

Task 1:

$$H(e^{j\omega}) = 1 + e^{-2j\omega} = e^{-j\omega} (e^{j\omega} + e^{-j\omega}) = e^{-j\omega} (2\cos(\omega))$$

So, the phase response is $-\omega$

The Group delay : $T(\omega) = -\frac{d\theta(\omega)}{d\omega} = -(-1) = 1$

Task 2: (a) $f_p = \frac{4000}{16000} = \frac{1}{4}$ $f_s = \frac{5000}{16000} = \frac{5}{16}$

$$\Delta f = \frac{5}{16} - \frac{1}{4} = \frac{1}{16}$$

So Normalized pass frequency is $\frac{1}{4}$, stop is $\frac{5}{16}$

the width of transition band is $\frac{1}{16}$

(b) i : as formula. $\Delta f = \frac{0.9}{N}$

$$\therefore N = \frac{0.9}{\Delta f} = \frac{0.9}{\frac{1}{16}} = 15$$

ii : $N = \frac{3.1}{\frac{1}{16}} = 51$

iii : $N = \frac{3.3}{\frac{1}{16}} = 53$

iv : $N = \frac{5.5}{\frac{1}{16}} = 89$

Task 3: $f_1 = \frac{12}{32} = \frac{3}{8}$ $f_2 = \frac{13.5}{32} = \frac{27}{64}$

$$\Delta f = \frac{27}{64} - \frac{24}{64} = \frac{3}{64}$$

$$f_c = \frac{f_1 + f_2}{2} = \frac{51}{128}$$

$$h(n) = \begin{cases} 2f_c \operatorname{sinc}(n \cdot 2\pi f_c) & n \neq 0 \\ 2f_c & n = 0 \end{cases}$$

$$= \begin{cases} \frac{51}{64} \operatorname{sinc}\left(\frac{51\pi}{64} \cdot n\right) & n \neq 0 \\ \frac{51}{64} & n = 0 \end{cases}$$

For Hamming: $N = \frac{3.3}{\Delta f} = 71$

$$w(n) = \begin{cases} 0.54 + 0.46 \cos\left(\frac{2\pi \cdot n}{71}\right) & |n| \leq \frac{N-1}{2} = 35 \\ 0 & \text{otherwise.} \end{cases}$$

$$h_t(n) = w(n)h(n)$$

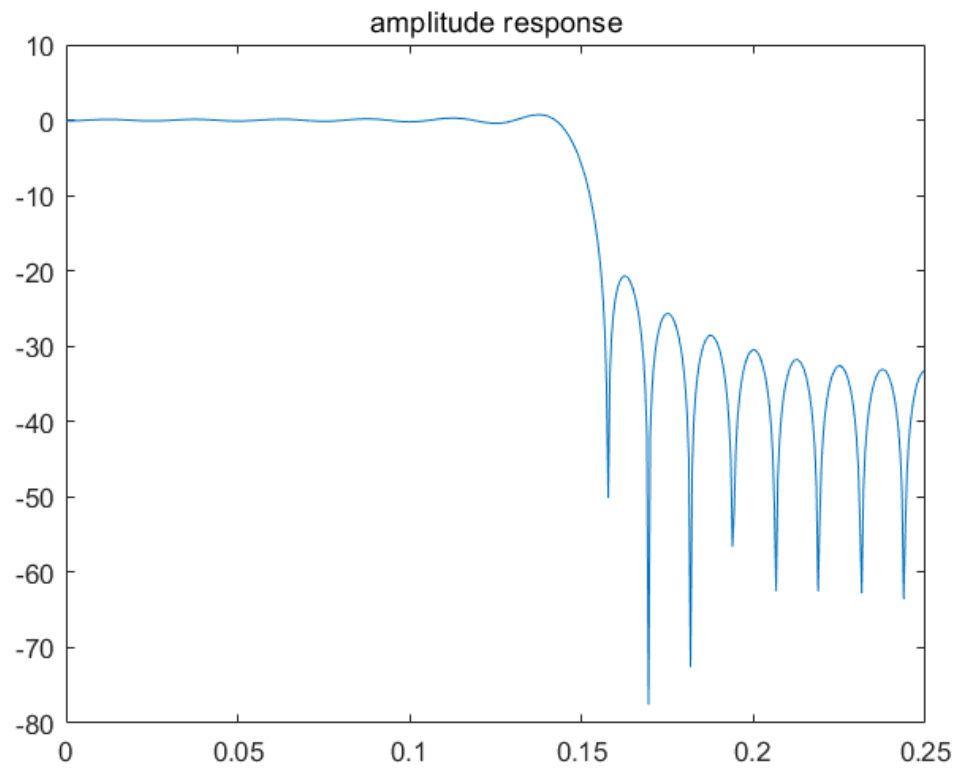
$$= \begin{cases} \frac{51}{64} \times (0.54 + 0.46 \cos(\frac{2\pi \cdot n}{71})) \times \operatorname{sinc}\left(\frac{51\pi}{64} \cdot n\right); & 0 \leq n \leq 35 \\ \frac{51}{64}; & n = 0 \\ 0; & \text{otherwise.} \end{cases}$$

For Blackman: $N = \frac{5.5}{\Delta f} = 119$

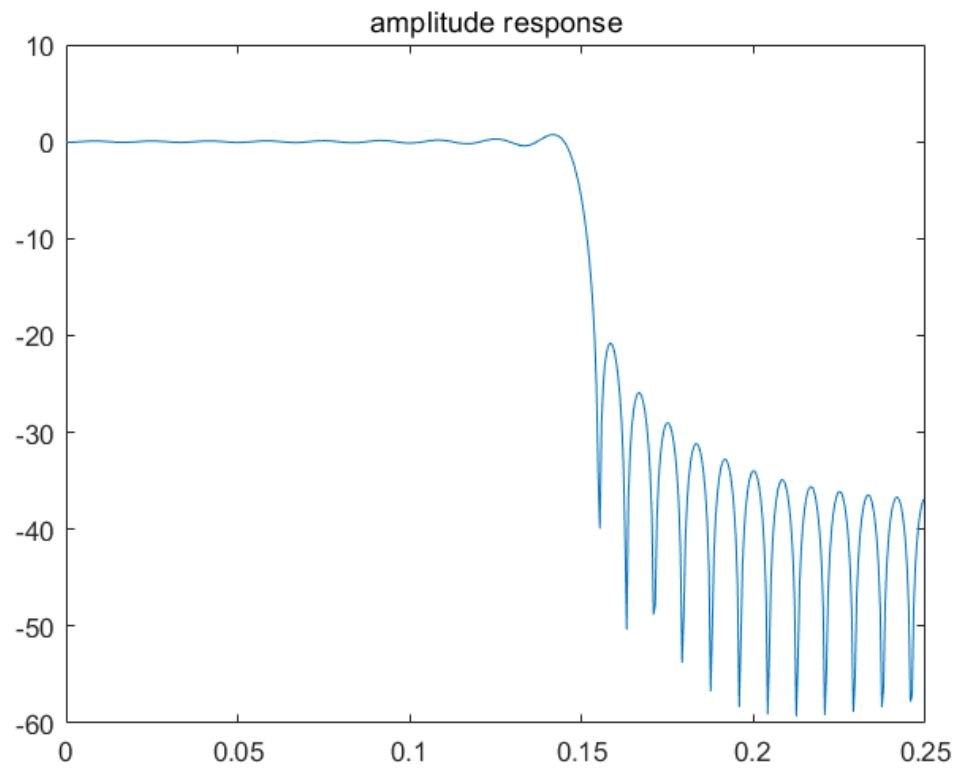
$$w(n) = \begin{cases} 0.42 + 0.5 \cos\left(\frac{2\pi n}{119}\right) + 0.08 \cos\left(\frac{4\pi n}{119}\right); & |n| \leq 59 \\ 0; & \text{otherwise.} \end{cases}$$

$$h_t = w(n)h(n) = \begin{cases} \frac{51}{64} \times (0.42 + 0.5 \cos(\frac{2\pi n}{119}) + 0.08 \cos(\frac{4\pi n}{119})) \times \operatorname{sinc}\left(\frac{51}{64} \cdot \pi \cdot n\right); & 0 \leq n \leq 59 \\ \frac{51}{64}; & n = 0 \\ 0; & \text{otherwise} \end{cases}$$

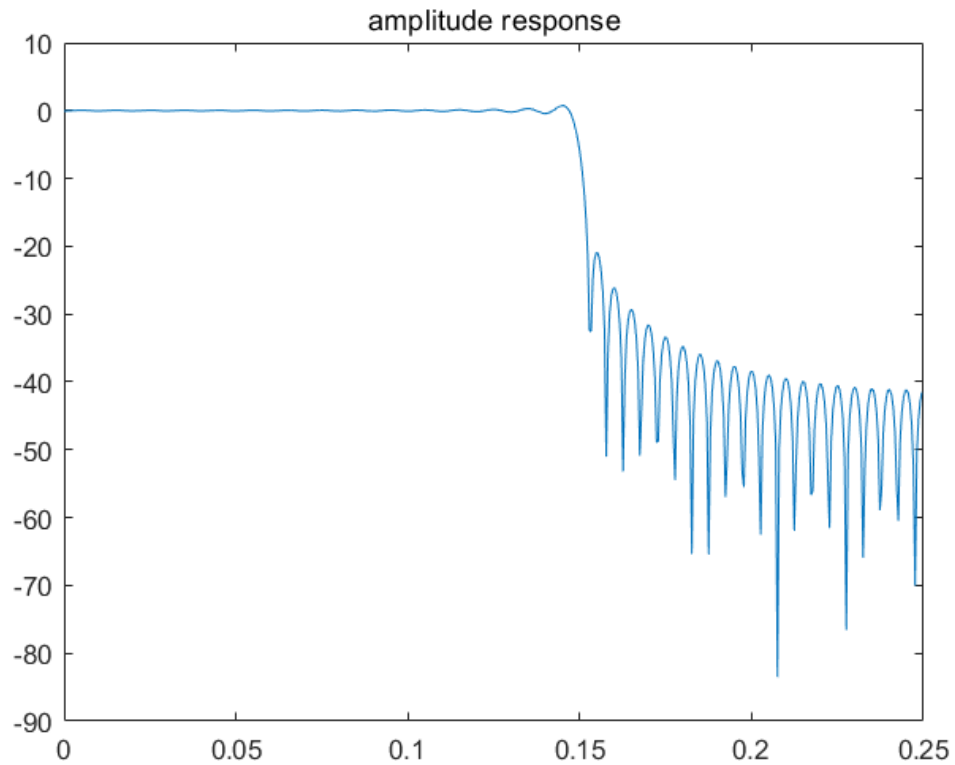
task4



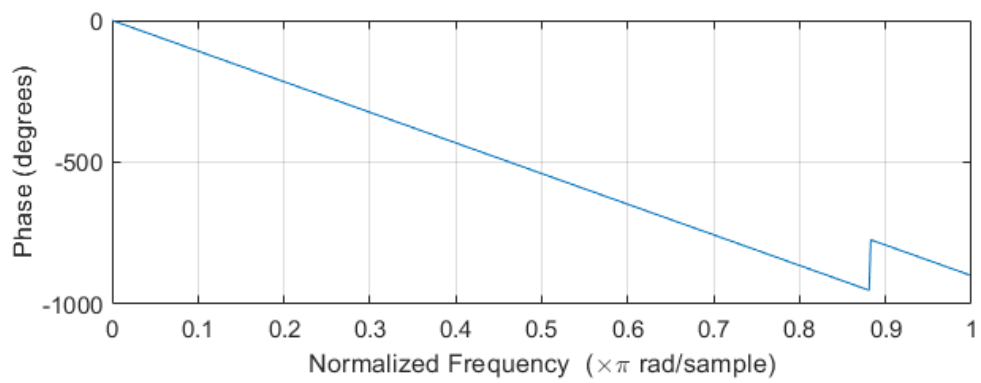
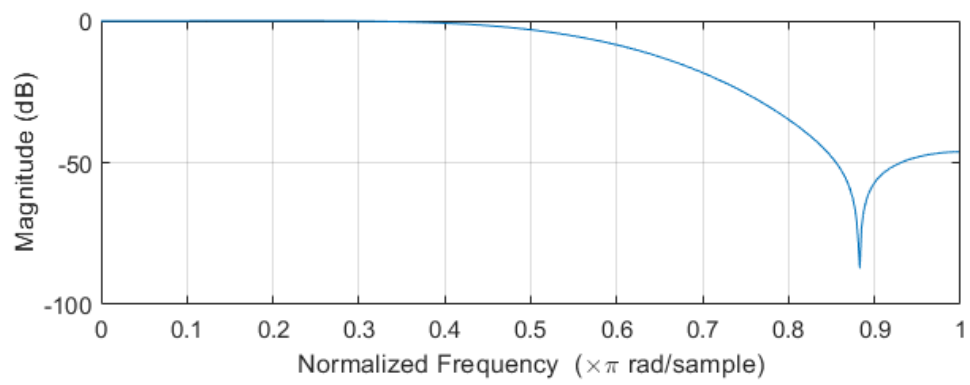
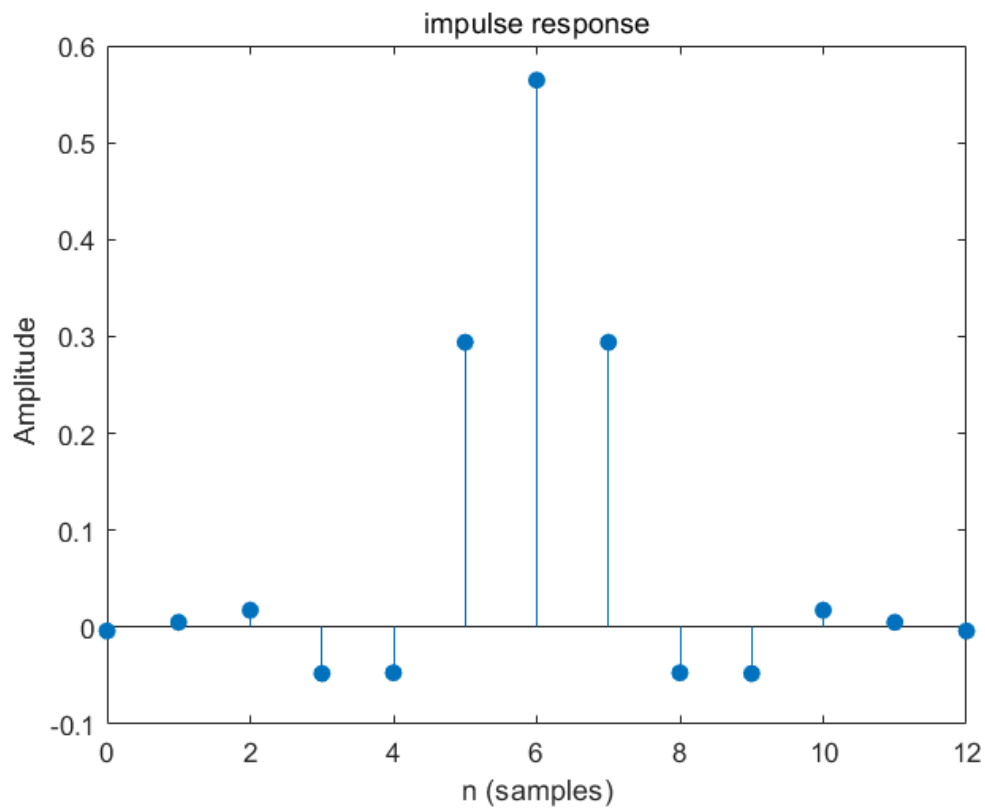
a) The attenuation of the first (the leftmost) oscillatory peak in the stopband is -20

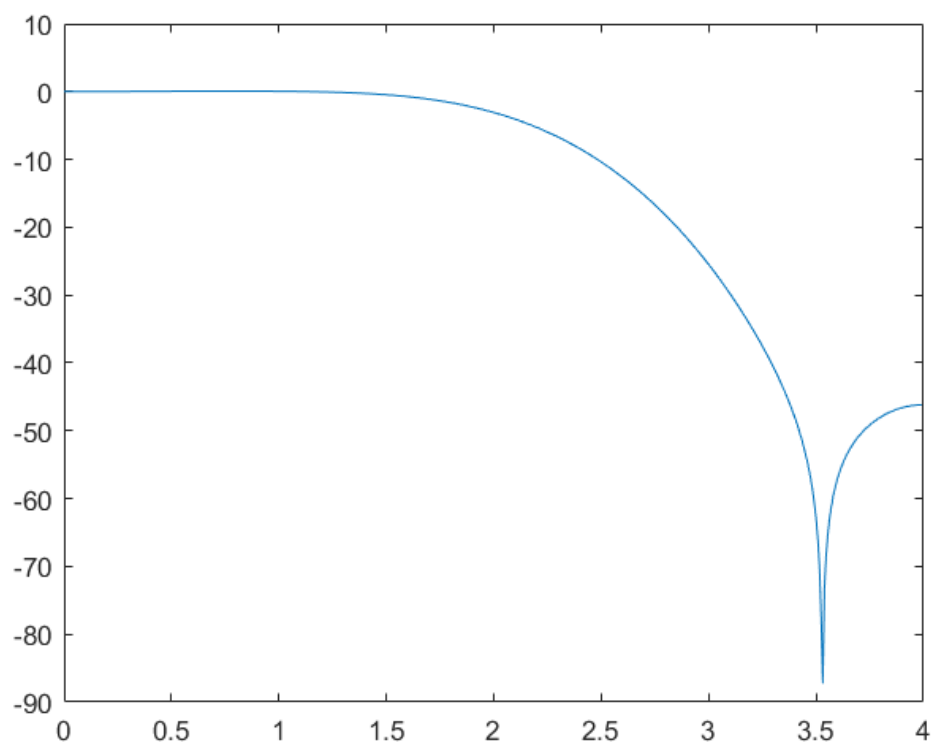


b) The first peak value is still -20, but it gets a little bit earlier on the x-axis

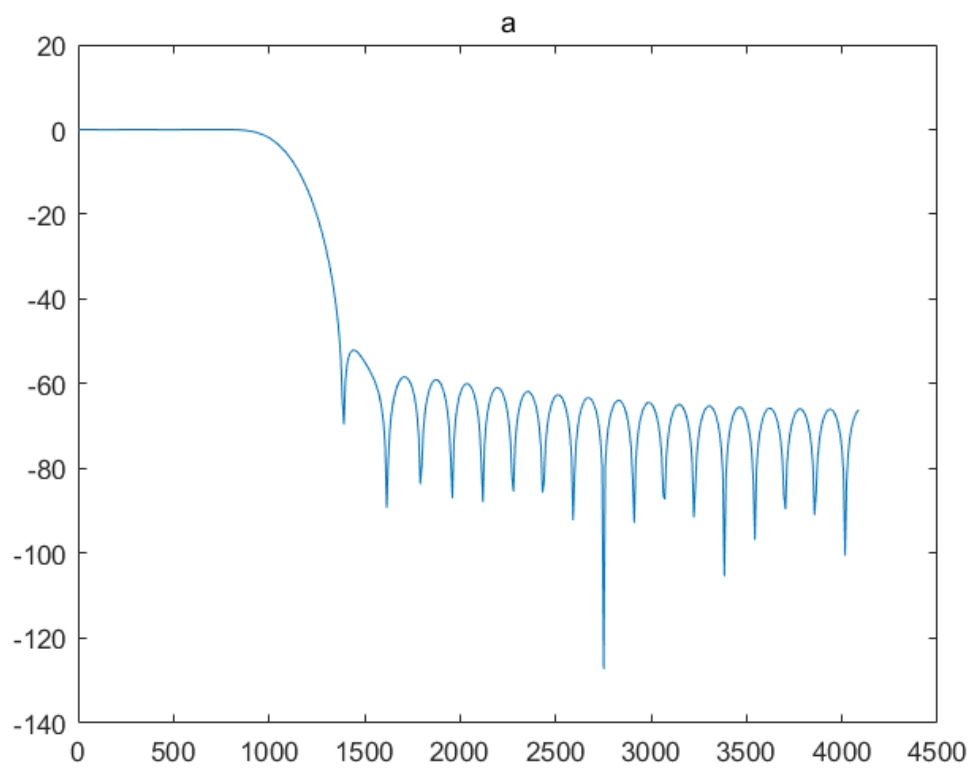


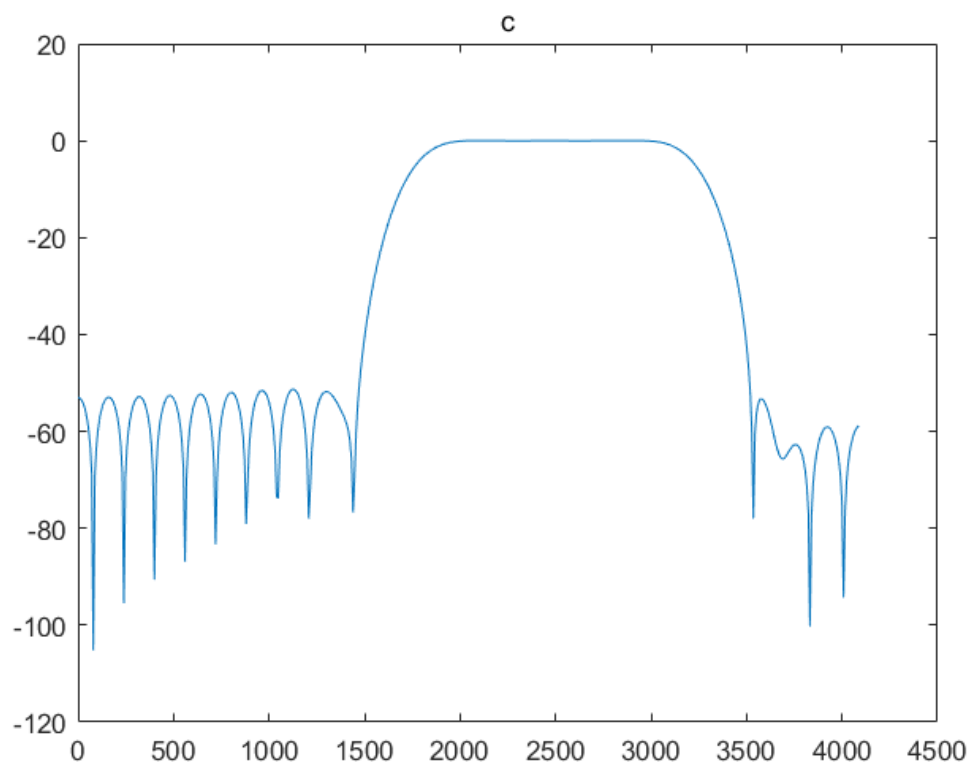
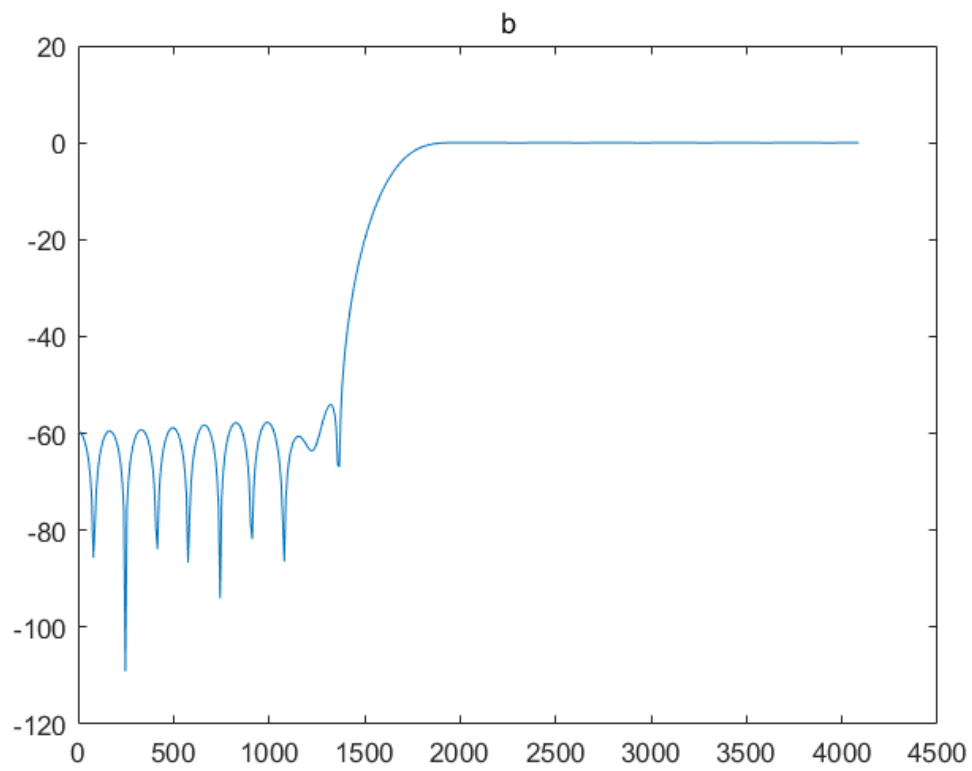
c) The first peak value is still -20, but it gets a little bit earlier on the x-axis. Change N cannot change the stopband attenuation
task5

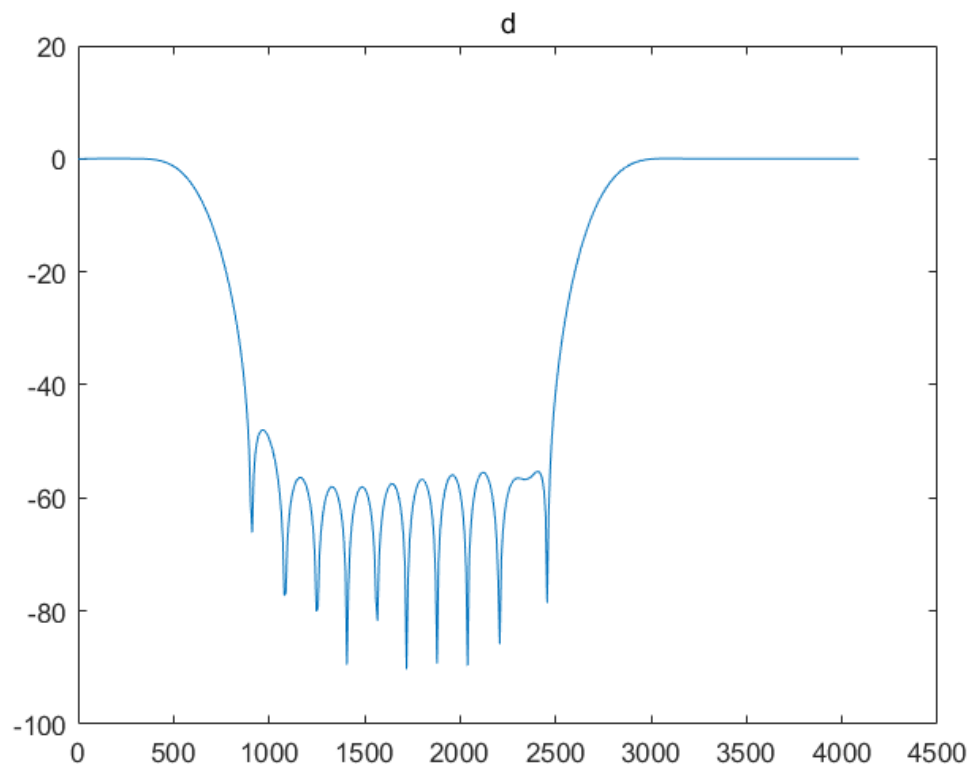




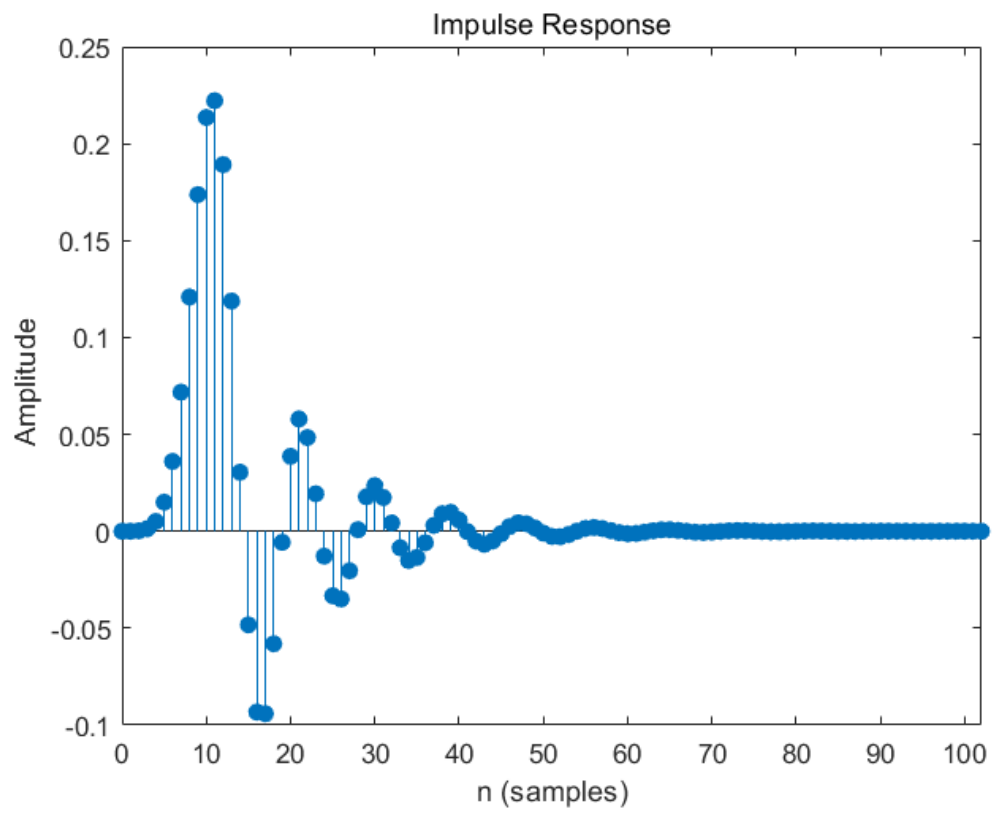
task6

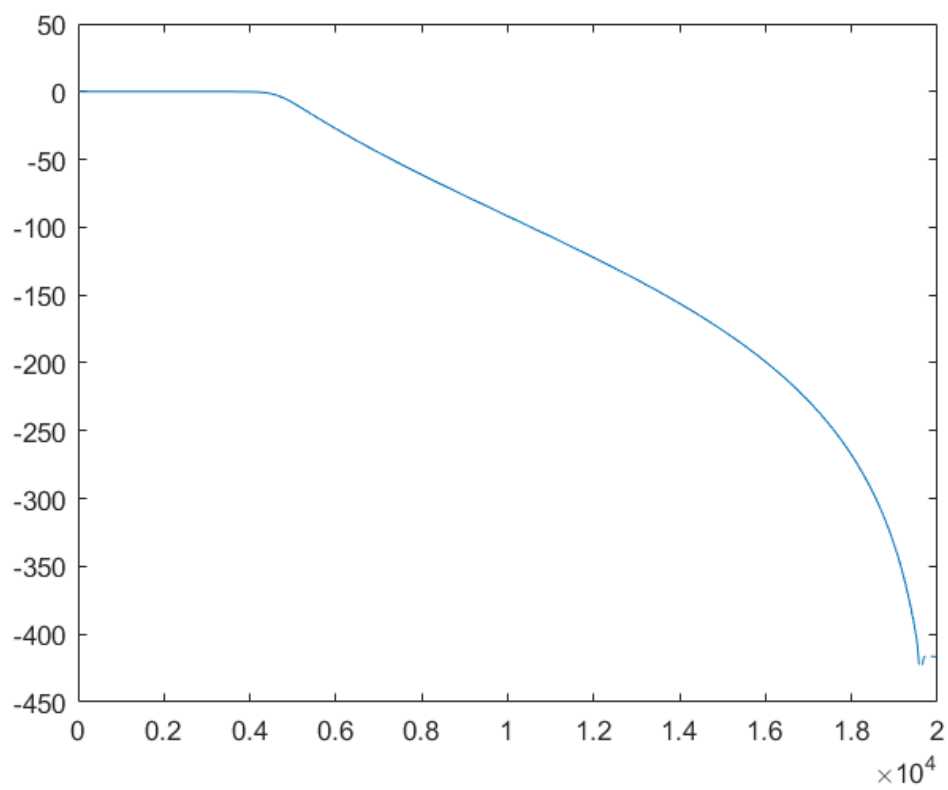






task7





-1

-1

-1

-1

-1

-1

-1

-1

-1

-1

-1

0.6800 + 0.6034i

0.6800 - 0.6034i

0.5829 + 0.4754i

0.5829 - 0.4754i

0.5181 + 0.3510i

0.5181 - 0.3510i

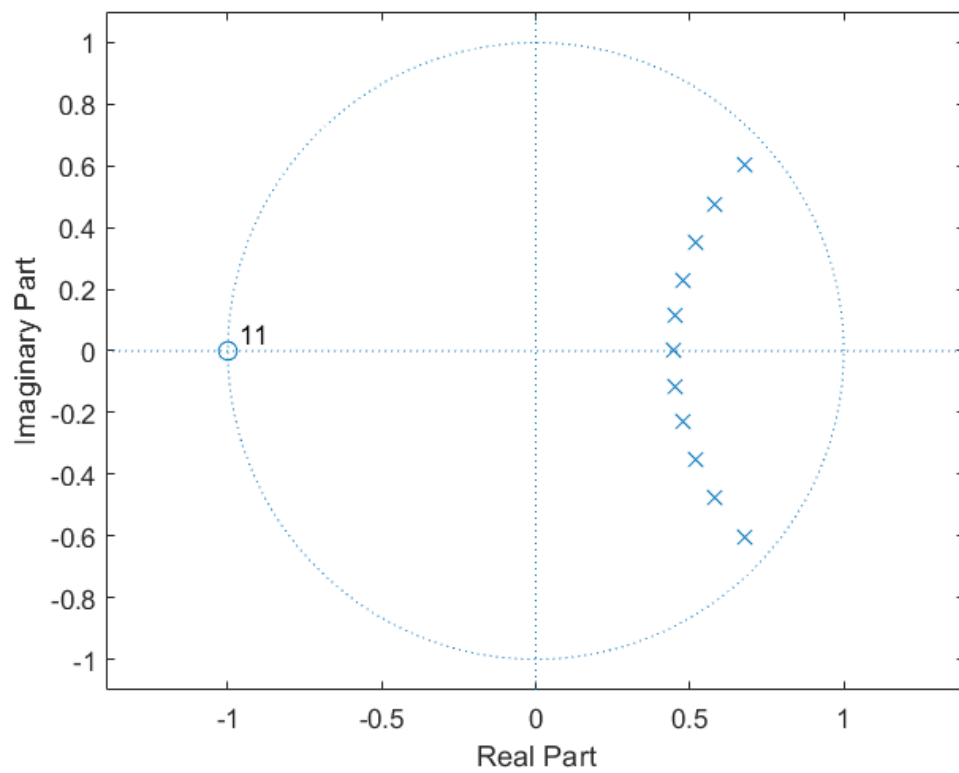
0.4768 + 0.2311i

0.4768 - 0.2311i

0.4539 + 0.1146i

0.4539 - 0.1146i

0.4465 + 0.0000i



task8 & task9, see the code in design_low_pass.m

task10

$N = 1 \times 4$

$10^{-4} \times$

0.1903	0.5708	0.5708	0.1903
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$D = 1 \times 4$

1.0000	-2.8913	2.7884	-0.8970
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