

Introduction to Algorithm Design

HW5 Report

Question 1:

In this part I design a dynamic programming algorithm that takes values for n , M , and sequences of operating costs " $N_1 \dots N_n$ " and " $S_1 \dots S_n$ ", and returns the cost of an optimal plan. First I create 2 array which size is equal to N and S and assign 0 all element of these arrays. After that I checked other citys (cost + M) is smaller than the current city cost. If its small assign other city cost + M to array. This calculation continue to end of list. End of the for loop we find optimal plan and return that value.

Complexity :

There is one loop in function. This function turns n time for every input so its time complexity is $O(n)$

Question 2:

In this part function take 2 array, one of them is start hour, the other one is finish hour of sessions. First I sort two array according to finish hours array. After that I start from first index of start array. If the sessions start time is equals or greater then the previous session finish time, I print it on screen.

Complexity :

I use python sort so it takes $O(n \log n)$ time to sort the sessions according to finish time. There is one loop in alorithm. This loop turn n time and each takes constant time. So complexity is $O(n + n \log n) \Rightarrow O(n \log n)$.

Question 3:

In this algorithm I search for subarray which is sum equal to zero. Find all subset algorithm complexity is $O(2^n)$. So I design dynamic algorithm. In this algorithm function stop the program when it finds the sum.

Complexity :

Time complexity of this algorithm is $O(n * \text{sum})$

n = number of the element

sum = sum of all the element.

Question 4:**Complexity**

x = first strings length

y = second strings length

For loop turns $x * y$ times. While loop turn $x + y$ times in worst case. Time complexity is $O(x*y)$.

Question 5:

I create two array for calculation. Because it can changeable for negative values. I append all items of input array to these two array for checking their signs. After that I start a while loop for sum these two arrays elements. After that loop I start another loop to finish array elements. At the end we find min operation number.

Complexity :

I use python sort so it takes $O(n \log n)$ time to sort the sessions according to finish time. T_m . While loop turns n time. N is size of array. So complexity is $O(n + n \log n) \Rightarrow O(n \log n)$.