
```

# Quantum Fourier Transform:
QFT | qureg

# Quantum arithmetic:
# Note: quint is a quantum register representing an integer
# Add integer a:
AddConstant(a) | quint
# Add a modulo N:
AddConstantModN(a, N) | quint
# Multiply by a modulo N:
MultiplyByConstantModN(a, N) | quint

# Apply  $\exp(-i*t*hamiltonian)$ 
# Hamiltonians can be specified using QubitOperators:
hamiltonian = QubitOperator("X0 X1") + QubitOperator("Y0 Y1")
TimeEvolution(hamiltonian, t) | qureg

# Turns state  $|0\rangle$  into state  $\sum_j \beta_j |j\rangle$ :
StatePreparation(beta) | qureg

```

Listing 1: Some of ProjectQ's n-qubit gates.















ProjectQ syntax	Name	Definition	Symbol
X qubit	Pauli X	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	
Y qubit	Pauli Y	$\begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}$	
Z qubit	Pauli Z	$\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$	
S qubit	S gate	$\begin{pmatrix} 1 & 0 \\ 0 & i \end{pmatrix}$	
Sdagger qubit	inverse of S	S^\dagger	
T qubit	T gate	$\begin{pmatrix} 1 & 0 \\ 0 & e^{i\pi/4} \end{pmatrix}$	
Tdagger qubit	inverse of T	T^\dagger	
H qubit	Hadamard	$\frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix}$	
Ph(theta) qubit	(global) Phase gate	$\begin{pmatrix} e^{i\theta} & 0 \\ 0 & e^{i\theta} \end{pmatrix}$	
R(theta) qubit	Phase-shift gate	$\begin{pmatrix} 1 & 0 \\ 0 & e^{i\theta} \end{pmatrix}$	
Rx(theta) qubit	Rotation around x	$e^{-i\theta X/2} = \begin{pmatrix} \cos(\frac{\theta}{2}) & -i \sin(\frac{\theta}{2}) \\ -i \sin(\frac{\theta}{2}) & \cos(\frac{\theta}{2}) \end{pmatrix}$	
Ry(theta) qubit	Rotation around y	$e^{-i\theta Y/2} = \begin{pmatrix} \cos(\frac{\theta}{2}) & -\sin(\frac{\theta}{2}) \\ \sin(\frac{\theta}{2}) & \cos(\frac{\theta}{2}) \end{pmatrix}$	
Rz(theta) qubit	Rotation around z	$e^{-i\theta Z/2} = \begin{pmatrix} e^{-i\theta/2} & 0 \\ 0 & e^{i\theta/2} \end{pmatrix}$	
Measure qubit	Measurement in computational basis $ 0\rangle, 1\rangle$		

Table 1: Some of the standard single qubit gates available in ProjectQ.


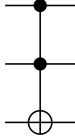

ProjectQ syntax	Definition	Symbol
CNOT (ctrl_qubit, qubit)	$\underbrace{ 1\rangle\langle 1 }_{\text{ctrl_qubit}} \otimes \underbrace{X}_{\text{qubit}} + 0\rangle\langle 0 \otimes I$	
Toffoli (ctrl_ureg, qubit)	$\underbrace{ 11\rangle\langle 11 }_{\text{ctrl_qureg}} \otimes \underbrace{X}_{\text{qubit}} + (I - 11\rangle\langle 11) \otimes I$	
Swap (qubit0, qubit1)	$\begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$	

Table 2: Some of the standard two and three qubit gates available in ProjectQ.

Meta-instructions

```
eng = projectq.MainEngine()
...
with Loop(eng, 10):
    U | qubits
```

```
get_inverse(T) | qubit # Equivalent to Tdagger | qubit
```

```
eng = projectq.MainEngine()
...
with Dagger(eng):
    # Anything executed in this context will be inverted
    T | qubit
    S | qubit
```

```
C(X, 2) | (ctrl_qureg, qubit) # ctrl_qureg contains two qubits
```

```
with Control(eng, ctrl_quireg):  
    # Anything executed in this context will be controlled  
    # on all qubits in ctrl_quireg being in state 1  
    T | qubit  
    S | qubit
```

```
eng = projectq.MainEngine()  
...  
with Compute(eng):  
    U | qureg  
V | qureg  
Uncompute(eng)
```

```
eng = projectq.MainEngine()  
...  
with Compute(eng):  
    U | qureg  
V | qureg  
with CustomUncompute(eng):  
    Udagger | qureg
```