## **Contents**

## 1 語法

### 1.1 c++

```
1 // c++ code
2 #include <bits/stdc++.h>
3 using namespace std;
4 int main(){
    std::ios::sync_with_stdio(false); // 加速
6
    return 0;
7 }
8
9 // struct宣告
10 struct s{
11 int x[100];
12
   int y[100];
13 };
14
15 s num; //一組s
16 num.x[1]=1;
17 num.y[1]=2;
18
19 // sort
20 sort(v.begin(), v.end())
                             // array 不能用
21 sort(v, v+n)
22 sort(v, v+n, greater<int>()) // 大到小
23
                             // 自己寫比較序列
24 sort(v, v+n, cmp)
25 bool cmp(型態 a, 型態 b){
                             // 大到小
26
    return a > b;
27 }
28
29 // set
30 s.insert(x) //將x插入s中 O(log(n))
31 s.count(x) //回傳x是否存在於s中() 0(log(n))
            //刪除在s中的x 0(log(n))
32 s.erase(x)
             //刪除s中所有元素 O(n)
33 s.clear()
             //回傳是否為空 0(1)
34 s.emptv()
             //回傳共有幾個元素 0(1)
35 s.size()
36
37 map
38 insert(x) //將 x 這個 pair 插入 map 中 0(log(n))
39 count(x) //回傳x這個key是否在map中 0(log(n))
40 erase(x) //刪除在map中key為x的 0(log(n))
41
42 // vector
43 vector<int> v // 宣告
44 v.push_back(1) // 推入數字
45 v.pop_back() // 拔出尾端數字
```

## 1.2 python

```
1 # EOF
    while True:
  2
        try:
  3
            你要執行的程式碼
  5
  6
        except EOFError:
  7
  8
           break
  9
 10
    # 有規定終止條件
3
 11
    while True:
3
3 13
 14
3
 15 # 數學符號
 16
    a//=10 # 整除
 17
    a**b # a^b
 18
6
 19 # 邏輯
 20 a=True
 21 b=False
    print(a and b) #False
 23
    print(a or b) #True
 24
 25 # scan
 26
    a = int(input())
    n=list(input().split(' '))
        連續輸入一串用空格隔開的數字
 28
 29
    for i in range(a):
        c, d = map(int, input().split()) # 連續輸入兩個數
 30
 31
 32 # print
    print('for is not a multiple of 11.'.format(a))
 34 print(a+" and "+b+" sitting in the tree")
 35 print('The parity of ',a,' is ',count,' (mod 2).')
 37 # 標頭檔math
 38
    import math
 39 math.gcd(a, b, c, d, e) # 最大公約數
 40 math.lcm(a, b, c, d, e) # 最小公倍數
                 #絕對值
    math.fabs(x)
    math.isqrt(n) #整數平方根
 43
    math.sqrt(x)
                 # 平方根
 44
    math.pow(x, y) # x^y
 45
 46 # count
 47 c+=b.count("商店") # 用在要計算好幾個字串時
                    # 一次算出一串字串有幾個'1'
    c=b.count('1')
 49
 50 # 進制轉換
    a = bin(a)[2:] # 10 to 2
 52
    a = hex(a)[2:] # 10 to 16
 53 \mid a = oct(a)[2:] \# 10 to 8
 54
 55 # 大小寫轉換
 56
    a.lower()
 57
    a.upper()
 58
 59 # 取長度
 60 a.len()
```

# 2 字串

## 2.1 KMP

```
1 #include <iostream>
2 using namespace std;
3
4 void KMP(string text, string pattern)
```

```
5 {
       int m = text.length();
6
7
       int n = pattern.length();
8
       // 如果模組沒東東
9
10
       if (n == 0)
11
       {
12
           cout << "The pattern occurs with shift 0";</pre>
13
      }
14
15
16
       // 如果文本的長度小於模組的長度
       if (m < n)
17
18
       {
           cout << "Pattern not found";</pre>
19
20
           return:
       }
21
22
       // next[i] 存儲下一個最佳部分匹配的索引
23
24
       int next[n + 1];
25
       for (int i = 0; i < n + 1; i++) {
26
27
           next[i] = 0;
28
29
       for (int i = 1; i < n; i++)</pre>
30
31
32
           int j = next[i];
33
           while (j > 0 && pattern[j] != pattern[i]) {
34
35
               j = next[j];
36
37
           if (j > 0 || pattern[j] == pattern[i]) {
38
39
               next[i + 1] = j + 1;
           }
40
      }
41
42
       for (int i = 0, j = 0; i < m; i++)
43
44
45
           if (text[i] ==
               pattern[j])//一樣如果+1j下一個檢查
46
           {
               if (++j == n) {
47
                   cout << "The pattern occurs with</pre>
48
                        shift " << i - j + 1 << endl;
49
               }
           }
50
           else if (j > 0)
51
52
               j = next[j]; //把她休崩變回來
53
                     // 還要回去啾啾
54
               i--;
           }
55
56
       }
57 }
58
59 int main()
60 {
61
       string text = "ABCABAABCABAC";
62
       string pattern = "CAB";
63
64
       KMP(text, pattern);
65
66
       return 0;
67 }
```

# 3 數論

### 3.1 曜

```
1 #include <iostream>
2 using namespace std;
3 int a[20];
4
```

```
5
  int main() {
       6
7
       bool flag;
       while (cin >> cases){
8
9
           while (cases--){
               cin >> target;
10
11
               cin >> sticks;
12
               for (int i = 0; i < sticks; i++){</pre>
                    cin >> a[i];
13
               }
14
15
               num = 1;
               for (int i = 1; i < sticks; i++){</pre>
16
17
                    num <<= 1;
                    num++;
18
19
               }
               flag = false;
20
21
               for (int _i = 0; _i <= num; _i++){</pre>
22
                    tmp = 0;
23
                    i = _i;
                    for (int j = 0; j < sticks; j++){</pre>
24
                        if (i & 1) tmp += a[j];
25
26
                        i >>= 1:
                    }
27
28
                    if (tmp == target){
29
                        flag = true;
                        break;
30
31
                    }
32
33
               if (flag) cout << "YES\n";</pre>
               else cout << "NO\n";</pre>
34
           }
35
36
       }
37 }
```

## 3.2 Fibonaccimal

```
1 #include <bits/stdc++.h>
2
  using namespace std;
 3
   int main(){
 4
 5
       int N;
       int Fibonacci[40] = {0, 1}; //開始的兩個數
 7
 8
       int i;
9
10
       for(i = 2; i < 40; i++){
            Fibonacci[i] = Fibonacci[i - 1] + Fibonacci[i
11
                - 2];
12
13
       scanf("%d", &N);
14
15
       while(N--){
16
17
18
            int num;
            bool flag = false;
19
20
            scanf("%d", &num);
21
22
            printf("%d = ", num);
23
            for(i = 39; i \ge 2; i - -){
24
25
                if(num >= Fibonacci[i]){
26
                     num = num - Fibonacci[i];
27
                     flag = true;
28
                     printf("1");
                }
29
30
                else if(flag){
                     printf("0");
31
32
            }
33
34
35
            printf(" (fib) \setminus n");
36
       }
37
38
       return 0;
39 }
```

//奇

#### 3.3 LCM 1 int GCD(int num1, int num2) 2 | { **if**(num2==0) 3 4 { 5 return num1; 6 } 7 return GCD(num2, num1%num2); 8 9 } 10 11 int LCM(int num1, int num2) //2個最小公倍數 12 { return((num1\*num2)/GCD(num1, num2)); 13 14 } 15 16 int LCM2(int num1, int num2, int num3) //3個最小公倍數 17 \ \ return((num1\*num2)/GCD((num1, num2), num3)); 18 19 } 20 21 int main() 22 | { cout << GCD (6,3); 23 24 cout << LCM(6,3); 25 cout << LCM2(6,3,3); 26 27 return 0; 28 }

## 3.4 LCS

```
1 #include <bits/stdc++.h>
2 using namespace std;
3 int main()
4 {
5
       string str1, str2;
6
       short lcs[2][1000];
       while (cin >> str1 >> str2)
7
8
9
           lcs[0][0] = str1[0] == str2[0];
10
           for (int j=1; j<str2.length(); j++) lcs[0][j]</pre>
                = max(lcs[0][j-1],
                short{str1[0]==str2[j]});
11
           for (int i=1; i<str1.length(); i++)</pre>
12
13
                bool r = i \& 1;
14
                lcs[r][0] = max(lcs[r^1][0],
                    short{str1[i]==str2[0]});
15
                for (int j=1; j<str2.length(); j++)</pre>
16
                    lcs[r][j] = str1[i]==str2[j] ?
                         lcs[r^1][j-1] + 1 :
                         max(lcs[r^1][j], lcs[r][j-1]);
17
           }
18
               lcs[(str1.length()-1)&1][str2.length()-1]
                << '\n';
       }
19
20
       return 0;
21 | }
```

### 3.5 LPS

```
1 #include < bits / stdc ++. h>
2 #include < iostream >
3
 using namespace std;
5
  int main(){
6
      string s;
7
      cin >> s;
8
      int maxlen=0, 1, r;
      for(int i=0; i<s.length(); i++){</pre>
```

```
int x = 0;
11
12
           while((s[i-x]==s[i+x]) && (i-x>=0) &&
               (i+x<s.length())){//當找到一個中心點以其為中間然後及
13
          }
14
15
           x - -;
          if(2*x+1)
16
               \maxlen){//只有第一次會\max==後後面就追不到那女孩
               maxlen = 2*x+1; //最大的
17
              1 = i-x;//計算頭頭
18
19
              r = i+x;//計算尾巴
20
          }
21
          //偶
22
          x = 0;
           while (s[i-x]==s[i+1+x]) \& (i-x>=0) \& 
23
               (i+1+x<s.length()))
              χ++;
24
25
          }
          if(2*x > maxlen){
26
27
               maxlen = 2*x;
              1 = i - x + 1;
28
29
              r = i + x;
30
          }
31
      }
32
       cout << maxlen << '\n';</pre>
      cout << 1+1 << ' ' << r+1 << '\n';
33
34
35 }
```

## 3.6 Pairty

```
1 #include <iostream>
  #include <algorithm>
3
  using namespace std;
  int main() {
5
       int I, n;
6
7
       while (cin >> I) {
           if (I == 0) break;
8
9
           string B = "";
           n = I:
10
           int cnt = 0;
11
12
           while (n){
13
                cnt += (n & 1);
                B += '0' + (n \& 1);
14
                n >>= 1;
15
16
           reverse(B.begin(), B.end());
17
           cout << "The parity of " << B << " is " <<
18
                cnt << " (mod 2).\n";</pre>
19
       }
20
       return 0;
21 }
```

## 圖論

## 最短路徑 dijkstra

```
1 // 邊權重皆為正數時使用
2 // 1.
     輸入有總點、總邊,接著輸入點,點,距離(權重)時使用
 #include <iostream>
  #include <vector>
  #include <climits>
7
  using namespace std;
  // 定義城市數量的上限
9
10
  #define MAX_CITIES 100
11
```

```
12 // 定義無限大的距離
                                                              3 #define N 100
13 #define INF INT_MAX
                                                                using namespace std;
14
15 // 城市數量、道路數量
                                                              6
                                                                int map[N][N], visited[N][N]={0};
                                                                typedef pair<int, int> p;
16 int numCities, numRoads;
                                                                int n,m,found=0;
17
                                                                deque path;
18 // 圖的鄰接矩陣表示法
                                                              10
19 vector < vector < int > > graph (MAX_CITIES,
                                                                void dfs(int x, int y){
                                                             11
       vector<int>(MAX_CITIES, INF));
                                                             12
                                                                  if (found==1) return;
20
                                                             13
                                                                  visited[x][y]=1;
21
                                                                  path.push_back(make_pair(x,y));
       Di jkstra演算法,計算從指定城市出發到其他城市的最短路性
                                                                  if (x==n-1 \&\& y==m-1){
   void dijkstra(int startCity) {
22
                                                                    found=1:
                                                             16
23
       vector<int> dist(numCities, INF);
                                                             17
                                                                    cout << "Path: ";</pre>
24
       vector < bool > visited(numCities, false);
                                                             18
                                                                    while(!path.empty()){
25
                                                             19
                                                                      cout<<"("<<path.front().first<<", "<<path.front().second<</pre>
26
       dist[startCitv] = 0:
                                                             20
                                                                      path.pop_front();
27
                                                                      \verb|cout|<<((path.empty())?" | n":" \rightarrow ");
                                                             21
       for (int i = 0; i < numCities - 1; i++) {</pre>
28
                                                             22
           int u = -1;
29
                                                             23
                                                                    cout << endl;
30
           for (int j = 0; j < numCities; j++) {</pre>
                                                             24
                                                                    return:
31
               if (!visited[j] && (u == -1 || dist[j] <</pre>
                                                                  }
                                                             25
                   dist[u])) {
                                                                  if (x+1<n && visited[x+1][y]==0 && map[x+1][y]==0){</pre>
                                                             26
                   u = j;
32
                                                             27
                                                                    dfs(x+1,y);
33
                                                             28
                                                                    path.pop_back();
34
           }
                                                             29
35
                                                                  30
36
           visited[u] = true;
                                                             31
                                                                    dfs(x.v+1):
37
                                                             32
                                                                    path.pop_back();
           for (int v = 0; v < numCities; v++) {</pre>
38
                                                             33
               if (!visited[v] && graph[u][v] != INF) {
39
                                                              34
                                                                  if (x-1)=0 \& visited[x-1][y]==0 \& map[x-1][y]==0){
40
                   dist[v] = min(dist[v], dist[u] +
                                                             35
                                                                    dfs(x-1,y);
                        graph[u][v]);
                                                             36
                                                                    path.pop_back();
               }
41
                                                             37
42
           }
                                                             38
                                                                  if (y-1>=0 && visited[x][y-1]==0 && map[x][y-1]==0){
      }
43
                                                             39
                                                                    dfs(x,y-1);
44
                                                             40
                                                                    path.pop_back();
       // 輸出最短路徑結果
45
                                                              41
46
       cout << "從城市 " << startCity << "
                                                             42 }
           出發到其他城市的最短路徑如下: " << endl;
                                                             43
47
       for (int i = 0; i < numCities; i++) {</pre>
                                                             44 int main(){
48
           if (i != startCity) {
                                                             45
                                                                  cin>>n>>m:
               cout << "到城市 " << i << " 的最短距離為
49
                                                                  for (int i=0; i<n; i++)</pre>
                                                             46
                    " << dist[i] << endl;
                                                                    for (int j=0; j<m; j++)</pre>
                                                             47
50
           }
                                                              48
                                                                      cin>>map[i][j];
51
                                                             49
                                                                  dfs(0,0);
52 }
                                                                  if (found==0){
                                                             50
53
                                                             51
                                                                    cout << "No routes accessible.\n";</pre>
54 int main() {
                                                                  }
                                                             52
       // 讀取城市數量和道路數量
55
                                                             53
                                                                  return 0;
       cin >> numCities >> numRoads;
56
                                                             54 }
57
                                                             55 // 顯示最短距離
       // 初始化圖的鄰接矩陣
58
                                                                #include <iostream>
                                                             56
59
       for (int i = 0; i < numRoads; i++) {</pre>
                                                                #include <utility>
60
           int city1, city2, distance;
                                                             58 #include <deque>
61
           cin >> city1 >> city2 >> distance;
                                                              59 #define N 100
62
           graph[city1][city2] = distance;
                                                             60 using namespace std;
           graph[city2][city1] = distance; //
63
               因為是雙向道路
                                                             62
                                                                int map[N][N], visited[N][N]={0};
                                                             63 typedef pair<int, int> p;
      }
64
65
                                                             64 int n,m,dis=-2;
       // 選擇起始城市,這裡以城市@為例
66
                                                             65
                                                                deque path;
                                                             66
67
       int startCity = 0;
                                                             67
                                                                void dfs(int x, int y){
68
                                                                  visited[x][y]=1;
                                                             68
69
       // 執行Dijkstra演算法
                                                             69
                                                                  path.push_back(make_pair(x,y));
70
       dijkstra(startCity);
                                                                  if (x==n-1 & y==m-1){
                                                             70
71
                                                                    if (dis==-1){
                                                             71
72
       return 0;
                                                             72
                                                                      dis=path.size()-1;
73 }
                                                             73
                                                             74
                                                                    else {
                                                                      if (path.size()-1<dis) dis=path.size()-1;</pre>
                                                             75
  4.2 DFS
                                                             76
                                                             77
                                                             78
                                                                  if (x+1<n && visited[x+1][y]==0 && map[x+1][y]==0){</pre>
1 // 印出最快路徑 (座標)
```

79

2 #include <bits/stdc++.h>

dfs(x+1,y);

```
80
        visited[x+1][y]=0;
                                                                    39
                                                                    40
81
        path.pop_back();
82
83
      if (y+1<m && visited[x][y+1]==0 && map[x][y+1]==0){</pre>
84
        dfs(x,y+1);
85
        visited[x][y+1]=0;
86
        path.pop_back();
87
      if (x-1)=0 \& visited[x-1][y]==0 \& map[x-1][y]==0){
88
89
        dfs(x-1,y);
90
        visited[x-1][y]=0;
        path.pop_back();
91
92
      if (y-1>=0 \&\& visited[x][y-1]==0 \&\& map[x][y-1]==0){
93
94
        dfs(x,y-1);
        visited[x][y-1]=0;
95
        path.pop_back();
96
97
98|}
99
100 int main(){
101
      cin>>n>>m;
102
      for (int i=0; i<n; i++)</pre>
103
        for (int j=0; j<m; j++)
          cin>>map[i][j];
104
105
      dfs(0.0):
      if (dis==-2)
106
107
        cout << "No routes accessible.\n";</pre>
108
      else
109
        cout << "Shortest distance: "<<dis<<endl;</pre>
110
      return 0;
111 }
```

## 4.3 merge sort

```
1 #include <iostream>
2 using namespace std;
3
4 //做比較大小的部分
5
  void merge(int arr[], int l, int m, int r, int size)
6 {
7
       int i = 1;
8
       int j = m + 1;
9
       int k = 1;
10
11
       /* create temp arrav */
12
       int temp[size];
13
14
       while (i <= m && j <= r) {</pre>
           if (arr[i] <= arr[j]) {</pre>
15
                temp[k] = arr[i];
16
17
                i++;
                k++;
18
19
           }
20
            else {
                temp[k] = arr[j];
21
22
                j++;
                k++;
23
           }
24
25
26
       / Copy the remaining elements of first half, if
            there are any /
27
       while (i <= m) {</pre>
28
            temp[k] = arr[i];
           i++;
29
30
           k++;
       }
31
32
33
       / Copy the remaining elements of second half, if
            there are any /
       while (j <= r) {
34
35
            temp[k] = arr[j];
36
            j++;
37
            k++;
       }
38
```

```
41
      for (int p = 1; p <= r; p++) {</pre>
           arr[p] = temp[p];
42
43
44
  }
45
  //做分開陣列的部分
46
47
  void mergeSort(int arr[], int 1, int r, int size)
48
  {
49
       if (1 < r) {
50
           // 找中間點 ex:陣列五個元素0-4 2是中間點
           //陣列分成兩組 0-2/3-4兩個部分
51
52
           //舉0-2陣列來說 中間點是1
           //陣列再分成 Ø-1/2兩個部分
53
           int m = (1 + r) / 2;
54
55
           / 遞迴第一和第二部分*/
56
57
           //(也就是不斷的分)
           mergeSort(arr, 1, m, size);
58
           mergeSort(arr, m + 1, r, size);
59
60
           // merge
61
62
           //當我分到不能再分 比較陣列內數值 小的放前面
63
           merge(arr, 1, m, r, size);
64
      }
65
  }
66
67 int main()
68
  {
       cout << "Enter size of array: " << endl;</pre>
69
70
      int size;
71
       cin >> size;
72
      int myarray[size];
73
       cout << "Enter " << size << " integers in any
74
           order: " << endl;</pre>
       for (int i = 0; i < size; i++) {</pre>
75
76
           cin >> myarray[i];
77
      cout << "Before Sorting" << endl;</pre>
78
79
      for (int i = 0; i < size; i++) {</pre>
80
           cout << myarray[i] << " ";</pre>
81
82
      cout << endl;</pre>
83
      mergeSort(myarray, 0, (size - 1), size); //
           mergesort(arr,left,right) called
84
85
       cout << "After Sorting" << endl;</pre>
86
      for (int i = 0; i < size; i++) {</pre>
           cout << myarray[i] << " ";</pre>
87
88
89
90
       return 0;
91 }
```

/ Copy the temp array to original array /

## 4.4 quick sort

```
1 include <iostream>
2 using namespace std;
  // quick sort sorting algorithm
3
4
  int Partition(int arr[], int s, int e)
5
  {
  int pivot = arr[e];
7
   int pIndex = s;
8
9
   for(int i = s;i<e;i++)</pre>
10
   {
11
       if(arr[i]<pivot)</pre>
12
13
       int temp = arr[i];
14
       arr[i] = arr[pIndex];
15
       arr[pIndex] = temp;
      //swapping 也就是說如果當前數值比指標小
16
           他就移到最前面
```

```
//也就是陣列0的位置
17
18
       pIndex++:
       //下一個比指標小的數值放進陣列1的位置
19
20
   }
21
22
23
   int temp = arr[e];
   arr[e] = arr[pIndex];
24
25 arr[pIndex] = temp;
   //比指標數值小的都去前面了
26
   //將指標放到目前計數到的陣列位置
27
   //那指標前都比她小 指標後都比他大
   return pIndex; //回傳給p值
29
30 }
31
32 void QuickSort(int arr[], int s, int e)
33 //s stand for start index
34 //e stand for end index also (size-1)
35 {
   if(s<e)</pre>
36
37 {
38 int p = Partition(arr,s, e);
39 QuickSort(arr, s, (p-1));
40 // recursive QS call for left partition
41 //做陣列前半部分 因為都比指標小 去進行內部排序
  QuickSort(arr, (p+1), e);
42
43 // recursive QS call for right partition
44 }
45 }
46
47 int main()
48 {
49
50
   int size=0;
51
   cout << "Enter Size of array: "<<endl;</pre>
52
   cin>>size:
   int myarray[size];
53
   cout<<"Enter "<<size<<" integers in any order:</pre>
55
        "<<endl;
   for(int i=0;i<size;i++)</pre>
56
57
   {
58
   cin>>myarray[i];
59
   cout << "Before Sorting" << endl;</pre>
60
   for(int i=0;i<size;i++)</pre>
61
62
   cout << myarray[i] << " ";</pre>
63
64
   cout << end1;
65
66
   QuickSort(myarray,0,(size-1)); // quick sort called
67
68
   cout << "After Sorting" << endl;</pre>
69
70
   for(int i=0;i<size;i++)</pre>
71
   cout << myarray[i] << " ";</pre>
72
73
   }
74
75
   return 0;
76 }
```

## 4.5 二分搜

```
#include < iostream >
using namespace std;

int binarySearch(int arr[], int left, int right, int
    x) {
    while (left <= right) {
        int mid = left + (right - left) / 2;

    if (arr[mid] == x) {
        return mid;
    }
}</pre>
```

```
11
        else if (arr[mid] < x) {</pre>
        left = mid + 1;
12
13
      }
14
        else {
15
         right = mid - 1;
16
17
    }
18
19
     return -1;
20
21
  int main() {
22
23
    int myarr[10];
    int num;
24
25
    int output;
26
27
    cout << "Please enter 10 elements ASCENDING order"</pre>
         << endl;
     for (int i = 0; i < 10; i++) {
28
29
      cin >> myarr[i];
30
31
    cout << "Please enter an element to search" << endl;</pre>
32
    cin >> num;
33
34
     output = binarySearch(myarr, 0, 9, num);
35
36
    if (output == -1) {
      cout << "No Match Found" << endl;</pre>
37
38
    } else {
       cout << "Match found at position: " << output <<</pre>
39
           endl:
40
    }
41
42
    return 0;
43 }
44 如果我們超過25頁我還可以再縮減程式區 這是比較完整的
45
  Floyd
46
  void floyd(){
47
           for(intk=0; k<n; k++){ //中間點
48
               for(int i=0;i<n;i++){</pre>
49
                    for(int j=0;j<n;j++){</pre>
                        dp[i][j]=min(dp[i][j],dp[i][k]+dp[k][j]);
50
                        //經過中間點k的路徑是否小於原始路徑
51
                        //小於則更新 不小於則不變動
52
                        //窮舉所有鬆弛的可能
53
                   }
54
55
               }
56
           }
57
      }
```