



Functional Programming--Scheme
(Variable, Expression, and Function)

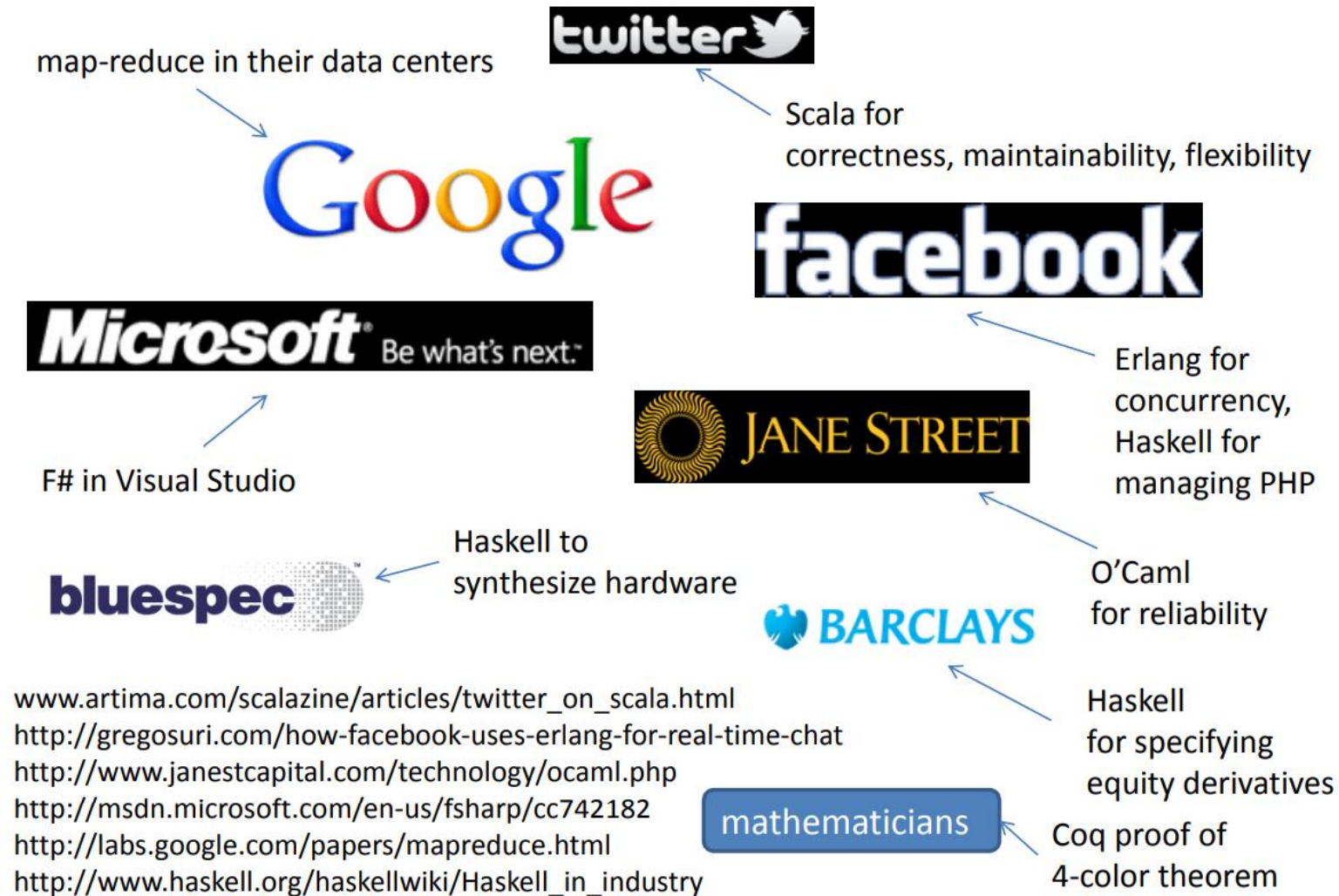
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Why Study Functional Programming ?



- Expose you to a new programming model
 - Functional Programming (FP) is drastically different
 - Scheme: no loops; recursion everywhere
- FP has had a long tradition
 - Lisp, Scheme, ML, Haskell, ...
 - The debate between FP and imperative programming
- FP continues to influence modern languages
 - Most modern languages are multi-paradigm languages
 - Delegates in C#: higher-order functions
 - Python: FP; OOP; imperative programming
 - Scala: mixes FP and OOP
 - C++11: added lambda functions
 - Java 8: added lambda functions in 2014
 - Erlang: behind WhatsApp

Who's using them?



A Functional Programming Language



λ Scheme

- An interactive, integrated, graphical programming environment for Scheme
- Installation
 - You could install it on your own machines
 - <http://racket-lang.org/>
- Be sure that the language “Standard (R5RS)” is selected
 - Click Run

Scheme is Simple



- Design for teaching” “A language for describing processes”
- Almost minimally simple syntax
- Only one thing you can do
- Only one data structure

Scheme is Simple: The one thing you can do



`(operator operand1 operand2 ...)`

Simple - Scheme Expressions

- Prefix notation (Polish notation):
 - $3+4$ is written in Scheme as $(+ 3 4)$
 - Parentheses are necessary
 - Compare to the infix notation: $(3 + 4)$
- $4+(5 * 7)$ is written as
 - $(+ 4 (* 5 7))$
 - Parentheses are necessary

Simple – Arithmetic

➤(+ 3 4)

7

➤(* 3 4)

12

➤(+ 5 (* 2 2))

?

Your Turn

- In Scheme, “ $(3+8)+2$ ” is written as

A. $(+ (3 + 8) 2)$

B. $(+ 2 (+ 3 8))$

C. $(+ (+ 3 8) 2)$

D. $+ (+ 3 8) 2$

E. $(+ + 3 8 2)$

Your Turn

- In Scheme, “3+8/2” is written as

A. $(+ (8 / 2) 3)$

B. $(+ 3 (/ 8 2))$

C. $(+ (/ 8 2) 3)$

D. $(+ 3 (/ 2 8))$

E. $3 + (/ 8 2)$

Scheme Variables

- Variables
 - (define pi 3.14)
 - No need to declare types
- Variables are case insensitive
 - pi is the same as Pi

Simple – Defining values

➤ (define foo 3)

➤ foo

3

➤ (* foo 4)

? 3 4
12

Scheme Expressions

- General syntax: $(E_1 \ E_2 \ \dots \ E_k)$

Function
to invoke

Function
arguments

- Applying the function E_1 to arguments E_2, \dots, E_k

- Examples: $(+ \ 3 \ 4)$, $(+ \ 4 \ (* \ 5 \ 7))$

$$4 + 3 \times 5 = 39$$

- Uniform syntax, easy to parse

$$(f, a, a_2, a_3)$$

User-Defined Functions

- Mathematical functions
 - Take some arguments; return some value

• E.g., $f(x) = x^2$

• $f(3) = 9$; $f(10) = 100$

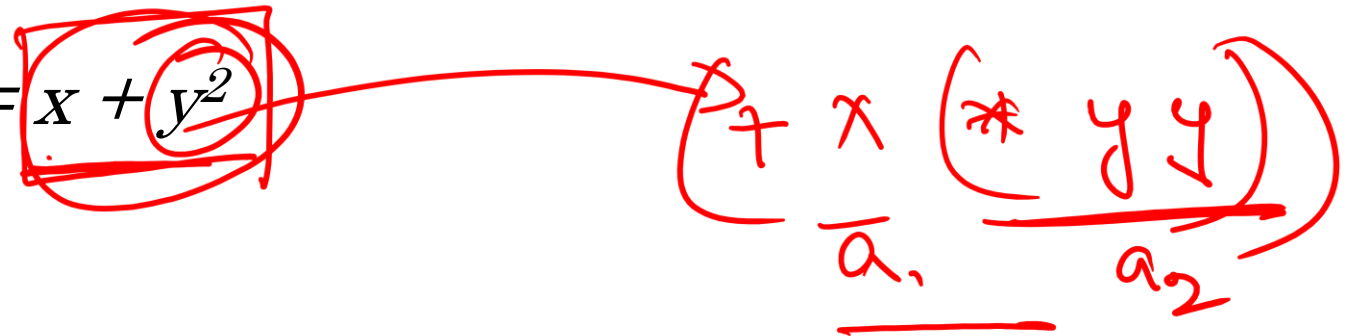
- Scheme syntax

• (define (square x) (* x x))

• A two-argument function: $f(x,y) = x + y^2$

• (define (f x y) (+ x (* y y)))

• calling the function: (f 3 4)



Simple – Defining function

➤ (define (square x) (* x x))

➤ (square 4) ✓

16

➤ (+ (square 2) (square 3))

?

(+ 4 9)

= 13

Built-in Functions

0 / 1 / more

- $+$, $*$
- take 0 or more parameters
- applies operation to all parameters together

• $(+ 2 4 5) = 11$

• $(* 3 2 4) = 24$

- zero or one parameter?

• $(+)$ $\rightarrow 0$

• $(*)$ $\rightarrow 1$

• $(+ 5)$ $\rightarrow 5$

• $(* 8)$ $\rightarrow 1 * 8 = 8$

$4 + 5$
 $(-)$

$3 * 4$
 $(-)$

def prod()

f.val = 1

list = [...]

for ()

f.val = f.val * list[i]

return f.val

def sum()

total = 0

list = [...]

for ()

total = total + list[i]

return total

Simple – Flow control

➤ (define (abs x)
 (if (< x 0)
 (- x) \Rightarrow \times
 x)

➤ (abs -3)
3

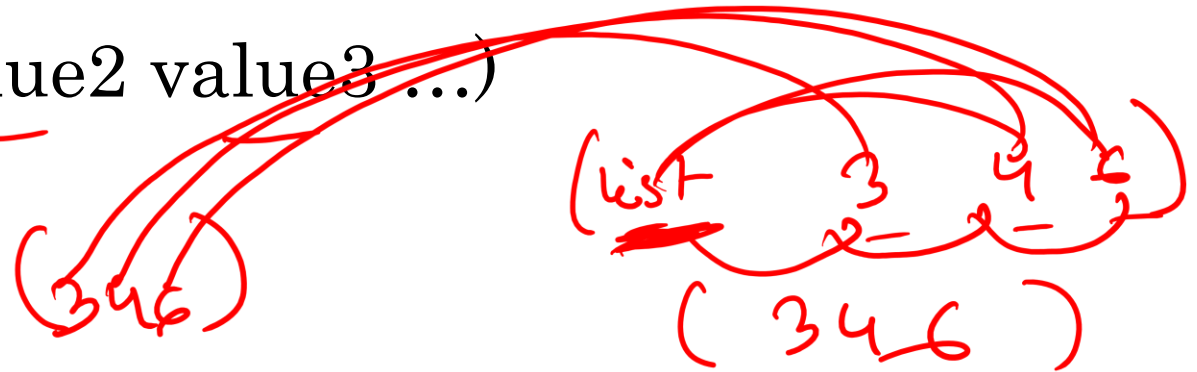
➤ (abs 3)
3

Scheme is Simple: The one data structure

(value1 value2 value3 ...)

; To make one, we write:

(list value1 value2 value3 ...)



Simple – Using data

➤ (sort (list 4 6 5))
(4 5 6)

➤ (length (list 1 2))
2
(1 2)

Scheme is Weird

- Functional
- Dynamic typing
- Functions are values

Weird – Functional – list manipulation

➤ (define my-list (list 1 2 3 4 5))

➤ my-list
(1 2 3 4 5)

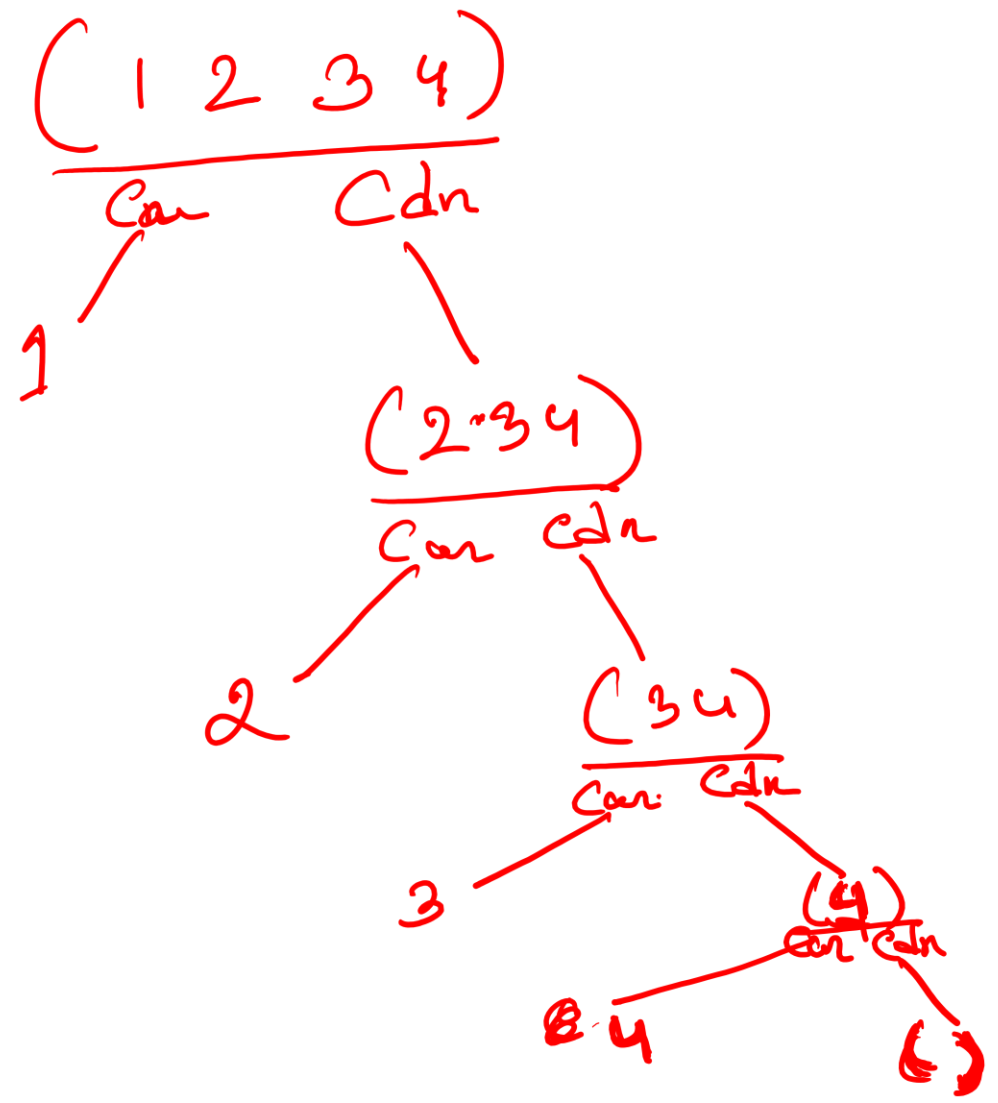


A diagram showing the list (1 2 3 4 5) with the first element 1 circled and labeled 'head' with a downward arrow. The remaining elements 2 3 4 5 are grouped under a horizontal line and labeled 'tail' with a downward arrow.

➤ (car my-list)
1

car → ()

➤ (cdr my-list) ✓
(2 3 4 5)





Weird – Dynamic typing

- (define (improved-code q) (* q 2))
poor (handwritten below q)
 - (define code-quality 4)
 - (improved-code code-quality)
8 (handwritten and circled to the left)
 - (define code-quality "poor")
↓ (handwritten arrow pointing to "poor")
 - (improved-code code-quality)
**: expects type as 1st argument, give.....* (handwritten below)
- ⇒ 8* (handwritten, with a red arrow pointing from the first line to this result)

*(* "poor" 2)* (handwritten)

Weird – Functions are values

➤ (define (double value) (* 2 value))

➤ (define (apply-twice fn value) (fn (fn value)))

➤ (apply-twice double 2)

8

(apply-twice (lambda(x) (* x x)) 2)

(fn . (fn value))

(double (double 2))

(double (* 2 2))

→ (* 2 (* 2 2)) ⇒ (* 2 4)
⇒ 8

Scheme is Cool



- Generic without all that syntax

➤ (sort (list 5 4 3 2 1) <)
(1 2 3 4 5)

➤ (sort (list "abc" "a" "ab") string<?)
("a" "ab" "abc")

Anonymous Functions

- Syntax based on Lambda Calculus: $\lambda x. x^2$
- Anonymous functions
 - (lambda (x) (* x x))
 - are small function can take any number of arguments, but can only have one expression
 - are often arguments being passed to higher-order function
 - are not bound to an identifier
 - can be used only once: ((lambda (x) (* x x)) 3)
 - Introduce names
 - (define square (lambda (x) (* x x)))
 - Same as (define (square x) (* x x))

Scheme Parenthesis

- Scheme is very strict on parentheses
 - which is reserved for function call (function invocation)
 - (+ 3 4) vs. (+ (3) 4)
 - (lambda (x) x) vs. (lambda (x) (x))
 - the second treats (x) as a function call
 - (lambda (x) (* x x)) vs. (lambda (x) (* (x) x))



(-)

x vs (x)

Defining Recursive Functions

- (define diverge (lambda (x) (diverge (+ x 1))))

- Call this a diverge function

3
4

~~3~~ + 3 1 = 4
+ 4 1 = 5

diverge 3
diverge 4
diverge 5