Assignment-6

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May 16, 2022

Outline

Question

Solution

Question

A man is known to speak truth 3 out of 4 times. He throws a die and reports that it is a six. Find the probability that it is actually a six.



Solution

Let the event that the man reports the actual six be E=1 and lies as six be E=0.

The event that six actually occurs on the die be X=1 and X=0 be the event that six does not occur.

Then,

Probability that die rolls
$$six = P(X = 1) = \frac{1}{6}$$
 (1)

Probability that die does not roll six =
$$P(X = 0) = \frac{5}{6}$$
 (2)

Probabilities when the man reports the result to be six,

Probability that six actually occurs
$$= P(E = 1|X = 1) = \frac{3}{4}$$
 (3)

Probability that it is not a six =
$$P(E = 0|X = 0) = \frac{1}{4}$$

(4)

Now by Bayes's Formula we get,

Probability that the man reports the result to be six is actually a six,

$$P(X=1|E) = \frac{P(X=1) \times P(E=1|X=1)}{P(X=1) \times P(E=1|X=1) + P(X=0) \times P(E=0|X=0)}$$
(5)

Now using the values from (1), (2), (3) and (4),

$$P(X = 1|E) = \frac{\frac{1}{6} \times \frac{3}{4}}{\frac{1}{6} \times \frac{3}{4} + \frac{5}{6} \times \frac{1}{4}}$$

$$= \frac{\frac{3}{24}}{3 + \frac{5}{6}}$$
(6)

$$= \frac{\frac{3}{24}}{\frac{8}{24}}$$

$$= \frac{3}{8}$$
(8)