

Chapter

Alphabet \rightarrow String \rightarrow Language.

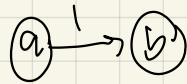
CFG context-free grammar languages.
CFL

Java 12 algorithm regex .*.ing

FA \rightarrow DFA
NFA

* Transition function

$$\delta(a, 1) = b$$



* Extended Transition Function.

$$\delta(q, wa) = \delta(\delta(q, w), a)$$

Example

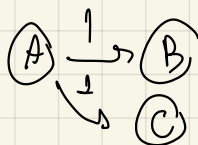
	0	1
A	A	B
B	A	C
C	C	C

$$\begin{aligned} \delta(b, 011) &= \delta(\delta(\delta(b, 0), 1), 1) \\ &= \delta(\delta(a, 1), 1) \\ &= \delta(b, 1) \\ &= C \end{aligned}$$

PL = accept DFA
NPL = $\{0^n 1^n \mid n \geq 1\}$

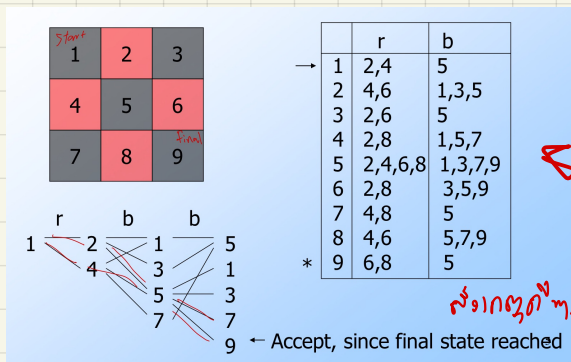
(NFA)

non-deterministic 1 final state, 3c 1s



$$\delta(A, 1) = \{B, C\}$$

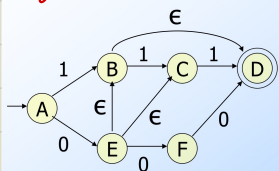
Subset Construction



	r	b
1	2,4	5
2	4,6	1,3,5
3	2,6	5
4	2,8	1,5,7
5	2,4,6,8	1,3,7,9
6	2,8	3,5,9
7	4,8	5
8	4,6	5,7,9
9	6,8	5

	r	b
$\rightarrow \{1\}$	$\{2,4\}$	$\{5\}$
$\{2,4\}$	$\{2,4,6,8\}$	$\{1,3,5,7\}$
$\{5\}$	$\{2,4,6,8\}$	$\{1,3,7,9\}$
$\{2,4,6,8\}$	$\{2,4,6,8\}$	$\{1,3,5,7,9\}$
$\{1,3,5,7\}$	$\{2,4,6,8\}$	$\{1,3,5,7,9\}$
* $\{1,3,7,9\}$	$\{2,4,6,8\}$	$\{5\}$
* $\{1,3,5,7,9\}$	$\{2,4,6,8\}$	$\{1,3,5,7,9\}$

ϵ -NFA



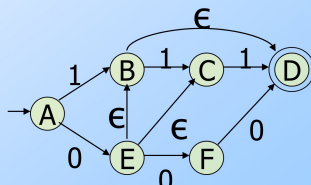
	0	1	ϵ
A	$\{E\}$	$\{B\}$	\emptyset
B	\emptyset	$\{C\}$	$\{D\}$
C	\emptyset	$\{D\}$	\emptyset
* D	\emptyset	\emptyset	\emptyset
E	$\{F\}$	\emptyset	$\{B, C\}$
F	$\{D\}$	\emptyset	\emptyset

3m3 21p-20.-

Closure of State

ϵ .

Example: $CL(A) = \{A\}$;
 $CL(E) = \{B, C, D, E\}$.



Example.

$$L(01) = \{01\}$$

$$L(01+0) = \{01, 010\}$$

$$L(0(1+0)) = \{01, 001\}$$

$$L(0)^* = \{0, 00, 000, \dots\}$$

Regular Expressions.

$$1^+ = \{1, 11, 111, \dots\}$$

$$1^* = \{\epsilon, 1, 11, 111, \dots\}$$

$$L(a) = \{a\}$$

$$L(\epsilon) = \{\epsilon\}$$

$$L(\emptyset) = \emptyset$$

$$E_1 + E_2 = L(E_1) \cup L(E_2)$$

$$E_1 E_2 = L(E_1) \cup L(E_2)$$

$$L(E_1)^* = L(E_1)^*$$

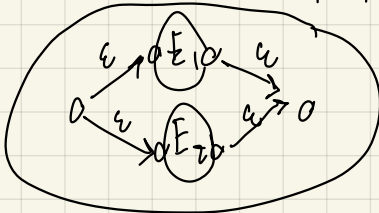
$*$ \rightarrow concat $\rightarrow \epsilon$

Decision Yes, No

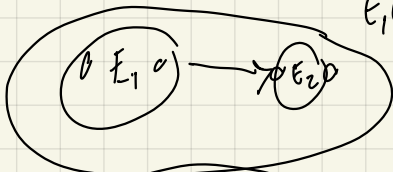
check in 1.1.1 PL 1.1.2 Pumping Lemma

RE ϵ -NFA

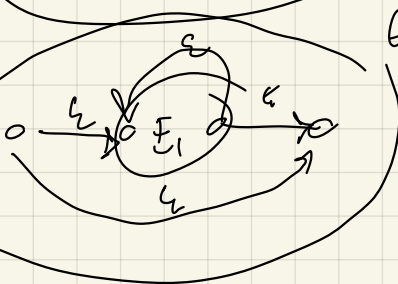
$E_1 \cup E_2$



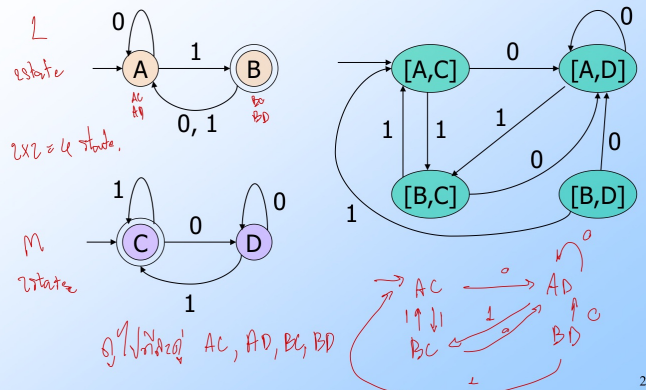
$E_1 E_2$



E_1^*



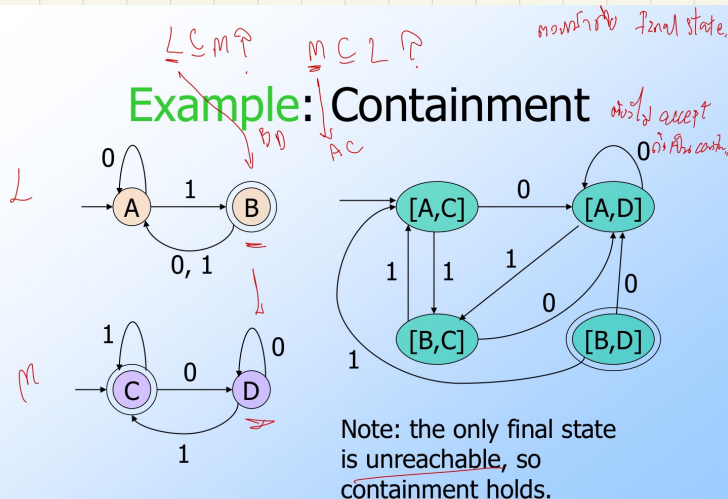
Example: Product DFA



Containment

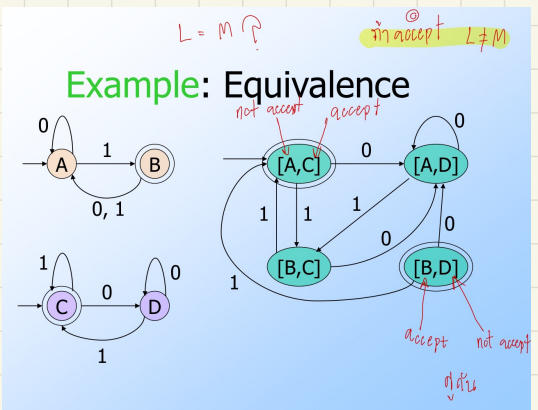
$$L \subseteq M$$

Example: Containment



$L = M$ คือ 2 DFA 1 ตัวก็รับ
 $L \neq M$ คือ 2 DFA 1 ตัวไม่รับ

Example: Equivalence



State Minimization 2m 5 min^d for example, 2x8 --

	r	b
→ A	B	C
B	D	E
C	D	F
D	D	G
E	D	G
*F	D	C
*G	D	G

	G	F	E	D	C	B
A	x	x				
B	x	x				
C	x	x				
D	x	x				
E	x	x				
F						

Start with marks for

Example: ϵ -NFA to NFA

ϵ -NFA

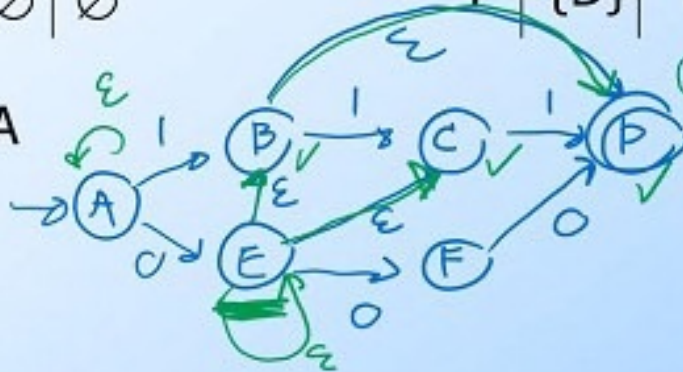
	0	1	ϵ
\rightarrow A	{E}	{B}	\emptyset
B	\emptyset	{C}	{D}
C	\emptyset	{D}	\emptyset
* D	\emptyset	\emptyset	\emptyset
E	{F}	\emptyset	{B, C}
F	{D}	\emptyset	\emptyset

NFA

	0	1
\rightarrow A	{E}	{B}
* B	\emptyset	{C}
C	\emptyset	{D}
* D	\emptyset	\emptyset
* E	{F}	{C, D}
F	{D}	\emptyset

$CL(A) = \{A\}$

ϵ -NFA



$CL(E) = \{B, C, D, E\}$

ทำแบบนี้ได้.

