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HW 4

Problem 1: Find

$$P(\text{Manu} = A) = \frac{100}{150} = \frac{2}{3}$$

$$P(\text{Damaged}) = \frac{8}{150} = \frac{4}{75}$$

$$P(\text{Damaged} | \text{Manu} = A) = \frac{5}{100} = \frac{1}{20}$$

$$P(\text{Manu} = A | \text{Damaged})$$

$$= \frac{P(\text{Damaged} | \text{Manu} = A) * P(\text{Manu} = A)}{P(\text{Damaged})}$$

$$= \frac{\frac{1}{20} * \frac{2}{3} * \frac{75}{42}}{\frac{4}{75}} = \frac{5}{8} = 0.625$$

Problem 3:

classify instance $y = (\text{Home Owner} = \text{yes}, \text{Marital} = \text{Single}, \text{Annual} = 95K)$

$$\begin{aligned} P(y | BD = \text{no}) &= P(HO = \text{yes} | BD = \text{no}) * P(MS = \text{Single} | BD = \text{no}) * P(AI = 95K | BD = \text{no}) \\ &= \frac{3}{7} * \frac{2}{7} * \frac{1}{7} = \frac{6}{343} = 0.0175 \end{aligned}$$

$$P(BD = \text{no} | y) = \frac{P(y | BD = \text{no}) * P(BD = \text{no})}{P(y)}$$

$$\begin{aligned} P(y | BD = \text{yes}) &= P(HO = \text{yes} | BD = \text{yes}) * P(MS = \text{Single} | BD = \text{yes}) * P(AI = 95K | BD = \text{yes}) \\ &= \frac{1}{3} * \frac{2}{3} * \frac{1}{3} = \frac{2}{27} \end{aligned}$$

$$P(BD = \text{yes} | y) = \frac{P(y | BD = \text{yes}) * P(BD = \text{yes})}{P(y)}$$

$$P(BD = \text{yes} | y) = \frac{\frac{2}{27} * \frac{3}{10}}{P(y)} \quad P(BD = \text{no} | y) = \frac{\frac{6}{343} * \frac{7}{10}}{P(y)}$$

$$\frac{\frac{2}{27} * \frac{3}{10}}{P(y)} + \frac{\frac{6}{343} * \frac{7}{10}}{P(y)} = 1$$

$$P(y) = 0.0345$$

$$P(BD = \text{no} | y) = \frac{\frac{2}{27} * \frac{3}{10}}{0.0345} = 0.645 \quad \text{and} \quad P(BD = \text{yes} | y) = 0.355$$