

WIA1002/ WIB1002

Data Structure

Sorting

Sorting

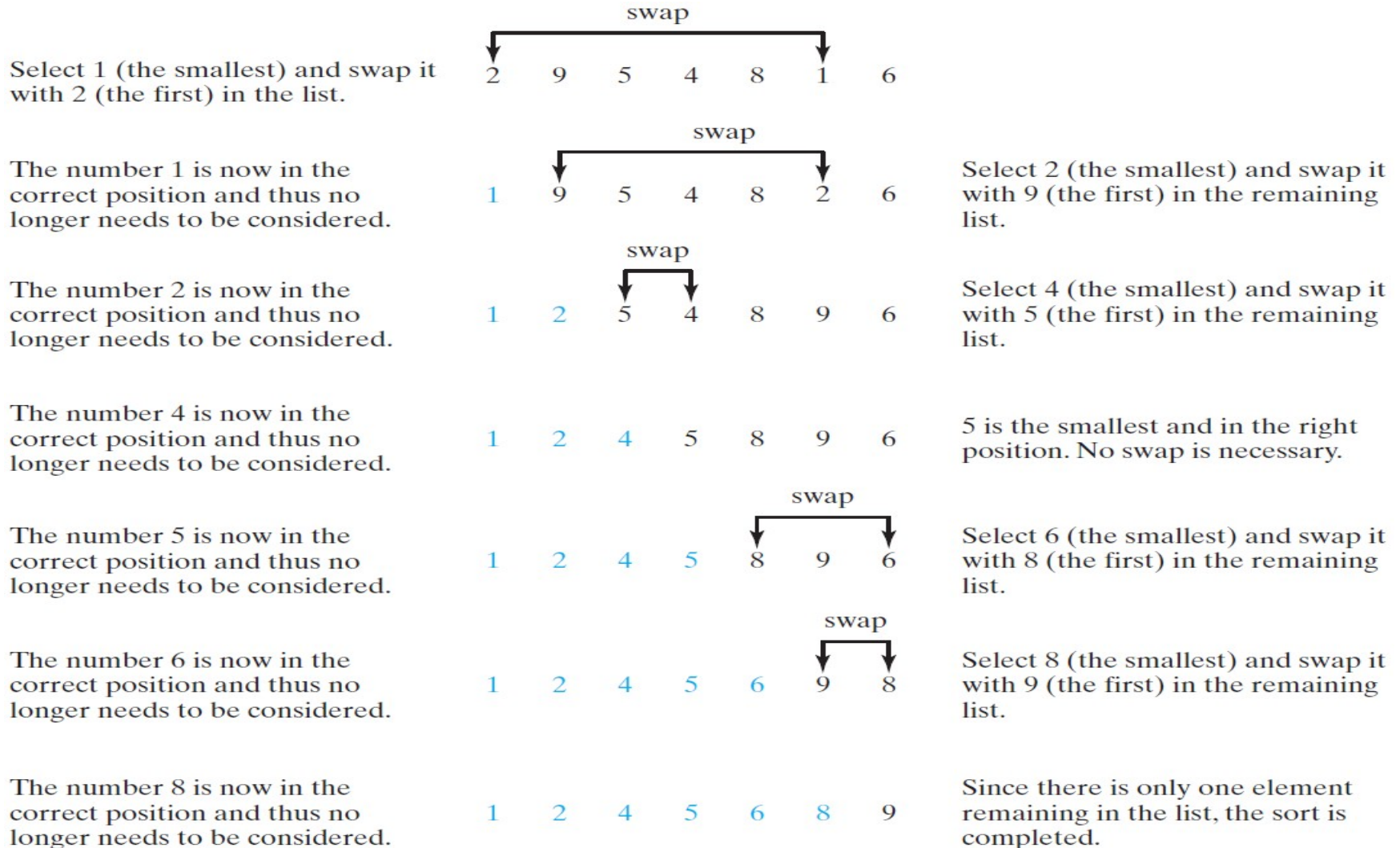
Sorting, like searching, is also a common task in computer programming.

Some sorting algorithms:

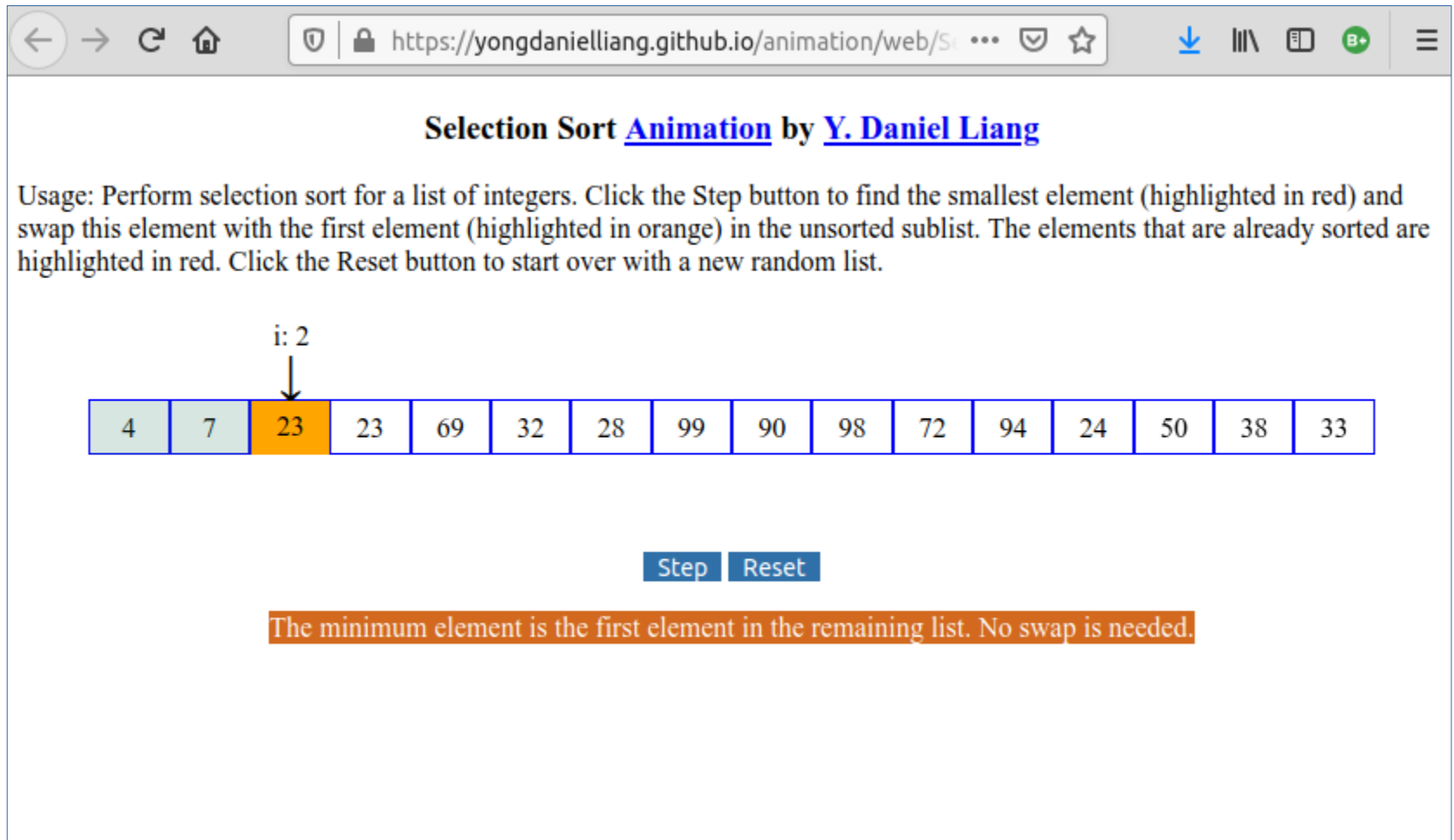
1. Selection sort
2. Insertion sort
3. Bubble sort
4. Merge Sort

Selection Sort

Selection sort finds the smallest number in the list and places it first. It then finds the smallest number remaining and places it second, and so on until the list contains only a single number.



Selection Sort Animation



Selection Sort [Animation](#) by [Y. Daniel Liang](#)

Usage: Perform selection sort for a list of integers. Click the Step button to find the smallest element (highlighted in red) and swap this element with the first element (highlighted in orange) in the unsorted sublist. The elements that are already sorted are highlighted in red. Click the Reset button to start over with a new random list.

i: 2

4	7	23	23	69	32	28	99	90	98	72	94	24	50	38	33
---	---	----	----	----	----	----	----	----	----	----	----	----	----	----	----

Step Reset

The minimum element is the first element in the remaining list. No swap is needed.

<https://yongdanielliang.github.io/animation/web/SelectionSortNew.html>

From Idea to Solution

```
for (int i = 0; i < list.length - 1; i++) {  
    select the smallest element in list[i..listSize-1];  
    swap the smallest with list[i], if necessary;  
    // list[i] is in its correct position.  
    // The next iteration applies on list[i+1..listSize-1]  
}
```

list[0]	list[1]	list[2]	list[3]	...	list[10]
list[0]	list[1]	list[2]	list[3]	...	list[10]
list[0]	list[1]	list[2]	list[3]	...	list[10]
list[0]	list[1]	list[2]	list[3]	...	list[10]
list[0]	list[1]	list[2]	list[3]	...	list[10]
					...
list[0]	list[1]	list[2]	list[3]	...	list[10]

```

/** The method for sorting the numbers */
public static void selectionSort(double[] list) {
    for (int i = 0; i < list.length - 1; i++) {
        // Find the minimum in the list[i..list.length-1]
        double currentMin = list[i];
        int currentMinIndex = i;
        for (int j = i + 1; j < list.length; j++) {
            if (currentMin > list[j]) {
                currentMin = list[j];
                currentMinIndex = j;
            }
        }

        // Swap list[i] with list[currentMinIndex] if necessary;
        if (currentMinIndex != i) {
            list[currentMinIndex] = list[i];
            list[i] = currentMin;
        }
    }
}

```

```

public class SelectionSort {
    /** The method for sorting the numbers */
    public static void selectionSort(double[] list) {
        for (int i = 0; i < list.length - 1; i++) {
            // Find the minimum in the list[i..list.length-1]
            double currentMin = list[i];
            int currentMinIndex = i;

            for (int j = i + 1; j < list.length; j++) {
                if (currentMin > list[j]) {
                    currentMin = list[j];
                    currentMinIndex = j;
                }
            }

            // Swap list[i] with list[currentMinIndex] if necessary;
            if (currentMinIndex != i) {
                list[currentMinIndex] = list[i];
                list[i] = currentMin;
            }
        }
    }

    public static void main(String[] args) {
        double[] list = {-2, 4.5, 5, 1, 2, -3.3};
        selectionSort(list);
        for (int i = 0; i < list.length; i++)
            System.out.print(list[i] + " ");
    }
}

```

Insertion Sort

```
int[] myList = {2, 9, 5, 4, 8, 1, 6}; // Unsorted
```

The insertion sort algorithm sorts a list of values by repeatedly inserting an unsorted element into a sorted sublist until the whole list is sorted.

Step 1: Initially, the sorted sublist contains the first element in the list. Insert 9 into the sublist.



Step2: The sorted sublist is {2, 9}. Insert 5 into the sublist.



Step 3: The sorted sublist is {2, 5, 9}. Insert 4 into the sublist.



Step 4: The sorted sublist is {2, 4, 5, 9}. Insert 8 into the sublist.



Step 5: The sorted sublist is {2, 4, 5, 8, 9}. Insert 1 into the sublist.



Step 6: The sorted sublist is {1, 2, 4, 5, 8, 9}. Insert 6 into the sublist.



Step 7: The entire list is now sorted.



Insertion Sort Animation



Insertion Sort [Animation](#) by [Y. Daniel Liang](#)

Usage: Perform insertion sort for a list of integers. click the Step button to insert the current element to a sorted sublist. Click the Reset button to start over with a new random list.

i: 1

11	92	98	63	56	22	79	23	70	2	57	44	1	23	67	35
----	----	----	----	----	----	----	----	----	---	----	----	---	----	----	----

Step Reset

Insert 11 to the 0th position.

<https://yongdanielliang.github.io/animation/web/InsertionSortNew.html>

Insertion Sort

```
int[] myList = {2, 9, 5, 4, 8, 1, 6}; // Unsorted
```

Insertion Sort

```
int[] myList = {2, 9, 5, 4, 8, 1, 6}; // Unsorted
```

2	9	5	4	8	1	6
---	---	---	---	---	---	---

Insertion Sort

```
int[] myList = {2, 9, 5, 4, 8, 1, 6}; // Unsorted
```

2	9	5	4	8	1	6
---	---	---	---	---	---	---

2	9	5	4	8	1	6
---	---	---	---	---	---	---

Insertion Sort

```
int[] myList = {2, 9, 5, 4, 8, 1, 6}; // Unsorted
```

2	9	5	4	8	1	6
---	---	---	---	---	---	---

2	9	5	4	8	1	6
---	---	---	---	---	---	---

2	5	9	4	8	1	6
---	---	---	---	---	---	---

Insertion Sort

```
int[] myList = {2, 9, 5, 4, 8, 1, 6}; // Unsorted
```

2	9	5	4	8	1	6
---	---	---	---	---	---	---

2	9	5	4	8	1	6
---	---	---	---	---	---	---

2	5	9	4	8	1	6
---	---	---	---	---	---	---

2	4	5	9	8	1	6
---	---	---	---	---	---	---

Insertion Sort

```
int[] myList = {2, 9, 5, 4, 8, 1, 6}; // Unsorted
```

2	9	5	4	8	1	6
---	---	---	---	---	---	---

2	9	5	4	8	1	6
---	---	---	---	---	---	---

2	5	9	4	8	1	6
---	---	---	---	---	---	---

2	4	5	9	8	1	6
---	---	---	---	---	---	---

2	4	5	8	9	1	6
---	---	---	---	---	---	---

Insertion Sort

```
int[] myList = {2, 9, 5, 4, 8, 1, 6}; // Unsorted
```

2	9	5	4	8	1	6
---	---	---	---	---	---	---

2	9	5	4	8	1	6
---	---	---	---	---	---	---

2	5	9	4	8	1	6
---	---	---	---	---	---	---

2	4	5	9	8	1	6
---	---	---	---	---	---	---

2	4	5	8	9	1	6
---	---	---	---	---	---	---

1	2	4	5	8	9	6
---	---	---	---	---	---	---

Insertion Sort

```
int[] myList = {2, 9, 5, 4, 8, 1, 6}; // Unsorted
```

2	9	5	4	8	1	6
---	---	---	---	---	---	---

2	9	5	4	8	1	6
---	---	---	---	---	---	---

2	5	9	4	8	1	6
---	---	---	---	---	---	---

2	4	5	9	8	1	6
---	---	---	---	---	---	---

2	4	5	8	9	1	6
---	---	---	---	---	---	---

1	2	4	5	8	9	6
---	---	---	---	---	---	---

1	2	4	5	6	8	9
---	---	---	---	---	---	---

How to Insert?

The insertion sort algorithm sorts a list of values by repeatedly inserting an unsorted element into a sorted sublist until the whole list is sorted.

list [0] [1] [2] [3] [4] [5] [6]
 [2 5 9 4]

Step 1: Save 4 to a temporary variable currentElement

list [0] [1] [2] [3] [4] [5] [6]
 [2 5 9]

Step 2: Move list[2] to list[3]

list [0] [1] [2] [3] [4] [5] [6]
 [2 5 9]

Step 3: Move list[1] to list[2]

list [0] [1] [2] [3] [4] [5] [6]
 [2 4 5 9]

Step 4: Assign currentElement to list[1]

From Idea to Solution

```
for (int i = 1; i < list.length; i++) {  
    insert list[i] into a sorted sublist list[0..i-1] so that  
    list[0..i] is sorted  
}
```

`list[0]`

`list[0] list[1]`

`list[0] list[1] list[2]`

`list[0] list[1] list[2] list[3]`

`list[0] list[1] list[2] list[3] ...`

From Idea to Solution

```
for (int i = 1; i < list.length; i++) {  
    insert list[i] into a sorted sublist list[0..i-1] so that  
    list[0..i] is sorted  
}
```



Expand

```
double currentElement = list[i];  
int k;  
for (k = i - 1; k >= 0 && list[k] > currentElement; k--) {  
    list[k + 1] = list[k];  
}  
// Insert the current element into list[k + 1]  
list[k + 1] = currentElement;
```

```

public class InsertionSort {
    public static void insertionSort(int[] list) {
        for (int i = 1; i < list.length; i++) {
            int currentElement = list[i];
            int k;
            for (k = i - 1; k >= 0 && list[k] > currentElement; k--) {
                list[k + 1] = list[k];
            }

            list[k + 1] = currentElement;
        }
    }

    public static void main(String[] args) {
        int[] list = {2, 3, 2, 5, 6, 1, -2, 3, 14, 12};
        insertionSort(list);
        for (int i = 0; i < list.length; i++)
            System.out.print(list[i] + " ");
    }
}

```

Bubble Sort

- ✦ The bubble sort algorithm makes several passes through the array.
- ▢ On each pass, successive neighboring pairs are compared. If a pair is in decreasing order, its values are swapped; otherwise, the values remain unchanged.
- ▢ The smaller values gradually “bubble” their way to the top and the larger values “sink” to the bottom.
- ▢ After the first pass, the last element becomes the largest in the array.
- ▢ After the second pass, the second-to-last element becomes the second largest in the array.
- ▢ This process is continued until all elements are sorted.

Bubble Sort

2 9 5 4 8 1	2 5 4 8 1 9	2 4 5 1 8 9	2 4 1 5 8 9	1 2 4 5 8 9
2 5 9 4 8 1	2 4 5 8 1 9	2 4 5 1 8 9	2 1 4 5 8 9	
2 5 4 9 8 1	2 4 5 8 1 9	2 4 1 5 8 9		
2 5 4 8 9 1	2 4 5 1 8 9			
2 5 4 8 1 9				
(a) 1st pass	(b) 2nd pass	(c) 3rd pass	(d) 4th pass	(e) 5th pass

Bubble Sort Animation

Usage: Perform bubble sort for a list of integers. click the Next button to move the index to the next position to perform a swap if necessary. Click the Reset button to start over with a new random list.

i: 2

11	64	30	65	34	20	53	10	17	88	48	52	37	2	62	91
----	----	----	----	----	----	----	----	----	----	----	----	----	---	----	----

Next Reset

Swap the current element with its next neighbor.

<https://yongdanielliang.github.io/animation/web/BubbleSortNew.html>

Algorithm: Bubble sort

```
1  for (int k = 1; k < list.length; k++) {  
2      // Perform the kth pass  
3      for (int i = 0; i < list.length - k; i++) {  
4          if (list[i] > list[i + 1])  
5              swap list[i] with list[i + 1];  
6      }  
7  }
```

Algorithm: Bubble sort

```
1  for (int k = 1; k < list.length; k++) {  
2      // Perform the kth pass  
3      for (int i = 0; i < list.length - k; i++) {  
4          if (list[i] > list[i + 1])  
5              swap list[i] with list[i + 1];  
6      }  
7  }
```

If no swap takes place in a pass, there is no need to perform the next pass, because all elements are sorted. So use, boolean operator to improve this algorithm.

Algorithm: Bubble sort

```
1  for (int k = 1; k < list.length; k++) {  
2      // Perform the kth pass  
3      for (int i = 0; i < list.length - k; i++) {  
4          if (list[i] > list[i + 1])  
5              swap list[i] with list[i + 1];  
6      }  
7  }
```

If no swap takes place in a pass, there is no need to perform the next pass, because all elements are sorted. So use, boolean operator to improve this algorithm.

```
1  boolean needNextPass = true;  
2  for (int k = 1; k < list.length && needNextPass; k++) {  
3      // Array may be sorted and next pass not needed  
4      needNextPass = false;  
5      // Perform the kth pass  
6      for (int i = 0; i < list.length - k; i++) {  
7          if (list[i] > list[i + 1]) {  
8              swap list[i] with list[i + 1];  
9              needNextPass = true; // Next pass still needed  
10         }  
11     }  
12 }
```

Algorithm: Bubble sort

```
1  for (int k = 1; k < list.length; k++) {
2      // Perform the kth pass
3      for (int i = 0; i < list.length - k; i++) {
4          if (list[i] > list[i + 1])
5              swap list[i] with list[i + 1];
6      }
7  }
```

If no swap takes place in a pass, there is no need to perform the next pass, because all elements are sorted. So use, boolean operator to improve this algorithm.

```
1  boolean needNextPass = true;
2  for (int k = 1; k < list.length && needNextPass; k++) {
3      // Array may be sorted and next pass not needed
4      needNextPass = false;
5      // Perform the kth pass
6      for (int i = 0; i < list.length - k; i++) {
7          if (list[i] > list[i + 1]) {
8              swap list[i] with list[i + 1];
9              needNextPass = true; // Next pass still needed
10         }
11     }
12 }
```

By default each iteration will set *needNextPass* to false

If swap still occurs it means that the list is not yet sort out
So we set the flag to true so that it will perform the next pass

```

public class BubbleSort {
    public static void bubbleSort(int[] list) {
        boolean needNextPass = true;
        for (int k = 1; k < list.length && needNextPass; k++) {
            needNextPass = false;
            for (int i = 0; i < list.length - k; i++) {
                if (list[i] > list[i + 1]) {
                    // Swap list[i] with list[i + 1]
                    int temp = list[i];
                    list[i] = list[i + 1];
                    list[i + 1] = temp;
                    needNextPass = true;
                }
            }
        }
    }

    /** A test method */
    public static void main(String[] args) {
        int[] list = {2, 3, 2, 5, 6, 1, -2, 3, 14, 12};
        bubbleSort(list);
        for (int i = 0; i < list.length; i++)
            System.out.print(list[i] + " ");
    }
}

```

Merge Sort

- ✦ can be described recursively as follows: divides the array into two halves and applies a merge sort on each half recursively. After the two halves are sorted, merge them.

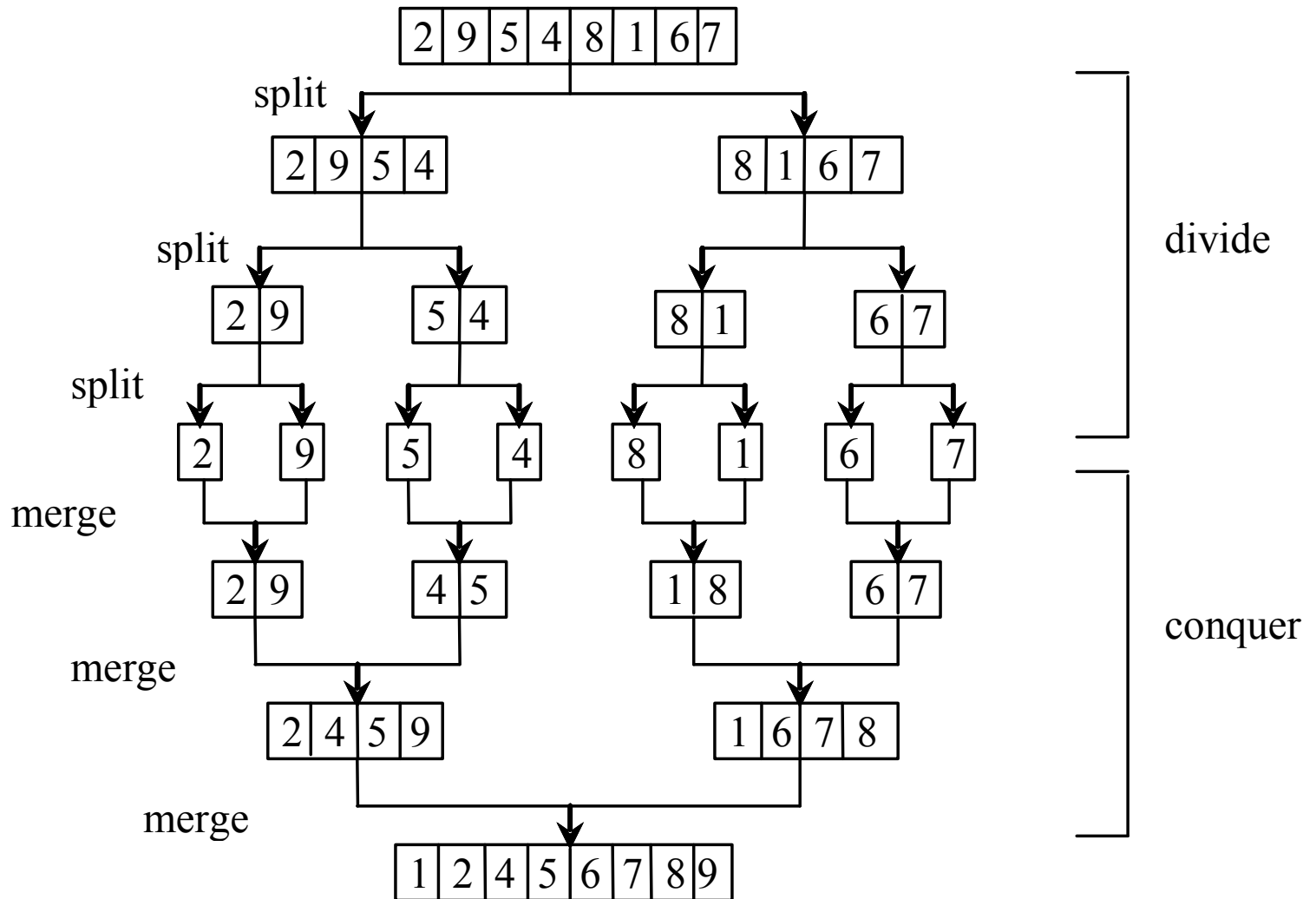
```
mergeSort(list) :  
    firstHalf = mergeSort(firstHalf);  
    secondHalf = mergeSort(secondHalf);  
    list = merge(firstHalf, secondHalf);
```

LISTING 23.5 Merge Sort Algorithm

```
1 public static void mergeSort(int[] list) {  
2     if (list.length > 1) {  
3         mergeSort(list[0 ... list.length / 2]);  
4         mergeSort(list[list.length / 2 + 1 ... list.length]);  
5         merge list[0 ... list.length / 2] with  
6         list[list.length / 2 + 1 ... list.length];  
7     }  
8 }
```

base condition
sort first half
sort second half
merge two halves

Merge Sort



Merging Two Sorted Lists

← → ↺ 🏠 <https://yongdanielliang.github.io/animation/web/MergeSort> ... 📄 🌟 ⚙️

Merge [Animation](#) by [Y. Daniel Liang](#)

Usage: Merge two sorted lists list1 and list2 into temp. Click the Step button to perform one comparison and move an element to temp. Click the Reset button to start over with two new random lists.

The screenshot shows the Merge Sort Animation web application. At the top, there is a browser address bar with the URL <https://yongdanielliang.github.io/animation/web/MergeSort>. Below the address bar, the title "Merge Animation by Y. Daniel Liang" is displayed. The usage instructions state: "Usage: Merge two sorted lists list1 and list2 into temp. Click the Step button to perform one comparison and move an element to temp. Click the Reset button to start over with two new random lists." The main visual area shows three arrays. The first array, labeled "current1", contains the values [15, 44, 47, 63, 76, 87, 90]. The second array, labeled "current2", contains the values [22, 22, 30, 51, 65, 82, 85]. The third array, labeled "current3", contains the values [15, 22, 22, 30, 44, 47, 51, followed by five empty slots]. The element 51 in the current3 array is highlighted in red. Below the arrays, there are two buttons: "Step" and "Reset". At the bottom, a status bar displays the text "Copy 51 from list2 to temp[6]."

current1	current2	current3
15	22	15
44	22	22
47	30	22
63	51	30
76	65	44
87	82	47
90	85	51

Step Reset

Copy 51 from list2 to temp[6].

<https://yongdanielliang.github.io/animation/web/MergeSortNew.html>

LISTING 23.6 MergeSort.java

```
1 public class MergeSort {
2     /** The method for sorting the numbers */
3     public static void mergeSort(int[] list) {
4         if (list.length > 1) {                                base case
5             // Merge sort the first half
6             int[] firstHalf = new int[list.length / 2];
7             System.arraycopy(list, 0, firstHalf, 0, list.length / 2);
8             mergeSort(firstHalf);                             sort first half
9
10            // Merge sort the second half
11            int secondHalfLength = list.length - list.length / 2;
12            int[] secondHalf = new int[secondHalfLength];
13            System.arraycopy(list, list.length / 2,
14                secondHalf, 0, secondHalfLength);
15            mergeSort(secondHalf);                             sort second half
16
17            // Merge firstHalf with secondHalf into list
18            merge(firstHalf, secondHalf, list);                merge two halves
19        }
20    }
21 }
```

```

22  /** Merge two sorted lists */
23  public static void merge(int[] list1, int[] list2, int[] temp) {
24      int current1 = 0; // Current index in list1
25      int current2 = 0; // Current index in list2
26      int current3 = 0; // Current index in temp
27
28      while (current1 < list1.length && current2 < list2.length) {
29          if (list1[current1] < list2[current2])
list1 to temp 30              temp[current3++] = list1[current1++];
31          else
list2 to temp 32              temp[current3++] = list2[current2++];
33      }
34
rest of list1 to temp 35      while (current1 < list1.length)
36          temp[current3++] = list1[current1++];
37
rest of list2 to temp 38      while (current2 < list2.length)
39          temp[current3++] = list2[current2++];
40      }
41
42  /** A test method */
43  public static void main(String[] args) {
44      int[] list = {2, 3, 2, 5, 6, 1, -2, 3, 14, 12};
45      mergeSort(list);
46      for (int i = 0; i < list.length; i++)
47          System.out.print(list[i] + " ");
48      }
49  }

```

Sort Phone List : generic sort

```
public class SortPhoneList {  
    // Creates an array of Contact objects, sorts them, then prints them.  
    public static void main(String[] args) {  
        Contact[] friends = new Contact[7];  
        friends[0] = new Contact("John", "Smith", "610-555-7384");  
        friends[1] = new Contact("Sarah", "Barnes", "215-555-3827");  
        friends[2] = new Contact("Mark", "Riley", "733-555-2969");  
        friends[3] = new Contact("Laura", "Getz", "663-555-3984");  
        friends[4] = new Contact("Larry", "Smith", "464-555-3489");  
        friends[5] = new Contact("Frank", "Phelps", "322-555-2284");  
        friends[6] = new Contact("Marsha", "Grant", "243-555-2837");  
  
        GenericSelectionSort.selectionSort(friends);  
        for (Contact friend : friends)  
            System.out.println(friend);  
  
        String[] strArray = {"B", "D", "A", "Z"};  
        GenericSelectionSort.selectionSort(strArray);  
        for (String str : strArray)  
            System.out.println(str);  
    }  
}
```

Sort Phone List : generic sort

```
Barnes, Sarah    215-555-3827
Getz, Laura 663-555-3984
Grant, Marsha    243-555-2837
Phelps, Frank    322-555-2284
Riley, Mark 733-555-2969
Smith, John 610-555-7384
Smith, Larry     464-555-3489
```

A

B

D

Z

Sort Phone List : generic sort

```
public class Contact implements Comparable<Contact>
{
    private String firstName, lastName, phone;
    public Contact(String first, String last, String telephone)
    {
        firstName = first;
        lastName = last;
        phone = telephone;
    }

    public String toString()
    {
        return lastName + ", " + firstName + "\t" + phone;
    }

    public int compareTo(Contact other)
    {
        int result;
        if (lastName.equals(other.lastName))
            result = firstName.compareTo(other.firstName);
        else
            result = lastName.compareTo(other.lastName);
        return result;
    }
}
```

Sort Phone List : generic sort

Modify the following SelectionSort to be a generic method

```
public static void selectionSort(double[] list) {  
    for (int i = 0; i < list.length - 1; i++) {  
        double currentMin = list[i];  
        int currentMinIndex = i;  
  
        for (int j = i + 1; j < list.length; j++) {  
            if (currentMin > list[j]) {  
                currentMin = list[j];  
                currentMinIndex = j;  
            }  
        }  
  
        if (currentMinIndex != i) {  
            list[currentMinIndex] = list[i];  
            list[i] = currentMin;  
        }  
    }  
}
```

Sort Phone List : generic sort

Modify the following SelectionSort to be a generic method

```
public static void selectionSort(double[] list) {  
    for (int i = 0; i < list.length - 1; i++) {  
        double currentMin = list[i];  
        int currentMinIndex = i;  
  
        for (int j = i + 1; j < list.length; j++) {  
            if (currentMin > list[j]) {  
                currentMin = list[j];  
                currentMinIndex = j;  
            }  
        }  
  
        if (currentMinIndex != i) {  
            list[currentMinIndex] = list[i];  
            list[i] = currentMin;  
        }  
    }  
}
```

Generic type that extends comparable

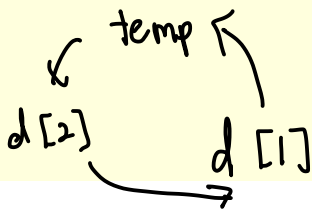
Comparable

Sort Phone List : generic sort

```
public class GenericSelectionSort {
    public static <T extends Comparable<T>> void selectionSort(T[] list)
    {
        for (int i = 0; i < list.length-1; i++) {
            T currentMin = list[i];
            int currentMinIndex = i;

            for (int j = i + 1; j < list.length; j++) {
                if (currentMin.compareTo(list[j]) > 0) {
                    currentMin = list[j];
                    currentMinIndex = j;
                }
            }
            swap(list, currentMinIndex, i);
        }
    }

    private static <T extends Comparable<T>> void swap(T[] data, int index1, int index2)
    {
        T temp = data[index1];
        data[index1] = data[index2];
        data[index2] = temp;
    }
}
```



References

Chapters 7 and 23, Liang, Introduction to Java Programming 10th edition,
Pearson 2015