

Let  $G$  be a group and  $E$  be a  $G$ -set. Let  $\mathcal{A}$  be a set of multisets over  $E$ . The action of  $G$  on  $E$  extends to action on each multiset and we say that  $G$  acts on  $\mathcal{A}$  if  $\mathcal{A}$  is  $G$ -invariant.

Let  $V$  denote the permutation representation of  $G$  on the set  $\mathcal{A}$ . For a multiset  $A \in \mathcal{A}$ , let  $G_A$  denote the stabilizer subgroup of  $A$  in  $G$  and  $T_{G_A}$  denote the trivial representation of  $G_A$ . Then,

$$V = \bigoplus_{\underline{A} \in \mathcal{A}/G} \text{Ind}_{G_A}^G(T_{G_A})$$

Let  $G$  be a group and  $E$  be a  $G$ -set. Let  $V$  denote the permutation representation of  $G$  on the set  $E$ . For  $x \in E$ , Let  $G_x$  denote the stabilizer subgroup of  $x$  in  $G$  and  $T_{G_x}$  denote the trivial representation of  $G_x$ . Then,

$$V = \bigoplus_{\underline{x} \in E/G} \text{Ind}_{G_x}^G(T_{G_x})$$