3'$

Prefix to infix translator



- The way to traverse is the same! Depth-first, left to right, all leaves!

Parsing

- In this section we assume that the lexical analyzer has already scanned the source input and converted it into a sequence of tokens.
- **Objective:** Given a string of tokens and a grammar, produce a parse tree yielding that string (or at least determine if such a tree exists).
- We will learn both top-down (begin with the start symbol, i.e. the **root** of the tree) and bottom up (begin with the **leaves**) technique
- In this chapter we just quickly go through bottom-up quickly.
- And little bit more in doing top-down, which is easier. In Ch.4 we will cover both (in detail).

Parsing

- **Bottom-up parsing**

- Input string: $a + b * c$ (forget about the precedence)
- The goal is try to reduce (not derive) the input string to the root
- Production rules:

```
S → E
E → E + T
E → E * T
E → T
T → id
```

- Read the input and check if any production matches with the input:
 - It can be reduced into S !
 - Try to build up your (bottom-up) parse tree!

a	+	b	*	c
T	+	b	*	c
E	+	b	*	c
E	+	T	*	c
E	*	c		
E	*	T		
E				
S				

Parsing

- Top-down parsing
 - Put the root on top is your first step!
 - Top (root) to down (leaves)
 - Given the following Pascal-like simple language, a high level idea, not the real Pascal (way more complicated)
 - 2 non-terminals
 - type: start symbol
 - simple: means the “simple type”
 - 8 terminals
 - 1. **integer** and **char**
 - 2. **id** for identifier
 - 3. **array** and **of** used in array declarations
 - 4. **↑** meaning pointer to
 - 5. **num** for a (positive whole) number
 - 6. **dotdot** for .. (used to give a range like 6..9)

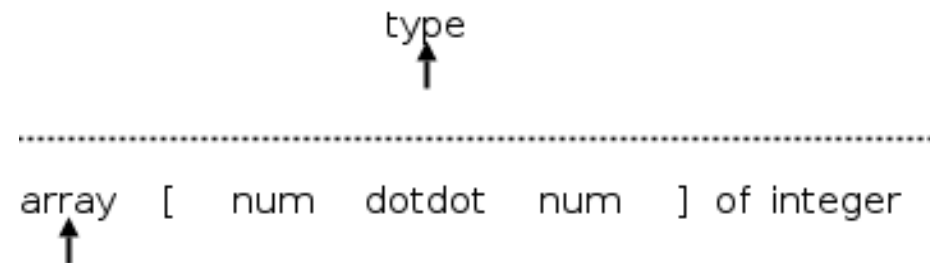
Parsing

- Top-down parsing (Cont.)

The productions are

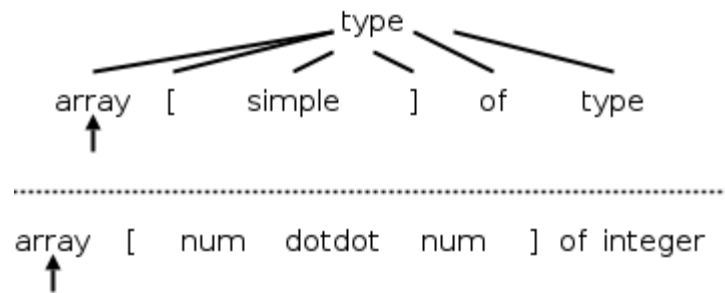
```
type  → simple
type  → ↑ id
type  → array [ simple ] of type
simple → integer
simple → char
simple → num dotdot num
```

- Here is a movie showing you,
the whole process in building the whole tree
(Up: Tree to be built, Down: input string)
- Step1

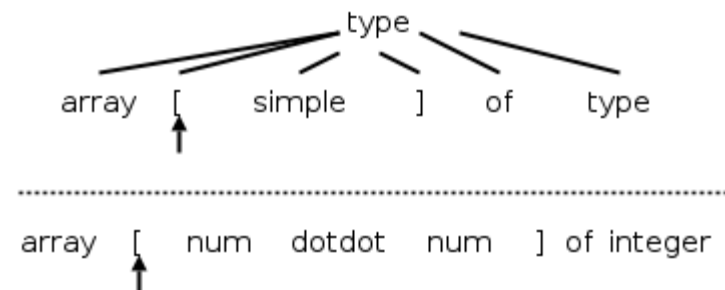


Parsing

- Top-down parsing (Cont.)
 - Step2

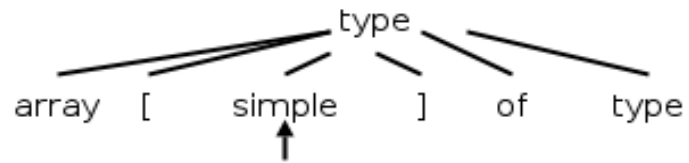


- Step3



Parsing

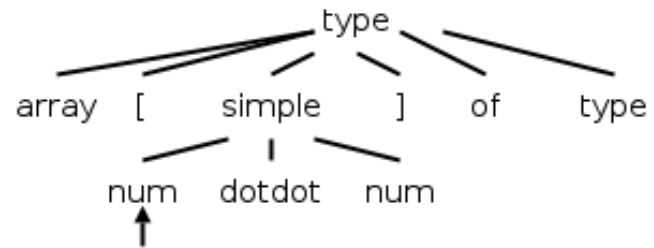
- Top-down parsing (Cont.)
 - Step4



array [num dotdot num] of integer

An upward-pointing arrow is positioned below the 'num' node.

- Step5

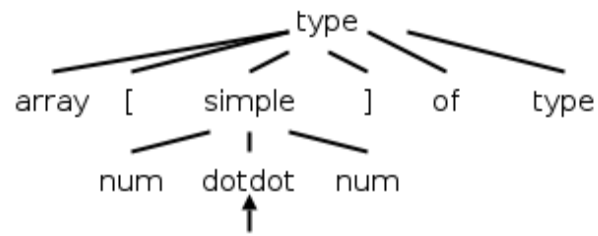


array [num dotdot num] of integer

An upward-pointing arrow is positioned below the first 'num' node.

Parsing

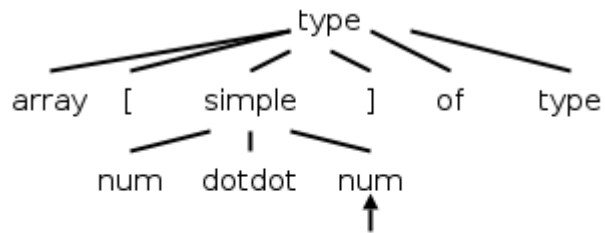
- Top-down parsing (Cont.)
 - Step6



array [num dotdot num] of integer

↑

- Step7

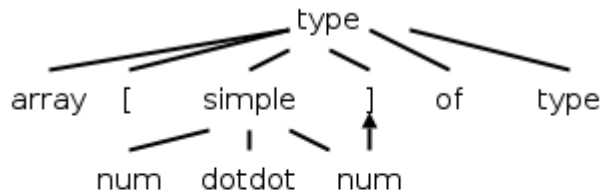


array [num dotdot num] of integer

↑

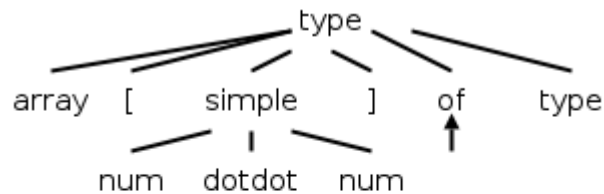
Parsing

- Top-down parsing (Cont.)
 - Step8~10



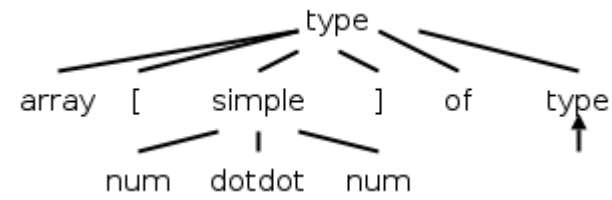
array [num dotdot num] of integer

An upward arrow points to the closing bracket ']' in the input string.



array [num dotdot num] of integer

An upward arrow points to the 'of' in the input string.

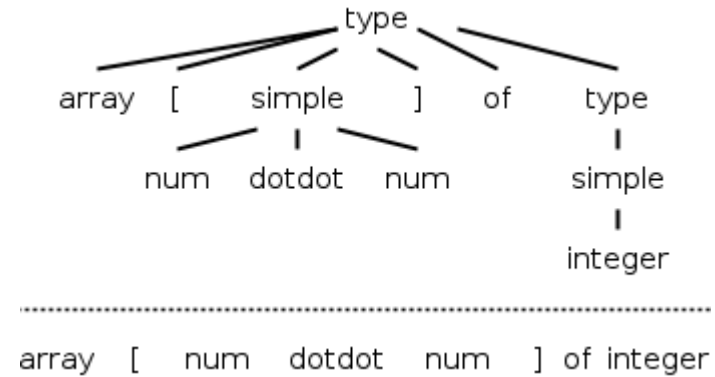
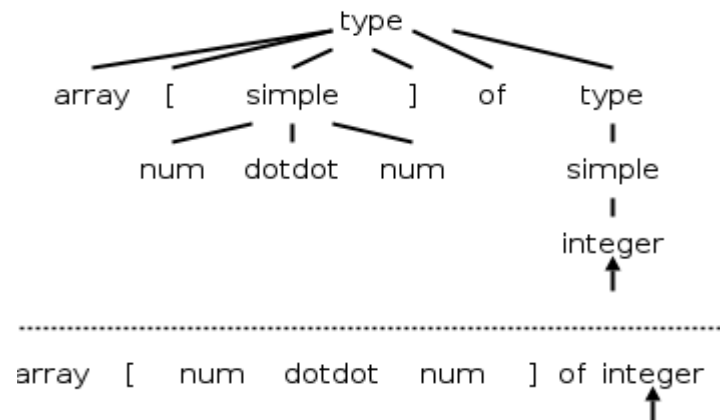
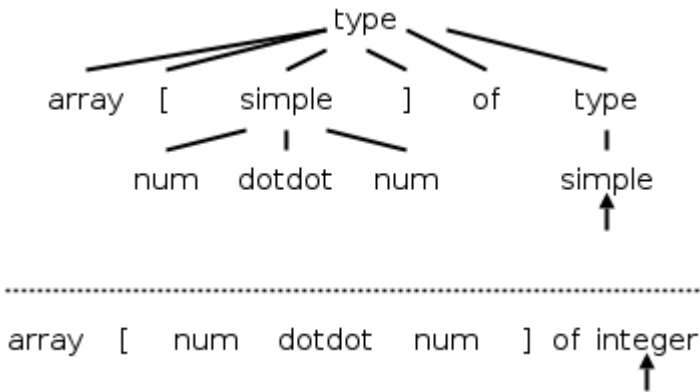


array [num dotdot num] of integer

An upward arrow points to the 'integer' in the input string.

Parsing

- Top-down parsing (Cont.)
 - Step11~13



Parsing

- Predictive Parsing
 - TBD, in Part3