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Assignment 5

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Question: A man is know to speak truth 3 out of 4 times. He throws a die and reports that it is a six. Find the probability that it is actually a six.

Solution: Let the event that the man reports the actual six be E=1 and lies as six be E=0. The event that six actually occurs on the die be X=1 and X=0 be the event that six does not occur. Then,

Description of event	Events
Die rolls the number six	X=1
Die does not roll the no. six	X=0
Man speaks truth	E=1
Man does not speaks truth	E=0

Now using the values from (??), (??), (??) and (??),

$$P(X = 1|E) = \frac{\frac{1}{6} \times \frac{3}{4}}{\frac{1}{6} \times \frac{3}{4} + \frac{5}{6} \times \frac{1}{4}}$$

$$= \frac{\frac{3}{24}}{\frac{3}{24} + \frac{5}{24}}$$
(6)

$$= \frac{\frac{3}{24}}{\frac{8}{24}}$$
 (8)
$$= \frac{3}{2}$$
 (9)

Probability that die rolls
$$\sin P(X=1) = \frac{1}{6}$$
 (1)

Probability that die does not roll $\sin P(X=0) = \frac{5}{6}$ (2)

Probabilities when the man reports the result to be six,

Probability that six actually occurs
$$=P(E=1|X=1)=\frac{3}{4}$$
 (3) Probability that it is not a six $=P(E=0|X=0)=\frac{1}{4}$ (4)

Now by Bayes's Formula we get, Probability that the man reports the result to be six is actually a six,

$$P(X=1|E) = \frac{P(X=1) \times P(E=1|X=1)}{P(X=1) \times P(E=1|X=1) + P(X=0) \times P(E=0|X=0)}$$
(5)