

fourier_assignment.py X

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1  import cv2 # for finding contours to extract points of figure
2  import matplotlib.pyplot as plt # for plotting and creating figures
3  import numpy as np # for easy and fast number calculation
4  from math import tau # tau is constant number = 2*PI
5  from scipy.integrate import quad_vec # for calculating definite integral
6  from tqdm import tqdm # for progress bar
7  import matplotlib.animation as animation # for compiling animation and exporting video
8
9  # function to generate x+iy at given time t
10 def f(t, t_list, x_list, y_list):
11     return np.interp(t, t_list, x_list + 1j*y_list)
12
13 # reading the image and converting to greyscale mode
14 img = cv2.imread("bangladesh_input.jpg")
15 img = cv2.resize(img, (500,500))
16 cv2.imshow('Input Colored Image', img)
17 cv2.waitKey(0)
18 cv2.destroyAllWindows()
19 img_gray = cv2.cvtColor(img, cv2.COLOR_BGR2GRAY)
20 cv2.imshow('Grey Image', img_gray)
21 cv2.imwrite("bangladesh_grey.jpg", img_gray)
22 cv2.waitKey(0)
23 cv2.destroyAllWindows()
24
25 # finding the contours in the image
26 # making pure black and white image
27 ret, thresh = cv2.threshold(img_gray, 127, 255, 0)
28 # finding available contours i.e closed loop objects
29 contours, hierarchy = cv2.findContours(thresh, cv2.RETR_TREE, cv2.CHAIN_APPROX_NONE)
30 # contour at index 1 is the one looking for
31 contours = np.array(contours[1])
32
33 # displaying the contours on the original image
34 cv2.drawContours(img, contours, -1, (0,255,0), 3)
35 cv2.imshow('Contours', img)
36 cv2.imwrite("bangladesh_contours.jpg", img)
37 cv2.waitKey(0)
38 cv2.destroyAllWindows()
39
40 # splitting the co-ordinate points of the contour
41 # reshaping this to make it 1D array
42 x_list, y_list = contours[:, :, 0].reshape(-1,), -contours[:, :, 1].reshape(-1,)
43
44 # centering the contour to origin
45 x_list = x_list - np.mean(x_list)
46 y_list = y_list - np.mean(y_list)
47
48 # visualizing the contour
49 fig = plt.figure()
50 ax = fig.add_subplot(111)
51 ax.plot(x_list, y_list)
52
53 # later these data will be needed to fix the size of figure
54 xlim_data = plt.xlim()
55 ylim_data = plt.ylim()
56 plt.show()
57

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58 # time data from 0 to 2*PI as x,y is the function of time
59 t_list = np.linspace(0, tau, len(x_list))
60 # now we can relate f(t) -> x,y
61
62 # Now finding fourier coefficient from -n to n circles
63 # ..., c-3, c-2, c-1, c0, c1, c2, c3, ...
64 order = 100 # -order to order i.e -100 to 100
65
66 print("generating coefficients ...")
67 # computing fourier coefficients from -order to order
68 c = []
69 pbar = tqdm(total=(order*2+1))
70 # calculating the coefficients from -order to order
71 for n in range(-order, order+1):
72     # calculating definite integration from 0 to 2*PI using formula
73     coef = 1/tau*quad_vec(lambda t: f(t, t_list, x_list, y_list)*np.exp(-n*t*1j), 0, tau, limit=100,
74     c.append(coef)
75     pbar.update(1)
76 pbar.close()
77 print("completed generating coefficients.")
78
79 # converting list into numpy array
80 c = np.array(c)
81
82 # saving the coefficients for later use
83 np.save("coeff.npy", c)
84
85 ## -- now to making animation with epicycle -- ##
86
87 # this is to store the points of last circle of epicycle which draws the required figure
88 draw_x, draw_y = [], []
89
90 # making figure for animation
91 fig, ax = plt.subplots()
92
93 # different plots to make epicycle
94 # there are -order to order numbers of circles
95 circles = [ax.plot([], [], 'r-')[0] for i in range(-order, order+1)]
96 # circle_lines are radius of each circles
97 circle_lines = [ax.plot([], [], 'b-')[0] for i in range(-order, order+1)]
98 # drawing is plot of final drawing
99 drawing = ax.plot([], [], 'k-', linewidth=2)
100
101 # original drawing
102 orig_drawing = ax.plot([], [], 'g-', linewidth=0.5)
103
104 # to fix the size of figure so that the figure does not get cropped/trimmed
105 ax.set_xlim(xlim_data[0]-200, xlim_data[1]+200)
106 ax.set_ylim(ylim_data[0]-200, ylim_data[1]+200)
107
108 # hiding axes
109 ax.set_axis_off()
110
111 # to have symmetric axes
112 ax.set_aspect('equal')
113
114 # setting up formatting for the video file
115 Writer = animation.writers['ffmpeg']
116 writer = Writer(fps=30, metadata=dict(artist='Amrit Aryal'), bitrate=1800)
117 print("compiling animation ...")
118 # setting number of frames
119 frames = 300
120 pbar = tqdm(total=frames)
121
122 # saving the coefficients in order 0, 1, -1, 2, -2, ...
123 # it is necessary to make epicycles
124 def sort_coeff(coeffs):
125     new_coeffs = []
126     new_coeffs.append(coeffs[order])
127     for i in range(1, order+1):
128         new_coeffs.extend([coeffs[order+i], coeffs[order-i]])
129     return np.array(new_coeffs)
130

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132 # making frame at time t
133 # t goes from 0 to 2*PI for complete cycle
134 def make_frame(i, time, coeffs):
135     global pbar
136     # getting t from time
137     t = time[i]
138
139     # exponential term to be multiplied with coefficient
140     # this is responsible for making rotation of circle
141     exp_term = np.array([np.exp(n*t*1j) for n in range(-order, order+1)])
142
143     # sorting the terms of fourier expression
144     coeffs = sort_coeff(coeffs*exp_term) # coeffs*exp_term makes the circle rotate.
145     # coeffs itself gives only direction and size of circle
146
147     # splitting into x and y coefficients
148     x_coeffs = np.real(coeffs)
149     y_coeffs = np.imag(coeffs)
150
151     # centering points for first circle
152     center_x, center_y = 0, 0
153
154     # making all circles i.e epicycle
155     for i, (x_coeff, y_coeff) in enumerate(zip(x_coeffs, y_coeffs)):
156         # calculating radius of current circle
157         r = np.linalg.norm([x_coeff, y_coeff]) # similar to magnitude: sqrt(x^2+y^2)
158
159         # draw circle with given radius at given center points of circle
160         # circumference points: x = center_x + r * cos(theta), y = center_y + r * sin(theta)
161         theta = np.linspace(0, tau, num=50) # theta should go from 0 to 2*PI to get all points
162         x, y = center_x + r * np.cos(theta), center_y + r * np.sin(theta)
163         circles[i].set_data(x, y)
164
165         # drawing a line to indicate the direction of circle
166         x, y = [center_x, center_x + x_coeff], [center_y, center_y + y_coeff]
167         circle_lines[i].set_data(x, y)
168
169         # calculating center for next circle
170         center_x, center_y = center_x + x_coeff, center_y + y_coeff
171
172     # centering points now are points from last circle
173     # these points are used as drawing points
174     draw_x.append(center_x)
175     draw_y.append(center_y)
176
177     # drawing the curve from last point
178     drawing.set_data(draw_x, draw_y)
179
180     # drawing the real curve
181     orig_drawing.set_data(x_list, y_list)
182
183     # updating progress bar
184     pbar.update(1)
185
186 # making animation
187 # time is array from 0 to tau
188 time = np.linspace(0, tau, num=frames)
189 anim = animation.FuncAnimation(fig, make_frame, frames=frames, fargs=(time, c), interval=5)
190 anim.save('bangladesh.mp4', writer=writer)
191 pbar.close()
192 print("completed: epicycle.mp4")

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