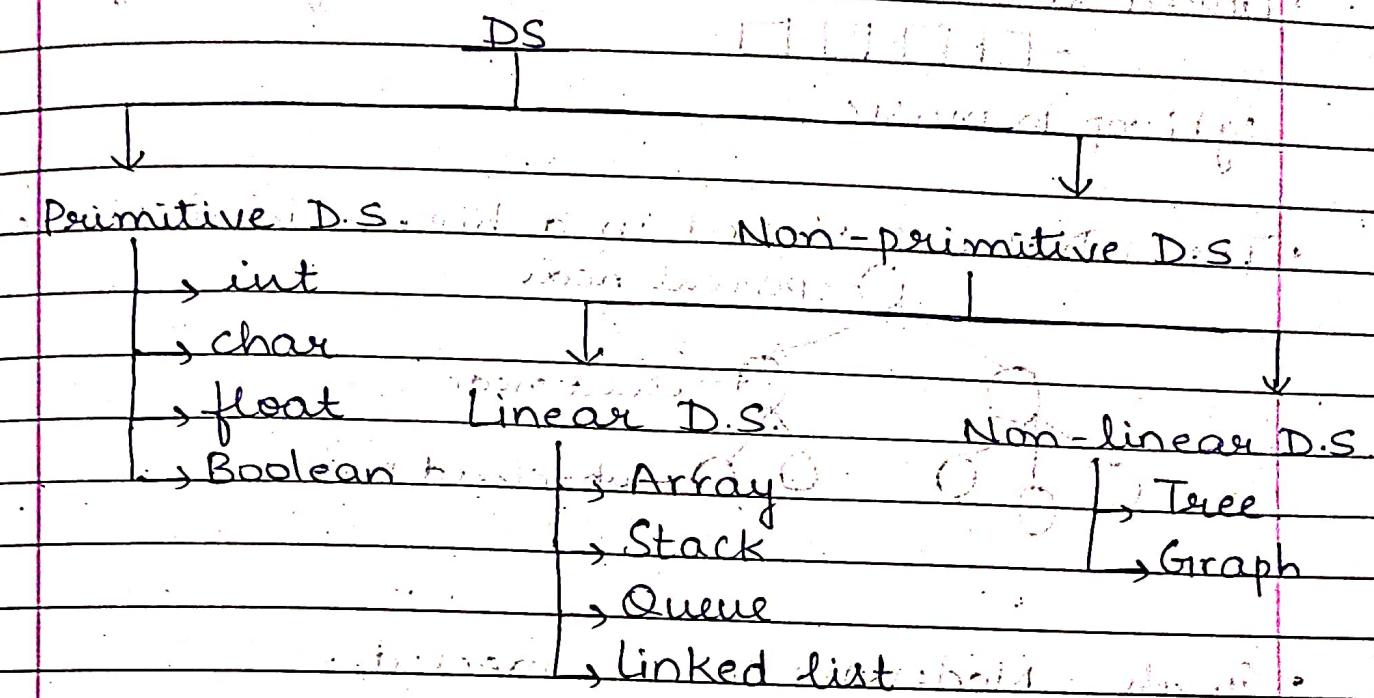


DATA STRUCTURES

- Data is the collection of raw facts and figures.
- Information is processed meaningful data.
- We organize data to reduce processing time and increase speed.
- Data structures are a set of algorithms written in a programming language which allow us to organize our data in an efficient manner in the main memory or primary memory.



• Linear D.S - A way of structuring or organizing the data in a linear form.

• Non-linear D.S - No particular order is followed while organizing the data.

• Operations on D.S. -

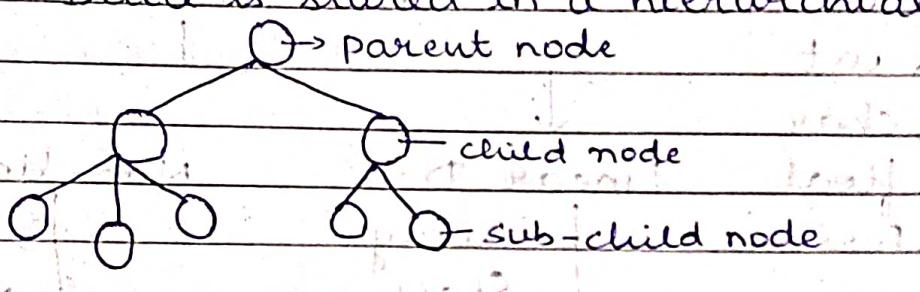
1. Insertion

2. Deletion

3. Update

4. Merge

5. Sort

- Stack : Stack follows LIFO
Last In First Out
eg) Stack of books, undo, back button on websites.
- Queue : Queue follows FIFO
First In First Out
eg) Any queue, playlist
- Linked list : Data is stored in the form of nodes.
-□-□-□-□-
- Tree : Data is stored in a hierarchical structure.


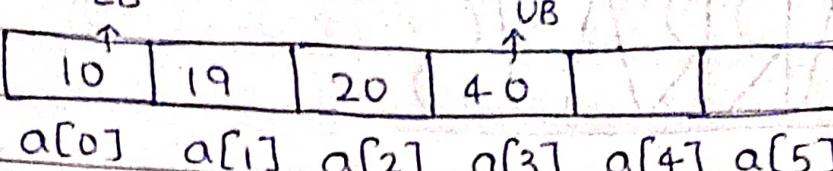
The diagram illustrates a tree structure with levels:
 - Root node**: The topmost circle.
 - Child node**: The two circles directly below the root.
 - Sub-child node**: The four circles directly below the child nodes.
 - Leaf node**: The bottom-most level of circles, resulting from the branching of the sub-child nodes.A small arrow points to the first child node with the label "parent node".
- Graph :- Nodes are interconnected.
eg) google maps.
- A program and an algorithm are step by step instructions to solve a problem. Program uses syntax, while algorithm is written in english.

ARRAYS

- An array is a linear data structure.
- It is a collection of similar types of data types stored in contiguous memory location.
- Index from 0 to $m-1$ where m is a number.
- Operations performed on an array are:
 1. Traversing
 2. Insertion
 - At beginning
 - At end
 - At specific location.
 3. Deletion
 4. Sorting
 5. Searching
 - Linear search
 - Binary search
 6. Merging

- ① **INSERTION**: When an element is inserted in an array, it is called insertion.
- When we want to insert an element in an array that is full, it is in overflow condition.
 - If overflow condition is false then we enter the element.

* INSERTION AT BEGINNING :



- LB : Lower bound (Index 0)
 - UB : Upper bound (Index $n-1$)
where, $n = \text{no. of elements}$
 - when $UB = m-1$, the array is full and in overflow condition. Here, m is max. Size of array
 - For insertion at beginning, the element will be entered at LB.

$$i = UB$$

```

while (i > LB) {
    a[i+1] = a[i]
    i--
}
    
```

} This clears the first position. IA ←

a[LB] = element

$$\underline{n = n + 1}$$

- ## Algorithm :-

Step 1: Start

Step 2: Let "a" be an array of max. size m containing 'n' elements.

Step 3: If $UB = m - 1$, then print overflow and exit.

Step 4: Read elements of array one by one

Step 5: If $i = \text{UB}$, then $(\text{UB} = n-1)$. Then i is found.

Step 6: Repeat Step 7 until condition while is true.

Step 7: $a[i+1] = a[i]$

Step 8: $a[LB] = \text{element}$

Step 9: $n = n + 1$

Step 10: Stop

* INSERTION AT END :-

• Algorithm -

Step 1 : Start

Step 2 : Let "a" be an array of max. size 'm', containing 'n' elements.

Step 3 : If $UB = m - 1$, then print overflow and exit

Step 4 : Read element.

Step 5 : $UB = UB + 1$ (where, $UB = n - 1$)

Step 6 : $a[UB] = \text{element}$.

Step 7 : $n = n + 1$

Step 8 : Stop.

* INSERTION AT SPECIFIC POSITION

• Algorithm :

Step 1 : Start

Step 2 : Let "a" be array of 'm' size and 'n' elements

Step 3 : If $UB = m - 1$, then print overflow and exit

Step 4 : Read element

Step 5 : Read position

Step 6 : $i = UB$

Step 7 : Repeat step 8 until condition, while

($i > \text{position}$) is true

Step 8: $a[i+1] = a[i]$

$i--$

Step 9: $a[position] = element$

Step 10: $n = n + 1$

Step 11: Stop

② TRAVERSING :-

• Algorithm -

Step 1 : Start

Step 2 : Let "a" be an array of max. size 'm' having 'n' elements.

Step 3 : $i = 0$

Step 4 : Repeat step 5 until the condition $(i \leq n)$ becomes false.

Step 5 : Process the element

$i++$

Step 6 : Stop.

③ DELETION :-

* DELETION AT END :

• Algorithm -

Step 1 : Start

Step 2 : Let "a" be an array of max. size 'n' having 'n' elements.

Step 3 : If $UB = 0 / \text{NULL}$, print underflow and

Step 4: $a[UB] = \text{NULL}$ (where, $UB = n-1$)

Step 5: $UB = UB - 1$

Step 6: Stop.

* DELETION AT BEGINNING : (ALGORITHM)

• Algorithm -

Step 1 : Start

Step 2 : Let "a" be an array of max. size 'm'
having 'n' elements

Step 3: If $UB = 0/\text{NULL}$, print underflow and exit

Step 4: $i = LB$

Step 5: Repeat step 6 until condition while
($i < UB$) is satisfied.

Step 6: $a[i] = a[i+1]$

$i = i + 1$

Step 7: $a[UB] = \text{NULL}$ (where, $UB = n-1$)

Step 8: $UB = UB - 1$

Step 9: Stop.

* DELETION AT SPECIFIC POSITION : (ALGORITHM)

• Algorithm -

Step 1 : Start

Step 2 : Let "a" be an array of max. size 'm'
having 'n' elements.

Step 3: If $UB = 0/\text{NULL}$, print underflow and exit

Step 4: Read position

Step 5: $i = LB$

Step 6: Repeat step 7 until condition while
($i \neq \text{position}$) becomes false.

Step 7: $i++$

Step 8: Repeat step 9 until condition while
($i < \text{UB}$) becomes false

Step 9: $a[i] = a[i+1]$

$i = i + 1$

Step 10: $a[\text{UB}] = \text{NULL}$

Step 11: $\text{UB} = \text{UB} - 1$

Step 12: Stop

④ SEARCHING

* LINEAR SEARCH

• Algorithm -

Step 1: Start

Step 2: Let "a" be an array of size n

Step 3: Read element to be searched

Step 4: Repeat $i = 0$

Step 5: Repeat step 6 while ($i < n$)

Step 6: if ($x == a[i]$)

 return success

else

 return failure

Step 7: Stop

* BINARY SEARCH :

- Algorithm = A binary search algorithm consists of following steps:

Step 1 : Start

Step 2 : Let "a" be an array of size n . (sorted)

Step 3 : Read element to be searched (x).

Step 4 : $L = 0, H = n - 1$

Step 5 : Repeat step 6 while ($L < H$)

Step 6 : $mid = \lfloor \frac{L+H}{2} \rfloor$

if $x = a[mid]$ then return success

return success

else

if $x > a[mid]$ then

$L = mid + 1$

else

$H = mid - 1$

Step 7 : If element is not found, return failure.

Step 8 : Stop.

* INSERTION ALGORITHM FOR END, SP & BEGINNING :

Step 1 : Insert (value, pos)

Step 2 : Set $I = UB + 1$

Step 3 : Repeat step 4 while ($I > pos$)

Step 4 : $A[I] = A[I + 1]$

$I = I - 1$

[End of loop]

Step 5 : $A[pos] = value$

Step 6 : $UB = UB + 1$

Step 7 : Stop.

* Calculating the Address of Array Elements:

Address of data element, $A[K] = BA(A) + w(k - \text{lower-bound})$

where,

k : index of element

BA : base address of array

w : size of one element in memory.

Q. Given an array,

`int marks = {99, 67, 78, 56, 88, 90, 34, 85};`

calculate the address of $\text{marks}[4]$ if the base address = 1000.

→ Address of data element,

$$A[K] = BA(A) + w(k - \text{lower-bound})$$

$$\text{marks}[4] = 1000 + 2(4 - 0)$$

$$= 1000 + 8$$

$$= 1008$$

* PROGRAM FOR OPERATIONS ON ARRAY :

```
#include <stdio.h>
#include <stdlib.h>
int insertion(int DATA[10], int n, int ITEM, int LOC);
int deletion(int DATA[10], int n, int ITEM, int LOC);
void selection(int DATA[10], int n, int ITEM, int LOC);
void display(int DATA[10], int n, int ITEM, int LOC);
void searching(int DATA[10], int n, int ITEM, int LOC);
int main()
{
    int DATA[10], n, ITEM, LOC, j;
    printf("Enter number of elements : ");
    scanf("%d", &n);
    printf("Enter elements of array : ");
    for (j=0, j<n; j++)
    {
        scanf("%d", &DATA[j]);
    }
    selection(DATA, n, ITEM, LOC);
    return 0;
}
void selection(int DATA[10], int n, int ITEM, int LOC)
{
    int CHOICE, p;
    printf("In Press 1 for insertion at beginning.\n");
    printf("Press 2 for insertion at end.\n");
    printf("In Press 3 for insertion at specific position.\n");
    printf("In Press 4 to display.\n");
    printf("In Press 5 for deletion at beginning.\n");
    printf("In Press 6 for deletion at end.\n");
    printf("In Press 7 for deletion at specific position.\n");
    printf("In Press 8 for");
}
```

```
searching element\nPress 0 to exit.");
scanf("%d", &CHOICE);
switch(CHOICE)
{
```

```
case 1: for (i=0; i<n; i++)
printf("Enter element to be inserted:");
scanf("%d", &ITEM);
LOC = 0;
n = insertion(DATA, n, ITEM, LOC);
display(DATA, n, ITEM, LOC);
Selection(DATA, n, ITEM, LOC);
break;
```

```
case 2: for (i=0; i<n; i++)
printf("Enter element to be inserted:");
scanf("%d", &ITEM);
LOC = n;
n = insertion(DATA, n, ITEM, LOC);
display(DATA, n, ITEM, LOC);
Selection(DATA, n, ITEM, LOC);
break;
```

case 3:

```
printf("Enter element to be inserted:");
scanf("%d", &ITEM);
printf("Enter location :");
scanf("%d", &p);
LOC = p - 1;
n = insertion(DATA, n, ITEM, LOC);
display(DATA, n, ITEM, LOC);
Selection(DATA, n, ITEM, LOC);
break;
```

Case 4: for selection for deletion

```
display (DATA, n, ITEM, LOC);
selection (DATA, n, ITEM, LOC);
break;
```

case 5:

```
LOC = 0;
n = deletion (DATA, n, ITEM, LOC);
display (DATA, n, ITEM, LOC);
selection (DATA, n, ITEM, LOC);
break;
```

case 6:

```
LOC = n - 1;
n = deletion (DATA, n, ITEM, LOC);
display (DATA, n, ITEM, LOC);
selection (DATA, n, ITEM, LOC);
break;
```

case 7:

```
printf ("Enter position of element to be
deleted:");
scanf ("%d", &p);
LOC = p - 1;
n = deletion (DATA, n, ITEM, LOC);
display (DATA, n, ITEM, LOC);
selection (DATA, n, ITEM, LOC);
break;
```

case 8:

```
Searching (DATA, n, ITEM, LOC);
selection (DATA, n, ITEM, LOC);
break;
```

case 0:

```
exit (0);
```

}

```
{  
int insertion(int DATA[10], int n, int ITEM, int LOC)  
{  
    int i = n - 1;  
    while (i >= LOC)  
    {  
        DATA[i + 1] = DATA[i];  
        i--;  
    }  
    DATA[LOC] = ITEM;  
    n = n + 1; selection(DATA, n, ITEM, LOC);  
    return n;  
}  
  
int deletion(int DATA[10], int n, int ITEM, int LOC)  
{  
    int i = LOC;  
    while (i < n - 1)  
    {  
        DATA[i] = DATA[i + 1];  
        i++;  
    }  
    DATA[n - 1] = NULL;  
    n = n - 1; selection(DATA, n, ITEM, LOC);  
    return n;  
}  
  
void display(int DATA[10], int n, int ITEM, int LOC)  
{  
    int j;  
    for (j = 0; j < n; j++)  
    {  
        printf("%d ", DATA[j]);  
    }  
}
```

```
    }  
selection (DATA, n, ITEM, LOC);  
}  
  
void searching (int DATA[10], int n, int ITEM, int LOC  
{  
    int i, k = 0; // k=0 means element not found  
    printf ("Enter element to be found:");  
    scanf ("%d", &ITEM);  
    for (i = 0; i < n; i++)  
    {  
        if (DATA[i] == ITEM)  
        {  
            K = 1; // k=1 means element found  
            LOC = i; // LOC is index of element found  
        }  
    }  
    if (K == 1)  
        printf ("Element found.");  
    else  
        printf ("Element not found.");  
    selection (DATA, n, ITEM, LOC);  
}
```

STACKS

- A stack is a linear data structure.
- It is called a LIFO (Last In First Out) data structure, as the element that was inserted last is the first one to come out.
- Stacks can be implemented using either arrays or linked lists.

* OPERATIONS ON A STACK :-

- 1) Push (Insertion at top)
- 2) Pop (Deletion at top)
- 3) Peep (View element at top)

- Push :- To insert we check overflow.
If $\text{top} = n - 1$, the stack is in overflow.
If overflow condition is false,
we increment top and then enter element.
- Pop :- To delete we check underflow.
If $\text{top} = -1$, the stack is underflow.
If underflow condition is false,
we delete element at top and then decrement top.

a[4]		
a[3]		
a[2]	→	Top when stack has two elements.
a[1]	→	Top when stack has one element.
a[0]	→	Top when stack is empty.

- Algorithm for Push (Insertion):

Step 1: Start

Step 2: Let "a" be a stack of 'n' elements.

Step 3: If $TOP = n - 1$, print overflow and exit

Step 4: Read element to be inserted

Step 5: $TOP = TOP + 1$

Step 6: Insert element at top.

stack [TOP] = element

Step 7: Stop

- Algorithm for Pop (Deletion):

Step 1: Start

Step 2: Let "a" be a stack of 'n' elements.

Step 3: If $TOP = -1$, print underflow and exit

Step 4: Delete element at TOP

stack [TOP] = NULL

Step 5: $TOP = TOP - 1$

Step 6: Stop.

- Algorithm for Peep:

Step 1: Start

Step 2: Let "a" be a stack of 'n' elements

Step 3: If $TOP = -1$, print underflow and exit

Step 4: Print element with index TOP

Step 5: Stop

* EVALUATION OF ARITHMETIC EXPRESSIONS

1. Infix : $a+b$: Operator is between operands
2. Prefix : $+ab$: Operator is before operands
3. Postfix : $ab+$: Operator is after operands.

⇒ Conversion of infix to postfix

$$1. (a+b)*c$$

$$ab+ * c$$

$$ab+c *$$

$$2. (A+B)/(C+C)-D*E$$

$$AB+ / (C+D) - (D*E)$$

$$AB+ / (CD+ - DE*)$$

$$AB+ / CD+ - DE*$$

$$AB+ CD+ / - DE*$$

$$AB+ CD+ / DE* -$$

$$3. A+B-C*D*E \wedge F \wedge G$$

$$A+B-C*D*E \wedge FG \wedge$$

$$A+B-C*D* EFG \wedge \wedge$$

$$A+B-C*D* EFG \wedge \wedge \wedge$$

$$A+B-C*D* EFG \wedge \wedge \wedge *$$

$$AB+ - CD* EFG \wedge \wedge \wedge *$$

$$AB+ CD* EFG \wedge \wedge \wedge * -$$

$$4. a+b*(c \wedge d - e) \wedge (f+g*h) - i$$

$$a+b*(cd \wedge - e) \wedge (f+g*h) - i$$

$$a+b*(cd \wedge e -) \wedge (f+g*h) - i$$

$$a+b* cd \wedge e - \wedge (f+gh*) - i$$

$$a + b * cd \wedge e - \wedge fgh * + - i$$

$$a + b * cd \wedge e - fgh * + \wedge - i$$

$$a + bcd \wedge e - fgh * + \wedge * - i$$

$$abcd \wedge e - fgh * + \wedge * + - i$$

$$abcd \wedge e - fgh * + \wedge * + - i$$

5. $a + b + (c \wedge d) * e / f / g * h + i$

$$a + b + cd \wedge e * e / f / g * h + i$$

$$a + b + cd \wedge e * ef / f / g * h + i$$

$$a + b + cds * ef / g / * h + i$$

$$a + b + cd \wedge ef / g / * h + i$$

$$a + b + cd \wedge ef / g / * h * + i$$

$$ab + cd \wedge ef / g / * h * + i$$

$$ab + cd \wedge ef / g / * h * + i$$

$$ab + cd \wedge ef / g / * h * + i$$

6. $A - C B / c + (D \cdot (E * F) / G) * H$

$$A - (B / c + (D \cdot EF * / G) * H)$$

$$A - (B / c + (DEF * \cdot / G) * H)$$

$$A - (B / c + (DEF * \cdot G /) * H)$$

$$A - (BC / + DEF * \cdot G / * H)$$

$$A - (BC / + DEF * \cdot G / H *)$$

$$A - BC / DEF * \cdot G / H * +$$

$$ABC / DEF * \cdot G / H * + -$$

⇒ Conversion from infix to prefix:

$$1. (A + B) * C$$

$$+AB * C$$

$$* +ABC$$

$$2. (A + B) / (C + D) - (D * E)$$

$$+AB / (C + D) - (D * E)$$

$$+AB / +CD - (D * E)$$

$$+AB / +CD - *DE$$

$$/ +AB + CD - *DE$$

$$- / +AB + CD * DE$$

$$3. A + B - C * D * E \wedge F \wedge G$$

$$A + B - C * D * E \wedge F \wedge G$$

$$A + B - C * D * \wedge F \wedge G$$

$$A + B - * CD * \wedge E \wedge F \wedge G$$

$$A + B - * * CD \wedge E \wedge F \wedge G$$

$$+ TAB - * * CD \wedge E \wedge F \wedge G$$

$$- + TAB * * CD \wedge E \wedge F \wedge G$$

$$4. 3. a + b * (c \wedge d - e) \wedge (f + g * h) - i$$

$$a + b * (\wedge cd - e) \wedge (f + g * h) - i$$

$$a + b * (- \wedge cde) \wedge (f + g * h) - i$$

$$a + b * - \wedge cde \wedge (f + * gh) - i$$

$$a + b * - \wedge cde \wedge + f * gh - i$$

$$a + * b \wedge - \wedge cde + f * gh - i$$

$$+ a * b \wedge - \wedge cde + f * gh - i$$

$$- + a * b \wedge - \wedge cde + f * ghi$$

$$5. a+b+(c \wedge d) * e/f/g * h+i$$

$$a+b+(c \wedge d) * e/f/g * h+i$$

$$a+b \wedge c d * e/f/g * h+i$$

$$a+b \wedge c d * /e/f/g * h+i$$

$$a+b * \wedge c d // e/f/g * h+i$$

$$a+b * * \wedge c d // e/f/g * h+i$$

$$+ab * * \wedge c d // e/f/g * h+i$$

$$++ab * * \wedge c d // e/f/g * h+i$$

$$+++ab * * \wedge c d // e/f/g * h+i$$

$$6. A-(B/c + (D \cdot (E * F) / G) * H)$$

$$A - (B/c + (D \cdot (E * F) / G) * H)$$

$$A - (B/c + (\cdot D * E F / G) * H)$$

$$A - (B/c + / \cdot D * E F G / H) * H$$

$$A - (B/c + / \cdot D * E F G / H) * H$$

$$A - (B/c + * / \cdot D * E F G / H) * H$$

$$A - +/B C * / \cdot D * E F G H * H$$

$$-A + /B C * / \cdot D * E F G H * H$$

\Rightarrow While doing this conversion or conversion using stack, always draw a priority chart with associativity.

11/05/22

* INFIX TO POSTFIX USING STACK

① Algorithm :-

- Step 1 : If stack is empty or it contains the left parenthesis on top; push the incoming operator on stack.
- Step 2 : If the incoming symbol is opening parenthesis C, push it into the stack.
- Step 3 : If the incoming symbol is closing parenthesis P, pop the stack and print the operator until the opening parenthesis C is found.
- Step 4 : If the incoming symbol has higher precedence than top of the stack then push it in stack.
- Step 5 : If the incoming symbol has lower precedence than top of the stack then print the top.
- Step 6 : If the incoming symbol has equal precedence with top of the stack, use the associativity rule.
- Step 7 : If you come to the end of the expression, pop and print all the operators of the stack.

Q. $a+b*(c\wedge d - e) \wedge (f+g*h) - i$

→

Scanned Element

Stack

Postfix Expression

a	a	a
+	+	a
b	+ b	ab
*	+ *	ab
c	+ * (ab
c	+ * (abc
\wedge	+ * (\wedge	abc
d	+ * (\wedge	abcd
-	+ * (-	abcd \wedge
e	+ * (-	abcd \wedge e
)	+ *	abcd \wedge e -
\wedge	+ * \wedge	abcd \wedge e -
(+ * \wedge (abcd \wedge e -
f	+ * \wedge (abcd \wedge e - f
+	+ \wedge +	abcd \wedge e - f
g	+ * \wedge (+	abcd \wedge e - fg
*	+ * \wedge (+ *	abcd \wedge e - fg
h	+ * \wedge (+ *	abcd \wedge e - fg h
i	+ * \wedge	abcd \wedge e - fg h * +
-	-	abcd \wedge e - fg h * + \wedge * +
i	-	abcd \wedge e - fg h * + \wedge * + i

Ans: abcd \wedge e - fg h * + \wedge * + i -

$$Q. A + (B * C) - (D / E \wedge F) + G) * H$$

Scanned Element

Postfix Expression

A		A
+	+B	A +
C	+C	AB
*	+(*	AB*
C	+(*C	ABC
-	+(-	ABC*
D	+(-D	ABC*D
/	+(-/	ABC*D
E	+(-/E	ABC*DE
\wedge	+(-/\wedge	ABC*DE
F	+(-/\wedge F	ABC*DEF
)	+(-/()	ABC*DEF\wedge
+	+(+	ABC*DEF\wedge
G	+(+G	ABC*DEF\wedge -G
)	+(+)	ABC*DEF\wedge -G+
*	+(*	ABC*DEF\wedge -G+
H	+(*H	ABC*DEF\wedge -G+H
+	+(*H)	ABC*DEF\wedge -G+H*+

Ans: ABC*DEF\wedge|-G+H*+

Q. $a+b+c \wedge d) * e / f / g * h + i$

Scanned element

a
+
b
+
c
+
^
d
)
*
e
/
f
/
g
*
h
+

Stack

Postfix Expression

a
ab
ab+
ab+c
ab+c
ab+cd
ab+cd^
ab+cd^
ab+cd^e
ab+cd^e
ab+cd^ef
ab+cd^ef/
ab+cd^ef/g
ab+cd^ef/g/*
ab+cd^ef/g/*h
ab+cd^ef/g/*h*i
ab+cd^ef/g/*h*i+

Ans : ab+cd^ef/g/*h*i+

Q. $A + B - C * D * E \wedge F \wedge G$

Scanned Element

Postfix Expression

A	
+	+
B	+
-	-
C	-
*	-*
D	-*
*	-*
E	-*
\wedge	-*
F	-*
\wedge	-*
G	-*

A	
A	
AB	
AB+	
AB+C	
AB+C	
AB+CD	
AB+CD*	
AB+CD*E	
AB+CD*E	
AB+CD*EF	
AB+CD*EFA	
AB+CD*EFAG	
AB+CD*EFAG\wedge-	

Ans : AB+CD*EFAG\wedge*-

$$Q. a+b*(c\wedge d - e) \wedge (f+g*h) - i$$

\rightarrow

Scanned
element

Stack

Postfix Expression

a		a
+	+	a
b	+	ab
*	+	ab
(+(ab
c	+(abc
\wedge	+*(\wedge	abc
d	+*(\wedge	abcd
-	+*(-	abcdn
e	+*(-	abcdne
)	+	abcdne-
\wedge	+*\wedge	abcdne-\wedge
(+*\wedge(abcdne-\wedge
f	+*\wedge(abcdne-\wedge f
+	+*\wedge(+	abcdne-\wedge f
g	+*\wedge(+	abcdne-\wedge fg
*	+*\wedge(+*	abcdne-\wedge fg
h	+*\wedge(+*	abcdne-\wedge fgh
)	+	abcdne-\wedge fgh*
-	-	abcdne-\wedge fgh* + \wedge *
i	-	abcdne-\wedge fgh* + \wedge * + i
		abcdne-\wedge fgh* + \wedge * + i -

Ans: abcdne-\wedge fgh* + \wedge * + i -

$$Q. A - (B / C + (D * (E * F) / G) * H)$$



Scanned element

Stack

Postfix Expression

A

A

-

A

(

- (d)

A

B

- (c)

AB

/

- (l)

AB

C

- (l)

ABC

+

- (+)

ABC /

(

- (l)

ABC / +

D

- (d)

ABC / + D

Y.

- (l)

ABC / + D

(

- (l)

ABC / + D

E

- (y.)

ABC / + DE

*

- (y.) *

ABC / + DF

F

- (f)

ABC / + DEF

)

- (l)

ABC / + DEF *

I

- (l)

ABC / + DEF *

G

- (g)

ABC / + DEF *

H

- (h)

ABC / + DEF *

*

- (y.) *

ABC / + DEF *

H

- (h)

ABC / + DEF *

*

- (y.) *

ABC / + DEF *

H

- (h)

ABC / + DEF *

*

- (y.) *

ABC / + DEF *

H

- (h)

ABC / + DEF *

*

- (y.) *

ABC / + DEF *

H

- (h)

ABC / + DEF *

*

- (y.) *

ABC / + DEF *

Ans : ABC / + DEF * y. G / H * -

QUEUE

Q. What is a queue?

→ A queue is a linear data structure.

- It is called a FIFO (First In First Out) data structure as the element that is inserted first is the first one to be removed.
- There are 4 types of queues:
 - 1) Linear queue
 - 2) Circular queue
 - 3) Priority queue
 - 4) Double Ended queue
- The operations that can be performed on a queue are :- i) Enqueue (Insertion) and ii) Dequeue (Deletion). For this, variable 'front' and 'rear' are used.
- Queues can be implemented using either arrays or linked lists.

a[4]	
a[3]	
a[2]	→ Rear when queue has 2 elements
a[1]	→ Rear when queue has 1 element
Front when queue is empty	← a[0] → Rear when queue is empty

- When we insert an element, rear is incremented, and when we delete an element, front is incremented.
- When front = rear, the queue has only one element

- Conditions for underflow:

① $\text{front} = -1$

② $\text{front} > \text{rear}$

- Condition for overflow:

① $\text{rear} = \text{max} - 1$

⇒ Let us consider a queue with maximum elements five.

- When the queue is empty,

$\text{front} = -1$	$\text{rear} = 0$
$\text{front} = -1$	$\text{rear} = 0$
$\text{front} = -1$	$\text{rear} = 0$
$\text{front} = -1$	$\text{rear} = 0$
$\text{front} = -1$	$\text{rear} = 0$

Here,

- When we insert element '1', rear is incremented

$\text{front} = -1$	$\text{rear} = 0$
$\text{front} = 0$	$\text{rear} = 1$
$\text{front} = 0$	$\text{rear} = 1$
$\text{front} = 0$	$\text{rear} = 1$
$\text{front} = 0$	$\text{rear} = 1$

Here,

$\text{rear} = 1$

$\text{front} = 0$

- When we insert element '2', rear is incremented

$\text{front} = 0$	$\text{rear} = 1$
$\text{front} = 0$	$\text{rear} = 2$
$\text{front} = 0$	$\text{rear} = 2$
$\text{front} = 0$	$\text{rear} = 2$
$\text{front} = 0$	$\text{rear} = 2$

Here,

$\text{rear} = 2$

$\text{front} = 0$

- When we insert element '3', rear is incremented

		→ rear
3		
2		
front ← 1		

Here,

$$\text{rear} = 3$$

$$\text{front} = 0$$

- When we insert element '4', rear is incremented

		→ rear
4		
3		
2		
front ← 1		

Here,

$$\text{rear} = 4$$

$$\text{front} = 0$$

- When element '5' is inserted, the queue is full

5	→ rear
4	
3	
2	
front ← 1	

Here,

$$\text{rear} = 4$$

$$\text{front} = 0$$

- When we delete an element, front is incremented

5	→ rear
4	
3	
2	
front ← 2	

Here,

$$\text{rear} = 4$$

$$\text{front} = 1$$

- When another element is deleted,

	5 → rear	Here, rear = 4
front ← 4		front = 2
	3	

- When another element is deleted,

	5 → rear	Here, rear = 4
front ← 4		front = 3
	3	

- When another element is deleted

front ← 5	→ rear	Here, rear = 4
		front = 4

- When the last element is deleted,

	→ rear	Here, rear = 4
		front = 5

- Here, $\text{rear} = \text{max} - 1$, so queue is in overflow condition.
- Disadvantage:- A simple queue gives us an overflow condition even when we have empty spaces.

① Algorithm for insertion (Enqueue)

Step 1 : Start

Step 2: Let "a" be a queue of elements 'm'.

Step 3: If $\text{rear} = \text{max} - 1$, print overflow and exit.

Step 4: Read element to be inserted

Step 5: If $\text{front} = -1$ and $\text{rear} = -1$, then set
 $\text{front} = \text{rear} = 0$

else,

$\text{rear} = \text{rear} + 1$

Step 6: $\text{queue}[\text{rear}] = \text{element}$

Step 7: Stop.

• Algorithm for deletion (Dequeue)

Step 1 : Start

Step 2: Let "a" be a queue of max. size 'm'

Step 3: If $\text{front} = -1$
or $\text{front} > \text{rear}$,
print underflow and exit

Step 4: $\text{queue}[\text{front}] = \text{NULL}$

Step 5: $\text{front} = \text{front} + 1$

Step 6: Stop.

14/05/22

* CIRCULAR QUEUE

① Algorithm for Enqueue (Insertion) in circular queue

Step 1: Start.

Step 2: Let "a" be a circular queue with 'max' elements.

Step 3: If $\text{front} = 0 \& \& \text{rear} = \text{max} - 1$
 or $F = 0 \& \& F = (\text{R} + 1) \% \text{max}$
 point overflow and exit.

Step 4: Read element to be inserted.

Step 5: if $\text{front} = -1 \& \& \text{rear} = -1$

Set $\text{front} = \text{rear} = 0$

else if ($\text{front} = 0 \& \& \text{rear} = \text{max} - 1$)

set $\text{rear} = 0$

else

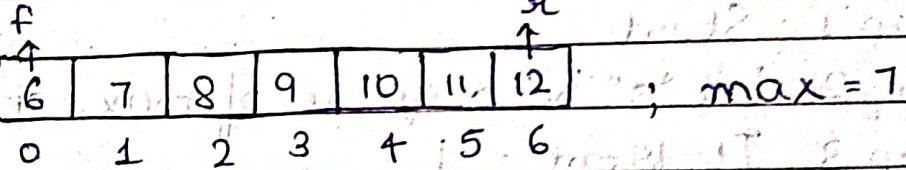
$\text{rear} = \text{rear} + 1$

Step 6: $\text{queue}[\text{rear}] = \text{element}$

Step 7: Stop.

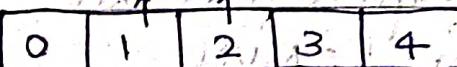
⇒ Overflow conditions:

① $\text{front} = 0 \& \& \text{rear} = \text{max} - 1$



② $\text{front} = (\text{rear} + 1) \% \text{max}$

F



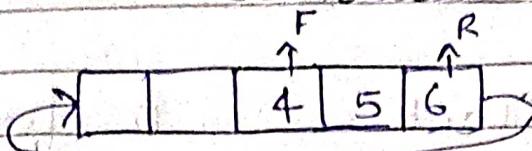
$$F = (R + 1) \% \text{max}$$

$$2 = (1 + 1) \% 5 = 2 \% 5$$

$\therefore 2 = 2 \Rightarrow \text{Overflow.}$

⇒ Step 5: front = 0 and rear = max - 1

set rear = 0



④ Algorithm for Deque (deletion) in circular queue:

Step 1 : Start

Step 2 : Let "a" be a circular queue with 'max' elements

Step 3 : If front = -1,

point underflow and exit.

Step 4 : queue[front] = NULL

Step 5 : if front = rear,

set front = rear = -1

else if front = max - 1

set front = 0

else

front = front + 1

Step 6 : Stop

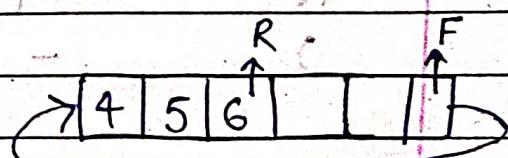
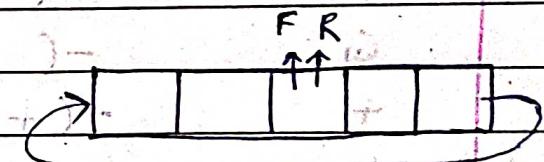
⇒ Step 5 :

① if front = rear

set front = rear = -1

② else if front = max - 1

front = 0



* Convert from Infix to Postfix using stack

$$Q. A \wedge B / C + (D * E) \wedge F - (G + H)$$

Scanned Element	Stack	Postfix Expression
A		A
\wedge	\wedge	$A \wedge B / C + (D * E) \wedge F - (G + H)$
B	\wedge	$A B / C + (D * E) \wedge F - (G + H)$
/	/	$A B / C + (D * E) \wedge F - (G + H)$
C	/	$A B \wedge C + (D * E) \wedge F - (G + H)$
+		$A B \wedge C + (D * E) \wedge F - (G + H)$
(+ ($A B \wedge C + (D * E) \wedge F - (G + H)$
D	+ C	$A B \wedge C + D * E) \wedge F - (G + H)$
*	+ C *	$A B \wedge C + D * E) \wedge F - (G + H)$
E	+ C *	$A B \wedge C + D * E) \wedge F - (G + H)$
)	+ C *	$A B \wedge C + D * E) \wedge F - (G + H)$
\wedge	+ \wedge	$A B \wedge C + D * E) \wedge F - (G + H)$
F	+ \wedge I	$A B \wedge C + D * E) \wedge F - (G + H)$
-	-	$A B \wedge C + D * E) \wedge F - (G + H)$
(- ($A B \wedge C + D * E) \wedge F - (G + H)$
G	- (-	$A B \wedge C + D * E) \wedge F - (G + H)$
+	- (+	$A B \wedge C + D * E) \wedge F - (G + H)$
H	- (+ -	$A B \wedge C + D * E) \wedge F - (G + H)$
)	-	$A B \wedge C + D * E) \wedge F - (G + H)$
		$A B \wedge C + D * E) \wedge F - (G + H) + -$
		$A B \wedge C + D * E) \wedge F - (G + H) + -$

Ans:- $A B \wedge C + D * E) \wedge F - (G + H) + -$

- Postfix notation is also called reverse polish notation. It is used to evaluate an expression without parenthesis or priority.

* Expression Evaluation using Stack:

Q. $A B C * D + E / -$, where, A = 9, B = 3, C = 4, D = 8 and E = 4.



Scanned Element

Stack

Operation.

9	9	push 9
3	9 3	push 3
4	9 3 4	push 4
*	9 12	evaluate $3 * 4$
8	9 12 8	push 8
+	9 20	evaluate $12 + 8$
4	9 20 4	push 4
/	9 5	evaluate $20 / 4$
-	4	evaluate $9 - 5$

LINKED LIST

- Array is a linear collection of data elements in which the elements are stored in consecutive memory locations. While declaring arrays, we have to specify the size of the array which will restrict the number of elements that the array can store.
- To make efficient use of memory, the elements must be stored randomly at any location. So there must be a data structure that removes the restrictions on the maximum number of elements and the storage condition.
- Linked list is a data structure that removes this restriction.

○ Limitation of Linked list :- A linked list does not allow random access of data elements. The elements of linked list can only be accessed in a sequential manner.

- DEFINITION :- A linked list is a linear collection of data elements. These data elements are called nodes. Every node in a linked list is having two parts - data and pointer to the next node connected to it. The last node will have no next node connected to it so it will store a special value called as NULL.

NODE :-	DATA	NEXT/LINK
---------	------	-----------

Linked List:



START

350

350

10 400

400

480

12

18

900

15

NUL

900

DATA

NEXT

START: 350

350

10

400

400

12

480

480

18

900

900

15

NUL (-1)

=> struct node { int data; struct node *next; };

int data;

struct node *next;

=> NAME | MARKS | ID | NUL

struct node { char name[10];

float marks;

int id;

struct node *next;

};

- Declare a pointer $START = \text{NULL}$ to indicate that the linked list is initially empty.

For traversal,

$p = \text{start}$

while ($p \neq \text{NULL}$)

$p = p \rightarrow \text{next}$

① Algorithm for traversing of linked list

Step 1 : Start

Step 2 : if ($\text{start} = \text{null}$)

 print linked list is empty and exit.

Step 3 : $p = \text{start}$; display data part of node

Step 4 : while ($p \rightarrow \text{next} \neq \text{null}$)

 display data part of node

$p = p \rightarrow \text{next}$

Step 5 : Stop

② Algorithm for counting number of elements in linked list

Step 1 : Start

Step 2 : if ($\text{start} = \text{null}$)

 print no elements in list and exit

Step 3 : $p = \text{start}$; $\text{count} = 0$

Step 4 : while ($p \rightarrow \text{next} \neq \text{null}$)

{

$\text{count}++$

$p = p \rightarrow \text{next};$

}

Step 5 : print count as number of elements

Step 6: Stop.

* INSERTION OF NODES AT BEGINNING

- ① Create a node
- ② If $\text{start} = \text{null}$; node created will be the only node.
- ③ Node will be inserted at front.

④ Algorithm for insertion of node at beginning.

Step 1: Start

Step 2: $\text{newnode} = (\text{struct node} *)\text{malloc}(\text{size of } \text{Node} + \text{size of } (\text{struct node}))$

Step 3: Get data from user input

Step 4: $\text{newnode} \rightarrow \text{link} = \text{null}$

Step 5: if ($\text{start} = \text{null}$)
 {

$\text{newnode} \rightarrow \text{link} = \text{null}$

$\text{start} = \text{newnode}$

 }

else

 {

$\text{newnode} \rightarrow \text{link} = \text{start}$

$\text{newnode} = \text{start}$

 }

Step 6: Stop.

* INSERTION OF NODE AT END

① Algorithm for insertion of node at end :

Step 1 : Start

Step 2 : newnode = (struct node*) malloc (sizeof
(struct node))

Step 3 : Get data part from user.

Step 4 : newnode → link = null

Step 5 : if (start = null)

{

 newnode → link = null

 start = newnode

}

else

{

 p = start

 while (p → link != null)

{

 p = p → link

}

 p → link = newnode.

}

Step 6 : Stop.