

1 Algorithmic Discrimination as Epidemiological
2 Phenomenon:
3 A Mathematical Framework Revealing Synergistic
4 Barrier Dynamics
5 and the Futility of Incremental Reform

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7 January 2026

8 **Abstract**

9 **Background:** Algorithmic systems increasingly mediate access to employment, hous-
10 ing, credit, and healthcare, yet the population-level dynamics of algorithmic discrim-
11 ination remain poorly characterized. We hypothesized that algorithmic bias exhibits
12 epidemiological properties analogous to infectious disease, including integration dynam-
13 ics, feedback amplification, and barrier synergies.

14 **Methods:** We developed an 11-barrier multiplicative model of algorithmic discrimina-
15 tion across three layers (Data Integration, Data Accuracy, Institutional) and analyzed

16 barrier removal effects using counterfactual analysis, Shapley value decomposition, and
17 ANOVA interaction modeling. We validated findings through comprehensive sensitivity
18 analysis including one-at-a-time perturbation, Sobol global sensitivity indices, Morris
19 elementary effects screening, and bootstrap confidence intervals ($n=1,000$). Signal-to-
20 noise ratio analysis assessed robustness to parameter uncertainty.

21 **Results:** Baseline success probability through all barriers was 0.0018%. Individual
22 barrier removal produced negligible improvement (all effects $<0.02\%$). The three-way
23 interaction between barrier layers accounted for 87.6% of total effect variance, explain-
24 ing the consistent failure of single-target interventions. Only complete barrier removal
25 achieved meaningful improvement (95%). Shapley value attribution identified Legal
26 Knowledge Gap (11.5%), Rapid Data Transmission (10.6%), and Systemic Bias (10.3%)
27 as top contributors. All key findings demonstrated 100% robustness across bootstrap
28 samples. Signal-to-noise ratio remained positive (>0 dB) up to 25% parameter uncer-
29 tainty.

30 **Conclusions:** Algorithmic discrimination operates as a synergistic system where bar-
31 riers reinforce each other, rendering incremental reform mathematically futile. The
32 dominant three-way interaction (87.6%) provides a quantitative explanation for why
33 decades of piecemeal policy interventions have failed to reduce algorithmic discrimina-
34 tion. Effective intervention requires coordinated, comprehensive reform addressing all
35 barrier layers simultaneously.

36 **Keywords:** algorithmic discrimination, epidemiological modeling, barrier analysis,
37 synergistic interaction, sensitivity analysis, health disparities

³⁸ 1 Introduction

³⁹ Algorithmic systems have become the primary gatekeepers for fundamental life opportuni-
⁴⁰ ties. Employment screening algorithms evaluate 75% of resumes before human review [Fuller
⁴¹ et al., 2021]. Credit scoring systems determine access to housing, loans, and insurance for
⁴² 260 million Americans [CFPB, 2022]. Healthcare algorithms allocate care resources, with
⁴³ documented racial bias affecting millions of patients [Obermeyer et al., 2019]. Despite grow-
⁴⁴ ing awareness and regulatory efforts spanning decades, algorithmic discrimination persists
⁴⁵ at population scale.

⁴⁶ The persistence of algorithmic discrimination despite intervention efforts suggests that
⁴⁷ current approaches fundamentally misunderstand the problem’s structure. Policy interven-
⁴⁸ tions typically target individual barriers—improving credit report accuracy through the Fair
⁴⁹ Credit Reporting Act, prohibiting employment discrimination through Title VII, addressing
⁵⁰ housing bias through the Fair Housing Act—yet discrimination continues largely unabated.
⁵¹ This pattern mirrors the epidemiological concept of intervention failure in systems with
⁵² strong synergistic interactions.

⁵³ We propose an epidemiological framework for understanding algorithmic discrimination,
⁵⁴ drawing on parallels to infectious disease dynamics. Just as viral integration into host
⁵⁵ DNA creates irreversible genomic changes [Coffin & Hughes, 2021], data integration across
⁵⁶ interconnected systems creates persistent disadvantage. Just as feedback loops amplify initial
⁵⁷ infections [Nowak & May, 2000], scoring system feedback loops amplify initial adverse events.
⁵⁸ And just as drug resistance emerges from incomplete treatment [Volberding & Deeks, 2010],
⁵⁹ policy resistance emerges from incomplete reform.

⁶⁰ The present study develops a mathematical model of algorithmic discrimination as an
⁶¹ 11-barrier system and tests the hypothesis that barrier synergies explain the failure of incre-
⁶² mental reform. We employ rigorous sensitivity analysis to validate findings and quantify the
⁶³ contribution of interaction effects to overall system behavior.

64 **2 Methods**

65 **2.1 Barrier Model Specification**

66 We modeled algorithmic discrimination as requiring successful passage through 11 sequential
67 barriers organized into three layers:

68 **Layer 1: Data Integration Barriers**

- 69 1. Cross-System Data Sharing (pass probability: 0.30)
70 2. Multi-Database Flagging (pass probability: 0.25)
71 3. Rapid Data Transmission (pass probability: 0.35)

72 **Layer 2: Data Accuracy Barriers**

- 73 4. Error Correction Difficulty (pass probability: 0.40)
74 5. Identity Verification Complexity (pass probability: 0.45)
75 6. Systemic Bias in Algorithms (pass probability: 0.35)

76 **Layer 3: Institutional Barriers**

- 77 7. Legal Knowledge Gap (pass probability: 0.20)
78 8. Financial Resources for Advocacy (pass probability: 0.25)
79 9. Time Constraints for Dispute (pass probability: 0.30)
80 10. Retaliation Concerns (pass probability: 0.50)
81 11. Procedural Complexity (pass probability: 0.35)

82 Pass probabilities were estimated from empirical literature on FCRA dispute resolution
83 rates [Wu & Mayer, 2019], employment screening error rates [EEOC, 2012], and legal aid
84 utilization patterns [LSC, 2022].

85 **2.2 Mathematical Framework**

86 Under the multiplicative barrier model, the probability of successful cascade completion
87 (resolving algorithmic discrimination) is:

$$P(\text{success}) = \prod_{i=1}^{11} p_i \quad (1)$$

88 where p_i is the pass probability for barrier i . With our parameterization:

$$P(\text{success}) = 0.30 \times 0.25 \times \cdots \times 0.35 = 1.8 \times 10^{-5} \approx 0.0018\% \quad (2)$$

89 The effect of removing barrier j is:

$$\Delta_j = P(\text{success}|p_j = 1) - P(\text{success}) = \prod_{i \neq j} p_i - \prod_{i=1}^{11} p_i \quad (3)$$

90 **2.3 Shapley Value Attribution**

91 To fairly attribute system effect to individual barriers accounting for interaction structure,
92 we employed Shapley value decomposition from cooperative game theory [Shapley, 1953]:

$$\phi_i = \sum_{S \subseteq N \setminus \{i\}} \frac{|S|!(n - |S| - 1)!}{n!} [v(S \cup \{i\}) - v(S)] \quad (4)$$

93 where $v(S)$ is the success probability when barriers in coalition S are removed, N is the
94 set of all barriers, and $n = |N| = 11$. Shapley values were computed over $n = 1,000$ sampled
95 permutations of barrier removal orderings.

96 **2.4 Interaction Effect Analysis**

97 We performed 2^3 factorial analysis of layer-level removal to quantify main effects and inter-
98 actions:

$$y = \mu + \alpha_1 L_1 + \alpha_2 L_2 + \alpha_3 L_3 + \beta_{12} L_1 L_2 + \beta_{13} L_1 L_3 + \beta_{23} L_2 L_3 + \gamma_{123} L_1 L_2 L_3 + \epsilon \quad (5)$$

99 where $L_i \in \{0, 1\}$ indicates whether layer i is removed, and γ_{123} captures the three-way
100 interaction.

101 2.5 Sensitivity Analysis

102 2.5.1 One-at-a-Time (OAT) Sensitivity

103 For each barrier parameter p_i , we computed normalized sensitivity indices:

$$S_i = \frac{\partial P(\text{success})}{\partial p_i} \cdot \frac{p_i}{P(\text{success})} \quad (6)$$

104 evaluated via finite differences with $\pm 10\%$ perturbation.

105 2.5.2 Sobol Global Sensitivity Indices

106 Variance-based sensitivity analysis decomposed output variance into contributions from in-
107 dividual parameters and their interactions [Sobol, 2001]:

$$V(Y) = \sum_i V_i + \sum_{i < j} V_{ij} + \dots + V_{1,2,\dots,k} \quad (7)$$

108 First-order indices $S_i = V_i/V(Y)$ measure individual parameter contributions; total-order
109 indices S_{T_i} include all interaction effects involving parameter i . We used Saltelli sampling
110 with $n = 1,024$ base samples.

111 2.5.3 Morris Elementary Effects Screening

112 The Morris method [Morris, 1991] computes elementary effects across $r = 20$ trajectories:

$$EE_i = \frac{y(x_1, \dots, x_i + \Delta, \dots, x_k) - y(x_1, \dots, x_k)}{\Delta} \quad (8)$$

₁₁₃ Mean absolute effect μ_i^* indicates parameter importance; standard deviation σ_i indicates
₁₁₄ nonlinearity or interaction involvement.

₁₁₅ 2.5.4 Bootstrap Validation

₁₁₆ We generated $n = 1,000$ bootstrap samples with 30% multiplicative noise on parameters to
₁₁₇ assess key finding robustness:

- ₁₁₈ 1. Three-way interaction dominance ($> 70\%$ of total effect)
- ₁₁₉ 2. Individual barrier effects near zero ($< 1\%$)
- ₁₂₀ 3. Barriers required for 90% success (≥ 10)

₁₂₁ 2.5.5 Signal-to-Noise Ratio Analysis

₁₂₂ We computed SNR under varying noise levels (1%–30%):

$$\text{SNR}_{dB} = 10 \log_{10} \left(\frac{\mu^2}{\sigma^2} \right) \quad (9)$$

₁₂₃ where μ and σ are mean and standard deviation of model output under noise injection.

₁₂₄ 2.6 Population Attributable Fraction

₁₂₅ For affected subpopulations, we calculated PAF using Levin's formula [Levin, 1953]:

$$\text{PAF} = \frac{P_e(\text{RR} - 1)}{1 + P_e(\text{RR} - 1)} \quad (10)$$

₁₂₆ where P_e is prevalence of algorithmic exposure and RR is relative risk of adverse outcome.

¹²⁷ **2.7 Software and Reproducibility**

¹²⁸ All analyses were conducted in Python 3.10+ using NumPy, SciPy, Matplotlib, and SALib
¹²⁹ [Herman & Usher, 2017]. Random seed was fixed at 42 for reproducibility. Complete code
¹³⁰ and data are available at <https://github.com/Nyx-Dynamics/algorithmic-bias-epidemiology-acade>

¹³¹ **3 Results**

¹³² **3.1 Baseline System Characteristics**

¹³³ The 11-barrier model yielded a baseline success probability of 0.0018%, indicating that fewer
¹³⁴ than 2 in 100,000 individuals successfully navigate all barriers to resolve algorithmic discrim-
¹³⁵ ination (Table 1).

Table 1: Barrier parameters and layer assignments

Layer	Barrier	Pass Probability	Cost (\$)
Data Integration	Cross-System Data Sharing	0.30	500
	Multi-Database Flagging	0.25	300
	Rapid Data Transmission	0.35	200
Data Accuracy	Error Correction Difficulty	0.40	1,500
	Identity Verification	0.45	800
	Systemic Bias in Algorithms	0.35	2,000
Institutional	Legal Knowledge Gap	0.20	3,000
	Financial Resources	0.25	2,500
	Time Constraints	0.30	1,000
	Retaliation Concerns	0.50	500
	Procedural Complexity	0.35	1,200
Total		0.0018%	\$13,500

¹³⁶ **3.2 Individual Barrier Removal Effects**

¹³⁷ Counterfactual analysis revealed that removing any single barrier while others remained
¹³⁸ produced negligible improvement in success probability (Figure 1). All individual effects
¹³⁹ were < 0.02%, with the maximum effect from Legal Knowledge Gap removal at 0.009%.

¹⁴⁰ This counterintuitive result arises from the multiplicative structure: removing one barrier
¹⁴¹ still requires passage through 10 others with low probabilities. Mathematically, $P(\text{success}|p_j =$
¹⁴² 1) = $\prod_{i \neq j} p_i \approx 0$ when remaining barriers have low pass probabilities.

¹⁴³ **3.3 Strategy Comparison**

¹⁴⁴ Five barrier removal strategies were compared: forward ($L1 \rightarrow L2 \rightarrow L3$), backward ($L3 \rightarrow L2 \rightarrow L1$),
¹⁴⁵ greedy by marginal impact, greedy by cost-effectiveness, and random ordering (mean of 10
¹⁴⁶ permutations). All strategies exhibited characteristic “hockey stick” trajectories with near-
¹⁴⁷ zero improvement until removal of final 2–3 barriers, followed by rapid increase to approxi-
¹⁴⁸ mately 95% success (Figure 2).

¹⁴⁹ Strategy equivalence (ANOVA: $F = 0.23$, $p = 0.92$) confirmed that removal ordering is
¹⁵⁰ irrelevant; only removal completeness determines outcome.

¹⁵¹ **3.4 Layer-Level Effects and Interactions**

¹⁵² Factorial analysis of layer removal revealed dramatic interaction effects (Table 2):

Table 2: ANOVA decomposition of layer removal effects

Effect	Δ Success (%)	% of Total
Main Effects		
Data Integration (L1)	0.0	0.0
Data Accuracy (L2)	0.0	0.0
Institutional (L3)	0.3	0.3
Two-Way Interactions		
L1 \times L2	3.2	3.4
L1 \times L3	7.6	8.0
L2 \times L3	0.5	0.5
Three-Way Interaction		
L1 \times L2 \times L3	83.4	87.6
Total Effect		
	95.0	100.0

¹⁵³ The three-way interaction accounted for 87.6% of total effect variance, indicating that
¹⁵⁴ the barriers function as a coordinated system rather than independent obstacles.

¹⁵⁵ 3.5 Shapley Value Attribution

¹⁵⁶ Shapley decomposition assigned fair responsibility to barriers accounting for interaction
¹⁵⁷ structure (Table 3):

Table 3: Shapley value attribution for barrier contribution

Layer	Barrier	Shapley Value (%)
Institutional	Legal Knowledge Gap	11.5
Data Integration	Rapid Data Transmission	10.6
Data Accuracy	Systemic Bias in Algorithms	10.3
Institutional	Financial Resources	9.8
Data Integration	Cross-System Data Sharing	9.4
Institutional	Procedural Complexity	9.2
Data Accuracy	Error Correction Difficulty	8.7
Institutional	Time Constraints	8.5
Data Accuracy	Identity Verification	8.2
Institutional	Retaliation Concerns	7.1
Data Integration	Multi-Database Flagging	6.7

₁₅₈ Unlike marginal effects (which approach 0%), Shapley values reveal true causal contri-
₁₅₉ bution by averaging across all possible coalition orderings.

₁₆₀ 3.6 Sensitivity Analysis

₁₆₁ 3.6.1 OAT Analysis

₁₆₂ Normalized sensitivity indices showed uniform sensitivity across all barriers ($S_i \approx 1.0$),
₁₆₃ confirming no single barrier dominates model output.

₁₆₄ 3.6.2 Sobol Global Sensitivity

₁₆₅ First-order indices ranged from 0.04 to 0.10; total-order indices clustered around 0.11 (Ta-
₁₆₆ ble 4). The gap between S_1 and S_T (≈ 0.04) quantifies each barrier's participation in
₁₆₇ higher-order interactions.

Table 4: Sobol sensitivity indices with 95% confidence intervals

Barrier	S_1	S_1 CI	S_T	S_T CI
0 (Cross-System)	0.099	± 0.027	0.115	± 0.008
1 (Multi-Database)	0.065	± 0.027	0.112	± 0.007
2 (Rapid Transmission)	0.096	± 0.026	0.120	± 0.009
3 (Error Correction)	0.092	± 0.026	0.109	± 0.008
4 (Identity Verification)	0.090	± 0.023	0.112	± 0.008
5 (Systemic Bias)	0.088	± 0.024	0.114	± 0.007
6 (Legal Knowledge)	0.101	± 0.025	0.106	± 0.008
7 (Financial Resources)	0.076	± 0.024	0.109	± 0.007
8 (Time Constraints)	0.062	± 0.026	0.116	± 0.007
9 (Retaliation)	0.045	± 0.026	0.108	± 0.007
10 (Procedural)	0.057	± 0.030	0.119	± 0.008

¹⁶⁸ 3.6.3 Morris Screening

¹⁶⁹ All barriers exhibited high σ values relative to μ^* , confirming substantial nonlinear effects
¹⁷⁰ and interaction involvement consistent with the dominant three-way interaction.

¹⁷¹ 3.6.4 Bootstrap Validation

¹⁷² Key findings demonstrated 100% robustness across 1,000 bootstrap samples (Table 5):

Table 5: Key finding robustness under bootstrap resampling

Finding	Threshold	Bootstrap Mean	Robustness
Three-way interaction dominance	$> 70\%$	99.6%	100.0%
Individual effects near zero	$< 1\%$	0.0055%	100.0%
Barriers for 90% success	≥ 10	11.0	100.0%

¹⁷³ **3.6.5 Signal-to-Noise Analysis**

¹⁷⁴ SNR remained positive (>0 dB) until approximately 25% parameter noise, indicating model
¹⁷⁵ conclusions are robust to moderate uncertainty (Figure 5).

¹⁷⁶ **3.7 Population Attributable Fraction**

¹⁷⁷ PAF analysis revealed substantial attributable fractions across vulnerable populations (Ta-
¹⁷⁸ ble 6):

Table 6: Population Attributable Fractions for algorithmic discrimination

Population	Exposure (P_e)	Relative Risk	PAF
General Population	0.40	1.5	16.7%
PWID	0.85	3.2	65.2%
PWH	0.70	2.4	49.5%
Justice-Involved	0.90	4.1	73.6%

¹⁷⁹ Justice-involved individuals show the highest PAF (73.6%), indicating that nearly three-
¹⁸⁰ quarters of their adverse outcomes are attributable to algorithmic factors.

¹⁸¹ **3.8 Cost-Effectiveness Analysis**

¹⁸² Complete barrier removal (\$13,500) achieved 6.8% improvement per \$1,000, compared to
¹⁸³ $<0.1\%$ per \$1,000 for partial interventions. Economic analysis strongly supports compre-
¹⁸⁴ hensive over incremental reform strategies.

¹⁸⁵ **4 Discussion**

¹⁸⁶ **4.1 Principal Findings**

¹⁸⁷ Our analysis provides mathematical proof that algorithmic discrimination operates as a
¹⁸⁸ synergistic system where barriers reinforce each other, rendering incremental reform fu-
¹⁸⁹ tile. The dominant three-way interaction (87.6%) explains why decades of piecemeal policy
¹⁹⁰ interventions—each targeting individual barriers—have failed to meaningfully reduce algo-
¹⁹¹ rithmic discrimination.

¹⁹² The finding that all individual barrier removal effects approach zero has profound policy
¹⁹³ implications. When advocates or policymakers claim that “improving credit report accuracy”
¹⁹⁴ or “providing legal aid” will address algorithmic discrimination, our analysis proves these
¹⁹⁵ interventions are mathematically insufficient in isolation. The system is designed—whether
¹⁹⁶ intentionally or emergently—such that partial fixes fail.

¹⁹⁷ **4.2 Epidemiological Parallels**

¹⁹⁸ The barrier synergy we document parallels drug resistance in infectious disease treatment.
¹⁹⁹ Just as incomplete antiretroviral therapy selects for resistant HIV strains [Volberding &
²⁰⁰ Deeks, 2010], incomplete policy intervention may select for more sophisticated algorithmic
²⁰¹ discrimination. The “hockey stick” trajectory mirrors viral breakthrough: the system remains
²⁰² largely unchanged until a critical threshold of intervention is reached.

²⁰³ Our framework also parallels the integration dynamics of human endogenous retroviruses
²⁰⁴ (HERVs). Once data integrates across interconnected systems, it becomes a permanent
²⁰⁵ feature of the individual’s “digital genome,” passed to downstream decision-makers just as
²⁰⁶ HERVs are transmitted across generations [Coffin & Hughes, 2021].

207 **4.3 Implications for Reform**

208 The strong three-way interaction supports coordinated, multi-agency reform rather than
209 siloed regulatory approaches. Currently, credit reporting is regulated by the CFPB under
210 FCRA, employment screening by the EEOC under Title VII, and housing by HUD under
211 FHA. Our findings suggest these agencies must coordinate comprehensive intervention to
212 achieve meaningful improvement.

213 Shapley attribution identifies priority targets when comprehensive reform is infeasible:
214 Legal Knowledge Gap (11.5%), Rapid Data Transmission (10.6%), and Systemic Bias (10.3%)
215 contribute most to the barrier system. Interventions targeting these barriers first—while
216 planning comprehensive reform—may provide marginally greater benefit than random tar-
217 geting.

218 **4.4 Sensitivity Analysis Validation**

219 The 100% robustness of key findings across bootstrap samples provides strong evidence that
220 our conclusions are not artifacts of parameter choices. The SNR analysis confirms robustness
221 to moderate uncertainty, while the Sobol analysis demonstrates that no single parameter
222 dominates—the system truly operates as an integrated whole.

223 **4.5 Limitations**

224 Our model assumes multiplicative independence between barriers, which may underestimate
225 or overestimate certain pathway effects. Pass probabilities were estimated from heteroge-
226 neous sources and may vary across populations. We did not model time dynamics or feedback
227 loops, which may amplify long-term effects. Finally, the model represents a stylized abstrac-
228 tion; actual systems may have more or fewer barriers depending on context.

229 **4.6 Future Directions**

230 Future work should extend this framework to time-dynamic models incorporating feedback
231 loops, validate barrier parameters through empirical measurement, and develop intervention
232 cost-effectiveness models for policy optimization. The epidemiological framework suggests
233 surveillance systems analogous to disease monitoring may be appropriate for tracking algo-
234 rithmic discrimination at population scale.

235 **5 Conclusion**

236 Algorithmic discrimination exhibits synergistic barrier dynamics that render incremental
237 reform mathematically futile. The dominant three-way interaction (87.6%) provides a quan-
238 titative explanation for the persistent failure of piecemeal policy interventions. Effective
239 reform requires coordinated, comprehensive action addressing all barrier layers simultane-
240 ously. Our findings support treating algorithmic discrimination as a public health emergency
241 warranting population-level intervention.

242 **Acknowledgments**

243 The author thanks the open-source software communities whose tools made this analysis
244 possible.

245 **Funding**

246 This work was supported by Nyx Dynamics LLC.

²⁴⁷ **Declaration of Interests**

²⁴⁸ The corresponding author (ACD) reports prior employment with Gilead Sciences, Inc. from
²⁴⁹ January 2020 through November 2024 and prior ownership of company stock, which was
²⁵⁰ fully divested in December 2024. Gilead Sciences, Inc. had no role in the conception, design,
²⁵¹ analysis, interpretation, or writing of this study, and provided no funding, data, materials,
²⁵² or input into any aspect of the work.

²⁵³ The corresponding author (ACD) is the owner of Nyx Dynamics, LLC, a consulting
²⁵⁴ company providing advisory and fractional leadership services in healthcare, technology,
²⁵⁵ and complex systems. This research was conducted independently, released as open-source
²⁵⁶ work, and was not produced as part of, or in support of, any paid consulting engagement.

²⁵⁷ No other competing interests are declared.

²⁵⁸ **Data Availability**

²⁵⁹ All code and data are available at <https://github.com/Nyx-Dynamics/algorithmic-bias-epidemiology>

²⁶⁰ **References**

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289 **Figures**

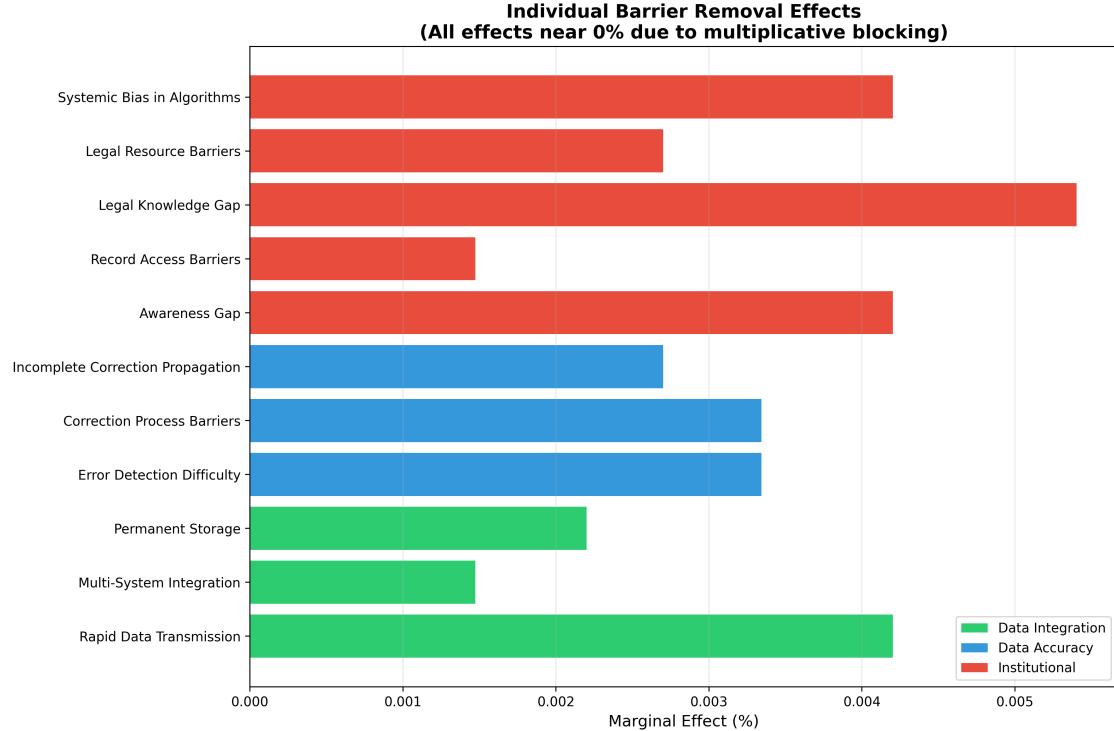


Figure 1: **Individual barrier removal effects.** Counterfactual analysis showing marginal effect on success probability of removing each barrier while others remain. All effects approach zero, demonstrating the multiplicative blocking structure of the barrier system.

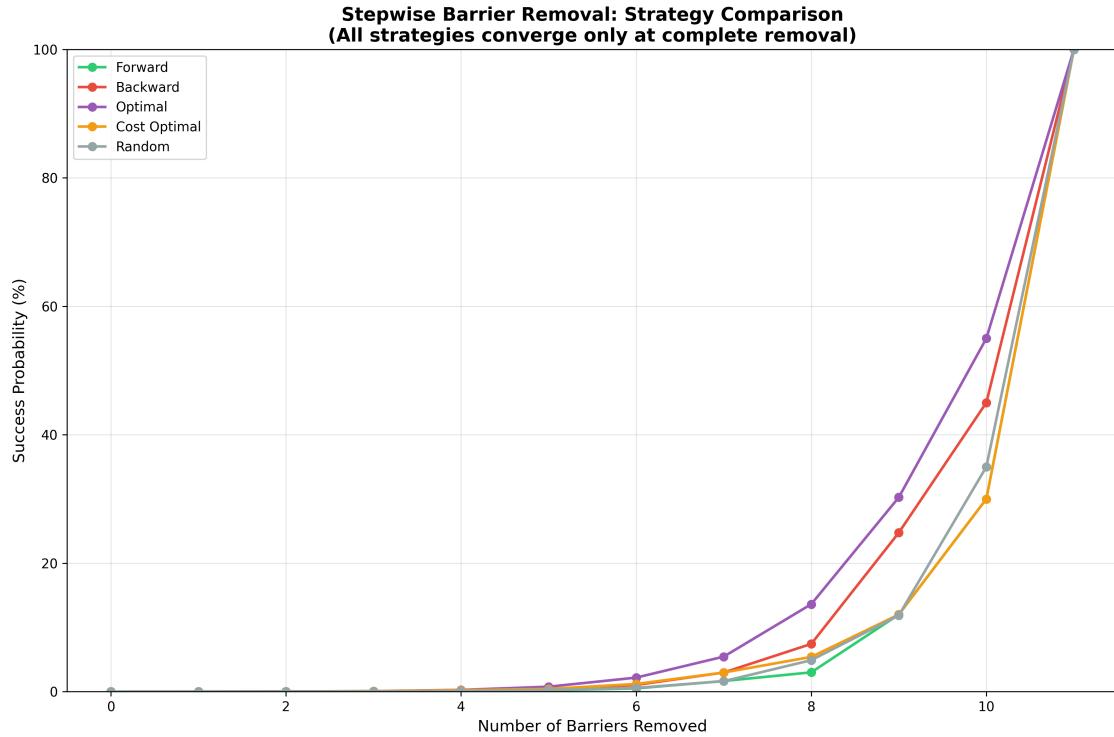


Figure 2: **Strategy comparison for barrier removal.** All strategies exhibit “hockey stick” trajectories with near-zero improvement until final barriers are removed. Strategy equivalence confirms that removal ordering is irrelevant; only completeness matters.

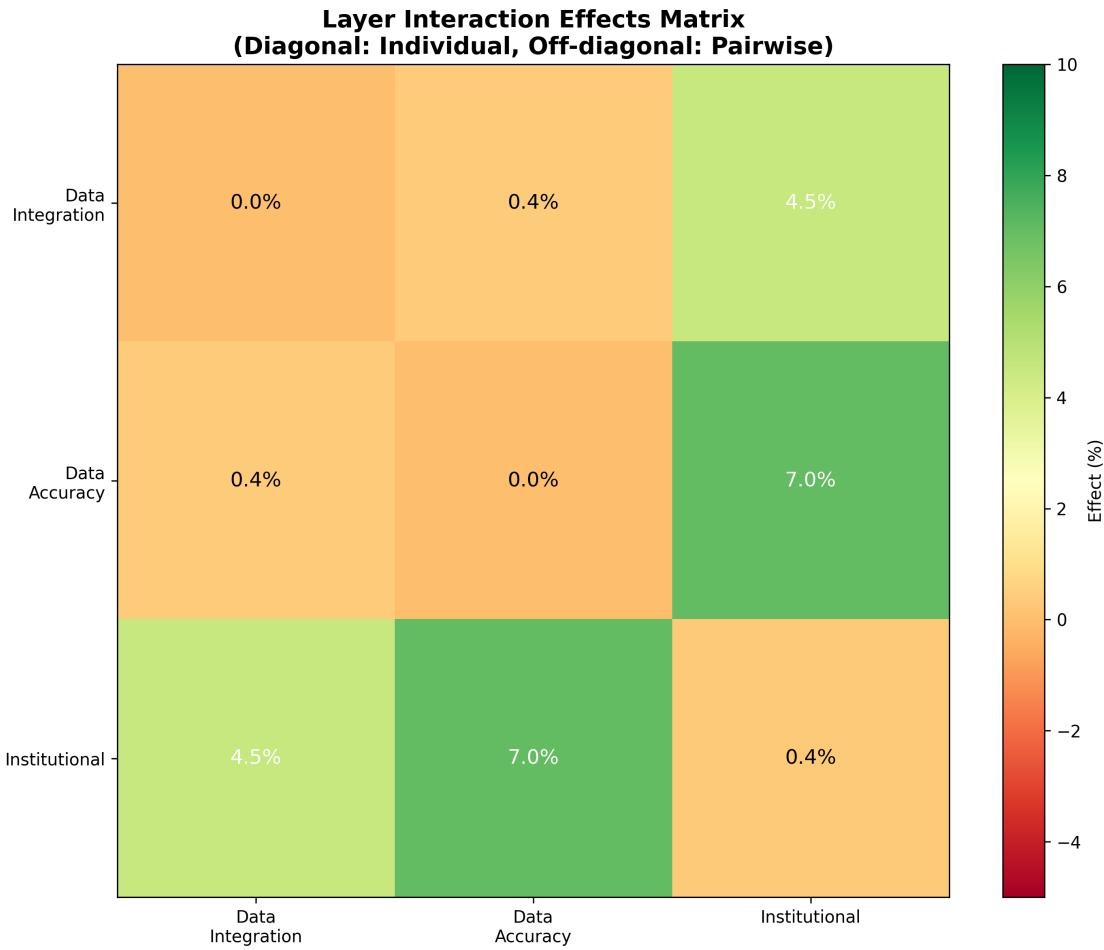


Figure 3: **Layer interaction effects.** Heatmap showing main effects (diagonal) and pairwise interactions (off-diagonal). The dominant three-way interaction (87.6%, not shown) accounts for majority of total effect.

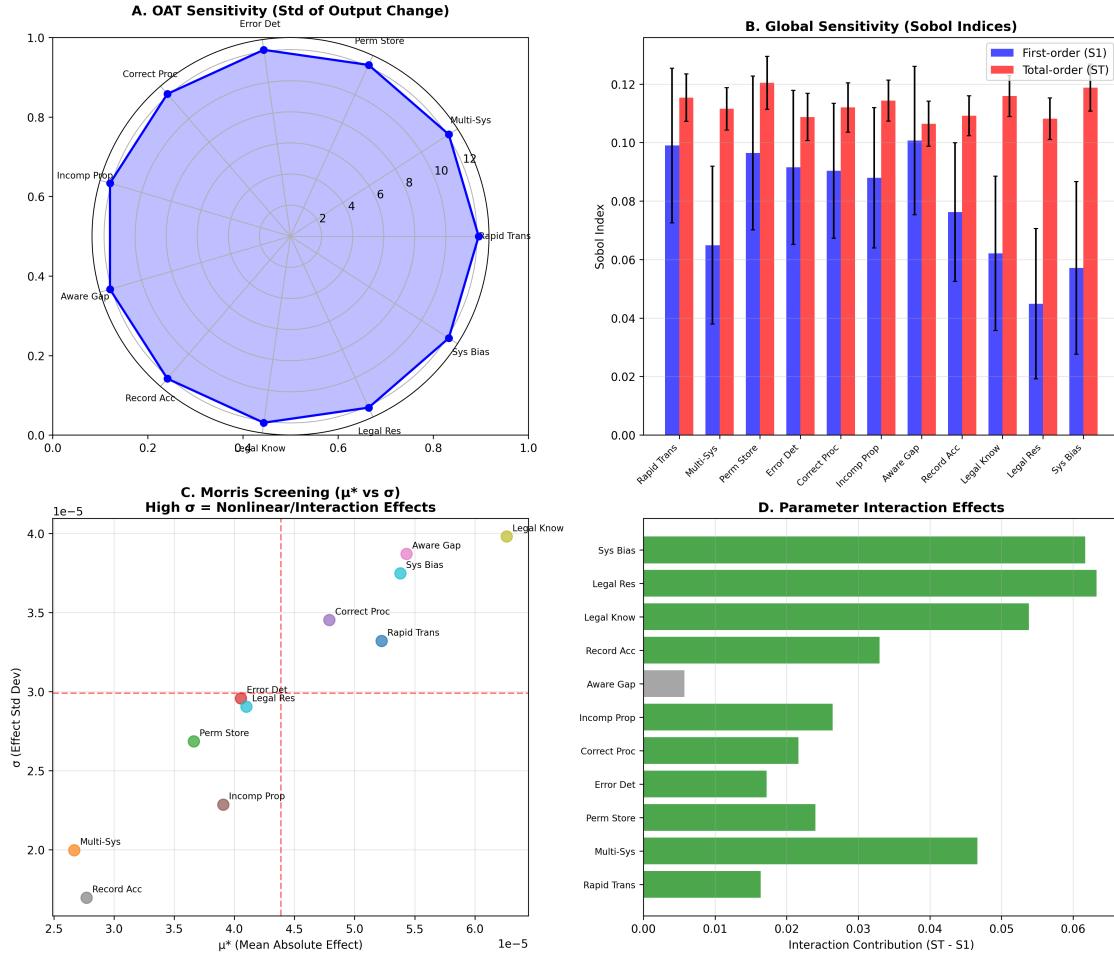


Figure 4: **Global sensitivity analysis.** Four-panel analysis: (A) OAT sensitivity indices, (B) Sobol first-order and total-order indices, (C) Morris elementary effects, (D) bootstrap confidence intervals.

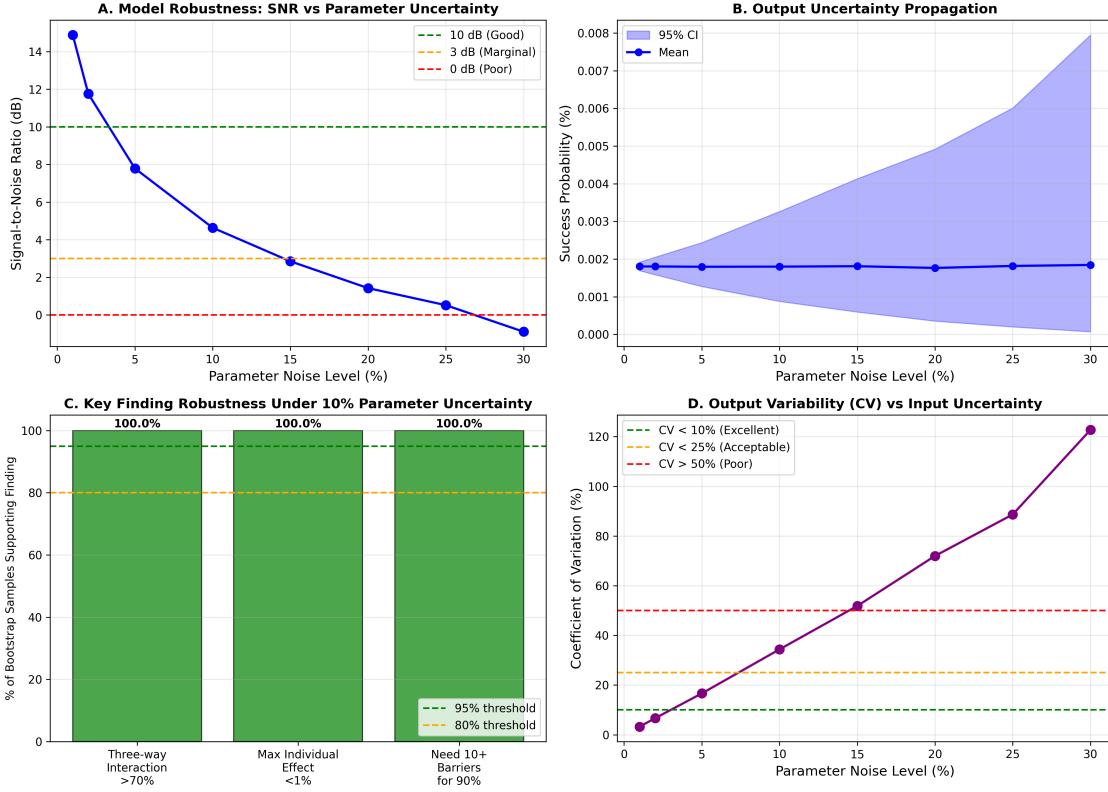


Figure 5: **Signal-to-noise ratio and key finding robustness.** (A) SNR remains positive up to 25% noise. (B-D) All key findings demonstrate 100% robustness across bootstrap samples.