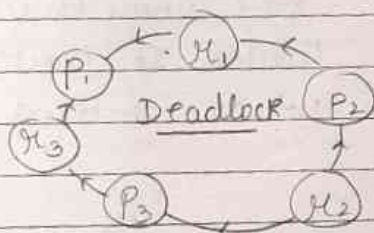


Unit-3

Deadlock

When several process compete for limited no. of resource if the resource is not available then the process enter into waiting state.

If the process gets enable to change its waiting state because the resource requested by it are held by another waiting process i.e. called deadlock.



System model for the deadlock

There are 3 steps:

- Step 1) Every process will request for the resource
- Step 2) If it is available then process will use the resource.
- Step 3) After use process must release the resource.

Necessary and sufficient condition for deadlock:

- 1) Mutual Exclusion: Atleast one resource type which can be used in non sharable mode i.e. mutual Exclusive.
- 2) Hold and Wait: A process is currently holding atleast one resource and requesting additional resource i.e. held by other process.
- 3) Non-preemption: A resource cannot be preempted i.e. resource will be released by process after completion.

task.

- 4) Circular wait: Each process must be waiting for a resource which is held by another process which in turn is waiting for the first process to release the resource.

Resource Allocation Graph (RAG)

The resource allocation graph is set of resource categories $\{R_1, R_2, \dots, R_j\}$ which appear as square nodes on the graph.

- DOTS inside the resource nodes indicate specific instances of the resource.
- A set of process $\{P_1, P_2, \dots, P_i\}$ is represented by circle node.
- Request edge: A set of directed arcs from P_i to R_j indicates that P_i has requested R_j and is currently waiting for the resource to become available.
- Assignment edge: It indicates that the resource R_j has been allocated to process P_i .

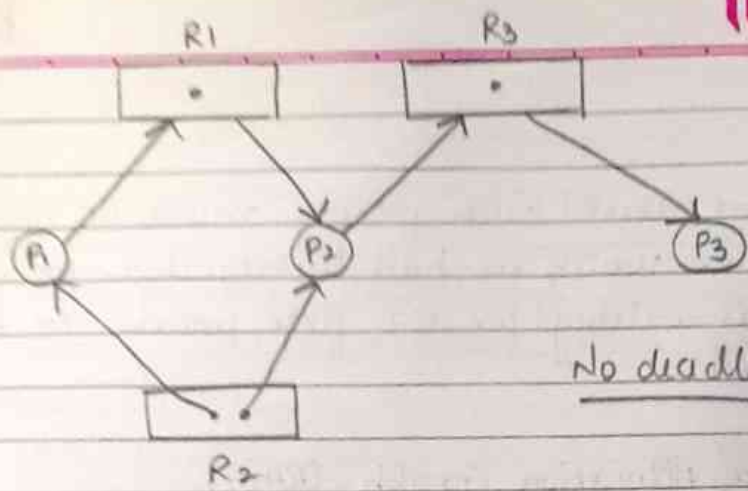
E1: The request edge can be converted into assignment edge when the request is granted.

E2: RAG contains no cycle then the system is not deadlock.

E3: If RAG contains cycle and each resource category contains only a single instance then a deadlock exist.

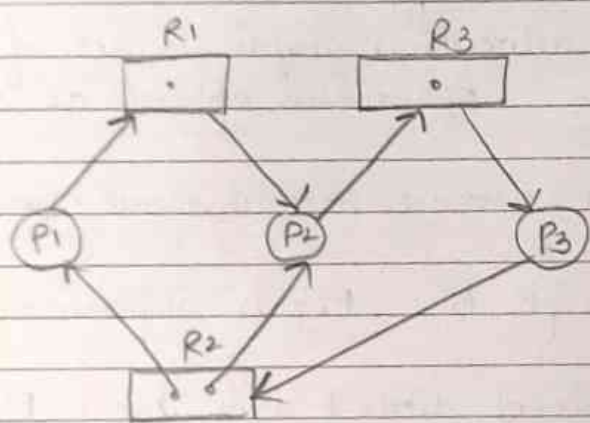
E4: If a resource category contains more than one instances then the presence of a cycle in RAG indicates the possibility of deadlock but does not give the guarantee of deadlock.

1)



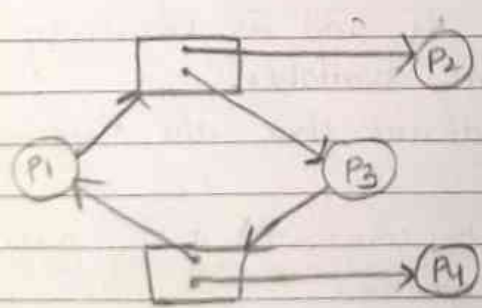
No deadlock

2)



Deadlock

3)



No deadlock

Deadlock Handling Methods

1. Prevention
2. Avoidance
3. Detection & Recovery
4. Ignorance

1. Prevention

It means we need to design such a system which atleast one of the four necessary condition of deadlock

ensures that Deadlock should not occur.

i) Mutual Exclusion

If a Resource is assigned more than one process that means the Resource is sharable, then Deadlock will not occur.

etc: There are some Resources that cannot be shared among several processes at a time.
Eg: Printer, CD, Recorder etc.

ii) Hold and Wait

Process will acquire only desired Resources but before making any fresh request, it must release all the Resources that is currently held.

iii) ~~No~~ Non-preemption:

forceful Preemption: We allow a Process to forcefully preempt the Resource holding by other processes.

This method may be used by higher priority process or other System.

iv) Circular Wait

It can be eliminated by just giving a Natural Number ($F: N \rightarrow R$) to each Resource.

Allow every Process to make request either only in the increasing order or decreasing order of Resource num.

If a process requires a Resource of lesser number in case of increasing order, then it must first release all the Resources larger than the required number.

11. Deadlock Avoidance

The general idea behind Deadlock Avoidance is to prevent Deadlock from ever happening.

So, we need to find the Safe state.

Safe State: The system can allocate all Resources requested by all process without entering into Deadlock State

If the safe sequence does not exist then system is Unsafe State, which may lead to Deadlock.

i. Banker's Algorithm

- When a process starts up, it must state in advance, the max allocation of resources
- It may request upto the amount of available in system
- When a request would leave system in safe state, if the process must wait until the request is granted safely

unsafe
deadlock
Safe

Based on Banker's Algo

Process	Allocation			Max need			Available			Remaining (max need - allocation)
	A	B	C	A	B	C	A	B	C	
P ₀	0	1	0	7	5	3	3	3	2	7 4
P ₁	2	0	0	3	2	2	5	3	2	1 2
P ₂	3	0	2	9	0	2	7	4	3	6 0
P ₃	2	1	1	4	2	2	7	4	5	2 1
P ₄	0	0	2	5	3	3	7	5	5	5 3

- Remaining need \leq available
if condition is true

$$\text{Available} = \text{Available} + \text{Allocation}$$

$$P_0 \quad 7 \ 4 \ 3 \leq 3 \ 3 \ 2$$

False

$$P_1 \quad 1 \ 2 \ 2 \leq 3 \ 3 \ 2$$

True

$$\Rightarrow 3 \ 3 \ 2 + 2 \ 0 \ 0 = 5$$

$P_1: 600 \leq 532$
false

$P_3: 211 \leq 532$

True

$$\Rightarrow 532 + 211 \\ = 743$$

$P_4: 531 \leq 743$

True

$$\Rightarrow 743 + 002 \\ = 745$$

$P_0: 743 \leq 745$

True

$$\Rightarrow 745 + 010 \\ = 755$$

$P_2: 600 \leq 755$

True

$$\Rightarrow 755 + 302$$

\therefore total amount of resources = 10 57

Safe sequence : $\{P_1, P_3, P_4, P_0, P_2\}$

Process	Allocation			Max need			Available			Remain need		
	A	B	C	A	B	C	A	B	C	A	B	C
P_1	1	0	1	4	3	1	3	3	0	3	3	0
P_2	1	1	2	2	1	4	4	3	1	1	0	2
P_3	1	0	3	1	3	3	5	3	4	0	3	0
P_4	2	0	0	5	4	1	6	4	6	3	4	1

$P_1: 330 \leq 330$

$$\text{True} \Rightarrow 330 + 101 = 431$$

$P_2: 102 \leq 431$

false

$P_3: 030 \leq 431$

$$\text{True} \Rightarrow 431 + 103 = 534$$

$P_4: 341 \leq 534$

false

$P_2: 102 \leq 534$

$$\text{True} \Rightarrow 534 + 112 \\ = 646$$

$P_4: 341 \leq 646$

$$\text{True} \Rightarrow 646 + 200 \\ = 846$$

Safe seq : $\{P_1, P_3, P_2, P_4\}$

III. Deadlock Detection

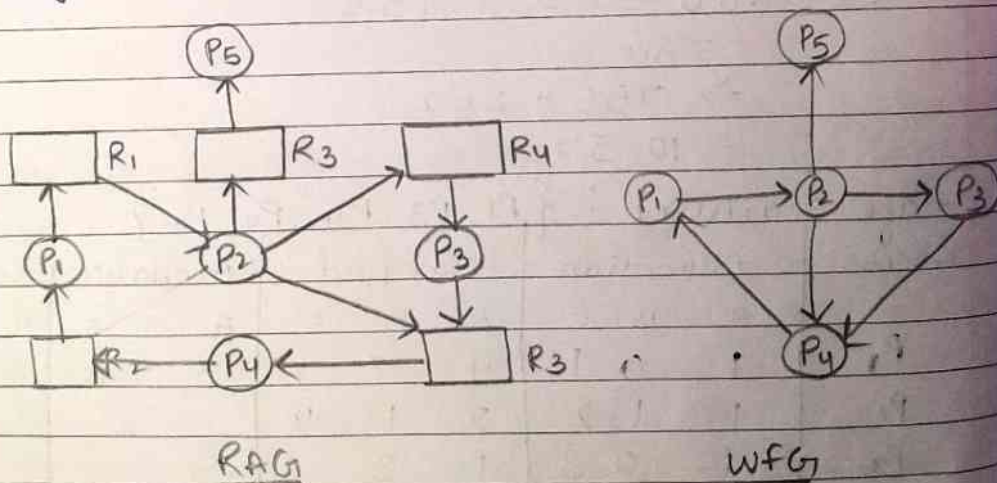
If deadlocks are not avoided then another approach used to detect when they have occurred.

So, there are 2 process to detect the deadlock:

- 1) Single Instance of Each resource type
- 2) Several instance of Each resource type

i) Single instance of each resource type:

- If each resource category has a single instance then we can use a variation of the resource allocation graph that is known as Wait for Graph (WFG).
- A WFG can be constructed from a RAG by eliminating the resources and collapsing the associated edges.



ii) Several instance of each resource type

The detection algorithm is same as the banker's algorithm

Step 1: The Banker's algorithm set fin

III. Deadlock Recovery.

When a deadlock detection algorithm determines that a deadlock has occurred in the system. The system must recover by using 2 approaches for breaking a deadlock.

1) Process Termination

2) Resource Preemption

1) Process Termination:

- Abort all the deadlocked process.
- Abort one process at a time until deadlock is eliminated.

2) Resource Preemption:

- To eliminate ^{deadlock} using preemption we preempt some resources from processes and give these resources to other processes.

Sometimes, this method will raise three issues.

1) Selection

- 1) Selecting a victim: We must determine which resource and which processes are to be preempted and also the order to ^{minimize} the cost.
- 2) Rollback: We must determine what should be done with the process from which resources are preempted. Simple idea is total rollback to process and restart it again.
- 3) Starvation: In a system it may happen that a process is always picked as a victim as a result the process will never complete its execution. So, the solution for this prob is we must ^(victim) picked up a resource only a finite no. of times.

10/10/23 Process Synchronization

1. Inter-Process Communication (IPC)

It refers to a mechanism which allows communication b/w two or more processes to perform the action simultaneously.

There are two types of processes:

- 1) Independent Processes: Which does not depend on execution of ^{other} processes.
- 2) Cooperative Processes: These are the processes which can effect or get affected by other process during execution.

Cooperative processes can share the data in terms of variable, memory, code and resources.

2. Race Condition

It is the situation arise due to concurrent execution of more than one processes which are accessing and manipulating the same shared data and the

of execution depends upon the specific order where the access takes place.

Eg: shared = 5

P1	P2
x = shared	y = shared
x++;	y--;
sleep(1)	sleep(1)
shared = x	shared = y

3. Critical Section

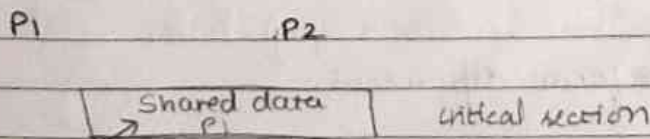
This is a piece of code which contains some shared code of variable which is accessible by each process concurrently in order to complete execution.

There must be only one process is allowed at the time in critical section otherwise more than one access may lead to inconsistency.

4. Mechanism to achieve Synchronization

- Mutual Exclusion
- Progress
- Bounded Wait
- No assumption related to the hardware

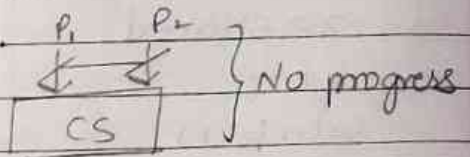
i) Mutual Exclusion.



P1 entered into critical section at the same time if P2 is requesting to enter into critical section then it will not allow.

ii) Progress.

If no process is in the critical section and if one or more process want to execute ~~then~~ ^{their} critical section then any one of them must be allowed to get into the critical section.



iii) Bounded wait

After a process makes a request for getting into critical section there is the limit called how many times other process can get into the critical section before the process request is granted.


So after the limit is reached system must grant the permission to get into the critical section.

Condition:
CS
used
times only

	P_1	P_2	P_1	P_2
1	0	0		
2	0	0		
3	0	0		
	0	0		
200	1			

CS

iv) No assumption related to hardware.

{ mai nahi likh nahi ab... } 
Thak gayi hun...

No platform dependent.

5. Solution to the Synchronization problem:

There are 3 solution:

- Hardware solution
- Software solution
- strict alteration

Inter Process Communication Synchronization Problem:

→ Producer-Consumer Problem

int count=0;

void produce(void)

{ int item;

while (True)

{ Produce item (item);

while (count == n);

Buffer [in] = item;

in = (in + 1) mod n;

count = count + 1;

}

}

void Consume(void)

{ int item;

while (true)

{ while (count == 0);

item = Buffer(out)

out = (out + 1) mod n;

Count = count - 1;

Process = item (item);

};

}

In

I₁ Load R_p, M[Count];

→ I₂ INCR R_p;

I₃ Store M[Count], R_p

count = 0

out

Buffer

0

x₀

1

x₁

2

x₂

3

x₃

4

5

6

Seq: Produce I₁, I₂ consume I₁, I₂

Produce I₃ consume I₃

P I₁ I₂ → x₃

P I₃ C = 4

* But; race around condition...

C I₁ I₂ → x₃

C I₃ C = 2

(Because 3 in Buffer and c = 4)

(Because 2 in Buffer and c = 2)

* It is a multiprocess sync problem also known as Bounded Buffer Problem. It describes that 2 processes, producer-consumer

who share a common fixed size Buffer. Producer process will produce some data and put it into the Buffer and Consumer process will consume the data and remove the item from Buffer.

* Condⁿ for inconsistency:

- Producer must not try any data item produce to the Buffer, if Buffer size is full.
- Consumer must not try to consume any data if Buffer size is Empty.

* Solⁿ of Producer:

- Producer either go to sleep or discard the data if Buffer is full.
- Once the consumer removes an item from Buffer, it notifies the producer to put data into Buffer.

* Solⁿ of Consumer:

- Consumer can go to sleep if Buffer is empty.
- Once the producer puts the data into Buffer it notifies Consumer to remove data from the Buffer.

16/10/23 Solⁿ to Sync problem

1) Software Solution.

Peter's algorithm →

P₀ interested \boxed{F} \boxed{F} → both are false initially
Turn $\boxed{0}$ → 0 means P₀'s turn is first &
1 means P₁'s turn is first

Entry Section

Entry Section (Process)

// Mutual Exclusion ✓

{ int other;

// Bounded waiting ✓

other = 1 - process;

// Progress ✓

interested (process) = true

turn = process

while (interested [other] == true && turn = process); }

exit Section

{ interested [process] = false; }

Note: It will not work for more than 2 processes.

Page No.
Date:

It is used for implementing any 2 process only & it uses two variable i.e. turn & interested.

IE: It does not give the guarantee to work on multiple core & latest model of computers.

Hardware solⁿ for synchronization problem

- 1) lock 2) Test & Set 3) swap

* Test & Set algorithm

```
lock = false
do {
    while (Test and Set (&lock));
    exit code { lock = false; } // critical section.
    while (true);
    boolean Test and Set (boolean *target)
    {
        boolean sv = *target;
        *target = true;
        return sv;
    }
}
```

// Mutual exclusion

// Bounded waiting

// Progress

lock	True	target	sv
False		1000	False
1000			

* Strict Alternation

Turn variable (Software based, work for 2 processes)
for process P₀

→ while (turn != 0);
CS

→ { turn = 1;
exit; }

for process P₁

→ while (turn != 1);
CS

→ { turn = 0;
exit; }

* It is a busy waiting problem solution which can be implemented only for 2 processes

Semaphore

- They are integer values that are used to solve critical section problem by using two atomic operation: wait & Signal
- That are used for the process Synchronization
- wait() \rightarrow decrement of n Signal() \rightarrow increment of n .
- There are two types of Semaphore: Counting & Binary
Range: Counting $\rightarrow -\infty$ to $+\infty$; Binary $\rightarrow 0$ to 1

17/10/23

- These are integers value Semaphore & have unrestricted value domain
- Binary Semaphore are like Counting Semaphore but their value are restricted
- wait() - P() - Down
- Signal() - V() - Up
- Counting Semaphore.

Down (Semaphore S)

```
{ value = Svalue - 1;
  if (Svalue <= 0)
    { put process in suspended list; }
  else
    return; }
```

Up (Semaphore S)

```
{ { value = Svalue + 1;
  if (Svalue <= 0)
    { Select a process from Suspended list
      wake up () }
  }
```

* Reader - Writer Problem.

P1	P2	
R	W	} causes problem
W	R	
W	W	
R	R	- no problem.

```

Reader
int rc = 0
Semaphore mutex = 1
Semaphore db = 1
void Reader(void)
{ while (true)
  { down (mutex)
    rc = rc + 1
    if (rc == 1)
      then
        down (db);
        up (mutex)
        [db]
        down (mutex)
        rc = rc - 1
        if (rc == 0)
          then
            up (db);
            up (mutex);
            process data;
          }
  }
}

```

```

Writer
void write(void)
{ while (true)
  { down (db);
    [db]
    up (db);
  }
}

```

- Q Consider a system with 'n' processes and 6 tape drives
 If each process requires 2 tape drives to complete their execution
 then what is the maximum value of 'n' which always
 ensures that deadlock free operations 3 4 5 None
- Q Consider a system 3 processes each process require two
 unit to comp. their execution. Then what is the min.
 no. of resources that ensures deadlock free system.

Q Each process P_i , where $i=1$ to g executes code P_i

repeat

$P(\text{mutex}) < CS \vee (\text{mutex})^2$

forever

The process P_0 execute the following code

repeat

$V(\text{mutex})$

CS

$V(\text{mutex})$

forever

$\text{Mutex} = 1$

What are max no of process that may present at any point of ~~cs~~ time?

2 3 ✓ 9 10

Dining Philosopher's Problem

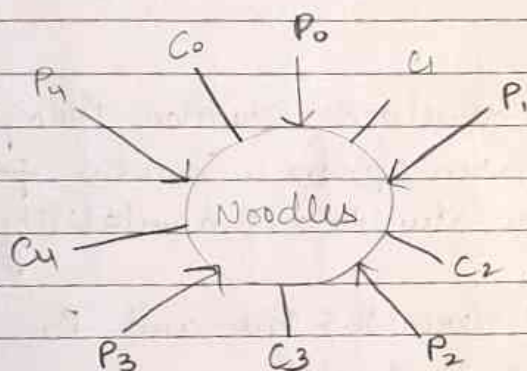
In this problem there are 4 philosophers are sitting at a dining table and given chopsticks are C_0, C_1, C_2, C_3 . Eat food on the table. Each philosopher requires 2 chopsticks at same time to eat.

At any step a philosopher is either eating or thinking.
If philosopher is eating, have to pick chopsticks from their left and one from their right.
If philosopher is thinking, it will keep the chopsticks on the table.

for eg: Philosopher P_0 wants to eat the food, it requires C_0 and C_1 , as considered here $I=0$, as 0^{th} location.

⊗ Case I: In this case one by one philosopher is eating.

and thinking which is best case. If philosopher P_0 is eating with chopstick C_0 and C_1 and then put the chopsticks on table and then other philosopher P_1 has come to eat which requires chopsticks C_1 and C_2 , as we see the chopstick C_1 is now available for P_1 because P_0 already put down the chopstick C_1 after eating. So, in this case there is no problem that can occur.



Case 2: In this case, Philosopher P_0 is eating with a chopstick C_0 and C_1 and at the same time Philosopher P_1 enter to eat. So it requires C_1 and C_2 . Now, in this case C_1 is not available for Philosopher P_1 because it already ~~is~~ hold by the Philosopher P_0 .

To deal with this situation binary semaphore is used.

When one Philosopher eat the food with needed chopsticks and case II situation occurs. Then it block that Philosopher otherwise it allow the another philosopher if it is require other chopsticks that are available on the table.

So at sometime, multiple philosopher can eat If their required chopsticks are available on table.


```

void philosopher(void)
{ while (true)
  { thinking();
    wait (take chopstick (si));
    wait (take chopstick (si+1) % N);
    eat();
    Signal (put chopstick (i));
    Signal (put chopstick (i+1) % N);
  }
}

```

NOTE: To avoid the deadlock situation Philosopher P_4 need to swipe there semaphore. So, when ~~people~~ P_4 comes it will not allow due to not availability of their first semaphore.

So, S_4 will remains one and P_3 will use S_4 and S_3 and put it back.

So, again S_3 and S_4 will be available. So further P_2 can use S_2 and S_3 and run further process.

P_0 S_0 S_1

P_1 S_1 S_2

P_2 S_2 S_3

P_3 S_3 S_4

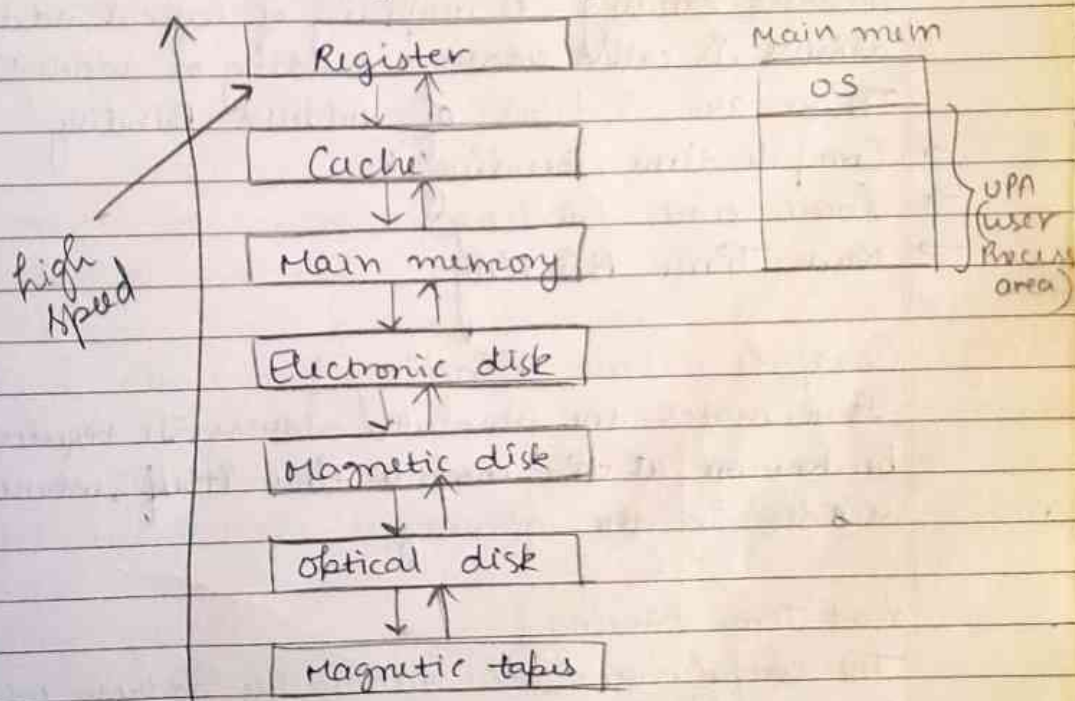
→ P_4 S_0 S_4

Unit-4

Memory management.

- To achieve a degree of multiprogramming and proper utilisation of memory, memory mgmt is required.
- The main memory comprises a large array or group of words or bytes each with its own location.
- The primary purpose of the computer system is to execute the program in the main memory.

Memory hierarchy



In a multiprogramming OS resides in a part of mem and the rest is used by multiple processes. The task of subdividing the memory among different process is called memory mgmt and it is a method in OS to manage operations b/w main mem & secondary mem. The main aim of the memory mgmt is to achieve efficient utilisation of memory.

Logical address v/s Physical address

* Logical address i.e. generated by CPU and also known as virtual address.

Absolute address *

* Physical address is the main memory address.

(LAS) * Logical address space : It is a set of all logical address generated by CPU i.

(PAS) * Physical address space : Set of all PA.

Address Binding : A mapping of logical address to a physical address is called address binding or address mapping.

There are 3 types of Address Binding :

- Compile time Binding :
- Load time Binding
- Run Time Binding

Compile Time Binding :

It generates the absolute address. It requires that it be known at the compile time itself, where will a program reside in the memory.

Load Time Binding :

The compiler generates relocatable address which are converted to absolute address at the load time.

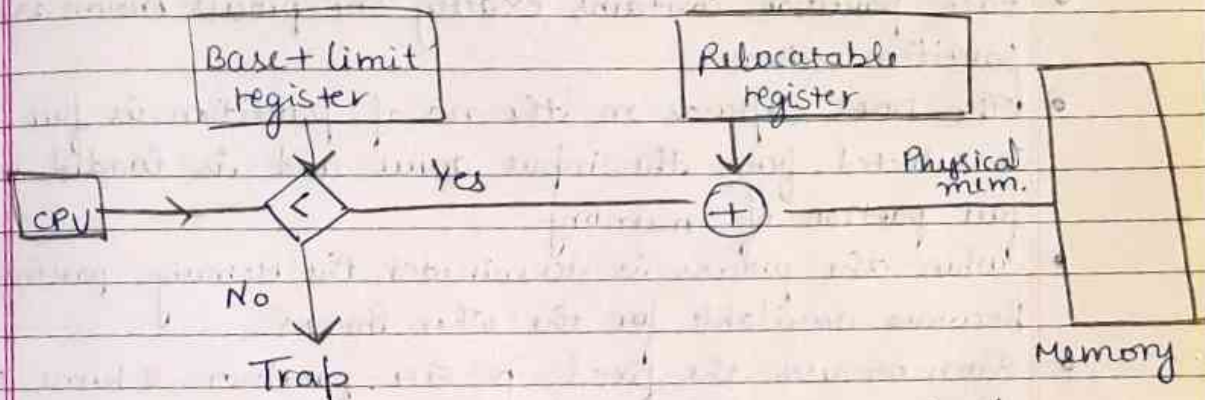
Run Time Binding :

The process may be moved from one mem. segment to other then binding must be delayed until runtime.

Memory Protection Hardware

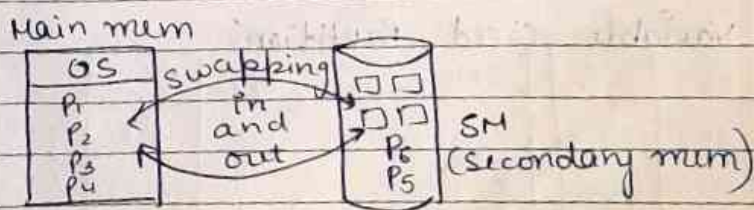
Base address

It is starting address of any mem. block and limit register gives the limit of any mem. block



- The protection means providing security from unauthorized access or usage of memory.
- The OS can protect the memory with the help of Base & limit register.
- The limit register is always the fencing register.
- Base register holds the smallest legal physical mem. address while the limit reg. contain the size of process.

Swapping



Memory allocation

- 1) Contiguous allocation
- 2) Non-contiguous allocation.

→ paging
 → segmentation
 → paging with segmentation

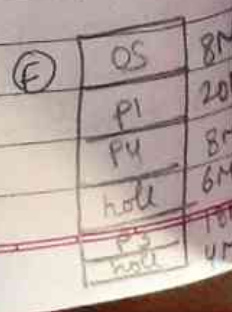
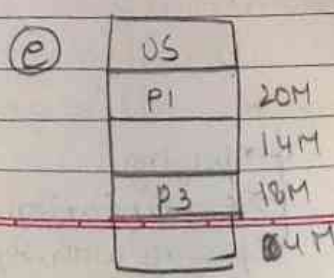
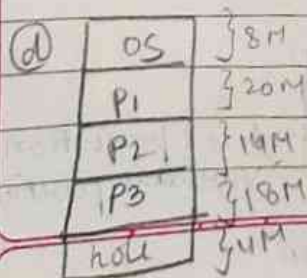
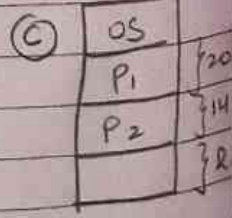
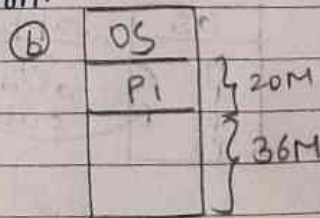
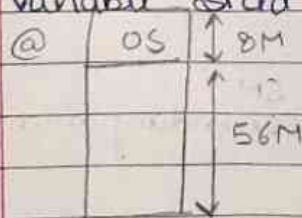
→ fixed partition scheme
 → variable partition scheme

Memory Allocation

1) Contiguous Memory Allocation.

- Single Contiguous allocation is a simple memory allocation that requires no special hardware for allocating memory. It is divided into the no. of fixed sized partition.
- Each partition contains exactly one process known as fixed partition scheme.
- The DQM depends on the no. of partition is free, the is selected from the input queue and is loaded into free portion of memory.
- When the process is terminated, the Memory partition becomes available for the other Process.
- Batch OS uses the fixed 'p' size partition scheme. OS keeps the record of mem. allocation and de-allocation in the form of table.
- When the Process arrives in the System and needs Memory then OS search for the large space for the Process. If it is available, the Process is allocated to that Memory.
- There are 2 difficulties with equal size partition:
 - A program may be too big to fit into the Partition.
 - Advantage: Simple to implement and less overhead.

Variable sized Partition:



①	OS	20M	②	OS
	P1	8M		P1
		6M		P2
	P2	18M		hole
		4M		P3
				P4

- for the Memory Allocation, there are 3 schemes:
First fit, Best fit, Worst fit.

1) first fit

Allocating the first hole, that is big enough.

Searching can start either at the beginning of the set of holes or where the previous first fit search ended

2) Best fit

Allocate the smallest hole that is fit enough. We must search the entire list, unless the list is ordered by size. This strategy produces the smallest left-over hole.

3) Worst fit

It allocated the largest hole. This strategy produces the largest leftover hole.

- first fit and Best fit are better than the worst fit, in terms of storage utilization.

fragmentation

Memory fragmentation is of 2 types.

- ① Internal fragmentation
- ② External fragmentation

1) Internal fragmentation.

There is a wastage of space internal due to the fact that the block of data loaded is smaller than the

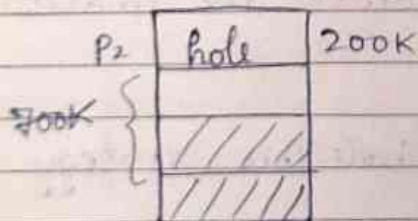
partition size.

for ex: The size of hole is 1054 bytes and the process request for 1052 bytes. If we allocate hole, then there is a hole created of 2 External fragmentation.

when in a total mem. space exist to satisfy a req. but it is not contiguous storage fragmented into large no. small holes.

for eg: There is a hole of 200K, 500K in various size partition scheme and next process for 700K of memory. Actually, 700K of is free which satisfy the request but not contiguous. So, this is an External fragmentation of mem. and Best-fit & Worst-fit can be affected by the external fragmentation.

7/11/23 Compaction



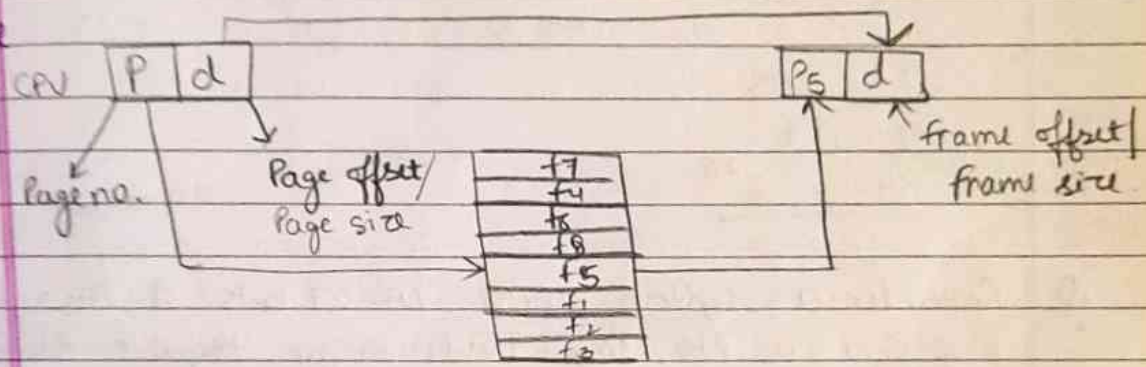
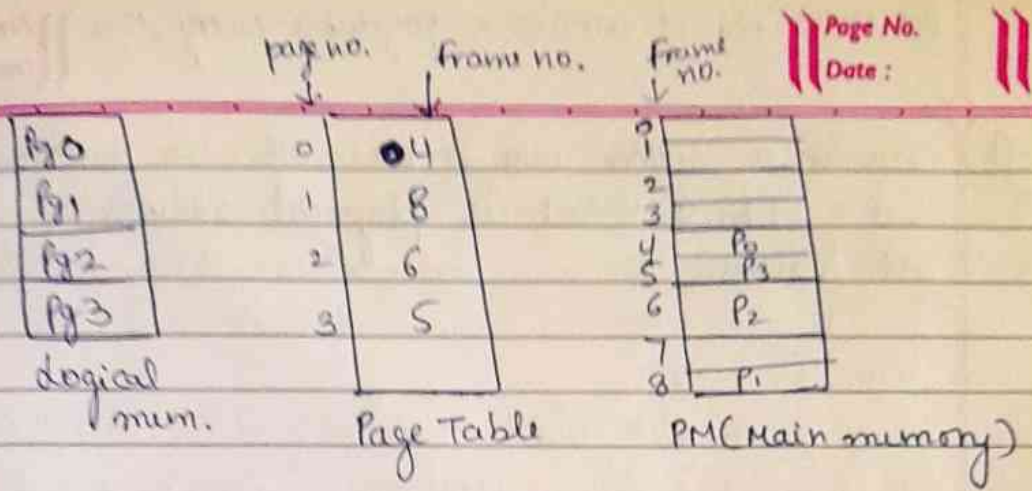
Paging

1) It is a non-contiguous memory allocation and physical memory is divided into physical address space and logical memory is divided into logical address space and logical address space is having two fields:

- no. of pages
- page offset

and physical memory is divided into 2 parts

- frame no.
- frame offset



① LA = 7 bit = $2^7 = 128$
 PA = 6 bit = $2^6 = 64$
 Page size = 8 bytes = 2^3
 calculate no. of pages & no. of frames.

no. of pages = $\frac{LA}{\text{page size}}$

= $\frac{2^7}{2^3} = 2^4$

= 4 bits

no. of frames = $\frac{PA}{(\text{frame size})}$

= $\frac{2^6}{2^3}$

= $2^3 = 3 \text{ bits}$

CPU | 4 | 3 |

Q LA = 4 GB = $2^2 \cdot 2^{30} = 32 \text{ bits}$
 PA = 6 MB = $2^6 \cdot 2^{20} = 26 \text{ bits}$
 Page size = 4 KB = $2^2 \cdot 2^{10} = 12 \text{ bits}$
 No. of Pages = ? = $\frac{2^{32}}{2^{12}} = 2^{20} = 1 \text{ MB} = 20 \text{ bits}$
 No. of frames = ? = $\frac{2^{26}}{2^{12}} = 2^{14} = 16 \text{ KB} = 14 \text{ bits}$
 No. of entries in PageTable = ? & Size of PT = ? $2^{20} \times 2^{14}$

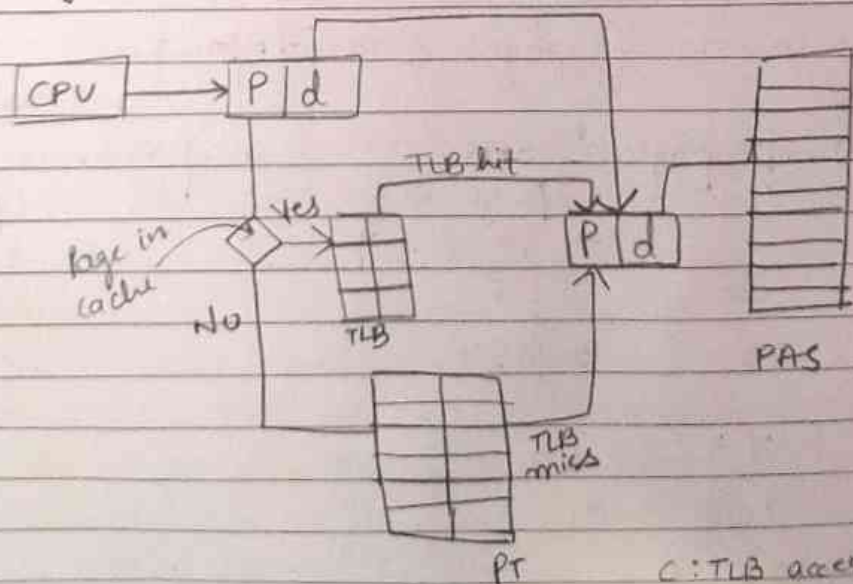
Q Consider a system with a PT with 4K entries
LA = 29 bits. What is physical address if system
512 frames

$$\begin{aligned} \text{LA} &= 29 \text{ bits} \\ \text{no. of frames} &= 512 = 2^9 \\ \text{no. of pages} &= 2^{12} = \text{LA} \\ &\quad \text{page size} \end{aligned} \quad \begin{aligned} \text{page size} &= 29 - 12 \\ &= 17 \end{aligned}$$

$$\begin{aligned} 2^9 &= \text{PAS} \\ \text{Answer } 2^{17} \\ \text{PAS} &= 2^{26} \end{aligned}$$

Q Consider a system with LA = 27 bits & PAS = 128
Page size is 8K. Page Table entry require 32 bits
what is the approximate size of PT in bytes

Paging with TLB (Translation look a Side Buffer)



Effective memory access time

$$\text{EMAT} = h * (C + M) + (1 - h) * (C + 2M)$$

\uparrow TLB hit ratio \uparrow TLB miss ratio
 C : TLB access time
 M : Mem.

Consider a system which has TLB access time (C) = 20 ns and main mem. access time (M) = 100 ns. and hit ratio is 85% and the system uses 10 level paging. Then what is EMAT with TLB?

$$\begin{aligned} \text{EMAT} &= h^* (C + M) + (1-h)^* (C + 2M) \\ &= 0.85^* (20 + 100) + 0.15 (20 + 200) \\ &= 0.85 (120) + 0.15 (220) \\ &= 102 + 33 \\ &= 135 \text{ ns} \end{aligned}$$

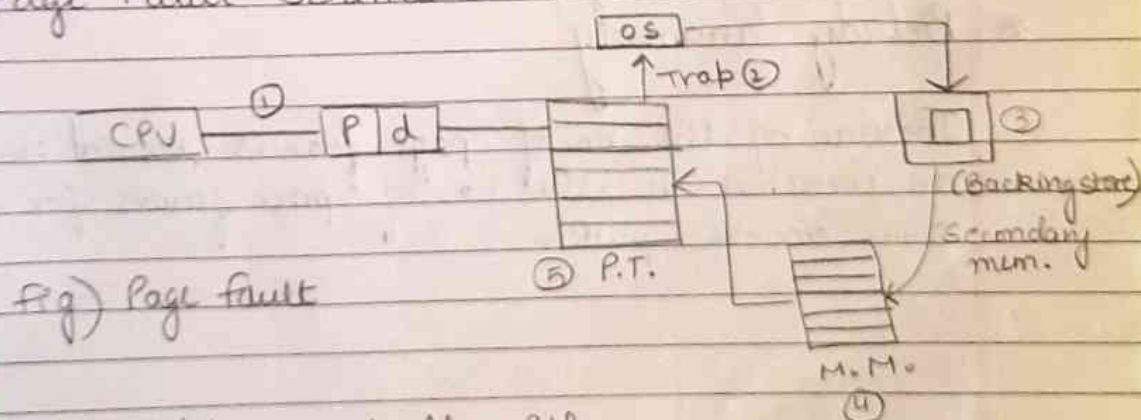
Types of paging (names online search)

Unit-5

Locality of Reference

Demand Paging and Page fault

The process of loading the pages into main mem. on demand.
Page Fault Scheme



Page replacement Algorithm
FIFO (first in first out)

Q1. Ref. string = 7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0
 ✓ 1 7 0 1

frame size = 4

Calculate no. of page faults.

Algo +IFO

frame size = 4				2	2	2	2	2	2	1	1	1	1	1		
			1	1	1	1	1	1	0	0	0	0	0	0		
		0	0	0	0	0	0	4	4	4	4	7	7	7		
	7	7	7	7	7	3	3	3	3	3	2	2	2	2		

* Page fault = 10

frame size = 3			1	1	1	0	0	0	3	3	3	2	2	2	1	
		0	0	0	3	3	3	2	2	2	1	1	1	0	0	
	7	7	7	2	2	2	4	4	4	0	0	0	0	7	7	

Page fault = 15

* Belady anomaly

Increasing the no. of page frames results in an increase in the no. of page faults for a given access pattern.