CS 61A Structure and Interpretation of Computer Programs Summer 2023 $$^{\rm MIDTERM}$$

INSTRUCTIONS

to begin.

This is your exam. Complete it either at exam.cs61a.org or, if that doesn't work, by emailing course staff with your solutions before the exam deadline.

This exam is intended for the student with email address <EMAILADDRESS>. If this is not your email address, notify course staff immediately, as each exam is different. Do not distribute this exam PDF even after the exam ends, as some students may be taking the exam in a different time zone.

For questions with **circular bubbles**, you should select exactly *one* choice.

You must choose either this option
Or this one, but not both!

For questions with **square checkboxes**, you may select *multiple* choices.

You could select this choice.
You could select this one too!

You may start your exam now. Your exam is due at <DEADLINE> Pacific Time. Go to the next page

Preliminaries

You can complete and submit these questions before the exam starts.

(a) What is your full name?

Oski the Bear

(b) What is your student ID number?

123456789

(c) What is your @berkeley.edu email address?

oski@berkeley.edu

(d) Sign (or type) your name to confirm that all work on this exam will be your own. The penalty for academic misconduct on an exam is an F in the course.

Oski Bear

1. (8.0 points) What Would Python Display

For each expression below, choose the correct option or write the output displayed by the interactive Python interpreter when the expression is evaluated. The output may have multiple lines.

- If an error occurs, write "Error", but include all output displayed before the error.
- If evaluation would run forever, write "Forever".
- To display a function value, write "Function".
- If the evaluated expression wouldn't display anything, write "Nothing". The interactive interpreter displays the value of a successfully evaluated expression, unless it is None.

i.	$(0.5 \mathrm{\ pt})$
	>>> (1 or 2) and (3 or 4)
	○ True
	○ False
	O 0
	O 1
	O 2
	○ 3
	○ 4
ii.	(0.5 pt)
	>>> ('Barbie' or 'Ken') * 2
	○ 'Barbie'
	○ 'BarbieBarbie'
	○ 'Ken'
	○ 'KenKen'
	○ 'BarbieKen'
	○ 'KenBarbie'
	○ 'BarbieBarbieKenKen'
	O 2
	○ Error
	○ Nothing
iii.	(0.5 pt) For the rest of this question, assume the following code has been executed.
	>>> it = iter([2, ['a', 'b'], 'c', 3])

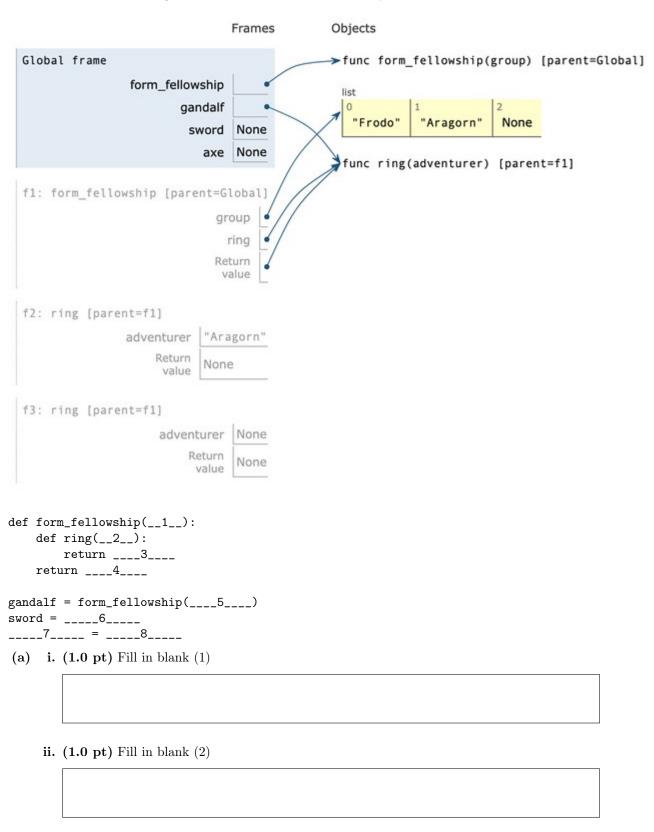
iv.	$(0.5 \mathrm{pt})$
	>>> next(it)
v.	$(1.0 \mathrm{pt})$
	>>> list(it)
vi	$(1.0 \mathrm{pt})$
	>>> next(it)

vii.	(1.0 pt) For the rest of this question, assume the following code has been executed.
	<pre>dreamhouse = 101 beach = lambda pink: pink(dreamhouse) dreamhouse = 102</pre>
	<pre>def is_even(n): return n % 2 == 0</pre>
	>>> beach(is_even)
	○ True
	○ False
	O 101
	O 102
	O 1
	O 0
	○ Function
	○ Error
	○ Nothing
viii.	(1.0 pt)
	>>> beach(dreamhouse)
	○ True
	○ False
	O 101
	\bigcirc 1
	○ 0
	○ Function
	○ Error
	○ Nothing

ix.	(1.0 pt)
	>>> pink = beach(print)
	○ True
	○ False
	O 101
	O 102
	O 1
	O 0
	\bigcirc Function
	○ Error
	\bigcirc Nothing
x.	(1.0 pt)
	>>> pink
	>>> pink (True
	_
	○ True
	<pre>True False</pre>
	<pre>True False 101</pre>
	True False 101 102
	True False 101 102
	True False 101 102 1 0

2. (10.0 points) The Fellowship of the List

Given the environment diagram and skeleton code, answer the questions below.



iii.	(1.5 pt) Which of these could go in 3? (select all that apply)
	☐ group + adventurer
	☐ adventurer + group
	☐ group.extend(adventurer)
	☐ group.extend([adventurer])
	☐ adventurer.extend(group)
	☐ adventurer.extend([group])
	☐ group.append(adventurer)
	☐ group.append([adventurer])
	☐ adventurer.append(group)
	☐ adventurer.append([group])
	☐ group + adventurer[:]
	☐ group[:] + adventurer
iv.	(1.0 pt) Fill in blank (4)
v.	(1.5 pt) Which of these could go in 5? (select one) ['Frodo'] 'Frodo'
	['Frodo', 'Aragorn']
	○ 'Aragorn'
	['Frodo', 'Aragorn', None]
	○ None
vi.	(2.0 pt) Fill in blank (6). You may only make one call expression and may not use or, and, if, o else.
vii.	(1.0 pt) Fill in blank (7)

viii.	$(1.0 \ \mathrm{pt})$ Which of these could go in 8? (select all that apply)
	☐ gandalf(sword)
	☐ gandalf(sword.append(None))
	☐ gandalf(group)
	☐ gandalf(adventurer)
	☐ gandalf(None)
	☐ sword('Aragorn')
	□ sword(None)

3. (13.0 points) Digit Widgets

In this question, we will be testing your understanding of both iterative and recursive solutions.

Hint: pow(b, n) raises b to the power of n. For example, pow(10, 3) is 1000.

(a) (5.0 points)

Implement the recursive version of digit_widget which takes digit d. It returns a function with positive integer parameter n that removes all instances of d from n. You may not use str or repr or [or] or for.

```
def digit_widget(d):
    Given a digit D, returns a function which accepts positive integer N that removes
    all instances of D from N. If there are no digits remaining in N, return O.
    >>> remove_5s = digit_widget(5)
    >>> remove_5s(1234512345)
    12341234
    >>> remove_5s(55555)
    0
    >>> remove_0s = digit_widget(0)
    >>> remove_0s(102001)
    >>> remove_0s(900)
    >>> remove_0s(0)
    0
    11 11 11
    def remove_digit(n):
        if ____:
              (a)
            return _____
                     (b)
        if n % 10 == ____:
                      (c)
            return _____
                 (d)
        return _____
                 (e)
    return _____
              (f)
 i. (0.5 pt) Fill in blank (a).
   \bigcirc n == d
   \bigcirc n == 0
   O n % 10 == 0
   \bigcirc n > 0
   \bigcirc n >= 0
   \bigcirc n < 0
```

ii.	(0.5 pt) Fill in blank (b)
	O 0
	O 1
	\bigcirc d
	O n - 1
	O pow(10, d)
	O pow(10, n)
iii.	(0.5 pt) Fill in blank (c)
	O 0
	O 1
	\bigcirc d
	O n - 1
	O pow(10, d)
	O pow(10, n)
iv.	(1.0 pt) Fill in blank (d)
	<pre> remove_digit(n % d)</pre>
	<pre> remove_digit(n // 10)</pre>
	<pre> remove_digit(n % 10)</pre>
	o Temeve_argrown % Toy
	remove_digit(n - 1)
	<pre> remove_digit(n - 1)</pre>
v.	<pre> remove_digit(n - 1) remove_digit(n % pow(10, d))</pre>
v.	<pre>remove_digit(n - 1) remove_digit(n % pow(10, d)) remove_digit(n // pow(10, d))</pre>
v.	<pre>remove_digit(n - 1) remove_digit(n % pow(10, d)) remove_digit(n // pow(10, d))</pre>
	<pre>remove_digit(n - 1) remove_digit(n % pow(10, d)) remove_digit(n // pow(10, d))</pre>
	<pre>remove_digit(n - 1) remove_digit(n % pow(10, d)) remove_digit(n // pow(10, d)) (2.0 pt) Fill in blank (e).</pre>

(b) (5.0 points)

Implement the iterative version of digit_widget, digit_widget_iter, which takes digit d. It returns a function with positive integer parameter n that removes all instances of d from n. You may not use str or repr or [or] or for.

```
def digit_widget_iter(d):
    Given a digit D, returns a function which accepts positive integer N that removes
    all instances of D from N. If there are no digits remaining in N, return 0.
    >>> remove_5s = digit_widget_iter(5)
    >>> remove_5s(1234512345)
    12341234
    >>> remove_5s(55555)
    >>> remove_0s = digit_widget_iter(0)
    >>> remove_0s(102001)
    121
    >>> remove_0s(900)
    >>> remove_0s(0)
    0
    11 11 11
    def remove_digit(n):
        result, i = 0, 0
        while ____:
                 (a)
            if ____:
                   (b)
                result += _____
                              (c)
                   (d)
               (e)
        return result
    return _____
              (f)
 i. (0.5 pt) Fill in blank (a).
   \bigcirc n == d
   \bigcirc n == 0
   O n % 10 == 0
   \bigcirc n > 0
   \bigcirc n >= 0
   \bigcirc n < 0
```

ii.	(0.5 pt) Fill in blank (b)
	O n % 10 == 0
	O n // 10 != 0
	○ n % 10 == d
	O n % 10 != d
	O n % pow(10, d) == 0
	O n // 10 == pow(10, d)
iii.	(2.0 pt) Fill in blank (c)
iv.	(0.5 pt) Fill in blank (d).
	$\bigcirc n = n \% pow(10, i)$
	() i = pow(10, i)
	○ i += 1
	\bigcirc n = n % 10
	\bigcirc n = n // 10
	O n -= 1
v.	(1.0 pt) Fill in blank (e).
	<pre> n = n % pow(10, i)</pre>
	<pre> i = pow(10, i) </pre>
	○ i += 1
	O n = n % 10
	$\bigcirc n = n // 10$
	O n -= 1
vi.	(0.5 pt) Fill in blank (f).

(c) (3.0 points)

Implement digit_machine, which takes a positive integer n. It returns n where all instances of 4 and 8 have been removed. You may not use str or repr or [or] or for. Assume digit_widget is implemented correctly (and you may use it).

lef	<pre>digit_machine(n):</pre>		
	Given an integer N, return a modified N such that all instances of 4 and 8 has >>> digit_machine(484848) 0 >>> digit_machine(123456789) 1235679 >>> digit_machine(208) 20 """	ve been	removed.
	return (a)		
i.	(3.0 pt) Fill in blank (a).		

4. (8.0 points) Goatda

This question will test the debugging skills you've learned in the class so far. We have included an implementation of the goatda function which accepts a single argument function lamb and a non-negative integer n. It returns a single argument function that applies lamb to the argument n times. However, the included implementation is buggy!

```
def goatda(lamb, n):
    11 11 11
    Implement goatda which accepts LAMB, a single argument function, and N the number of times
    to apply LAMB. Return a single argument function that applies LAMB to the argument N times.
    >>> add3 = goatda(lambda x: x+1, 3)
    >>> add3(10) # (((10 + 1) + 1) + 1)
    >>> add3(2) # (((2 + 1) + 1) + 1)
    >>> print2 = goatda(print, 2)
    >>> print2("hi") # print(print("hi"))
    hi
    >>> identity = goatda(lambda x: x+3, 0) # The function is applied 0 times
    >>> identity(0)
    11 11 11
    if n == 0:
                                               # line 1
        return lambda x: x
                                               # line 2
    return lambda x: lamb(goatda(lamb, n-1)) # line 3
(a) After implementing goatda, we execute the following lines of code in the terminal.
    >>> add3 = goatda(lambda x: x+1, 3)
    >>> add3(10)
    The call to add3(10) results in an error!
     i. (2.0 pt) What kind of error does this result in?
        RecursionError: too much recursion
        TypeError: unsupported operand type(s)
        O TypeError: 'NoneType' object is not callable
        ○ IndentationError
        ○ IndexError
        ○ NameError
```

ii.	(2.0 pt) Let's modify the code, so that it no longer errors. Select how to replace the 3 lines, so that
	the function passes the doctests and no longer errors. Select No change if you do not want to modify
	the line. Indentation will remain the same.

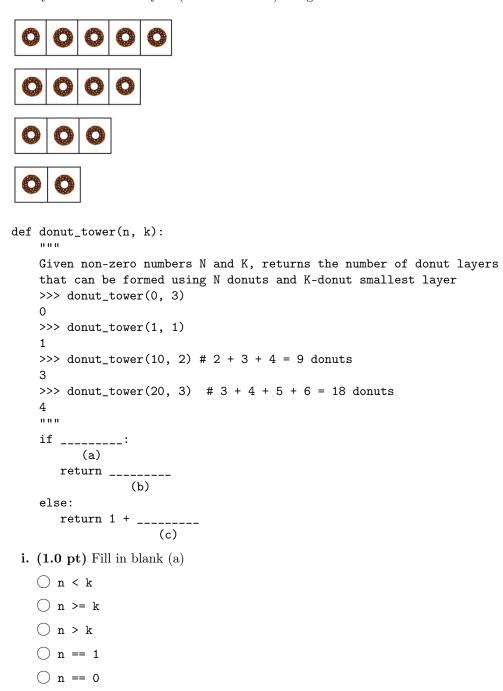
	How would you modify line 1?
	○ if n > 0:
	○ if n < 0:
	<pre> if n >= 0:</pre>
	O if n % 10 > 0:
	<pre> if n % 10 >= 0:</pre>
	<pre> if lamb(n) == 0:</pre>
	O if lamb(n):
	○ No change
	(0.0.1) II. 11. 11. 11. 11. 11.
111.	(2.0 pt) How would you modify line 2?
	O return lamb(n)
	O return n
	O return lambda x: n
	O return lambda x: 0
	<pre> return lambda x: lamb(x)</pre>
	O return lambda x: lambda y: lamb(y)
	○ No change
iv.	(2.0 pt) How would you modify line 3?
	return goatda(lamb, lamb(n-1))
	return lamb(goatda(lamb, n-1))
	return lambda x: lamb(x) + goatda(lamb, n-1)
	return lambda x: goatda(lamb(x), n-1)
	return lambda x: lamb(goatda(lamb, n-1)(x))
	return lambda x: goatda(lamb, n-1)(n)
	No change
	○ · · · · · · · · · · · · · · · · · · ·

 \bigcirc n < 1

5. (13.0 points) Sweetness Overload

(a) (3.0 points)

Implement donut_tower which takes in the number of donuts n and positive integer k. It returns the number of layers one can fill using n donuts, given the smallest layer consists of k donuts and each subsequent layers consists of one more donut than the previous one. For instance, if n is 16 and k is 2, then you can create 4 layers (as shown below) using 14 donuts.



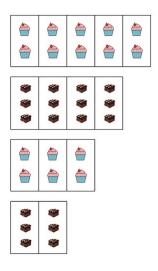
ii. (1.0 pt) Fill in blank (b)

iii. (1.0 pt) Fill in blank (c)

- max(donut_tower(n, k + 1), donut_tower(n k, k))
- donut_tower(n, k + 1)
- O donut_tower(n k, k + 1)
- donut_tower(n k, k)
- O donut_tower(n k + 1, k)
- donut_tower(n 1, k)

(b) (4.0 points)

Implement alternating_tower, which takes a positive integer c, the number of cupcakes, positive integer b, the number of brownies, and k, the size of the smallest layer that can hold k donuts. It returns the maximum numbers of dessert layers that can be formed using brownies and cupcakes. Since those items are smaller than donuts, each k-sized donut layer can hold twice as many cupcakes and thrice as many brownies. Also, a dessert tower has alternating layers of brownies and cupcakes, but the first layer must always consist of brownies. For instance, if b is 20, c is 20 and k is 2, then you can create a maximum of 4 layers (as shown below) using 18 brownies and 16 cupcakes.



i.	(1.0 pt) Fill in blank (a)
	○ b_item < 0 or c_item < 0
	○ b_item
	<pre>D_item == 0 or c_item == 0</pre>
	<pre>○ b_item > 0 or c_item > 0</pre>
	○ c_item
	○ b_item < 0 and c_item < 0
	<pre>C_item * 2 == k or b_item * 3 == k</pre>
	<pre>D_item * 3 <= k</pre>
ii.	(1.0 pt) Fill in blank (b)
	<pre>O helper(b_item - 3 * curr_layer, c_item, curr_layer + 1, is_cupcakes) - 1</pre>
	<pre>1 + helper(b_item - 3 * curr_layer, c_item - 2 * curr_layer, curr_layer - 1, not is_cupcake</pre>
	<pre>1 + helper(b_item, c_item - 2 * curr_layer, curr_layer + 1, not is_cupcakes)</pre>
	O helper(b_item - 3 * curr_layer, c_item - 2 * curr_layer, curr_layer - 1, is_cupcakes)
	<pre>O helper(b_item, b_item - 2 * curr_layer, curr_layer + 1, not is_cupcakes)</pre>
	<pre>helper(b_item - 3 * curr_layer, c_item, curr_layer + 1, not is_cupcakes) + helper(b_item, c_item - 2 * curr_layer, curr_layer + 1, is_cupcakes)</pre>
iii.	(1.0 pt) Fill in blank (c)
	○ b_item
	O b_item - 3 * (curr_layer + 1)
	O b_item - 3 * curr_layer
	<pre>3 * b_item</pre>
	O b_item + c_item * 3 * curr_layer
	<pre>O b_item // 3 * (curr_layer + 1)</pre>
	O b_item // 3 * curr_layer
	O b_item - 3 // curr_layer
iv.	(1.0 pt) Fill in blank (d)

(c) (6.0 points)

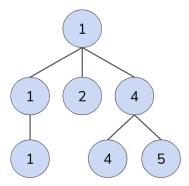
Implement sweetest_tower, which takes a positive integer c, the number of cupcakes, positive integer b, the number of brownies, and k, the size of the smallest layer that can hold k donuts. It returns the maximum number of dessert layers that can be formed using brownies and cupcakes. As previously stated, since those items are smaller than donuts, each k-sized donut layer can hold twice as many cupcakes and thrice as many brownies. Unlike alternating_tower, layers can be in any order.

```
def sweetest_tower(b, c, k):
    >>> sweetest_tower(0, 2, 1) # 1st layer with 2 cupcakes
    >>> sweetest_tower(5, 4, 4)
    >>> sweetest_tower(17, 19, 3) # layer 1 has 6 cupcakes, 2nd has 8 cupcakes, 3rd has 15 brownie
    >>> sweetest_tower(30, 8, 4)
                                      # 1st layer has 12 brownies, 2nd has 15 brownies
    2
    11 11 11
    with_brownies, with_cupcakes = 0,0
    if ____:
          (a)
        with_brownies = _____
                            (b)
    if ____:
          (c)
        with_cupcakes = _____
    return _____(with_brownies, with_cupcakes)
              (e)
 i. (1.0 pt) Fill in blank (a)
   \bigcirc b >= 3 * k
   \bigcirc b > 3 * k
   ○ b
   \bigcirc b == 3 * k
   ○ b > c
   \bigcirc b // 3 < k
   \bigcirc b // 3 == k
   \bigcirc b >= 0
```

ii. (1.0 pt) Fill in blank (b)								
\bigcirc 1 + sweetest_tower(b // 3 - k, c, k - 1)								
\bigcirc sweetest_tower(b - 3 * k, c, k + 1)								
\bigcirc 1 + sweetest_tower(b - 3 * k, c, k + 1)								
<pre>Sweetest_tower(b - 3 * k, c, k - 1)</pre>								
\bigcirc 3 * sweetest_tower(b, c - 2 * k, k + 1)								
<pre>3 + sweetest_tower(b, c - 2 * k, k + 1)</pre>								
<pre>Sweetest_tower(b - 3 // k, c - 2 * k, k + 1)</pre>								
i. (1.0 pt) Fill in blank (c)								
(1.0 pt) Fill in blank (d)								
(1.0 pt) Fill in blank (e)								

6. (12.0 points) All Treeils Lead to Rome

Definition: A **Treeil** is a tree where *exactly* one of the child node(s) of each non-leaf node has a label equal to the label of the node. Alternatively, a treeil is a tree where every node has a singular path from the node to a leaf consisting entirely of nodes with the same label. Here is an example of a valid treeil:



(a) (7.0 points) Treeil Trial

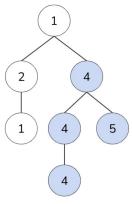
Implement is_treeil which takes in a tree t and determines whether t is a treeil.

```
def is_treeil(t):
   11 11 11
   Returns whether a tree is a treeil. A treeil is a tree where exactly one of
   the branches of each non-leaf node has a label equal to the label of the node.
   >>> t1 = tree(1)
   >>> is_treeil(t1)
   >>> t2 = tree(1, [tree(2), tree(3)])
   >>> is_treeil(t2)
   >>> t3 = tree(1, [tree(1, [tree(1), tree(3)]), tree(2)])
   >>> is_treeil(t3)
   >>> t4 = tree(1, [tree(1, [tree(1), tree(1)]), tree(2)])
   >>> is_treeil(t4)
   False
   >>> t5 = tree(2, [tree(3, [tree(1)]), tree(2, [tree(2)])])
   >>> is_treeil(t5)
   False
         (a)
       return True
       match_one = _____([b for b in branches(t) if _____]) == 1
                      (b)
       return _____ and ____([____ for b in branches(t)])
                               (e)
                                          (f)
```

i.	(1.0 pt) Fill in blank (a). Select all that apply.
	☐ True
	☐ False
	☐ is_leaf(t)
	☐ branches(t)
	□ not branches(t)
	☐ label(t)
	☐ not label(t)
	□ branches(t) == []
ii.	(1.0 pt) Fill in blank (b).
	\bigcirc sum
	o max
	\bigcirc min
	○ len
	\bigcirc any
	\bigcirc all
iii.	(2.0 pt) Fill in blank (c).
iv.	(1.0 pt) Fill in blank (d).
v.	(1.0 pt) Fill in blank (e).
	\bigcirc sum
	\bigcirc max
	\bigcirc min
	\bigcirc any
	O all
vi.	(1.0 pt) Fill in blank (f).

(b) (5.0 points) Treeil Trail

Implement max_treeil which takes in a tree t and determines the highest number of nodes in a treeil that is a subtree of t. You may assume is_treeil is implemented correctly from the previous question. The following diagram displays a tree t, which is not a treeil. The treeil subtree of t with the highest number of nodes is highlighted. Calling max_treeil on this tree t should give a result of 4.



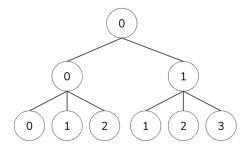
```
def max_treeil(t):
   Given a tree (that is not necessarily a treeil), returns
   the highest number of nodes in a treeil in the tree.
   >>> t1 = tree(1)
   >>> max_treeil(t1)
   >>> t2 = tree(1, [tree(2), tree(3)])
   >>> max_treeil(t2)
    1
   >>> t3 = tree(1, [tree(1, [tree(1), tree(3)]), tree(2)])
   >>> max_treeil(t3)
   >>> t4 = tree(1, [tree(1, [tree(1), tree(1)]), tree(2)])
   >>> max_treeil(t4)
   >>> t5 = tree(2, [tree(3, [tree(1)]), tree(2, [tree(2)])])
   >>> max_treeil(t5)
   2
    11 11 11
    if ____:
          (a)
        return 1
    elif ____:
            (b)
        return 1 + _____
    else:
       return max([_____ for b in branches(t)])
                       (d)
```

i.	i. (1.0 pt) Fill in blank (a).								
	<pre> is_treeil(t)</pre>								
	<pre> not is_treeil(t)</pre>								
	<pre> is_leaf(t)</pre>								
	<pre> is_treeil(t) or is_leaf(t)</pre>								
	<pre>O not is_treeil(t) and is_leaf(t)</pre>								
ii.	. (1.5 pt) Fill in blank (b).								
•••	(1.0 mt) Fill in blank (1)								
111.	(1.0 pt) Fill in blank (c).								
	<pre>max([max_treeil(b) for b in branches(t)])</pre>								
	<pre> len([max_treeil(b) for b in branches(t)])</pre>								
	<pre> sum([max_treeil(b) for b in branches(t)])</pre>								
	<pre> sum([b for b in branches(t) if is_treeil(b)])</pre>								
	<pre>O len([b for b in branches(t) if is_treeil(b)])</pre>								
iv.	<pre>O len([b for b in branches(t) if is_treeil(b)]) (1.5 pt) Fill in blank (d).</pre>								

(c) (0.0 points) Treeil Treeatment (A+ Question)

This A+ question is not worth any points. This can only affect your course grade if you have a high A and might receive an A+. Finish the rest of the exam first!

Implement make_treeil which takes in a non-negative integer n and returns a treeil of depth n. Each node of the treeil has exactly one more child than its parent node. The first branch of a node will have value equal to its parent. Subsequent branches will have a label of exactly one more than the previous branch. The root has a label of 0 and has exactly two children for a tree of depth 1. Here's an example of a treeil of depth 2.



```
def make_treeil(n):
```

Returns a treeil of depth n where each node has one more child than its parent. The first branch of a node will have label equal to its parent with subsequent branches having label of exactly one more than the previous branch.

```
>>> t2 = make_treeil(2)
>>> print_tree(t2)
0
  0
    0
    1
    2
    1
    2
    3
def treeil_tracker(k, parent):
    if n == k:
        return tree(parent)
    return __
               (a)
return treeil_tracker(0, 0)
```

i. (0.0 pt) Fill in blank (a).

No more questions.