

United International University

Department of Computer Science and Engineering CSE 2233 - Theory of Computation, Term Final Exam, Fall 2020

Total Marks: 25, Time: 1 hour 15 minutes

Answer all the questions

1. Consider the following context-free language:

[2+3]

- $L = \{w_1 \, a^{3n} \, b^{2n} \, c^m \mid \, w_1 \, \text{represents any binary string, } m = \text{length of string } w_1 \, \text{and } n >= 0\}$
- a) Define context-free grammar (CFG) for the language L.
- b) Design a pushdown automaton (PDA) for the language L.
- 2. Consider the following context-free grammar, G₁:

[5]

```
V = { E, F, A, C }

Σ = { +, -, (, ), x, y, z, *, %, 0, 1 }

R = {

E → E + E | E - E | (E) | F,

F → x | y | z | A,

A → A * A | A % A | C,

C → 0 | 1

}

Start variable = E
```

Now using parse tree decide the ambiguity of this grammar G_1 for the string (0%1*1) – z

3. Convert the following context-free grammar into Chomsky Normal Form (show each step clearly):

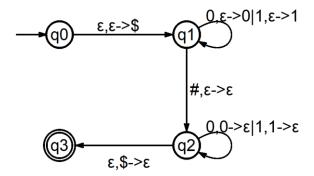
[5]

```
V = \{ S, A \}
\Sigma = \{ 0, 1 \}
R = \{
S \rightarrow 0S1 \mid A
A \rightarrow 1A0 \mid S \mid \varepsilon
\}
Start variable = S
```

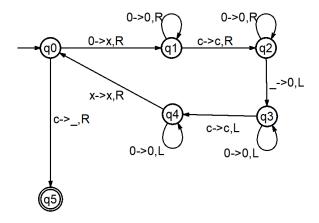
4. Show instantaneous description (show each step) for the following PDA and sample input 011#110

 $L = \{ w \# w^R \mid w \text{ is any binary string and } w^R \text{ is the reverse string of } w \}$

[5]



5. Consider the following state diagram of a Turing Machine:



Now check the acceptability of string **00c0** for the above TM. (show each configuration strings step by step)