— MACROS —

```
// Macros
#define forn(i,e) for(ll i = 0; i < e; i++)
#define forsn(i,s,e) for(ll i = s; i < e; i++)
#define rforn(i,s) for(ll i = s; i >= 0; i--)
#define ln "\\n"
#define mp make_pair
#define pb push_back
#define fi first
#define se second
#define all(x) (x).begin(), (x).end()
#define sz(x) ((ll)(x).size())
#define INF 2e9

// Typedefs
typedef long long ll;
typedef long double ld;
typedef pair<int,int> pii;
typedef pair<ll,ll> pll;
typedef vector<ll> vll;
typedef vector<int> vi;
typedef vector<bool> vb;
typedef vector<vector<int>> vv;
typedef vector<pll> vpll;
```

— MAIN FUNCTION —

```
int main() {
    ios_base::sync_with_stdio(false);
    cin.tie(NULL);
    cout.tie(NULL);

    ll t;
    cin >> t;
    for (ll i = 0; i < t; i++) {
        solve();
    }
    return 0;
}
```

— DYNAMIC PROGRAMMING —

Coin Change Min Coins

```
//Retorna INF caso seja impossivel
ll min_coins(ll change, vll &coins){
        vll dp(change + 1, INF);
        dp[0] = 0;

        forsn(sub, 1, change + 1){
                for(auto coin: coins){
                        if(coin <= sub){
                                dp[sub] = min(dp[sub], dp[sub-coin] + 1);
                        }
                }
        }
        return dp[change];
}

void solve(){
        vll coins = {5, 4, 1};
        ll change = 13;

        cout << min_coins(change, coins) << endl;
}
```

Coin Change Number of Combinations

```
void solve(){
        int n, change;
        cin >> n >> change;
        vi coins(n);
        for(int &i: coins){
                cin >> i;
        }

        vi dp(change+1, 0);
        dp[0] = 1;
        forsn(sub, 1, change+1){
                for(int coin = 0; coin < n; coin++){
                        if(coins[coin] <= sub){
                                (dp[sub] += dp[sub-coins[coin]]) %= 1000000007;
                        }
                }
        }

        cout << dp[change] << endl;
}
```

Coin Change Number of Combinations (Ordered)

```
ll combs (ll change, vll coins){
```

```cpp
        vll dp(change+1, 0);
        dp[0] = 1;

        forn(coin, sz(coins)){
                forn(sub, change+1){
                        if(coins[coin] <= sub){
                                dp[sub] += dp[sub - coins[coin]] % 1000000007;
                        }
                }
        }
        return dp[change];
}

void solve(){
        ll n, change;
        cin >> n >> change;
        vll coins(n);
        for(ll &i: coins){
                cin >> i;
        }

        cout << combs(change, coins) % 1000000007 << endl;
}
```

Box Stacking

```cpp
// FIND TALLEST POSSIBLE STACK (LENGTH, WIDTH, HEIGHT)
bool compareLength(vll Box1, vll Box2){
        return Box1[0] < Box2[0];
}

bool canBeStacked(ll wTop, ll lTop, ll wBottom, ll lBottom){
        return wTop < wBottom && lTop < lBottom;
}

ll tallestStack (vvll boxes, ll n){
        sort(all(boxes), compareLength); // sort all boxes by length
        map<vll, ll> heights; // memoize the tallest stack with box n at the base
        for(auto box: boxes){
                heights[box] = box[2];
        }

        for(auto box_i: boxes){
                vll S; // vector of heights of stacks starting at boxes that can be stacked
                    ↪ on top of box_i
                for(auto j: boxes){
                        if(canBeStacked(j[1], j[0], box_i[1], box_i[0]))
                                S.pub(heights[j]);
                }
                if(!S.empty())
                        heights[box_i] = heights[box_i] + (*max_element(all(S)));
        }

        ll maxHeight = 0;
        for(auto i: heights){
                if(i.second > maxHeight)
```

```cpp
                        maxHeight = i.second;
        }
        return maxHeight;
}

void solve(){
        ll n = 6;
        vvll boxes = {{1, 2, 2}, {1, 5, 4}, {2, 3, 2}, {2, 4, 1}, {3, 6, 2}, {4, 5, 3}};
        cout << tallestStack(boxes, n) << endl;
}
```

Knapsack (Top-Down)

```cpp
// Returns the value of maximum profit
int knapSackRec(int W, int wt[], int val[], int index, int** dp)
{
        // base condition
        if (index < 0)
                return 0;
        if (dp[index][W] != -1)
                return dp[index][W];

        if (wt[index] > W) {

                // Store the value of function call
                // stack in table before return
                dp[index][W] = knapSackRec(W, wt, val, index - 1, dp);
                return dp[index][W];
        }
        else {
                // Store value in a table before return
                dp[index][W] = max(val[index]
                                                + knapSackRec(W - wt[index], wt, val,
                                                                         index - 1,
                                                                         ↪ dp)
                                                                         ↪ ,
                                        knapSackRec(W, wt, val, index - 1, dp));

                // Return value of table after storing
                return dp[index][W];
        }
}

int knapSack(int W, int wt[], int val[], int n)
{
        // double pointer to declare the
        // table dynamically
        int** dp;
        dp = new int*[n];

        // loop to create the table dynamically
        for (int i = 0; i < n; i++)
                dp[i] = new int[W + 1];

        // loop to initially filled the
        // table with -1
```

```
        for (int i = 0; i < n; i++)
            for (int j = 0; j < W + 1; j++)
                dp[i][j] = -1;
        return knapSackRec(W, wt, val, n - 1, dp);
}

// Driver Code
int main()
{
        int profit[] = { 60, 100, 120 };
        int weight[] = { 10, 20, 30 };
        int W = 50;
        int n = sizeof(profit) / sizeof(profit[0]);
        cout << knapSack(W, weight, profit, n);
        return 0;
}
```

Knapsack (Bottom-Up)

```
int knapsack(int W, int n, vi &price, vi &weight){ //linear memory
vi aux(W+1, 0);
for (int i = 0; i < n; i++){
        for (int j = W; j > 0; j--){
                if (weight[i] <= j){
                        aux[j] = max(aux[j - weight[i]] + price[i], aux[j]);
                }
        }
}
return aux[W];
}
```

Longest Increasing Subsequence

```
void printLIS(int i, vi &p, vi &arr){ //imprime LIS, sabendo o ultimo indice
        if (p[i] == -1){
                cout<<arr[i];
                return;
        }
        printLIS(p[i], p, arr);
        cout<<' '<<arr[i];
}

pii LIS(int n, vi &p, vi &arr){ //retorna maior LIS e o ultimo indice do maior LIS
        int k= 0, lis_end = 0;
        vi L(n, 0), L_id(n, 0);
        p.assign(n, -1);

        for (int i = 0; i < n; i++){
                int pos = lower_bound(L.begin(), L.begin() + k, arr[i]) - L.begin();
                L[pos] = arr[i];
                L_id[pos] = i;
                p[i] = pos ? L_id[pos-1]:-1;
                if (pos == k){
                        k = pos + 1;
                        lis_end = i;
```

```
                }
        }
        return mp(k, lis_end);
}
```

Monotonic Paths

```
//n e m arestas, NAO vertices
ll Monotonic(int n, int m, ll p){     //Se for n*n, usar mod(Catalan(n)*(n+1), m)
        n++;
        m++;
        vvll T(n, vll(m));
        for (int i = 0; i < n; i++){
        T[i][0] = 1;
        }
        for (int i = 0; i < m; i++){
        T[0][i] = 1;
        }
        for (int i = 1; i < n; i++){
                for (int j = 1; j < n; j++){
                        T[i][j] = mod(mod(T[i-1][j], p) + mod(T[i][j-1], p), p);
                }
        }
        return mod(T[n-1][m-1], p);
}
```

— DATA STRUCTURES —

Order Statistic Tree (Map and Set)

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;

using oset = tree<int, // key type
            null_type, // value type
            less<int>, // compare function
            rb_tree_tag,
            tree_order_statistics_node_update>;
auto s = oset();

// ------------------------------------

#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;

using omap = tree<int, // key type
            int, // value type
            less<int>, // compare function
            rb_tree_tag,
            tree_order_statistics_node_update>;
auto m = omap();
```

Segment Tree

```cpp
#define op(l, r) (l + r);
#define DEFAULTVALUE 0
const ll inf = 1e9;

struct Node {
        Node *l = 0, *r = 0;
        ll lo, hi, mset = inf, madd = 0;
        ll val = DEFAULTVALUE;
        Node(ll lo,ll hi):lo(lo),hi(hi){} // Large interval of -inf
        Node(vector<int>& v, ll lo, ll hi) : lo(lo), hi(hi) {
                if (lo + 1 < hi) {
                        ll mid = lo + (hi - lo)/2;
                        l = new Node(v, lo, mid);
                        r = new Node(v, mid, hi);
                        val = op(l->val, r->val);
                }
                else val = v[lo];
        }
        ll query(ll L, ll R) {
                if (R <= lo || hi <= L) return 0;
                if (L <= lo && hi <= R) return val;
                push();
                return op(l->query(L, R), r->query(L, R));
        }
        void set(ll L, ll R, ll x) {
                if (R <= lo || hi <= L) return;
                if (L <= lo && hi <= R) mset = val = x, madd = 0;
                else {
                        push(), l->set(L, R, x), r->set(L, R, x);
                        val = op(l->val, r->val);
                }
        }
        void add(ll L, ll R, ll x) {
                if (R <= lo || hi <= L) return;
                if (L <= lo && hi <= R) {
                        if (mset != inf) mset += x;
                        else madd += x;
                        val += x;
                }
                else {
                        push(), l->add(L, R, x), r->add(L, R, x);
                        val = op(l->val, r->val);
                }
        }
        void push() {
                if (!l) {
                        ll mid = lo + (hi - lo)/2;
                        l = new Node(lo, mid); r = new Node(mid, hi);
                }
                if (mset != inf)
                        l->set(lo,hi,mset), r->set(lo,hi,mset), mset = inf;
                else if (madd)
                        l->add(lo,hi,madd), r->add(lo,hi,madd), madd = 0;
        }
```

```cpp
};

void solve(){
        int type, k, u, n, q;
        cin >> n >> q;

        vector<int> v(n);
        for(auto &i: v) cin >> i;

        Node *root = new Node(v, 0, n);

        while(q--){
                cin >> type >> k >> u;
                if(type == 1){ // Point update index k-1 to u
                        root->set(k-1, k, u);
                        continue;
                }
                cout << root->query(k-1, u) << endl; // Get the sum from index k-1 to u (
                        ↪ exclusive end)
        }
}
```

Segment Tree (Max Prefix Sum)

```cpp
const ll inf = 1e9;
#define DEFAULTVALUE -inf

//#define op(l, r) max(l, r+1)
pair<ll, ll> op(pair<ll, ll> l, pair<ll, ll> r){
        return make_pair((max(l.first, r.first + l.second)), (l.second + r.second));
}

struct Node {
        Node *l = 0, *r = 0;
        ll lo, hi, mset = inf, madd = 0;
        pair<ll, ll> val = {DEFAULTVALUE, 0};

        Node(ll lo,ll hi):lo(lo),hi(hi){} // Large interval of -inf
        Node(vector<int>& v, ll lo, ll hi) : lo(lo), hi(hi) {
                if (lo + 1 < hi) {
                        ll mid = lo + (hi - lo)/2;
                        l = new Node(v, lo, mid);
                        r = new Node(v, mid, hi);
                        val = op(l->val, r->val);
                        //cout << lo << " " << hi << " " << val << endl;
                }
                else {
                        val = {v[lo], v[lo]};
                        // cout << val << endl;
                }
        }
        pair<ll, ll> query(ll L, ll R) {
                if (R <= lo){
                        return make_pair(DEFAULTVALUE, 0);
                }else if (hi <= L){
                        return make_pair(DEFAULTVALUE, 0);
```

```cpp
            }
            if (L <= lo && hi <= R) return val;
            // cout << "prepush: " << lo << " " << hi << " " << val << endl;
            push();
            // cout << "pospush: " << lo << " " << hi << " " << val << endl;
            // cout << "\n\n\n";

            return op(l->query(L, R), r->query(L, R));
    }
    void set(ll L, ll R, ll x) {
            if (R <= lo || hi <= L) return;
            if (L <= lo && hi <= R){
                    mset = val.first = x, madd = 0;
                    val.second -= val.second;
                    val.second += x;
            }
            else {
                    push(), l->set(L, R, x), r->set(L, R, x);
                    val = op(l->val, r->val);
            }
    }
    void add(ll L, ll R, ll x) {
            if (R <= lo || hi <= L) return;
            if (L <= lo && hi <= R) {
                    if (mset != inf) mset += x;
                    else madd += x;
                    val.first += x;
            }
            else {
                    push(), l->add(L, R, x), r->add(L, R, x);
                    val = op(l->val, r->val);
            }
    }
    void push() {
            if (!l) {
                    ll mid = lo + (hi - lo)/2;
                    l = new Node(lo, mid); r = new Node(mid, hi);
            }
            if (mset != inf)
                    l->set(lo,hi,mset), r->set(lo,hi,mset), mset = inf;
            else if (madd)
                    l->add(lo,hi,madd), r->add(lo,hi,madd), madd = 0;
    }
};
```

Persistent Segtree

```cpp
struct Node{ int mn, l, r; };

int init(int l, int r, Node st[], int* curr){
    if (l == r){ st[++(*curr)].mn = INF; return (*curr); }
    int m = l+(r-1)/2;
    int p = ++(*curr);
    st[p] = {0, init(l, m, st, curr), init(m+1, r, st, curr)};
    st[p].mn = min(st[st[p].l].mn, st[st[p].r].mn);
    return p;
```

```cpp
}

int update(int i, int l, int r, int k, int x, Node st[], int* curr){
    if (l == r){ st[++(*curr)].mn = x; return *curr; }
    int m = l+(r-1)/2;
    int p = ++(*curr);
    if (k <= m){
            st[p] = {0, update(st[i].l, l, m, k, x, st, curr), st[i].r};
    } else {
            st[p] = {0, st[i].l, update(st[i].r, m+1, r, k, x, st, curr)};
    }
    st[p].mn = min(st[st[p].l].mn, st[st[p].r].mn);
    return p;
}

int query(int i, int l, int r, int tl, int tr, Node st[]){
    if (l > tr || r < tl) return INF;
    if (tl <= l && r <= tr) return st[i].mn;
    int m = l+(r-1)/2;
    return min(query(st[i].l, l, m, tl, tr, st), query(st[i].r, m+1, r, tl, tr, st));
}

int arr[n+1], root[n+2], curr = 1;    //Tres linhas seguintes por no solve
map<int, int> pos;
Node st[22*n];
```

Trie

```cpp
template<char MIN_CHAR = 'a', int ALPHABET = 26>
struct array_trie {
    struct trie_node {
            array<int, ALPHABET> child;
            int words_here = 0, starting_with = 0;

            trie_node() {
                    memset(&child[0], -1, ALPHABET * sizeof(int));
            }
    };

    static const int ROOT = 0;

    vector<trie_node> nodes = {trie_node()};

    array_trie(int total_length = -1) {
            if (total_length >= 0)
                    nodes.reserve(total_length + 1);
    }

    int get_or_create_child(int node, int c) {
            if (nodes[node].child[c] < 0) {
                    nodes[node].child[c] = int(nodes.size());
                    nodes.emplace_back();
            }
            return nodes[node].child[c];
    }
```

```cpp
    int build(const string &word, int delta) {
        int node = ROOT;
        for (char ch : word) {
            nodes[node].starting_with += delta;
            node = get_or_create_child(node, ch - MIN_CHAR);
        }
        nodes[node].starting_with += delta;
        return node;
    }

    int add(const string &word) {
        int node = build(word, +1);
        nodes[node].words_here++;
        return node;
    }

    int erase(const string &word) {
        int node = build(word, -1);
        nodes[node].words_here--;
        return node;
    }

    int find(const string &str) const {
        int node = ROOT;
        for (char ch : str) {
            node = nodes[node].child[ch - MIN_CHAR];
            if (node < 0)
                break;
        }
        return node;
    }

    int count_prefixes(const string &str, bool include_full) const {
        int node = ROOT, count = 0;
        for (char ch : str) {
            count += nodes[node].words_here;
            node = nodes[node].child[ch - MIN_CHAR];
            if (node < 0)
                break;
        }
        if (include_full && node >= 0)
            count += nodes[node].words_here;
        return count;
    }

    int count_starting_with(const string &str, bool include_full) const {
        int node = find(str);
        if (node < 0)
            return 0;
        return nodes[node].starting_with - (include_full ? 0 : nodes[node].
            ↪ words_here);
    }
};
```

Persistent Trie

```cpp
// Node for lowercase strings
struct Node {
    array<shared_ptr<Node>, 26> children;
    bool end; // whether this node represents the end of a key
    size_t count; // optional (depending on queries)

    Node() : children{}, end{false}, count{0} {}
};

class Trie {
private:
    shared_ptr<Node> root;
    explicit Trie(shared_ptr<Node> root) : root(root) {}

public:
    Trie() : root(new Node()) {}
    size_t size() const {
        return root->count;
    }

    bool exists(string_view s) const {
        auto node = root;
        for (auto c : s) {
            auto idx = c - 'a';
            if (node->children[idx]) {
                node = node->children[idx];
            } else {
                return false;
            }
        }
        return node->end;
    }

    optional<Trie> insert(string_view s) {
        if (exists(s)) {
            return {};
        }

        auto nroot = make_shared<Node>(*root);
        auto node = nroot;
        node->count += 1;
        for (auto c : s) {
            auto idx = c - 'a';
            if (node->children[idx]) {
                node = node->children[idx] = make_shared<Node>(*(node->
                    ↪ children[idx]));
            } else {
                node = node->children[idx] = make_shared<Node>();
            }
            node->count += 1;
        }
        node->end = true;
        return Trie(nroot);
    }

    size_t count(string_view prefix) const {
```

```
        auto node = root.get();
        for (auto c : prefix) {
                auto idx = c - 'a';
                if (node->children[idx]) {
                        node = node->children[idx].get();
                } else {
                        return 0;
                }
        }
        return node->count;
    }
};
```

Sparse Table

```
class SparseTable{
        private:
                vi A, P2, L2; //A -> o array, P2 -> P2[x] = 2^x, L2 -> L2[x] = floor(log2(x
                    ↪ ))
                vv SpT;
        public:
                SparseTable(){}

                SparseTable(vi &initialA){
                A = initialA;
                int n = (int) A.size();
                int L2_n = (int) log2(n)+1;
                P2.assign(L2_n+1, 0);
                L2.assign((1<<L2_n)+1, 0);
                for (int i = 0; i <= L2_n; i++){
                        P2[i] = (1<<i);
                                L2[(1<<i)] = i;
                        }
                for (int i = 2; i < P2[L2_n]; i++){
                                if (L2[i] == 0) L2[i] = L2[i-1];
                }

                // the initialization phase
                SpT = vv (L2[n]+1, vi(n));
                for (int j = 0; j < n; j++){
                        SpT[0][j] = j;
                }

                //the two nested loops below have overall time complexity = O(n log(n))
                for (int i = 1; P2[i] <= n; i++){
                        for (int j = 0; j+P2[i]-1 < n; j++){
                    int x = SpT[i-1][j];
                                        int y = SpT[i-1][j+P2[i-1]];
                                        SpT[i][j] = A[x] <= A[y] ? x : y;
                                }
                }
                }

                int RMQ(int i, int j){
                int k = L2[j-i+1];
                int x = SpT[k][i];
```

```
                int y = SpT[k][j-P2[k]+1];
                return A[x] <= A[y] ? x : y;
                }
        };

        //Dentro de solve ou main
        SparseTable Spt = SparseTable(L);
```

— GRAPHS —

DFS

```
void dfs (int v, vector<bool> &visited, vv &graph){
        visited[v] = true;
        for(int no: graph[v]){
                if (!visited[no]){
                        dfs(no, visited, graph);
                }
        }
        return;
}
```

BFS

```
vector<bool> visited(1001, false);
vv graph(1001);

void BFS (int root, int goal){
        int cur;
        queue<int> Q;
        visited[root] = true;
        cout << "visiting root\n";
        Q.push(root);

        while(!Q.empty()){
                cur = Q.front(); Q.pop();
                cout << "visiting node " << cur << endl;

                if (cur == goal)
                        return;

                for(auto w: graph[cur]){
                        if(visited[w] == false){
                                visited[w] = true;
                                Q.push(w);
                        }
                }
        }
}
```

Flood Fill

```cpp
bool valid(int i, int j, int n, int m, vector<vector<char>> &grid){
        return i>=0 && j>= 0 && i < n && j < m && grid[i][j] == '.';
}

void dfs(int i, int j, int n, int m, vv& visited,vector<vector<char>> &grid){
        visited[i][j] = 1;
        for (int k = 0; k < 4; k++){
                int ni = i + di[k], nj = j + dj[k];
                if (valid(ni, nj, n, m, grid) && !visited[ni][nj]){
                        dfs(ni, nj, n, m, visited, grid);
                }
        }
}

void solve(){
        int n, m;
        cin>>n>>m;
        vector<vector<char>> grid(n, vector<char> (m));
        vv visited(n, vi (m));
        for (int i = 0; i < n; i++){
                for (int j = 0; j < m; j++){
                        cin>>grid[i][j];
                }
        }
        int ans = 0;
        for (int i = 0; i < n; i++){
                for (int j = 0; j < m; j++){
                        if (valid(i, j, n, m, grid) && !visited[i][j]){
                                dfs(i, j, n, m, visited, grid);
                                ans++;
                        }
                }
        }
        cout<<ans<<endl;
}
```

Monsters/Avalanche Flood Fill

```cpp
vector<vector<ll>> dist;
vector<vector<char>> grid;
vector<vector<pair<ll, ll>>> parents;
queue<pair<ll, ll>> q;
ll n, m;
string out;

bool possible = false;
bool advPath = false;

const int di[] = {1, 0, -1, 0};
const int dj[] = {0, -1, 0, 1};

bool edge(pair<ll, ll> coords){
    return (coords.first == 0 || coords.second == 0 || coords.first == n-1 || coords.
        ↪ second == m-1);
}
```

```cpp
bool valid(ll i, ll j){
    return i >= 0 && j >= 0 && i < n && j < m && grid[i][j] == '.';
}

void getPath(pair<ll, ll> node){
    pair<ll, ll> parent = parents[node.first][node.second];
    if(parent.first == -1)
        return;
    if(parent.first == node.first + 1)
        out.push_back('U');
    if(parent.first == node.first - 1)
        out.push_back('D');
    if(parent.second == node.second + 1)
        out.push_back('L');
    if(parent.second == node.second - 1)
        out.push_back('R');
    getPath(parent);
}

void bfs(){
    ll curDist = 0;
    while(!q.empty()){
        pair<ll, ll> cur = q.front(); q.pop();
        curDist = dist[cur.first][cur.second];

        for(int k = 0; k < 4; k++){
            pair<ll, ll> next = {cur.first + di[k], cur.second + dj[k]};

            // curDist + 1 < dist[next.first][next.second] ensures that it is worth it to
                ↪ visit de adjacent node
            if((valid(next.first, next.second) && (curDist + 1 < dist[next.first][next.
                ↪ second]))){
                dist[next.first][next.second] = curDist + 1; // The distance from the
                    ↪ origin to the next node is always the current distance + 1
                q.push(next);
                parents[next.first][next.second] = cur; // The next node's parent is the
                    ↪ current one
            }
        }

        if(advPath && (edge(cur))){
            cout << "YES" << endl << dist[cur.first][cur.second] << endl;
            getPath(cur);
            reverse(out.begin(), out.end());
            cout << out << endl;
            possible = true;
        }
    }
}

void solve(){
    cin >> n >> m;
    char add;
    grid.resize(n, vector<char>(m));
    dist.resize(n, vector<ll>(m, INT_MAX));
```

```cpp
    pair<ll, ll> start;
    parents.resize(n, vector<pair<ll, ll>>(m));

    for(int i = 0; i < n; ++i){
        for(int j = 0; j < m; ++j){
            cin >> add;
            if(add == 'A'){
                start = {i, j};
            }
            if(add == 'M'){
                q.push({i, j});
                dist[i][j] = 0;
            }
            grid[i][j] = add;
        }
    }

    // BFS for each one of the monsters
    bfs();

    advPath = true; // Flag to indicate that the next BFS will define the adventurer's
        ↪ path
    q.push(start);
    parents[start.first][start.second] = {-1, -1}; // This is set to {-1, -1} in order for
        ↪ the getPath function to know when it has reached the origin
    dist[start.first][start.second] = 0;

    bfs();

    if(!possible)
        cout << "NO" << endl;
}
```

Disjoint Set Union (Union Find)

```cpp
//Cada valor comeca por ser o seu proprio set
void makeSet(int v, vi &parent) {
    parent[v] = v;
}
int findSet(int v, vi &parent) {
    if (v != parent[v])
        parent[v] = findSet(parent[v], parent);
    return parent[v];
}
void unionSets(int u, int v, vi &parent) {
    int root1 = findSet(u, parent);
    int root2 = findSet(v, parent);
    parent[root2] = root1;
}
bool check(int u, int v, vi &parent) {
    return findSet(u, parent) == findSet(v, parent);
}
```

Dijkstra

```cpp
vector<int> dijkstra(vector<vector<pii>>& adjMatrix, int source, int target) {
    int n = adjMatrix.size();
    vector<int> dist(n, INF);
    vector<bool> visited(n, false);
    dist[source] = 0;
    priority_queue<pii, vector<pii>, greater<pii>> pq;
    pq.push(make_pair(0, source));
    while (!pq.empty()) {
        int u = pq.top().second;
        pq.pop();
        if (visited[u]) {
            continue;
        }
        visited[u] = true;
        if (u == target) {
            break;
        }
        for (auto& neighbor : adjMatrix[u]) {
            int v = neighbor.first;
            int weight = neighbor.second;
            if (dist[v] > dist[u] + weight) {
                dist[v] = dist[u] + weight;
                pq.push(make_pair(dist[v], v));
            }
        }
    }
    return dist;
}
```

Bellman-Ford

```cpp
vi BF(vvpii &adjList, int source){
    int n = adjList.size();
    vi dist(n+1, INF);
    dist[source] = 0;
    for (int i = 1; i < n; i++){
        bool modified = false;
        for (int j = 1; j <= n; j++){
            if (dist[j] != INF){
                for (auto nbr: adjList[j]){
                    int v = nbr.fi;
                    int weight = nbr.se;
                    if (dist[v] > dist[j] + weight){
                        dist[v] = dist[j] +weight;
                        modified = true;
                    }
                }
            }
        }
        if (!modified) break;
    }
    bool hasNegativeCycle = false;
    for (int i = 1; i <= n; i++){
        if (dist[i] != INF){
            for (auto nbr: adjList[i]){
```

```
                int v = nbr.fi;
                int weight = nbr.se;
                if (dist[v] > dist[i] + weight){
                        hasNegativeCycle = true;
                }
            }
        }
    }
    if (hasNegativeCycle){
        for (int i = 0; i <= n; i++){
            dist[i] = -1;
        }
    }
    return dist;
}
```

Floyd-Warshall

```
void FW(vv &matrix, vv *p = NULL){
    int numVertices = (int) matrix.size();
    if (p){
        for (int i = 0; i < numVertices; i++){
            for (int j = 0; j < numVertices; j++){
                p[i][j] = i;
            }
        }
    }
    for (int k = 0; k < numVertices; k++){
        for (int i = 0; i < numVertices; i++){
            for (int j = 0; j < numVertices; j++){
                if (matrix[i][k] != INT_MAX && matrix[k][j] != INT_MAX){
                    matrix[i][j] = min(matrix[i][j], matrix[i][k] + matrix
                    ↪ [k][j]);
                    if (p) p[i][j] = p[k][j];
                }
            }
        }
    }
}

void printPath(int i, int j){       //Nao sei se esta funcao esta 100% correta mas a ideia
    ↪ esta la
    if (i != j) printPath(i, p[i][j]);
    cout<<j<<endl;
}
```

Bipartite Matching

```
vv graph(1001);
vi color (1001, -1);

bool bipartite(int start){
    int cur;
    queue<int> Q;
    color[start] = 1;
```

```
    Q.push(start);

    while(!Q.empty()){
        cur = Q.front(); Q.pop();

        for(auto u: graph[cur]){
            if(color[u] == -1){
                color[u] = 1 - color[cur];
                Q.push(u);
            }
            else if(color[u] == color[cur])
                return false;
        }
    }
    return true;
}

int main(){
    int m, u, v, start;
    cin >> m;
    forn(i, m){
        cin >> u >> v;
        graph[u].push_back(v);
        graph[v].push_back(u);
    }
    cin >> start;

    if (bipartite(start) == true)
        cout << "Yes\n";
    else
        cout << "No\n";

    return 0;
}
```

Tarjan (Strongly Connected Components)

```
vector<vector<ll>> graph;
vector<vector<ll>> SCCs;
vector<bool> visited;
vector<ll> ids;
vector<ll> low;
ll counter;
stack<ll> S;
vector<bool> onStack;
ll id;

void dfs(ll cur){
    S.push(cur);
    onStack[cur] = true;
    ids[cur] = low[cur] = id;
    id++;

    for(auto adj: graph[cur]){
```

```
                if(ids[adj] == -1){
                        dfs(adj);
                }
                // If statement after the DFS callback
                if(onStack[adj]){
                        low[cur] = min(low[cur], low[adj]);
                }
        }

        // SCC root found
        ll top = -1;
        if(ids[cur] == low[cur]){
                vector<ll> newSCC;
                while(top != cur){
                        top = S.top(); S.pop();
                        onStack[top] = false;
                        low[top] = ids[cur];
                        newSCC.push_back(top);
                }
                SCCs.push_back(newSCC);
                counter++;
        }
}

void tarjan(){
        id = 1;
        counter = 0;

        for(ll i = 1; i <= n; ++i){
                if(ids[i] == -1){
                        dfs(i);
                }
        }

}
```

Eulerian Path

```
//Para grafo direcionado, nao e preciso arestas. Guarda-se o vertices de saida diretamente
     ↪ na list. Outras mudancas sao necessarias
//Verificar se e conexo (dfs) e todos os vertices tem grau par. Para semi-eulariano, 2
     ↪ vertices com grau impar, restantes par
vi hierholzer(int s, vector<list<int>> &graph, vector<pair<pii, bool>> &arestas){
        int n = graph.size();
        vi ans, idx(n, 0), st;
        st.pb(s);
        while (!st.empty()){
                int u = st.back();
                //ciclo nao necessario para grafo direcionado
                while (!graph[u].empty() && arestas[graph[u].front()].se){
                        graph[u].pop_front();
                }
                if (!graph[u].empty()){
                        pii are = arestas[graph[u].front()].fi;
                        if (are.fi == u) st.pb(are.se);
                        else st.pb(are.fi);
```

```
                        arestas[graph[u].front()].se = true;
                        graph[u].pop_front();
                }else{
                        ans.pb(u);
                        st.pop_back();
                }
        }
        reverse(all(ans));
        return ans;
}
```

Max-Flow/Min-Cut

```
template<class T> void dfs(int s, vector<unordered_map<int, T>> &graph, vv &adjacency, vb
     ↪ &visited){
        visited[s] = true;
        for (int ver: adjacency[s]){
                if (!visited[ver] && graph[s][ver] != 0){
                        dfs(ver, graph, adjacency, visited);
                }
        }
}

#define rep(i, a, b) for(int i = a; i < (b); ++i)
template<class T> T edmondsKarp(vector<unordered_map<int, T>>&graph, int source, int sink,
     ↪ vpii *arestas = NULL) {
        assert(source != sink);
        T flow = 0;
        vi par(sz(graph)), q = par;
        int n = graph.size();
        vv adjacency(n);
        if (arestas){
                for (int i = 0; i < n; i++){
                        for (pii are: graph[i]){
                                adjacency[i].pb(are.fi);
                        }
                }
        }
        for (;;) {
                fill(all(par), -1);
                par[source] = 0;
                int ptr = 1;
                q[0] = source;

                rep(i,0,ptr) {
                        int x = q[i];
                        for (auto e : graph[x]) {
                                if (par[e.first] == -1 && e.second > 0) {
                                        par[e.first] = x;
                                        q[ptr++] = e.first;
                                        if (e.first == sink) goto out;
                                }
                        }
                }
                if (arestas){
                        vb visited(n, false);
```

```
                dfs(source, graph, adjacency, visited);
                for (int i = 0; i < n; i++){
                        for (pair<int, T> ver: graph[i]){
                                if (!visited[i] && visited[ver.fi] && graph[ver.fi][i]
                                ↪  == 0){
                                        (*arestas).pb(mp(ver.fi, i));
                                }
                        }
                }
        }
        return flow;
out:

        T inc = numeric_limits<T>::max();
        for (int y = sink; y != source; y = par[y])
                inc = min(inc, graph[par[y]][y]);

        flow += inc;
        for (int y = sink; y != source; y = par[y]) {
                int p = par[y];
                if ((graph[p][y] -= inc) <= 0) graph[p].erase(y);
                graph[y][p] += inc;
        }
    }
}
```

MIUP 2022 B (Max-Flow/Min-Cut Example)

```
void solve(){
        //reset e leitura de valores
        ll n, m;
        cin>>n>>m;
        //criar sempre um "novo" sink e source
        ll i_source = 0, i_sink = n*2 + 1;
        vi pop(n + 1);
        vi custos(n + 1);
        vector<unordered_map<int, ll>> graph((n+1)*2);
        for (ll i = 1; i <= n; i++){
                cin>>pop[i]>>custos[i];
                graph[(i*2) - 1][i*2] = custos[i];
        }
        while(m--) {
                //Se a aresta nao for de duplo sentido, o res do sentido contrario tem de
                ↪  ser 0
                ll n_1, n_2;
                cin>>n_1>>n_2;
                graph[n_1*2][(n_2*2) - 1] = INF;
                graph[n_2*2][(n_1*2) - 1] = INF;
        }
        ll safe;
        cin>>safe;
        //ligar source e sink aos vertices necessarios
        for (ll i = 1; i <= n; i++){
                graph[i_source][(i*2) - 1] = pop[i];
        }
```

```
        graph[(safe*2) - 1][i_sink] = INF;
        ll maxFlow = edmondsKarp(graph, i_source, i_sink);
        cout<<maxFlow<<endl;
}
```

Min-Cost/Max-Flow

```
typedef tuple<int, ll, ll, ll> edge;
class min_cost_max_flow {
private:
        int V;
        ll total_cost;
        vector<edge> EL;
        vector<vi> AL;
        vll d;
        vi last, vis;

        bool SPFA(int s, int t) { // SPFA to find augmenting path in residual graph
        d.assign(V, INF); d[s] = 0; vis[s] = 1;
        queue<int> q({s});
        while (!q.empty()) {
                int u = q.front(); q.pop(); vis[u] = 0;
                for (auto &idx : AL[u]) { // explore neighbors of u
                auto &[v, cap, flow, cost] = EL[idx]; // stored in EL[idx]
                if ((cap-flow > 0) && (d[v] > d[u] + cost)) { // positive residual edge
                        d[v] = d[u]+cost;
                        if(!vis[v]) q.push(v), vis[v] = 1;
                }
                }
        }
        return d[t] != INF; // has an augmenting path
        }

        ll DFS(int u, int t, ll f = INF) { // traverse from s->t
        if ((u == t) || (f == 0)) return f;
        vis[u] = 1;
        for (int &i = last[u]; i < (int)AL[u].size(); ++i) { // from last edge
                auto &[v, cap, flow, cost] = EL[AL[u][i]];
                if (!vis[v] && d[v] == d[u]+cost) { // in current layer graph
                if (ll pushed = DFS(v, t, min(f, cap-flow))) {
                                total_cost += pushed * cost;
                        flow += pushed;
                        auto &[rv, rcap, rflow, rcost] = EL[AL[u][i]^1]; // back edge
                        rflow -= pushed;
                        vis[u] = 0;
                        return pushed;
                }
                }
        }
        vis[u] = 0;
        return 0;
        }

public:
        min_cost_max_flow(int initialV) : V(initialV), total_cost(0) {
        EL.clear();
```

```
        AL.assign(V, vi());
        vis.assign(V, 0);
        }

        // if you are adding a bidirectional edge u<->v with weight w into your
        // flow graph, set directed = false (default value is directed = true)
        void add_edge(int u, int v, ll w, ll c, bool directed = true) {
        if (u == v) return; // safeguard: no self loop
        EL.emplace_back(v, w, 0, c); // u->v, cap w, flow 0, cost c
        AL[u].push_back(EL.size()-1); // remember this index
        EL.emplace_back(u, 0, 0, -c); // back edge
        AL[v].push_back(EL.size()-1); // remember this index
        if (!directed) add_edge(v, u, w, c); // add again in reverse
        }

        pair<ll, ll> mcmf(int s, int t) {
        ll mf = 0; // mf stands for max_flow
        while (SPFA(s, t)) { // an O(V^2*E) algorithm
                last.assign(V, 0); // important speedup
                while (ll f = DFS(s, t)) // exhaust blocking flow
                mf += f;
        }
        return {mf, total_cost};
        }
};

void solve(){
        int v, e, s, t;
        cin>>v>>e>>s>>t;
        min_cost_max_flow mf(v);
        for (int i = 0; i < e; i++){
                int a, b, cap, cost;
                cin>>a>>b>>cap>>cost;
                mf.add_edge(a, b, cap, cost);
        }
        pll res = mf.mcmf(s, t);
        cout<<res.fi<<' '<<res.se<<endl;
}
```

MIUP 2023 E (Min-Cost/Max-Flow Example)

```
void solve(){
        int d, n, c, m, vals, valc, source = 0;
        cin>>d>>n>>c>>m;
        vi capacity(n+1);
        int sink = c + n + 1, maxProfit = 100;
        min_cost_max_flow mf(c + n + 2);
        for (int i = 1; i <= n; i++){
                        cin>>capacity[i];
        }
        vi shipTime(n+1);
        for (int i = 1; i <= n; i++){
                        cin>>shipTime[i];
                        int count = 0, aux = d;
```

```
                        while ((aux > 0)){
                                aux -= shipTime[i];
                                int cap = capacity[i];
                                while ((aux > 1) && (cap > 0)){
                                        aux-=2;
                                        cap--;
                                        count++;
                                }
                                aux -= shipTime[i];
                        }
                        capacity[i] = count;
        }
        vi lucro(c+1);
        for (int i = 1; i <= c; i++){
                cin>>lucro[i];
        }
        for (int i = 0; i < m; i++){
                cin>>vals>>valc;
                mf.add_edge(valc, c + vals, 1, maxProfit-lucro[valc]);
        }
        for (int i = 1; i <= n; i++){
                mf.add_edge(c + i, sink, capacity[i], 0);
        }
        for (int i = 1; i <= c; i++){
                mf.add_edge(source, i, 1, 0);
        }
        pll res = mf.mcmf(source, sink);
        cout<<res.fi*maxProfit - res.se<<endl;
}
```

Articulation Points

```
void AP(int v, vv &adj, vb &check, vi &dfs, vi &low, vi &parent, int &t, int &c){
        low[v] = dfs[v] = t++;
        for (auto nbr: adj[v]){
                if (dfs[nbr] == 0){
                        parent[nbr] = v;
                        AP(nbr, adj, check, dfs, low, parent, t, c);
                        low[v] = min(low[v], low[nbr]);
                        if (!check[v]){
                                if (dfs[v] == 1){
                                        if (dfs[nbr] != 2) c++;
                                }else{
                                        if (low[nbr] >= dfs[v]) c++;
                                }
                        }
                        check[v] = true;
                }else if (parent[v] != nbr){
                        low[v] = min(low[v], dfs[nbr]);
                }
        }
}

void solve(){
        int n, m;
        cin>>n>>m;
```

```
        vv adj(n+1);
        vb check(n+1);
        vi dfs(n+1, 0);
        vi low(n+1, -1);
        vi parent(n+1, -1);
        int t = 1;
        int c = 0;
        AP(1, adj, check, dfs, low, parent, t, c);
}
```

Kruskal (Minimum Spanning Tree)

```
//Cada valor comeca por ser o seu proprio set
void makeSet(int v, vi &parent) {
        parent[v] = v;
}
int findSet(int v, vi &parent) {
        if (v != parent[v]) parent[v] = findSet(parent[v], parent);
        return parent[v];
}
void unionSets(int u, int v, vi &parent) {
        int root1 = findSet(u, parent);
        int root2 = findSet(v, parent);
        parent[root2] = root1;
}
bool check(int u, int v, vi &parent) {
        return findSet(u, parent) == findSet(v, parent);
}

template<class T> T KruskalMST(vector<tuple<T, int, int>> edges, int V){
        sort(all(edges));
        vi parent(V);
        for (int i = 0; i < V; i++){
                makeSet(i, parent);
        }
        T mst_cost = 0, num_taken = 0;
        for (auto &[w, u, v]: edges){
                if (check(u, v, parent)) continue;
                mst_cost += w;
                unionSets(u, v, parent);
                ++num_taken;
                if (num_taken == V-1) break;
        }
        return mst_cost;
}
```

Lowest Common Ancestor

```
void dfs(int cur, int depth, vv &adjMatrix, vb &visited, vi &L, vi &E, vi &H, int &idx){
        H[cur] = idx;
        E[idx] = cur;
        L[idx++] = depth;
        visited[cur] = true;
        for (int nxt: adjMatrix[cur]){
                if (!visited[nxt]){
```

```
                        dfs(nxt, depth+1, adjMatrix, visited, L, E, H, idx);
                        E[idx] = cur;
                        L[idx++] = depth;
                }
        }
}

void buildRMQ(int n, vv &adjMatrix, int m){
        vi L(2*n), E(2*n), H(n, -1);
        vb visited(n, false);
        int idx = 0;
        dfs(0, 0, adjMatrix, visited, L, E, H, idx);
        //LCA(i, j) e o E[ indice do min( L(H[i]...H[j]) ) ]. Para isto usamos uma SegTree
        ↪ ou SparseTable em L (E[SpT.query(H[i], H[j])])
        SparseTable Spt = SparseTable(L);
        int a, b;
        for (int i = 0; i < m; i++){
                cin>>a>>b;
                a--;b--;
                int lca = E[Spt.RMQ(min(H[a], H[b]), max(H[a], H[b]))];
        }
}
```

— MATH —

Cicle Finding

```
        int f(int x){ //Avancar na expressao onde estamos a encontrar ciclo
        return (26*x + 11)%80;
}

pii floydCicleFinding(int x){ //Index (x) onde comeca a sequencia (arr)
        int t = f(x), h = f(f(x));
        while (t != h){
                t = f(t);
                h = f(f(h));
        }
        int fase = 0, h = x;
        while (t != h){
                t = f(t);
                h = f(h);
                fase++;
        }
        int T = 1;
        h = f(t);
        while (t != h){
                h = f(h);
                T++;
        }
        return mp(T, fase);
}
```

Count Digits

```
int countDigits(double num, double baseNum, double baseNova){
        return floor(1 + log(num)/log(baseNova));
}
```

Max Range Sum (1D and 2D)

```
ll maxRangeSum1D(int n, vll &arr){
        ll ans = 0;
        //limpeza dos negativos
        ans = arr[0];
        for (int j = 0; j < n; j++){
                if (arr[j] >= 0){
                        ans = 0;
                        break;
                }else{
                        if (arr[j] > ans) ans = arr[j];
                }
        }
        if (ans < 0) return ans;
        //fim de limpeza
        ans = 0;
        ll sum = 0;
        for (int j = 0; j < n; j++){
                sum += arr[j];
                ans = max(ans, sum);
                if (sum < 0) sum = 0;
        }
        return ans;
}

// ----------------------------

ll maxRangeSum2D(int n, vvll &mat){
        for (int i = 0; i < n; i++){
                for (int j = 1; j < n; j++){
                        mat[i][j] += mat[i][j-1];
                }
        }
        ll maior = -INF;
        for (int i = 0; i < n; i++){
                for (int j = i; j < n; j++){
                        ll subrect = 0;
                        for (int k = 0; k < n; k++){
                                if (i > 0) subrect += mat[k][j] - mat[k][i-1];
                                else subrect += mat[k][j];
                                if (subrect < 0) subrect = 0;
                                maior = max(maior, subrect);
                        }
                }
        }
        return maior;
}
```

Max Subarray Sum

```
ll MaximumSubarraySumN(int n, vll &arr){
        ll maior = 0;
        //limpeza dos negativos
        maior = arr[0];
        for (int j = 0; j < n; j++){
                if (arr[j] >= 0){
                        maior = 0;
                        break;
                }else{
                        if (arr[j] > maior) maior = arr[j];
                }
        }
        if (maior < 0) return maior;
        //fim de limpeza
        ll atual = 0, cache = -1, flag = 0;
        for (int j = 0; j < n; j++){
                if ((atual + arr[j]) < 0){
                        if (cache != -1){
                                if (cache > maior) maior = cache;
                                cache = -1;
                                flag = 0;
                        }else{
                                if (atual > maior) maior = atual;
                        }
                        atual = 0;
                }else{
                        if ((atual + arr[j] >= atual) || flag){
                                atual += arr[j];
                                if (atual > cache){
                                        cache = -1;
                                        flag = 0;
                                }
                        }else{
                                cache = atual;
                                atual += arr[j];
                                flag = 1;
                        }
                }
        }
        if (cache != -1){
                if (cache > maior) maior = cache;
        }else{
                if (atual > maior) maior = atual;
        }
        return maior;
}
```

— MODULAR / MATRICES —

Modular Arithmetic

```
// Modular function to avoid negative results
inline int mod(int a, int m) {
```

```
        return ((a % m) + m) % m;
}

int modPow(int b, int p, int m){
        if (p == 0) return 1;
        int ans = modPow(b, p/2, m);
        ans = mod(ans*ans, m);
        if (p&1) ans = mod(ans*b, m);
        return ans;
}

int modInverse(int A, int M){
        int m0 = M;
        int y = 0, x = 1;

        if (M == 1)
                return 0;

        while (A > 1) {
                // q is quotient
                int q = A / M;
                int t = M;

                // m is remainder now, process same as
                // Euclid's algo
                M = A % M, A = t;
                t = y;

                // Update y and x
                y = x - q * y;
                x = t;
        }
}
```

Matrix Operations

```
vvll matMul(vvll &a, vvll &b, int MOD){ //Duas matrizes nao nulas, i -> linhas, j ->
    ↪ colunas
        int lin = a.size();
        int col = b[0].size();
        vvll ans(lin, vll(col, 0));
        int par = b.size();
        for (int i = 0; i < lin; i++){
                for (int k = 0; k < par; k++){
                        if (a[i][k] == 0) continue;
                        for (int j = 0; j < col; j++){
                                ans[i][j] += mod(a[i][k], MOD) * mod(b[k][j], MOD);
                                ans[i][j] = mod(ans[i][j], MOD);
                        }
                }
        }
        return ans;
}

vvll matPow(vvll base, int p, int MOD){ //So matrizes quadradas
        int lin = base.size();
        vvll ans(lin, vll(lin));
```

```
        for (int i = 0; i < lin; i++){
                for (int j = 0; j < lin; j++){
                        ans[i][j] = (i == j);
                }
        }
        while (p){
                if (p&1){
                        ans = matMul(ans, base, MOD);
                }
                base = matMul(base, base, MOD);
                p >>= 1;
        }
        return ans;
}
```

Gaussian Elimination

```
#define MAX_N 100 //adjust this value as needed
struct AugmentedMatrix{ double mat[MAX_N][MAX_N + 1];};
struct ColumnVector{ double vec[MAX_N];};
ColumnVector GaussianElimination(int N, AugmentedMatrix Aug){ //O(n^3)
        //input: N, Augmented Matriz aug; output: Column Vector x, the answer
        for (int i = 0; i < N-1; i++){          //forward elimination
                int l = i;
                for (int j = i + 1; j < N; j++){          row with max col value
                        if (fabs(Aug.mat[j][i]) > fabs(Aug.mat[l][i])) l = j;      remember
                            ↪ this row l
                }
                //swap this pivot row, reason: minimize floating point error
                for (int k = i; k <= N; k++){
                        swap(Aug.mat[i][k], Aug.mat[l][k]);
                }
                for (int j = i+1; j < N; j++){     //actual fwd elimination
                        for (int k = N; k >= i; k--){
                                Aug.mat[j][k] -= Aug.mat[i][k] * Aug.mat[j][i] / Aug.mat[i][i
                                    ↪ ];
                        }
                }
        }
        ColumnVector Ans;           //back substition phase
        for (int j = N-1; j >= 0; j--){     //start from back
                double t = 0.0;
                for (int k = j+1; k < N; k++){
                        t += Aug.mat[j][k] * Ans.vec[k];
                }
                Ans.vec[j] = (Aug.mat[j][N]-t) / Aug.mat[j][j];     //the answer is here
        }
        return Ans;
}

int main(){
        AugmentedMatrix Aug;
        Aug.mat[0][0] = 1; Aug.mat[0][1] = 1; Aug.mat[0][2] = 2; Aug.mat[0][3] = 9; //x + y
            ↪ + 2z = 9
        Aug.mat[1][0] = 2; Aug.mat[1][1] = 4; Aug.mat[1][2] = 3; Aug.mat[1][3] = 1; //2x +
            ↪ 4y - 3z = 1
```

```
        Aug.mat[2][0] = 3; Aug.mat[2][1] = 6; Aug.mat[2][2] = 5; Aug.mat[2][3] = 0; //3x +
            ↪ 6y - 5z = 0
        ColumnVector X = GaussianElimination(3, Aug);
        cout<<"x = "<<X.vec[0]<<endl;
        cout<<"y = "<<X.vec[1]<<endl;
        cout<<"z = "<<X.vec[2]<<endl;
}
```

— Number Theory —

Combinatorics

```
int modInverse(int A, int M){
        int m0 = M;
        int y = 0, x = 1;

        if (M == 1)
                return 0;

        while (A > 1) {
                // q is quotient
                int q = A / M;
                int t = M;

                // m is remainder now, process same as
                // Euclid's algo
                M = A % M, A = t;
                t = y;

                // Update y and x
                y = x - q * y;
                x = t;
        }

        // Make x positive
        if (x < 0)
                x += m0;

        return x;
}

vpll fat;

void fatoriais(int tam, int m, vpll &res){
        res.pb(mp(1,1));
        for (int j = 1; j <= tam; j++){
                res.pb(mp((res[j-1].fi*j)%m, 0));
        }
        ll inv = modInverse(res[tam].fi, m);
        res[tam].se = inv;
        for (int j = tam-1; j > 0; j--){
                res[j].se = (res[j+1].se*(j+1))%m;
        }
```

```
}

ll comb(int c, int d, int m){
        if (d == 0) return 1;
        if ((d > 0) && (d > c)) return 0;
        return (((fat[c].fi*fat[d].se)%m)*fat[c-d].se)%m;
}
fatoriais(5000, MOD, fat); //Colocar dentro da main
```

Number Theory

```
int extEuclidean(int a, int b, int &x, int &y){
        int xx = y = 0;
        int yy = x = 1;
        while (b){
                int q = a/b;
                int t = b;
                b = a%b;
                a = t;
                t = xx;
                xx = x-q*xx;
                x = t;
                t = yy;
                yy = y - q*yy;
                y = t;
        }
        return a;
}

int modInverse(int A, int M){ //Para combinacoes/fatoriais, escrever comb ou fatoriais
        int x, y;
        int d = extEuclidean(A, M, x, y);
        if (d != 1) return -1;
        return mod(x, M);
}

di
pii diophantine(int a, int b, int sol){ //a*x + b*y = sol
        int x, y;
        int d = extEuclidean(a, b, x, y); //gcd(a, b)
        int mult = sol/d;
        x *= mult;
        y *= mult;
        b /= d;
        a /= d;
        int liminf = 0, limsup = INF;
        if ((x < 0) != (b < 0)){
                liminf = abs(x/b);
                if (x%b) liminf++;
        }else{
                limsup = abs(x/b);
        }
        if ((y < 0) != (a < 0)){
                int aux = abs(y/a);
                if (y%a) aux++;
                liminf = max(liminf, aux);
```

```cpp
        }else{
                limsup = min(limsup, abs(y/a));
        }
        if (liminf > limsup) return mp(-1, -1); //So devolve uma solucao para a equacao,
            ↪ mas ha um limite (finito ou infinito de solucoes)
        else return mp(x + b*liminf, y + a*liminf);
}

int crt(vi &r, vi &m){
        int mt = accumulate(m.begin(), m.end(), 1, multiplies<>());
        int x = 0;
        for (int i = 0; i < (int) m.size(); i++){
                int a = mod((ll)r[i] * modInverse(mt/m[i], m[i]), m[i]);
                x = mod(x + (ll)a * (mt/m[i]), mt);
        }
        return x;
}

vll Catalan(int n, ll m){ //n inclusive
        vll cat(n+1);
        cat[0] = 1;
        for (int i = 0; i < n; i++){
                cat[i+1] = mod(mod(mod((4*i)+2,m) * mod(cat[i],m), m) * modInverse(i+2, m),
                    ↪ m);
        }
        return cat;
}

inline long long int gcd(int a, int b){
        while (b) {
                a %= b;
                swap(a, b);
        }
        return a;
}

inline long long int lcm (int a, int b){
        return (a / gcd(a, b)) * b;
}
```

Primes

```cpp
ll sieve_size;
bitset<10000010> bs;
vll p;

void gerador(ll upperbound){ //Nao maior de 10^7
        sieve_size = upperbound+1;
        bs.set();
        bs[0] = bs[1] = 0;
        for (ll i = 0; i < sieve_size; i++){
                if (bs[i]){
                        for (ll j = i*i; j < sieve_size; j+=i) bs[j] = 0;
                        p.push_back(i);
                }
        }
```

```cpp
}

bool isPrime(ll N){
        if (N < sieve_size) return bs[N];
        for (int i = 0; i < (int) p.size() && p[i]*p[i] <= N; i++){
                if (N%p[i] == 0) return false;
        }
        return true;
}


//Por no solve
gerador(10000000);

vll primeFactor(ll N){ //Fatorizar em numeros primos, nao esquecer de gerar numeros primos
        vll factors;
        int tam = p.size();
        for (int i = 0; (i < tam) && (p[i]*p[i] <= N); i++){
                while (N%p[i] == 0){
                        N /= p[i];
                        factors.pb(p[i]);
                }
        }
        if (N != 1) factors.pb(N);
        return factors;
}

int numFatPrimos(ll N){ //Quantos fatores primos tem um numero
        int ans = 1;
        for (int i = 0; (i < (int) p.size()) && (p[i]*p[i] <= N); i++){
                while (N%p[i] == 0) {
                        N/=p[i];
                        ans++;
                }
        }
        return ans + (N != 1);
}

int numDivisores(ll N){ //Multiplicatorio de (n+1), sendo 'n' o numero de vezes que cada
    ↪ fator primos aparece
        int ans = 0;
        for (int i = 0; (i < (int) p.size()) && (p[i]*p[i] <= N); i++){
                int power = 0;
                while (N%p[i] == 0){
                        N /= p[i];
                        ++power;
                }
                ans *= power+1;
        }
        return (N != 1) ? 2*ans : ans;
}

ll sumDivisores(ll N){ //Multiplicatorio de (a^(n+1) - 1)/(a-1), sendo 'a' cada fator
    ↪ primo e 'n' o numero de vezes que 'a' se repete
        ll ans = 1;
        for (int i = 0; (i < (int) p.size()) && (p[i]*p[i] <= N); i++){
                ll multiplier = p[i], total = 1;
```

```
                while (N%p[i] == 0){
                        N /= p[i];
                        total += multiplier;
                        multiplier *= p[i];
                }
                ans *= total;
        }
        if (N != 1) ans *= (N+1);
        return ans;
}


ll numCoprimos(ll N){ //N * Multiplicatorio de (1 - 1/a), sendo 'a' cada fator primo de N
        ll ans = N;
        for (int i = 0; (i < (int) p.size()) && (p[i]*p[i] <= N); i++){
                if (N%p[i] == 0) ans -= ans/p[i];
                while (N%p[i] == 0) N/=p[i];
        }
        if (N != 1) ans -= ans/N;
        return ans;
}


vi numDiffFatPrimos(ll MAX_N){ //MAX_N <= 10^7 Numero de fatores primos diferentes para mt
    ↪   queries
        vi arr(MAX_N + 10, 0);
        for (int i = 2; i <= MAX_N; i++){
                if (arr[i] == 0){
                        for (int j = i; j <= MAX_N; j+=i){
                                ++arr[j];
                        }
                }
        }
        return arr;
}

vi numCoprimosMtQueries(ll Max_n){ //Max_n <= 10^7 Numero de coprimos para mt queries
        vi arr(Max_n);
        for (int i = 1; i <= Max_n; i++) arr[i] = i;
        for (int i = 2; i <= Max_n; i++){
                if (arr[i] == i){
                        for (int j = i; j <= Max_n; j+=i){
                                arr[j] = (arr[j]/i) * (i-1);
                        }
                }
        }
        return arr;
}
```

— Strings —

Aho-Corasick

```
string text; //Text
int n; //Size of text,
```

```
int k; //Number of keys
int maxs = 0; // Should be equal to the sum of the length of all keywords.
int maxc = 26; // Maximum number of characters in input alphabet

// Returns the number of states that the built machine has.
// States are numbered 0 up to the return value - 1, inclusive .
int buildMatchingMachine(string arr[], int k, vector<map<int, bool>> &out, vi &f, vv &g){
        int states = 1;
        for ( int i = 0; i < k; ++i){ // Construct values for goto function, i .e ., fill g
                const string &word = arr[i];
                int currentState = 0;
                for ( int j = 0; j < (int) word.size(); ++j){
                        int ch = word[j]-'a';
                        if (g[currentState][ch] == -1){ // Allocate a new node (create a new
                            ↪   state) if a node for ch doesnt exist .
                                g[currentState][ch] = states++;
                        }
                        currentState = g[currentState][ch];
                }
                out[currentState][i] = true; // Add current word in output function
        }
        for ( int ch = 0; ch < maxc; ++ch){
                if (g[0][ch] == -1){
                        g[0][ch] = 0;
                }
        }
        queue<int> q;
        for ( int ch = 0; ch < maxc; ++ch){
                if (g[0][ch] != 0){
                        f [g[0][ch]] = 0;
                        q.push(g[0][ch]) ;
                }
        }
        while (q.size () ) {
                int state = q.front () ;
                q.pop();
                for ( int ch = 0; ch < maxc; ++ch){
                        if (g[state][ch] != -1){
                                int failure = f [state];
                                while (g[ failure][ch] == -1){ // Find the deepest node
                                    ↪   labeled by proper suffix of string from root to
                                    ↪   current state .
                                        failure = f [ failure ];
                                }
                                failure = g[failure][ch];
                                f [g[state][ch]] = failure ;
                                for (pair<int, bool> par: out[failure]){
                                        out[g[state][ch]][par.fi] = par.se;
                                }
                                q.push(g[state][ch]) ;
                        }
                }
        }
        return states ;
}
```

```cpp
int findNextState(int currentState, char nextInput, vector<map<int, bool>> &out, vi &f, vv
    ↪ &g){ //Returns the next state the machine will transition to using goto and
    ↪ failure functions.
    int answer = currentState;
    int ch = nextInput -'a';
    while (g[answer][ch] == -1){
        answer = f[answer];
    }
    return g[answer][ch];
}

void searchWords(string arr[], int k, string text, vector<map<int, bool>> &out, vi &f, vv
    ↪ &g, vv &ocor, vi &tam) {
    buildMatchingMachine(arr, k, out, f, g); // Build machine with goto, failure and
        ↪ output functions
    int currentState = 0;
    for ( int i = 0; i < (int) text.size() ; ++i){
        currentState = findNextState(currentState, text[i], out, f, g) ;
        /*if (out[currentState] == 0){ // If match not found, move to next state,
            ↪ uncomment if number of keys is less of 64
                continue;
        }*/
        for (pair<int, bool> par: out[currentState]){ // Match found, print all
            ↪ matching words of arr[]
                ocor[i-tam[par.fi]+1].pb(par.fi);
        }
    }
}

void solve(){
    cin>>text;
    n = (int) text.size();
    vv ocor(n); //To store the index where each key starts in texts
    cin>>k;
    string arr[k]; //Stores every key
    vi tam(k); //Stores every key size
    for (int j = 0; j < k; j++){
        cin>>arr[j];
        tam[j] = arr[j].size();
        maxs += tam[j];
    }
    vector<map<int, bool>> out(maxs); // Stores the word number for each state (letter
        ↪ in text)
    //vi out(maxs, 0); // Bit i in this mask is one if the word with index i in that
        ↪ state. To use if there are less than 64 keys
    vi f (maxs, -1); // FAILURE FUNCTION IS IMPLEMENTED USING f[]
    vv g (maxs, vi(maxc, -1)); // GOTO FUNCTION (OR TRIE) IS IMPLEMENTED USING g[][]
    searchWords(arr, k, text, out, f, g, ocor, tam); // Each state (char in text) has
        ↪ the key numbers of the keys that start in that state in ocor
    return;
}
```

Word Combination (Aho-Corasick Example)

```cpp
void solve(){
    cin>>text;
    n = (int) text.size();
    vv ocor(n); //To store the index where each key starts in texts
    cin>>k;
    string arr[k]; //Stores every key
    vi tam(k); //Stores every key size
    for (int j = 0; j < k; j++){
        cin>>arr[j];
        tam[j] = arr[j].size();
        maxs += tam[j];
    }
    vector<map<int, bool>> out(maxs); // Stores the word number for each state (letter
        ↪ in text)
    //vi out(maxs, 0); // Bit i in this mask is one if the word with index i in that
        ↪ state. To use if there are less than 64 keys
    vi f (maxs, -1); // FAILURE FUNCTION IS IMPLEMENTED USING f[]
    vv g (maxs, vi(maxc, -1)); // GOTO FUNCTION (OR TRIE) IS IMPLEMENTED USING g[][]
    searchWords(arr, k, text, out, f, g, ocor, tam); // Each state (char in text) has
        ↪ the key numbers of the keys that start in that state in ocor
    return;
}
```

Edit Distance

```cpp
int EditDistance(string a, string b, int tamA, int tamB){
    vv bu(tamA + 1, vi(tamB + 1, 0));
    for (int i = 0; i <= tamA; i++){
        bu[i][0] = i;
    }
    for (int i = 0; i <= tamB; i++){
        bu[0][i] = i;
    }
    for (int i = 1; i <= tamA; i++){
        for (int j = 1; j <= tamB; j++){
            if (a[i-1] == b[j-1]) bu[i][j] = min(min(bu[i-1][j-1], bu[i-1][j] +
                ↪ 1), bu[i][j-1] + 1);
            else bu[i][j] = min(min(bu[i-1][j] + 1, bu[i][j-1] + 1), bu[i-1][j
                ↪ -1] + 1);
        }
    }
    return bu[tamA][tamB];
}
```

KMP

```cpp
string T, P; // T = text, P = pattern
int n, m; // n = |T|, m = |P|

void kmpPreprocess(vi &b) { // call this first
    int i = 0, j = -1; b[0] = -1; // starting values
    while (i < m) { // pre-process P
    while ((j >= 0) && (P[i] != P[j])) j = b[j]; // different, reset j
        ++i; ++j; // same, advance both
        b[i] = j;
```

```
        }
}

void kmpSearch(vi &b) { // similar as above
        int i = 0, j = 0; // starting values
        while (i < n) { // search through T
        while ((j >= 0) && (T[i] != P[j])) j = b[j]; // if different, reset j
                ++i; ++j; // if same, advance both
                if (j == m) { // a match is found
                        printf("P is found at index %d in T\n", i-j);
                        j = b[j]; // prepare j for the next
                }
        }
}

void solve(){
        cin>>T;
        cin>>P;
        n = (int) T.size();
        m = (int) P.size();
        vi b(m+1); // b = back table
        kmpPreprocess(b);
        kmpSearch(b);
}
```

String Matching (KMP Example)

```
void solve(){
    cin>>T;
    cin>>P;
    n = (int) T.size();
    m = (int) P.size();
    vi b(m+1); // b = back table
    kmpPreprocess(b);
    kmpSearch(b);
}
```

Longest Common Subsequence

```
int LCS(string a, string b, int tamA, int tamB){
        vv bu(tamA + 1, vi(tamB + 1, 0));
        for (int i = 1; i <= tamA; i++){
                for (int j = 1; j <= tamB; j++){
                        if (a[i-1] == b[j-1]) bu[i][j] = bu[i-1][j-1] + 1;
                        else bu[i][j] = max(bu[i-1][j], bu[i][j-1]);
                }
        }
        return bu[tamA][tamB];
```

```
}
```

— MISCELLANEOUS —

Binary Search

```
bool F(ll target){
    return true or false;
}

ll bestXforF (){
    ll leftBound = 0, rightBound = 1, mid;

    while(F(rightBound) == false)
        rightBound *= 2;

    while(rightBound > leftBound + 1){
        mid = leftBound + (rightBound - leftBound)/2;
        if(F(mid) == true)
            rightBound = mid;
        else
            leftBound = mid;
    }

    return leftBound;
}
```

Permutations

```
//l = 0, r = n-1
void permute(vector<int> &a, int l, int r){
        if (l >= r){
                //verificar permutacao, guarda-la leva a MLE
                verifica();
        }
        else{
                //Fazer todas as permutacoes
                for (int i = l; i <= r; i++){
                        swap(a[l], a[i]);
                        permute(a, l+1, r);
                        swap(a[l], a[i]);
                }
        }
}
```