

MBARARA UNIVERSITY OF SCIENCE AND TECHNOLOGY
FACULTY OF COMPUTING AND INFORMATICS

MID SEMESTER EXAMINATIONS

Course Code : MTH 1111
Course Name : DISCRETE MATHEMATICS
Course Year : BCS/BSE YEAR 1
Date : 26/10/2021
Duration : 1 HOUR
Time : 11:00 am-12:00 Noon

Instructions: Do all numbers.

(a) Given that the universal set $U = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$, $A = \{2, 4, 6, 8, 10\}$, and $B = \{1, 3, 5, 7, 9, 10\}$, find;

(i) $(A \cup B)^c$ (2 marks)

(ii) $(B - A)^c$ (2 marks)

(iii) $(A \cap B)^c$ (2 marks)

(b) Write the following in set-builder form; $D = \{-3, -6, -9, -12\}$. (2 marks)

(c) (i) Define a power set. (2 marks)

(ii) Write the power set of the following set: $B = \{y : y \in \mathbb{N} \text{ and } 1 \leq y \leq 3\}$. (2 marks)

(d) Using examples explain the following in relation to sets;

(i) relative complement of sets (2 marks)

(ii) symmetric difference of sets (2 marks)

(e) prove that for any two sets A and B, $(A \cup B)^c = A^c \cap B^c$

(f) Explain the following types of relations;

(i) a binary relation (2 marks) $A = B$

(ii) symmetric relation (2 marks)

(iii) Transitive relation (2 marks)

(g) If R is a relation from \mathbb{N} to \mathbb{N} defined by $R = \{(x, y) : 4x + y = 12, x, y \in \mathbb{N}\}$ find the domain and the range of R (2 marks)

(h) Using examples explain the following terms in mathematical logic;

(i) A proposition. (2 marks)

(ii) A primitive proposition (2 marks)

(j) Construct truth table for the following statement:

$$(p \wedge \neg q) \rightarrow p \quad (4 \text{ marks})$$

(k) Explain the following as applied in graph theory

(i) multiple edges (2 marks)

(ii) degree of a vertex (2 marks)

(iii) complete graph (2 marks)

(iv) complement of a graph (2 marks)

END