



BSM307

İşaretler ve Sistemler

Dr. Seçkin Arı

z-Dönüşümü Özellikleri

- Doğrusallık
- Zamanda Öteleme
- z-Domeninde Ölçekleme
- Zamanda Ters Çevirme
- z-Domeninde Türev
- İki işaretin konvolüsyonu

Doğrusallık

- $x_1(n) \rightarrow X_1(z)$, YB1 ve $x_2(n) \rightarrow X_1(z)$, YB2

Doğrusallık

- $x_1(n) \rightarrow X_1(z)$, YB1 ve $x_2(n) \rightarrow X_2(z)$, YB2
- $x(n) = ax_1(n) + bx_2(n)$ ise

Doğrusallık

- $x_1(n) \rightarrow X_1(z)$, YB1 ve $x_2(n) \rightarrow X_2(z)$, YB2
- $x(n) = ax_1(n) + bx_2(n)$ ise
- $X(z) =$

Doğrusallık

- $x_1(n) \rightarrow X_1(z)$, YB1 ve $x_2(n) \rightarrow X_2(z)$, YB2
- $x(n) = ax_1(n) + bx_2(n)$ ise
- $X(z) = aX_1(z) + bX_2(z) \rightarrow$

Doğrusallık

- $x_1(n) \rightarrow X_1(z)$, YB1 ve $x_2(n) \rightarrow X_2(z)$, YB2
- $x(n) = ax_1(n) + bx_2(n)$ ise
- $X(z) = aX_1(z) + bX_2(z) \rightarrow YB: YB1 \cap YB2$

Örnek 1

- $x(n) = (3(2)^n - 4(3)^n)u(n) \rightarrow X(z) = ?$ ve YB=?

Örnek 1

- $x(n) = (3(2)^n - 4(3)^n)u(n) \rightarrow X(z) = ?$ ve YB=?
- $x(n) = 3(2)^n u(n) - 4(3)^n u(n)$

Örnek 1

- $x(n) = (3(2)^n - 4(3)^n)u(n) \rightarrow X(z) = ?$ ve YB=?
- $x(n) = 3 \underbrace{(2)^n u(n)}_{x_1(n)} - 4 \underbrace{(3)^n u(n)}_{x_2(n)}$

Örnek 1

- $x(n) = (3(2)^n - 4(3)^n)u(n) \rightarrow X(z) = ?$ ve YB=?
- $x(n) = 3 \underbrace{(2)^n u(n)}_{x_1(n)} - 4 \underbrace{(3)^n u(n)}_{x_2(n)}$
- $X_1(z) =$

Örnek 1

- $x(n) = (3(2)^n - 4(3)^n)u(n) \rightarrow X(z) = ?$ ve YB=?
- $x(n) = 3 \underbrace{(2)^n u(n)}_{x_1(n)} - 4 \underbrace{(3)^n u(n)}_{x_2(n)}$
- $X_1(z) = \frac{1}{1-2z^{-1}}, \text{ YB1: } |z|$

Örnek 1

- $x(n) = (3(2)^n - 4(3)^n)u(n) \rightarrow X(z) = ?$ ve YB=?
- $x(n) = 3 \underbrace{(2)^n u(n)}_{x_1(n)} - 4 \underbrace{(3)^n u(n)}_{x_2(n)}$
- $X_1(z) = \frac{1}{1-2z^{-1}}, \text{ YB1: } |z| > 2$

Örnek 1

- $x(n) = (3(2)^n - 4(3)^n)u(n) \rightarrow X(z) = ?$ ve YB=?
- $x(n) = 3 \underbrace{(2)^n u(n)}_{x_1(n)} - 4 \underbrace{(3)^n u(n)}_{x_2(n)}$
- $X_1(z) = \frac{1}{1-2z^{-1}}, \text{ YB1: } |z| > 2$
- $X_2(z) =$

Örnek 1

- $x(n) = (3(2)^n - 4(3)^n)u(n) \rightarrow X(z) = ?$ ve YB=?
- $x(n) = 3 \underbrace{(2)^n u(n)}_{x_1(n)} - 4 \underbrace{(3)^n u(n)}_{x_2(n)}$
- $X_1(z) = \frac{1}{1-2z^{-1}}, \text{ YB1: } |z| > 2$
- $X_2(z) = \frac{1}{1-3z^{-1}}, \text{ YB2: } |z|$

Örnek 1

- $x(n) = (3(2)^n - 4(3)^n)u(n) \rightarrow X(z) = ?$ ve YB=?
- $x(n) = 3 \underbrace{(2)^n u(n)}_{x_1(n)} - 4 \underbrace{(3)^n u(n)}_{x_2(n)}$
- $X_1(z) = \frac{1}{1-2z^{-1}}, \text{ YB1: } |z| > 2$
- $X_2(z) = \frac{1}{1-3z^{-1}}, \text{ YB2: } |z| > 3$
- $X(z) =$

Örnek 1

- $x(n) = (3(2)^n - 4(3)^n)u(n) \rightarrow X(z) = ?$ ve YB=?
- $x(n) = \underbrace{3(2)^n u(n)}_{x_1(n)} - \underbrace{4(3)^n u(n)}_{x_2(n)}$
- $X_1(z) = \frac{1}{1-2z^{-1}}, \text{ YB1: } |z| > 2$
- $X_2(z) = \frac{1}{1-3z^{-1}}, \text{ YB2: } |z| > 3$
- $X(z) = \frac{3}{1-2z^{-1}} - \frac{4}{1-3z^{-1}}, \text{ YB:}$

Örnek 1

- $x(n) = (3(2)^n - 4(3)^n)u(n) \rightarrow X(z) = ?$ ve YB = ?
- $x(n) = \underbrace{3(2)^n u(n)}_{x_1(n)} - \underbrace{4(3)^n u(n)}_{x_2(n)}$
- $X_1(z) = \frac{1}{1-2z^{-1}}, \text{ YB1: } |z| > 2$
- $X_2(z) = \frac{1}{1-3z^{-1}}, \text{ YB2: } |z| > 3$
- $X(z) = \frac{3}{1-2z^{-1}} - \frac{4}{1-3z^{-1}}, \text{ YB: } |z| > 2 \cap |z| > 3 \rightarrow$

Örnek 1

- $x(n) = (3(2)^n - 4(3)^n)u(n) \rightarrow X(z) = ?$ ve YB=?
- $x(n) = \underbrace{3(2)^n u(n)}_{x_1(n)} - \underbrace{4(3)^n u(n)}_{x_2(n)}$
- $X_1(z) = \frac{1}{1-2z^{-1}}, \text{ YB1: } |z| > 2$
- $X_2(z) = \frac{1}{1-3z^{-1}}, \text{ YB2: } |z| > 3$
- $X(z) = \frac{3}{1-2z^{-1}} - \frac{4}{1-3z^{-1}}, \text{ YB: } |z| > 2 \cap |z| > 3 \rightarrow |z| > 3$

Örnek 2

- $x(n) = \cos(\omega_0 n) u(n) \rightarrow X(z) = ?$ ve YB=?

Örnek 2

- $x(n) = \cos(\omega_0 n) u(n) \rightarrow X(z) = ?$ ve YB = ?
- $x(n) = \frac{e^{j\omega_0 n} + e^{-j\omega_0 n}}{2} u(n)$

Örnek 2

- $x(n) = \cos(\omega_0 n) u(n) \rightarrow X(z) = ?$ ve YB=?
- $x(n) = \frac{e^{j\omega_0 n} + e^{-j\omega_0 n}}{2} u(n) = \frac{1}{2} e^{j\omega_0 n} u(n) + \frac{1}{2} e^{-j\omega_0 n} u(n)$

Örnek 2

- $x(n) = \cos(\omega_0 n) u(n) \rightarrow X(z) = ?$ ve YB=?
- $x(n) = \frac{e^{j\omega_0 n} + e^{-j\omega_0 n}}{2} u(n) = \frac{1}{2} e^{j\omega_0 n} u(n) + \frac{1}{2} e^{-j\omega_0 n} u(n)$
- $x(n) = \frac{1}{2} \underbrace{e^{j\omega_0 n} u(n)}_{x_1(n)} + \frac{1}{2} \underbrace{e^{-j\omega_0 n} u(n)}_{x_2(n)}$
- $X_1(z) =$

Örnek 2

- $x(n) = \cos(\omega_0 n) u(n) \rightarrow X(z) = ?$ ve YB = ?
- $x(n) = \frac{e^{j\omega_0 n} + e^{-j\omega_0 n}}{2} u(n) = \frac{1}{2} e^{j\omega_0 n} u(n) + \frac{1}{2} e^{-j\omega_0 n} u(n)$
- $x(n) = \frac{1}{2} \underbrace{(e^{j\omega_0})^n u(n)}_{x_1(n)} + \frac{1}{2} \underbrace{(e^{-j\omega_0})^n u(n)}_{x_2(n)}$
- $X_1(z) =$

Örnek 2

- $x(n) = \cos(\omega_0 n) u(n) \rightarrow X(z) = ?$ ve YB=?
- $x(n) = \frac{e^{j\omega_0 n} + e^{-j\omega_0 n}}{2} u(n) = \frac{1}{2} e^{j\omega_0 n} u(n) + \frac{1}{2} e^{-j\omega_0 n} u(n)$
- $x(n) = \frac{1}{2} \underbrace{\left(e^{j\omega_0}\right)^n u(n)}_{x_1(n)} + \frac{1}{2} \underbrace{\left(e^{-j\omega_0}\right)^n u(n)}_{x_2(n)}$
- $X_1(z) = \frac{1}{1 - e^{j\omega_0} z^{-1}},$ YB1:

Örnek 2

- $x(n) = \cos(\omega_0 n) u(n) \rightarrow X(z) = ?$ ve YB = ?
- $x(n) = \frac{e^{j\omega_0 n} + e^{-j\omega_0 n}}{2} u(n) = \frac{1}{2} e^{j\omega_0 n} u(n) + \frac{1}{2} e^{-j\omega_0 n} u(n)$
- $x(n) = \frac{1}{2} \underbrace{(e^{j\omega_0})^n u(n)}_{x_1(n)} + \frac{1}{2} \underbrace{(e^{-j\omega_0})^n u(n)}_{x_2(n)}$
- $X_1(z) = \frac{1}{1 - e^{j\omega_0} z^{-1}}, \text{ YB1: } |z| > |e^{j\omega_0}| \rightarrow$

Örnek 2

- $x(n) = \cos(\omega_0 n) u(n) \rightarrow X(z) = ?$ ve YB = ?
- $x(n) = \frac{e^{j\omega_0 n} + e^{-j\omega_0 n}}{2} u(n) = \frac{1}{2} e^{j\omega_0 n} u(n) + \frac{1}{2} e^{-j\omega_0 n} u(n)$
- $x(n) = \frac{1}{2} \underbrace{(e^{j\omega_0})^n u(n)}_{x_1(n)} + \frac{1}{2} \underbrace{(e^{-j\omega_0})^n u(n)}_{x_2(n)}$
- $X_1(z) = \frac{1}{1 - e^{j\omega_0} z^{-1}},$ YB1: $|z| > |e^{j\omega_0}| \rightarrow |z| > 1$

Örnek 2

- $x(n) = \cos(\omega_0 n) u(n) \rightarrow X(z) = ?$ ve YB = ?
- $x(n) = \frac{1}{2} \underbrace{(e^{j\omega_0})^n u(n)}_{x_1(n)} + \frac{1}{2} \underbrace{(e^{-j\omega_0})^n u(n)}_{x_2(n)}$
- $X_1(z) = \frac{1}{1 - e^{j\omega_0} z^{-1}},$ YB1: $|z| > |e^{j\omega_0}| \rightarrow |z| > 1$
- $X_2(z) =$

Örnek 2

- $x(n) = \cos(\omega_0 n) u(n) \rightarrow X(z) = ?$ ve YB = ?
- $x(n) = \frac{1}{2} \underbrace{(e^{j\omega_0})^n u(n)}_{x_1(n)} + \frac{1}{2} \underbrace{(e^{-j\omega_0})^n u(n)}_{x_2(n)}$
- $X_1(z) = \frac{1}{1 - e^{j\omega_0} z^{-1}}$, YB1: $|z| > |e^{j\omega_0}| \rightarrow |z| > 1$
- $X_2(z) = \frac{1}{1 - e^{-j\omega_0} z^{-1}}$, YB2:

Örnek 2

- $x(n) = \cos(\omega_0 n) u(n) \rightarrow X(z) = ?$ ve YB = ?
- $x(n) = \frac{1}{2} \underbrace{(e^{j\omega_0})^n u(n)}_{x_1(n)} + \frac{1}{2} \underbrace{(e^{-j\omega_0})^n u(n)}_{x_2(n)}$
- $X_1(z) = \frac{1}{1 - e^{j\omega_0} z^{-1}}$, YB1: $|z| > |e^{j\omega_0}| \rightarrow |z| > 1$
- $X_2(z) = \frac{1}{1 - e^{-j\omega_0} z^{-1}}$, YB2: $|z| > |e^{-j\omega_0}| \rightarrow$

Örnek 2

- $x(n) = \cos(\omega_0 n) u(n) \rightarrow X(z) = ?$ ve YB = ?
- $x(n) = \frac{1}{2} \underbrace{(e^{j\omega_0})^n u(n)}_{x_1(n)} + \frac{1}{2} \underbrace{(e^{-j\omega_0})^n u(n)}_{x_2(n)}$
- $X_1(z) = \frac{1}{1 - e^{j\omega_0} z^{-1}},$ YB1: $|z| > |e^{j\omega_0}| \rightarrow |z| > 1$
- $X_2(z) = \frac{1}{1 - e^{-j\omega_0} z^{-1}},$ YB2: $|z| > |e^{-j\omega_0}| \rightarrow |z| > 1$
- $X(z) =$

Örnek 2

- $x(n) = \cos(\omega_0 n) u(n) \rightarrow X(z) = ?$ ve YB = ?
- $x(n) = \underbrace{\frac{1}{2} (e^{j\omega_0})^n u(n)}_{x_1(n)} + \underbrace{\frac{1}{2} (e^{-j\omega_0})^n u(n)}_{x_2(n)}$
- $X_1(z) = \frac{1}{1 - e^{j\omega_0} z^{-1}}, \text{ YB1: } |z| > |e^{j\omega_0}| \rightarrow |z| > 1$
- $X_2(z) = \frac{1}{1 - e^{-j\omega_0} z^{-1}}, \text{ YB2: } |z| > |e^{-j\omega_0}| \rightarrow |z| > 1$
- $X(z) = \frac{1}{2} \frac{1}{1 - e^{j\omega_0} z^{-1}} + \frac{1}{2} \frac{1}{1 - e^{-j\omega_0} z^{-1}}, \text{ YB: }$

Örnek 2

- $x(n) = \cos(\omega_0 n) u(n) \rightarrow X(z) = ?$ ve YB = ?
- $x(n) = \underbrace{\frac{1}{2} (e^{j\omega_0})^n u(n)}_{x_1(n)} + \underbrace{\frac{1}{2} (e^{-j\omega_0})^n u(n)}_{x_2(n)}$
- $X_1(z) = \frac{1}{1 - e^{j\omega_0} z^{-1}}, \text{ YB1: } |z| > |e^{j\omega_0}| \rightarrow |z| > 1$
- $X_2(z) = \frac{1}{1 - e^{-j\omega_0} z^{-1}}, \text{ YB2: } |z| > |e^{-j\omega_0}| \rightarrow |z| > 1$
- $X(z) = \frac{1}{2} \frac{1}{1 - e^{j\omega_0} z^{-1}} + \frac{1}{2} \frac{1}{1 - e^{-j\omega_0} z^{-1}}, \text{ YB: } |z| > 1$

Zamanda Öteleme

- $\mathcal{Z}\{x(n)\} = X(z)$ ve YB biliniyorsa

Zamanda Öteleme

- $\mathcal{Z}\{x(n)\} = X(z)$ ve YB biliniyorsa
- $\mathcal{Z}\{x(n - k)\} = z^{-k}X(z)$, YB

Zamanda Öteleme

- $\mathcal{Z}\{x(n)\} = X(z)$ ve YB biliniyorsa
- $\mathcal{Z}\{x(n - k)\} = z^{-k}X(z)$, YB $\cap \begin{cases} |z| \neq 0, & k > 0 \\ |z| \neq \infty, & k < 0 \end{cases}$

Örnek 3

- $x(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X(z) =$

Örnek 3

- $x(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB:}$

Örnek 3

- $x(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$

Örnek 3

- $x(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_1(n) = 4 \left(\frac{1}{2}\right)^n u(n - 2) \rightarrow X_1(z) =$

Örnek 3

- $x(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_1(n) = 4 \left(\frac{1}{2}\right)^n u(n-2) = \left(\frac{1}{2}\right)^{n-2} u(n-2) =$

Örnek 3

- $x(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_1(n) = 4 \left(\frac{1}{2}\right)^n u(n-2) = \left(\frac{1}{2}\right)^{n-2} u(n-2) = x(n-2)$
- $X_1(z) =$

Örnek 3

- $x(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_1(n) = 4 \left(\frac{1}{2}\right)^n u(n-2) = \left(\frac{1}{2}\right)^{n-2} u(n-2) = x(n-2)$
- $X_1(z) = z^{-2} X(z) = \frac{z^{-2}}{1 - \frac{1}{2}z^{-1}}, \text{ YB: }$

Örnek 3

- $x(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_1(n) = 4 \left(\frac{1}{2}\right)^n u(n-2) = \left(\frac{1}{2}\right)^{n-2} u(n-2) = x(n-2)$
- $X_1(z) = z^{-2}X(z) = \frac{z^{-2}}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$

Örnek 4

- $x(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_2(n) = \left(\frac{1}{2}\right)^n u(n - 2) \rightarrow X_2(z) =$

Örnek 4

- $x(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_2(n) = \left(\frac{1}{2}\right)^n u(n-2) = \frac{1}{4} \left(\frac{1}{2}\right)^{n-2} u(n-2) =$

Örnek 4

- $x(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_2(n) = \left(\frac{1}{2}\right)^n u(n-2) = \frac{1}{4} \left(\frac{1}{2}\right)^{n-2} u(n-2) = \frac{1}{4} x(n-2)$
- $X_2(z) =$

Örnek 4

- $x(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_2(n) = \left(\frac{1}{2}\right)^n u(n-2) = \frac{1}{4} \left(\frac{1}{2}\right)^{n-2} u(n-2) = \frac{1}{4} x(n-2)$
- $X_2(z) = \frac{1}{4} z^{-2} \frac{1}{1 - \frac{1}{2}z^{-1}} = \frac{\frac{1}{4}z^{-2}}{1 - \frac{1}{2}z^{-1}}, \text{ YB: }$

Örnek 4

- $x(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_2(n) = \left(\frac{1}{2}\right)^n u(n-2) = \frac{1}{4} \left(\frac{1}{2}\right)^{n-2} u(n-2) = \frac{1}{4} x(n-2)$
- $X_2(z) = \frac{1}{4} z^{-2} \frac{1}{1 - \frac{1}{2}z^{-1}} = \frac{\frac{1}{4}z^{-2}}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$

z-Domeninde Ölçekleme

- $\mathcal{Z}\{x(n)\} = X(z)$ ve YB: $b_2 < |z| < b_1$ biliniyorsa

z-Domeninde Ölçekleme

- $\mathcal{Z}\{x(n)\} = X(z)$ ve YB: $b_2 < |z| < b_1$ biliniyorsa
- $\mathcal{Z}\{a^n x(n)\} = X(a^{-1}z)$, YB: $|a|b_2 < |z| < |a|b_1$

Örnek 5

- $x(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_3(n) = (-4)^n \left(\frac{1}{2}\right)^n u(n)$
- $X_3(z) =$

Örnek 5

- $x(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_3(n) = (-4)^n \left(\frac{1}{2}\right)^n u(n) = (-4)^n x(n)$
- $X_3(z) =$

Örnek 5

- $x(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_3(n) = (-4)^n \left(\frac{1}{2}\right)^n u(n)$
- $X_3(z) = X\left(-\frac{1}{4}z\right) =$

Örnek 5

- $x(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_3(n) = (-4)^n \left(\frac{1}{2}\right)^n u(n)$
- $X_3(z) = X\left(-\frac{1}{4}z\right) = \frac{1}{1 + \frac{1}{2}4z^{-1}}$

Örnek 5

- $x(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_3(n) = (-4)^n \left(\frac{1}{2}\right)^n u(n)$
- $X_3(z) = X\left(-\frac{1}{4}z\right) = \frac{1}{1 + \frac{1}{2}4z^{-1}} = \frac{1}{1 + 2z^{-1}}, \text{ YB: }$

Örnek 5

- $x(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_3(n) = (-4)^n \left(\frac{1}{2}\right)^n u(n)$
- $X_3(z) = X\left(-\frac{1}{4}z\right) = \frac{1}{1 + \frac{1}{2}4z^{-1}} = \frac{1}{1 + 2z^{-1}}, \text{ YB: } |z| > 2$

Zamanda Ters Çevirme

- $\mathcal{Z}\{x(n)\} = X(z)$ ve YB: $b_2 < |z| < b_1$ biliniyorsa

Zamanda Ters Çevirme

- $\mathcal{Z}\{x(n)\} = X(z)$ ve YB: $b_2 < |z| < b_1$ biliniyorsa
- $\mathcal{Z}\{x(-n)\} = X(z^{-1})$ ve YB: $\frac{1}{b_1} < |z| < \frac{1}{b_2}$

Örnek 6

- $x(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_4(n) = (2)^n u(-n)$
- $X_4(z) =$

Örnek 6

- $x(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_4(n) = (2)^n u(-n) = x(-n)$
- $X_4(z) =$

Örnek 6

- $x(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_4(n) = (2)^n u(-n) = x(-n)$
- $X_4(z) = X(z^{-1})$

Örnek 6

- $x(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_4(n) = (2)^n u(-n) = x(-n)$
- $X_4(z) = X(z^{-1}) = \frac{1}{1 - \frac{1}{2}z}, \text{ YB: }$

Örnek 6

- $x(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_4(n) = (2)^n u(-n) = x(-n)$
- $X_4(z) = X(z^{-1}) = \frac{1}{1 - \frac{1}{2}z}, \text{ YB: } |z| < 2$

Örnek 7

- $x(n) = (2)^n u(-n + 3)$ ise $X(z) = ?$ ve YB=?

Örnek 7

- $x(n) = (2)^n u(-n + 3)$ ise $X(z) = ?$ ve YB=?
- 1. yol
- $x_1(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X_1(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$

Örnek 7

- $x(n) = (2)^n u(-n + 3)$ ise $X(z) = ?$ ve YB=?
- 1. yol
- $x_1(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X_1(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_2(n) = x_1(n + 3)$

Örnek 7

- $x(n) = (2)^n u(-n + 3)$ ise $X(z) = ?$ ve YB=?
- 1. yol
- $x_1(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X_1(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_2(n) = x_1(n + 3) = \left(\frac{1}{2}\right)^{n+3} u(n + 3) \rightarrow X_2(z) =$

Örnek 7

- $x(n) = (2)^n u(-n + 3)$ ise $X(z) = ?$ ve YB=?
- 1. yol
- $x_1(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X_1(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_2(n) = x_1(n + 3) = \left(\frac{1}{2}\right)^{n+3} u(n + 3) \rightarrow X_2(z) = z^3 X_1(z) = \frac{z^3}{1 - \frac{1}{2}z^{-1}}, \text{ YB: }$

Örnek 7

- $x(n) = (2)^n u(-n + 3)$ ise $X(z) = ?$ ve YB=?
- 1. yol
- $x_1(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X_1(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_2(n) = x_1(n + 3) = \left(\frac{1}{2}\right)^{n+3} u(n + 3) \rightarrow X_2(z) = z^3 X_1(z) = \frac{z^3}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_3(n) = x_2(-n)$

Örnek 7

- $x(n) = (2)^n u(-n + 3)$ ise $X(z) = ?$ ve YB=?
- 1. yol
- $x_1(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X_1(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_2(n) = x_1(n + 3) = \left(\frac{1}{2}\right)^{n+3} u(n + 3) \rightarrow X_2(z) = z^3 X_1(z) = \frac{z^3}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_3(n) = x_2(-n) = \left(\frac{1}{2}\right)^{-n+3} u(-n + 3) \rightarrow X_3(z) =$

Örnek 7

- $x(n) = (2)^n u(-n + 3)$ ise $X(z) = ?$ ve YB=?
- 1. yol
- $x_1(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X_1(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_2(n) = x_1(n + 3) = \left(\frac{1}{2}\right)^{n+3} u(n + 3) \rightarrow X_2(z) = z^3 X_1(z) = \frac{z^3}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_3(n) = x_2(-n) = \left(\frac{1}{2}\right)^{-n+3} u(-n + 3) \rightarrow X_3(z) = X_2(z^{-1}) = \frac{z^{-3}}{1 - \frac{1}{2}z}, \text{ YB: }$

Örnek 7

- $x(n) = (2)^n u(-n + 3)$ ise $X(z) = ?$ ve YB=?
- 1. yol
- $x_1(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X_1(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_2(n) = x_1(n + 3) = \left(\frac{1}{2}\right)^{n+3} u(n + 3) \rightarrow X_2(z) = z^3 X_1(z) = \frac{z^3}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_3(n) = x_2(-n) = \left(\frac{1}{2}\right)^{-n+3} u(-n + 3) \rightarrow X_3(z) = X_2(z^{-1}) = \frac{z^{-3}}{1 - \frac{1}{2}z}, \text{ YB: } |z| < 2$
- $x_3(n) = \left(\frac{1}{2}\right)^{-n+3} u(-n + 3) = \left(\frac{1}{2}\right)^3 (2)^n u(-n + 3) =$

Örnek 7

- $x(n) = (2)^n u(-n + 3)$ ise $X(z) = ?$ ve YB=?
- 1. yol
- $x_1(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X_1(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_2(n) = x_1(n + 3) = \left(\frac{1}{2}\right)^{n+3} u(n + 3) \rightarrow X_2(z) = z^3 X_1(z) = \frac{z^3}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_3(n) = x_2(-n) = \left(\frac{1}{2}\right)^{-n+3} u(-n + 3) \rightarrow X_3(z) = X_2(z^{-1}) = \frac{z^{-3}}{1 - \frac{1}{2}z}, \text{ YB: } |z| < 2$
- $x_3(n) = \left(\frac{1}{2}\right)^{-n+3} u(-n + 3) = \left(\frac{1}{2}\right)^3 (2)^n u(-n + 3) = \frac{1}{8} x(n)$
- $x(n) = 8x_3(n) \rightarrow X(z) =$

Örnek 7

- $x(n) = (2)^n u(-n + 3)$ ise $X(z) = ?$ ve YB=?
- 1. yol
- $x_1(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X_1(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_2(n) = x_1(n + 3) = \left(\frac{1}{2}\right)^{n+3} u(n + 3) \rightarrow X_2(z) = z^3 X_1(z) = \frac{z^3}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_3(n) = x_2(-n) = \left(\frac{1}{2}\right)^{-n+3} u(-n + 3) \rightarrow X_3(z) = X_2(z^{-1}) = \frac{z^{-3}}{1 - \frac{1}{2}z}, \text{ YB: } |z| < 2$
- $x_3(n) = \left(\frac{1}{2}\right)^{-n+3} u(-n + 3) = \left(\frac{1}{2}\right)^3 (2)^n u(-n + 3) = \frac{1}{8} x(n)$
- $x(n) = 8x_3(n) \rightarrow X(z) = 8X_3(z) = \frac{8z^{-3}}{1 - \frac{1}{2}z}, \text{ YB: }$

Örnek 7

- $x(n) = (2)^n u(-n + 3)$ ise $X(z) = ?$ ve YB=?
- 1. yol
- $x_1(n) = \left(\frac{1}{2}\right)^n u(n) \rightarrow X_1(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$
- $x_2(n) = x_1(n + 3) = \left(\frac{1}{2}\right)^{n+3} u(n + 3) \rightarrow X_2(z) = z^3 X_1(z) = \frac{z^3}{1 - \frac{1}{2}z^{-1}}, \text{ YB: } |z| > \frac{1}{2}$ Öteleme
- $x_3(n) = x_2(-n) = \left(\frac{1}{2}\right)^{-n+3} u(-n + 3) \rightarrow X_3(z) = X_2(z^{-1}) = \frac{z^{-3}}{1 - \frac{1}{2}z}, \text{ YB: } |z| < 2$ Ters çevirme
- $x_3(n) = \left(\frac{1}{2}\right)^{-n+3} u(-n + 3) = \left(\frac{1}{2}\right)^3 (2)^n u(-n + 3) = \frac{1}{8} x(n)$ Do rusallık özelli ini kullanılarak sonucu bulduk
- $x(n) = 8x_3(n) \rightarrow X(z) = 8X_3(z) = \frac{8z^{-3}}{1 - \frac{1}{2}z}, \text{ YB: } |z| < 2$

Örnek 7

- $x(n) = (2)^n u(-n + 3)$ ise $X(z) = ?$ ve YB=?
- 2. yol
- $x_1(n) = (2)^n u(-n - 1) \rightarrow X_1(z) =$

Örnek 7

- $x(n) = (2)^n u(-n + 3)$ ise $X(z) = ?$ ve YB=?
- 2. yol
- $x_1(n) = (2)^n u(-n - 1) \rightarrow X_1(z) = \frac{-1}{1-2z^{-1}}$, YB:

Örnek 7

- $x(n) = (2)^n u(-n + 3)$ ise $X(z) = ?$ ve YB=?
- 2. yol
- $x_1(n) = (2)^n u(-n - 1) \rightarrow X_1(z) = \frac{-1}{1-2z^{-1}}, \text{ YB: } |z| < 2$
- $x_2(n) = x_1(n - 4) =$

Örnek 7

- $x(n) = (2)^n u(-n + 3)$ ise $X(z) = ?$ ve YB=?
- 2. yol
- $x_1(n) = (2)^n u(-n - 1) \rightarrow X_1(z) = \frac{-1}{1-2z^{-1}}, \text{ YB: } |z| < 2$
- $x_2(n) = x_1(n - 4) = (2)^{n-4} u(-n + 3) \rightarrow X_2(z) =$

Örnek 7

- $x(n) = (2)^n u(-n + 3)$ ise $X(z) = ?$ ve YB=?
- 2. yol
- $x_1(n) = (2)^n u(-n - 1) \rightarrow X_1(z) = \frac{-1}{1-2z^{-1}}, \text{ YB: } |z| < 2$
- $x_2(n) = x_1(n - 4) = (2)^{n-4} u(-n + 3) \rightarrow X_2(z) = z^{-4} X_1(z) = \frac{-z^{-4}}{1-2z^{-1}}, \text{ YB: } |z| < 2$
- $x_2(n) = (2)^{-4} (2)^n u(-n + 3) =$

Örnek 7

- $x(n) = (2)^n u(-n + 3)$ ise $X(z) = ?$ ve YB=?
- 2. yol
- $x_1(n) = (2)^n u(-n - 1) \rightarrow X_1(z) = \frac{-1}{1-2z^{-1}}, \text{ YB: } |z| < 2$
- $x_2(n) = x_1(n - 4) = (2)^{n-4} u(-n + 3) \rightarrow X_2(z) = z^{-4} X_1(z) = \frac{-z^{-4}}{1-2z^{-1}}, \text{ YB: } |z| < 2$
- $x_2(n) = (2)^{-4} (2)^n u(-n + 3) = \frac{1}{16} x(n)$
- $x(n) = 16x_2(n) \rightarrow X(z) =$

Örnek 7

- $x(n) = (2)^n u(-n + 3)$ ise $X(z) = ?$ ve YB=?
- 2. yol
- $x_1(n) = (2)^n u(-n - 1) \rightarrow X_1(z) = \frac{-1}{1-2z^{-1}}, \text{ YB: } |z| < 2$
- $x_2(n) = x_1(n - 4) = (2)^{n-4} u(-n + 3) \rightarrow X_2(z) = z^{-4} X_1(z) = \frac{-z^{-4}}{1-2z^{-1}}, \text{ YB: } |z| < 2$
- $x_2(n) = (2)^{-4} (2)^n u(-n + 3) = \frac{1}{16} x(n)$
- $x(n) = 16x_2(n) \rightarrow X(z) = 16X_2(z) = \frac{-16z^{-4}}{1-2z^{-1}}, \text{ YB: }$

Örnek 7

- $x(n) = (2)^n u(-n + 3)$ ise $X(z) = ?$ ve YB=?
- 2. yol
- $x_1(n) = (2)^n u(-n - 1) \rightarrow X_1(z) = \frac{-1}{1-2z^{-1}}, \text{ YB: } |z| < 2$
- $x_2(n) = x_1(n - 4) = (2)^{n-4} u(-n + 3) \rightarrow X_2(z) = z^{-4} X_1(z) = \frac{-z^{-4}}{1-2z^{-1}}, \text{ YB: } |z| < 2$
- $x_2(n) = (2)^{-4} (2)^n u(-n + 3) = \frac{1}{16} x(n)$
- $x(n) = 16x_2(n) \rightarrow X(z) = 16X_2(z) = \frac{-16z^{-4}}{1-2z^{-1}}, \text{ YB: } |z| < 2$

z-Domeninde Türev

- $\mathcal{Z}\{x(n)\} = X(z)$ ve YB: $b_2 < |z| < b_1$ biliniyorsa
- $\mathcal{Z}\{nx(n)\} = -z \frac{\partial X(z)}{\partial z}$, YB: $b_2 < |z| < b_1$

Örnek 8

- $x(n) = n(2)^n u(-n + 3)$ ise $X(z) = ?$ ve YB=?
- 2. yol
- $x_1(n) = (2)^n u(-n - 1) \rightarrow X_1(z) = \frac{-1}{1-2z^{-1}}, \text{ YB: } |z| < 2$
- $x_2(n) = x_1(n - 4) = (2)^{n-4} u(-n + 3)$
- $X_2(z) = z^{-4} X_1(z) = \frac{-z^{-4}}{1-2z^{-1}}, \text{ YB: } |z| < 2$
- $x_2(n) = (2)^{-4} (2)^n u(-n + 3) = \frac{1}{16} x_3(n)$
- $x_3(n) = 16x_2(n) \rightarrow X_3(z) = 16X_2(z) = \frac{-16z^{-4}}{1-2z^{-1}}, \text{ YB: } |z| < 2$
- $x(n) = nx_3(n) \rightarrow X(z) =$

Örnek 8

- $x(n) = n(2)^n u(-n + 3)$ ise $X(z) = ?$ ve YB=?
- 2. yol
- $x_1(n) = (2)^n u(-n - 1) \rightarrow X_1(z) = \frac{-1}{1-2z^{-1}}, \text{ YB: } |z| < 2$
- $x_2(n) = x_1(n - 4) = (2)^{n-4} u(-n + 3)$
- $X_2(z) = z^{-4} X_1(z) = \frac{-z^{-4}}{1-2z^{-1}}, \text{ YB: } |z| < 2$
- $x_2(n) = (2)^{-4} (2)^n u(-n + 3) = \frac{1}{16} x_3(n)$
- $x_3(n) = 16x_2(n) \rightarrow X_3(z) = 16X_2(z) = \frac{-16z^{-4}}{1-2z^{-1}}, \text{ YB: } |z| < 2$
- $x(n) = nx_3(n) \rightarrow X(z) = -z \frac{\partial X_3(z)}{\partial z} = -z \frac{\partial}{\partial z} \left(\frac{-16z^{-4}}{1-2z^{-1}} \right) =$

Örnek 8

- $x(n) = n(2)^n u(-n + 3)$ ise $X(z) = ?$ ve YB=?
- 2. yol
- $x_1(n) = (2)^n u(-n - 1) \rightarrow X_1(z) = \frac{-1}{1-2z^{-1}}, \text{ YB: } |z| < 2$
- $x_2(n) = x_1(n - 4) = (2)^{n-4} u(-n + 3)$
- $X_2(z) = z^{-4} X_1(z) = \frac{-z^{-4}}{1-2z^{-1}}, \text{ YB: } |z| < 2$
- $x_2(n) = (2)^{-4} (2)^n u(-n + 3) = \frac{1}{16} x_3(n)$
- $x_3(n) = 16x_2(n) \rightarrow X_3(z) = 16X_2(z) = \frac{-16z^{-4}}{1-2z^{-1}}, \text{ YB: } |z| < 2$
- $x(n) = nx_3(n) \rightarrow X(z) = -z \frac{\partial X_3(z)}{\partial z} = -z \frac{\partial}{\partial z} \left(\frac{-16z^{-4}}{1-2z^{-1}} \right) = \frac{106z^{-5} - 64z^{-4}}{(1-2z^{-1})^2}, \text{ YB: }$

Örnek 8

- $x(n) = n(2)^n u(-n + 3)$ ise $X(z) = ?$ ve YB=?
- 2. yol
- $x_1(n) = (2)^n u(-n - 1) \rightarrow X_1(z) = \frac{-1}{1-2z^{-1}}, \text{ YB: } |z| < 2$
- $x_2(n) = x_1(n - 4) = (2)^{n-4} u(-n + 3)$
- $X_2(z) = z^{-4} X_1(z) = \frac{-z^{-4}}{1-2z^{-1}}, \text{ YB: } |z| < 2$
- $x_2(n) = (2)^{-4} (2)^n u(-n + 3) = \frac{1}{16} x_3(n)$
- $x_3(n) = 16x_2(n) \rightarrow X_3(z) = 16X_2(z) = \frac{-16z^{-4}}{1-2z^{-1}}, \text{ YB: } |z| < 2$
- $x(n) = nx_3(n) \rightarrow X(z) = -z \frac{\partial X_3(z)}{\partial z} = -z \frac{\partial}{\partial z} \left(\frac{-16z^{-4}}{1-2z^{-1}} \right) = \frac{106z^{-5} - 64z^{-4}}{(1-2z^{-1})^2}, \text{ YB: } |z| < 2$

Örnek 9

- $x(n) = |n| \left(\frac{1}{2}\right)^{|n|}$ ise $X(z) = ?$ Ve YB=?

Örnek 9

- $x(n) = |n| \left(\frac{1}{2}\right)^{|n|}$ ise $X(z) = ?$ ve YB=?
- $x(n) = n \left(\frac{1}{2}\right)^n u(n) + \dots$

Örnek 9

- $x(n) = |n| \left(\frac{1}{2}\right)^{|n|}$ ise $X(z) = ?$ ve YB=?
- $x(n) = n \underbrace{\left(\frac{1}{2}\right)^n u(n)}_{x_1(n)} - n(2)^n u(-n - 1)$
- $X_1(z) =$

Örnek 9

- $x(n) = |n| \left(\frac{1}{2}\right)^{|n|}$ ise $X(z) = ?$ ve YB=?
- $x(n) = n \underbrace{\left(\frac{1}{2}\right)^n u(n)}_{x_1(n)} - n(2)^n u(-n - 1)$
- $X_1(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}$, YB1:

Örnek 9

- $x(n) = |n| \left(\frac{1}{2}\right)^{|n|}$ ise $X(z) = ?$ ve YB=?
- $x(n) = \underbrace{n \left(\frac{1}{2}\right)^n u(n)}_{x_1(n)} + \underbrace{n \left(-(2)^n u(-n - 1)\right)}_{x_2(n)}$
- $X_1(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}$, YB1: $|z| > \frac{1}{2}$
- $X_2(z) =$

Örnek 9

- $x(n) = |n| \left(\frac{1}{2}\right)^{|n|}$ ise $X(z) = ?$ ve YB=?
- $x(n) = \underbrace{n \left(\frac{1}{2}\right)^n u(n)}_{x_1(n)} + \underbrace{n \left(-(2)^n u(-n - 1)\right)}_{x_2(n)}$
- $X_1(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}$, YB1: $|z| > \frac{1}{2}$
- $X_2(z) = \frac{1}{1 - 2z^{-1}}$, YB2:

Örnek 9

- $x(n) = |n| \left(\frac{1}{2}\right)^{|n|}$ ise $X(z) = ?$ ve YB=?
- $x(n) = \underbrace{n \left(\frac{1}{2}\right)^n u(n)}_{x_1(n)} + \underbrace{n \left(-(2)^n u(-n - 1)\right)}_{x_2(n)}$
- $X_1(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}$, YB1: $|z| > \frac{1}{2}$
- $X_2(z) = \frac{1}{1 - 2z^{-1}}$, YB2: $|z| < 2$

Örnek 9

- $x(n) = |n| \left(\frac{1}{2}\right)^{|n|}$ ise $X(z) = ?$ ve YB=?
- $X_1(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}$, YB1: $|z| > \frac{1}{2}$
- $X_2(z) = \frac{1}{1 - 2z^{-1}}$, YB2: $|z| < 2$
- $x(n) = nx_1(n) + nx_2(n)$
- $X(z) =$

Örnek 9

- $x(n) = |n| \left(\frac{1}{2}\right)^{|n|}$ ise $X(z) = ?$ ve YB=?
- $X_1(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}$, YB1: $|z| > \frac{1}{2}$
- $X_2(z) = \frac{1}{1 - 2z^{-1}}$, YB2: $|z| < 2$
- $x(n) = nx_1(n) + nx_2(n)$
- $$X(z) = -z \frac{\partial}{\partial z} \left(\frac{1}{1 - \frac{1}{2}z^{-1}} \right) - z \frac{\partial}{\partial z} \left(\frac{1}{1 - 2z^{-1}} \right) = \frac{\frac{1}{2}z^{-1}}{\left(1 - \frac{1}{2}z^{-1}\right)^2} + \frac{2z^{-1}}{(1 - 2z^{-1})^2}$$
- YB:

Örnek 9

- $x(n) = |n| \left(\frac{1}{2}\right)^{|n|}$ ise $X(z) = ?$ ve YB=?
- $X_1(z) = \frac{1}{1 - \frac{1}{2}z^{-1}}$, YB1: $|z| > \frac{1}{2}$
- $X_2(z) = \frac{1}{1 - 2z^{-1}}$, YB2: $|z| < 2$
- $x(n) = nx_1(n) + nx_2(n)$
- $$X(z) = -z \frac{\partial}{\partial z} \left(\frac{1}{1 - \frac{1}{2}z^{-1}} \right) - z \frac{\partial}{\partial z} \left(\frac{1}{1 - 2z^{-1}} \right) = \frac{\frac{1}{2}z^{-1}}{\left(1 - \frac{1}{2}z^{-1}\right)^2} + \frac{2z^{-1}}{(1 - 2z^{-1})^2}$$
- YB: $|z| > \frac{1}{2} \cap |z| < 2 \equiv \frac{1}{2} < |z| < 2$

Örnek 10

- $x(n) = \frac{1}{n}u(n-1)$ ise $X(z) = ?$ ve YB: ?

Örnek 10

- $x(n) = \frac{1}{n}u(n-1)$ ise $X(z) = ?$ ve YB: ?
- $nx(n) = u(n-1)$

Örnek 10

- $x(n) = \frac{1}{n}u(n-1)$ ise $X(z) = ?$ ve YB: ?
- $\mathcal{Z}\{nx(n)\} = \mathcal{Z}\{u(n-1)\}$

Örnek 10

- $x(n) = \frac{1}{n}u(n-1)$ ise $X(z) = ?$ ve YB: ?
- $\mathcal{Z}\{nx(n)\} = \mathcal{Z}\{u(n-1)\}$
- $-z \frac{\partial X(z)}{\partial z} =$

Örnek 10

- $x(n) = \frac{1}{n}u(n-1)$ ise $X(z) = ?$ ve YB: ?
- $\mathcal{Z}\{nx(n)\} = \mathcal{Z}\{u(n-1)\}$
- $-z \frac{\partial X(z)}{\partial z} = \frac{z^{-1}}{1-z^{-1}} \rightarrow \frac{\partial X(z)}{\partial z} = -\frac{z^{-2}}{1-z^{-1}}$

Örnek 10

- $x(n) = \frac{1}{n}u(n-1)$ ise $X(z) = ?$ ve YB: ?
- $\mathcal{Z}\{nx(n)\} = \mathcal{Z}\{u(n-1)\}$
- $-z \frac{\partial X(z)}{\partial z} = \frac{z^{-1}}{1-z^{-1}} \rightarrow \frac{\partial X(z)}{\partial z} = -\frac{z^{-2}}{1-z^{-1}}$
- $X(z) =$

Örnek 10

- $x(n) = \frac{1}{n}u(n-1)$ ise $X(z) = ?$ ve YB: ?
- $\mathcal{Z}\{nx(n)\} = \mathcal{Z}\{u(n-1)\}$
- $-z \frac{\partial X(z)}{\partial z} = \frac{z^{-1}}{1-z^{-1}} \rightarrow \frac{\partial X(z)}{\partial z} = -\frac{z^{-2}}{1-z^{-1}}$
- $X(z) = \int \frac{\partial X(z)}{\partial z} = -\int \frac{z^{-2}}{1-z^{-1}} =$

Örnek 10

- $x(n) = \frac{1}{n}u(n-1)$ ise $X(z) = ?$ ve YB: ?
- $\mathcal{Z}\{nx(n)\} = \mathcal{Z}\{u(n-1)\}$
- $-z \frac{\partial X(z)}{\partial z} = \frac{z^{-1}}{1-z^{-1}} \rightarrow \frac{\partial X(z)}{\partial z} = -\frac{z^{-2}}{1-z^{-1}}$
- $X(z) = \int \frac{\partial X(z)}{\partial z} = -\int \frac{z^{-2}}{1-z^{-1}} = -\log(1-z^{-1})$
- YB:

Örnek 10

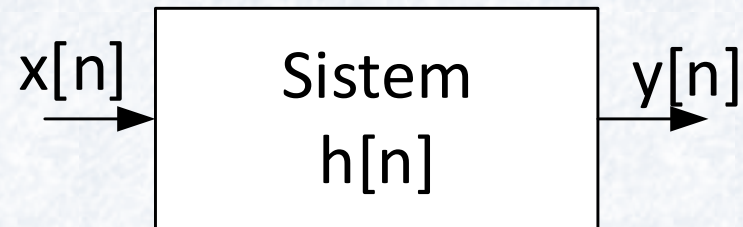
- $x(n) = \frac{1}{n}u(n-1)$ ise $X(z) = ?$ ve YB: ?
- $\mathcal{Z}\{nx(n)\} = \mathcal{Z}\{u(n-1)\}$
- $-z \frac{\partial X(z)}{\partial z} = \frac{z^{-1}}{1-z^{-1}} \rightarrow \frac{\partial X(z)}{\partial z} = -\frac{z^{-2}}{1-z^{-1}}$
- $X(z) = \int \frac{\partial X(z)}{\partial z} = -\int \frac{z^{-2}}{1-z^{-1}} = -\log(1-z^{-1})$
- YB: $|z| > 1$

Konvolüsyon

- $\mathcal{Z}\{x_1(n)\} = X_1(z)$ ve YB1 biliniyorsa
- $\mathcal{Z}\{x_2(n)\} = X_2(z)$ ve YB2 biliniyorsa
- $\mathcal{Z}\{x_1(n) * x_2(n)\} = X_1(z)X_2(z),$
 - ♦ YB: Paydadaki çarpanlara bağlı

Konvolüsyon

- $\mathcal{Z}\{x_1(n)\} = X_1(z)$ ve YB1 biliniyorsa
- $\mathcal{Z}\{x_2(n)\} = X_2(z)$ ve YB2 biliniyorsa
- $\mathcal{Z}\{x_1(n) * x_2(n)\} = X_1(z)X_2(z)$, YB: YB1 \cap YB2

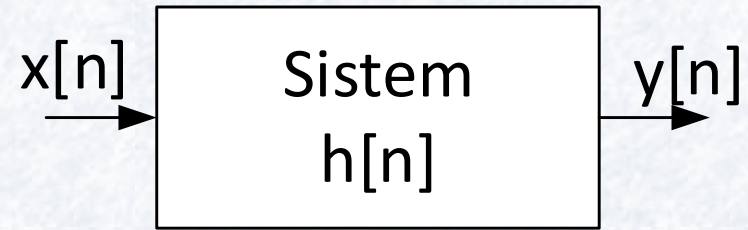


- $y(n) =$

Konvolüsyon

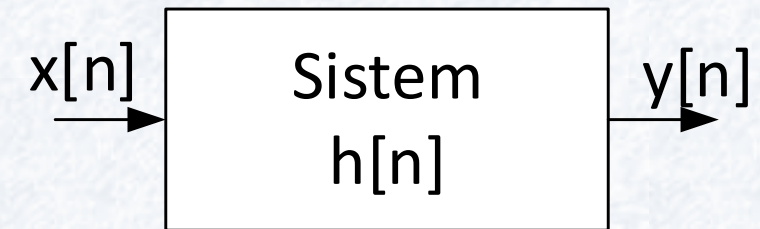
- $\mathcal{Z}\{x_1(n)\} = X_1(z)$ ve YB1 biliniyorsa
- $\mathcal{Z}\{x_2(n)\} = X_2(z)$ ve YB2 biliniyorsa
- $\mathcal{Z}\{x_1(n) * x_2(n)\} = X_1(z)X_2(z)$
 - ♦ YB: Paydadaki çarpanlara bağlı $YB1 \cap YB2$

- $y(n) = x(n) * h(n)$
- $Y(z) =$



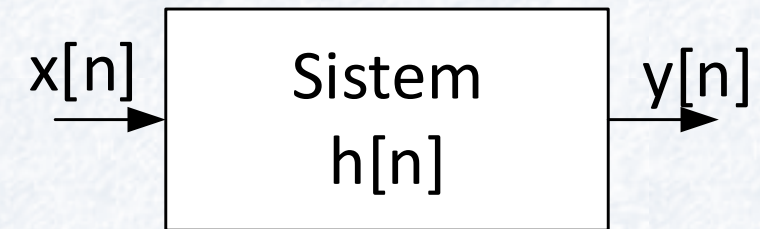
Konvolüsyon

- $\mathcal{Z}\{x_1(n)\} = X_1(z)$ ve YB1 biliniyorsa
- $\mathcal{Z}\{x_2(n)\} = X_2(z)$ ve YB2 biliniyorsa
- $\mathcal{Z}\{x_1(n) * x_2(n)\} = X_1(z)X_2(z)$
 - ♦ YB: Paydadaki çarpanlara bağlı $YB1 \cap YB2$
- $y(n) = x(n) * h(n)$
- $Y(z) = X(z)H(z)$



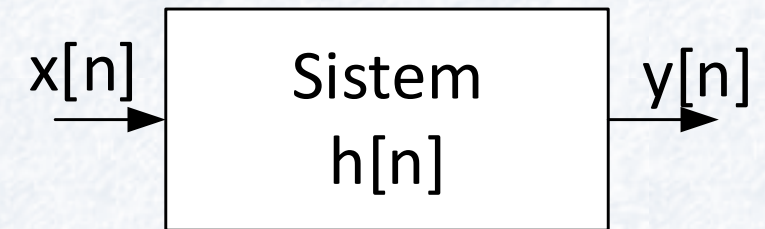
Konvolüsyon

- $\mathcal{Z}\{x_1(n)\} = X_1(z)$ ve YB1 biliniyorsa
- $\mathcal{Z}\{x_2(n)\} = X_2(z)$ ve YB2 biliniyorsa
- $\mathcal{Z}\{x_1(n) * x_2(n)\} = X_1(z)X_2(z)$
 - ♦ YB: Paydadaki çarpanlara bağlı $YB1 \cap YB2$
- $y(n) = x(n) * h(n)$
- $Y(z) = X(z)H(z)$
- $H(z) = \frac{Y(z)}{X(z)}$, Transfer Fonksiyonu



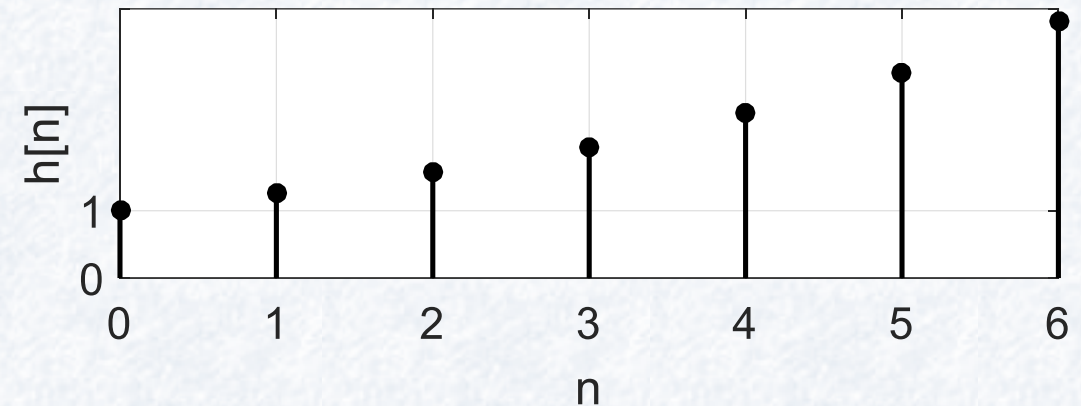
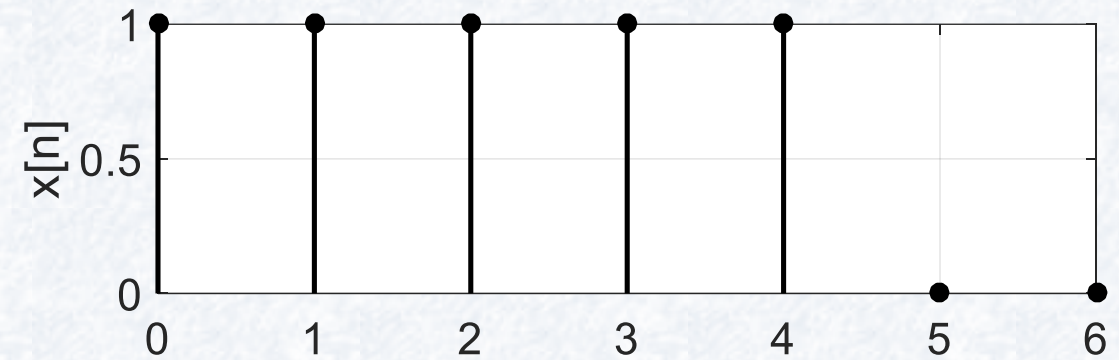
Konvolüsyon

- $\mathcal{Z}\{x_1(n)\} = X_1(z)$ ve YB1 biliniyorsa
- $\mathcal{Z}\{x_2(n)\} = X_2(z)$ ve YB2 biliniyorsa
- $\mathcal{Z}\{x_1(n) * x_2(n)\} = X_1(z)X_2(z)$
 - ♦ YB: Paydadaki çarpanlara bağlı YB1 \cap YB2
- $y(n) = x(n) * h(n)$
- $Y(z) = X(z)H(z)$
- $H(z) = \frac{Y(z)}{X(z)}$, Transfer Fonksiyonu
 - ♦ YB: Paydadaki çarpanlara bağlıdır.



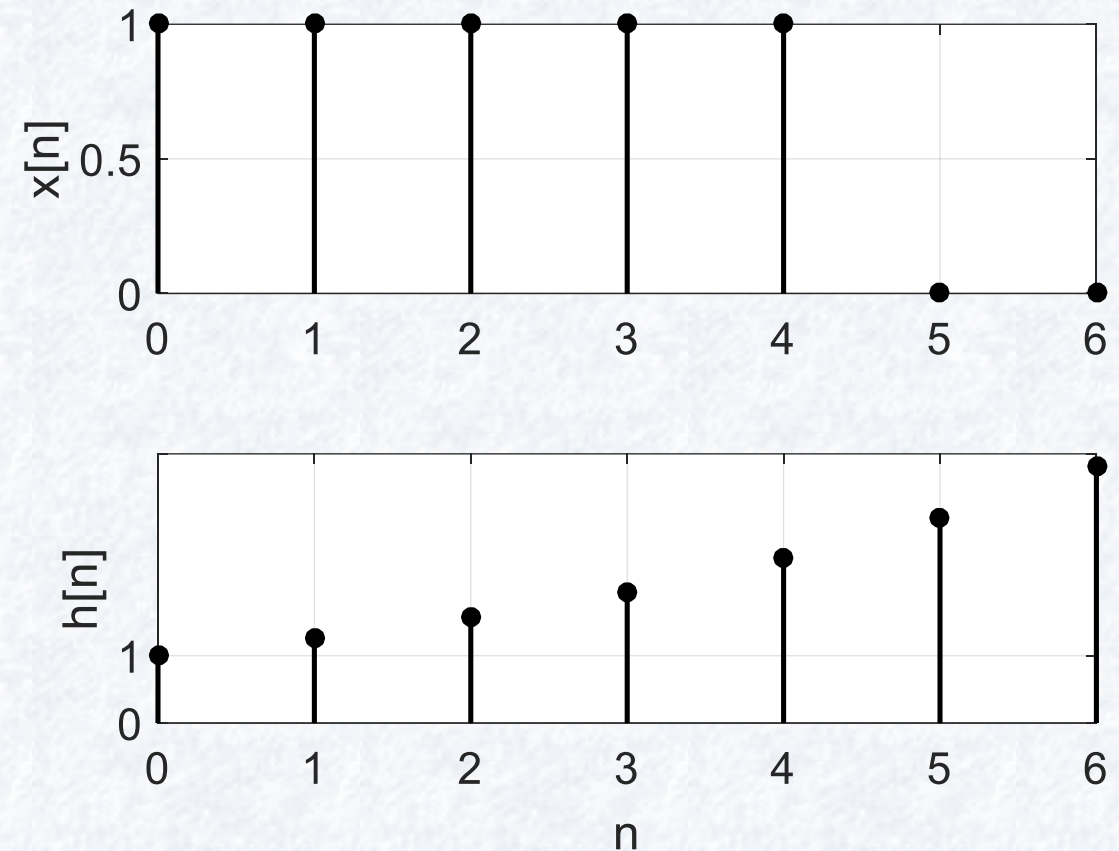
Örnek 11

- $x[n] = \begin{cases} 1, & 0 \leq n \leq 4 \\ 0, & \text{diğer} \end{cases}$
- $h[n] = \begin{cases} \alpha^n, & 0 \leq n \leq 6 \\ 0, & \text{diğer} \end{cases}$
- $Y(z) = ?$



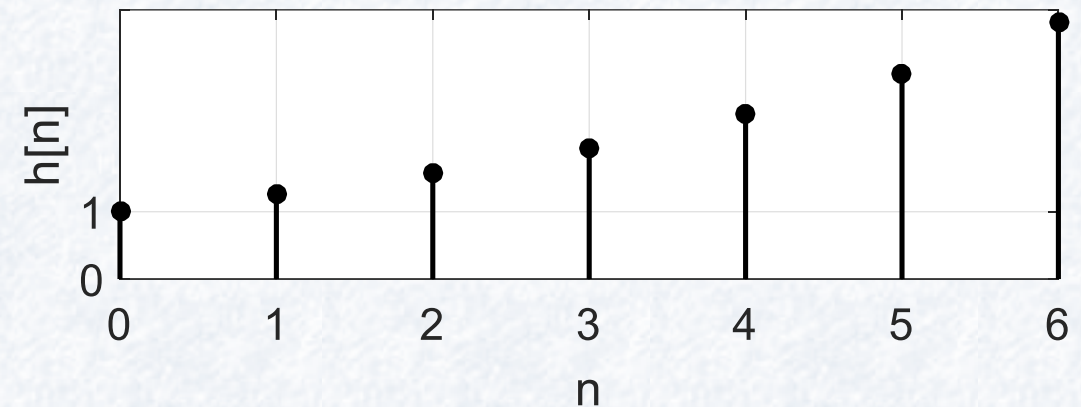
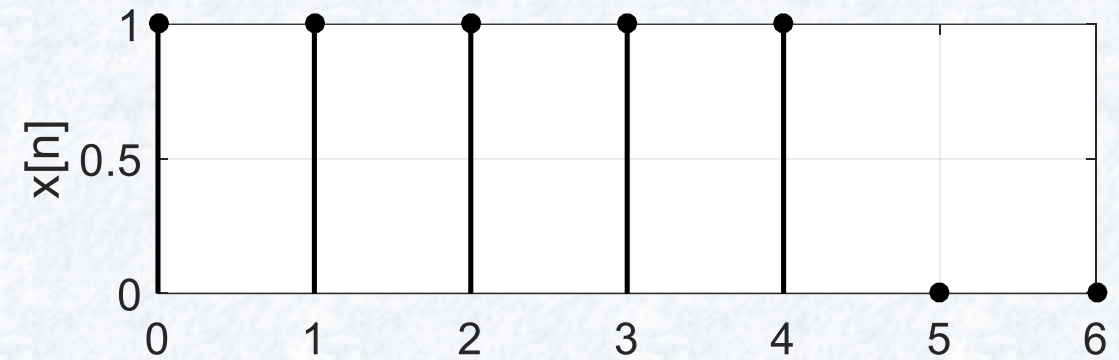
Örnek 11

- $x[n] = \begin{cases} 1, & 0 \leq n \leq 4 \\ 0, & \text{diğer} \end{cases}$
- $h[n] = \begin{cases} \alpha^n, & 0 \leq n \leq 6 \\ 0, & \text{diğer} \end{cases}$
- $Y(z) = X(z)H(z)$
- $X(z) = ?$



Örnek 11

- $x[n] = \begin{cases} 1, & 0 \leq n \leq 4 \\ 0, & \text{diğer} \end{cases}$
- $h[n] = \begin{cases} \alpha^n, & 0 \leq n \leq 6 \\ 0, & \text{diğer} \end{cases}$
- $Y(z) = X(z)H(z)$
- $X(z) = \sum_{n=0}^4 1z^{-n} =$



Örnek 12

- $x[n] = \begin{cases} 1, & 0 \leq n \leq 4 \\ 0, & \text{diğer} \end{cases}$
- $h[n] = \begin{cases} \alpha^n, & 0 \leq n \leq 6 \\ 0, & \text{diğer} \end{cases}$
- $Y(z) = X(z)H(z)$
- $X(z) = \sum_{n=0}^4 1z^{-n} = 1 + z^{-1} + z^{-2} + z^{-3} + z^{-4}$ YB:
- $H(z) = ?$

Örnek 12

- $x[n] = \begin{cases} 1, & 0 \leq n \leq 4 \\ 0, & \text{diğer} \end{cases}$
- $h[n] = \begin{cases} \alpha^n, & 0 \leq n \leq 6 \\ 0, & \text{diğer} \end{cases}$
- $Y(z) = X(z)H(z)$
- $X(z) = \sum_{n=0}^4 1z^{-n} = 1 + z^{-1} + z^{-2} + z^{-3} + z^{-4}$, YB: $|z| \neq 0$
- $H(z) = ?$

Örnek 12

- $x[n] = \begin{cases} 1, & 0 \leq n \leq 4 \\ 0, & \text{diğer} \end{cases}$
- $h[n] = \begin{cases} \alpha^n, & 0 \leq n \leq 6 \\ 0, & \text{diğer} \end{cases}$
- $Y(z) = X(z)H(z)$
- $X(z) = \sum_{n=0}^4 1z^{-n} = 1 + z^{-1} + z^{-2} + z^{-3} + z^{-4} = \frac{1-z^{-5}}{1-z^{-1}}, \text{ YB: } |z| \neq 0$
- $H(z) = \sum_{n=0}^6 \alpha^n z^{-n} =$

Örnek 12

- $x[n] = \begin{cases} 1, & 0 \leq n \leq 4 \\ 0, & \text{diğer} \end{cases}$
- $h[n] = \begin{cases} \alpha^n, & 0 \leq n \leq 6 \\ 0, & \text{diğer} \end{cases}$
- $Y(z) = X(z)H(z)$
- $X(z) = \sum_{n=0}^4 1z^{-n} = 1 + z^{-1} + z^{-2} + z^{-3} + z^{-4} = \frac{1-z^{-5}}{1-z^{-1}}, \text{ YB: } |z| \neq 0$
- $H(z) = \sum_{n=0}^6 \alpha^n z^{-n} = 1 + \alpha z^{-1} + \alpha^2 z^{-2} + \dots + \alpha^6 z^{-6} =$
 - ♦ YB:

Örnek 12

- $x[n] = \begin{cases} 1, & 0 \leq n \leq 4 \\ 0, & \text{diğer} \end{cases}$
- $h[n] = \begin{cases} \alpha^n, & 0 \leq n \leq 6 \\ 0, & \text{diğer} \end{cases}$
- $Y(z) = X(z)H(z)$
- $X(z) = \sum_{n=0}^4 1z^{-n} = 1 + z^{-1} + z^{-2} + z^{-3} + z^{-4} = \frac{1-z^{-5}}{1-z^{-1}}, \text{ YB: } |z| \neq 0$
- $H(z) = \sum_{n=0}^6 \alpha^n z^{-n} = 1 + \alpha z^{-1} + \alpha^2 z^{-2} + \dots + \alpha^6 z^{-6} =$
 - ♦ YB: $|z| \neq 0$

Örnek 12

- $x[n] = \begin{cases} 1, & 0 \leq n \leq 4 \\ 0, & \text{diğer} \end{cases}$
- $h[n] = \begin{cases} \alpha^n, & 0 \leq n \leq 6 \\ 0, & \text{diğer} \end{cases}$
- $Y(z) = X(z)H(z)$
- $X(z) = \sum_{n=0}^4 1z^{-n} = 1 + z^{-1} + z^{-2} + z^{-3} + z^{-4} = \frac{1-z^{-5}}{1-z^{-1}}, \text{ YB: } |z| \neq 0$
- $H(z) = \sum_{n=0}^6 \alpha^n z^{-n} = 1 + \alpha z^{-1} + \alpha^2 z^{-2} + \dots + \alpha^6 z^{-6} = \frac{1-(\alpha z^{-1})^7}{1-\alpha z^{-1}}$
 - ♦ YB: $|z| \neq 0$

Örnek 12

- $x[n] = \begin{cases} 1, & 0 \leq n \leq 4 \\ 0, & \text{diğer} \end{cases}$
- $h[n] = \begin{cases} \alpha^n, & 0 \leq n \leq 6 \\ 0, & \text{diğer} \end{cases}$
- $Y(z) = X(z)H(z)$
- $X(z) = \sum_{n=0}^4 1z^{-n} = 1 + z^{-1} + z^{-2} + z^{-3} + z^{-4} = \frac{1-z^{-5}}{1-z^{-1}}$
- $H(z) = \sum_{n=0}^6 \alpha^n z^{-n} = 1 + \alpha z^{-1} + \alpha^2 z^{-2} + \dots + \alpha^6 z^{-6} = \frac{1-(\alpha z^{-1})^7}{1-\alpha z^{-1}}$
- $Y(z) = \frac{1-z^{-5}}{1-z^{-1}} \frac{1-(\alpha z^{-1})^7}{1-\alpha z^{-1}} = \frac{1-z^{-5}-\alpha^7 z^{-7}+\alpha^7 z^{-12}}{(1-z^{-1})(1-\alpha z^{-1})}$

Örnek 12

- $x[n] = \begin{cases} 1, & 0 \leq n \leq 4 \\ 0, & \text{diğer} \end{cases}$
- $h[n] = \begin{cases} \alpha^n, & 0 \leq n \leq 6 \\ 0, & \text{diğer} \end{cases}$
- $Y(z) = X(z)H(z)$
- $X(z) = \sum_{n=0}^4 1z^{-n} = 1 + z^{-1} + z^{-2} + z^{-3} + z^{-4} = \frac{1-z^{-5}}{1-z^{-1}}$
- $H(z) = \sum_{n=0}^6 \alpha^n z^{-n} = 1 + \alpha z^{-1} + \alpha^2 z^{-2} + \dots + \alpha^6 z^{-6} = \frac{1-(\alpha z^{-1})^7}{1-\alpha z^{-1}}$
- $Y(z) = \frac{1-z^{-5}}{1-z^{-1}} \frac{1-(\alpha z^{-1})^7}{1-\alpha z^{-1}} = \frac{1-z^{-5}-\alpha^7 z^{-7}+\alpha^7 z^{-12}}{(1-z^{-1})(1-\alpha z^{-1})}, \text{ YB: } |z| \neq 0$