



Types

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# Basic Types



- Types that are not defined on top of other types
  - Examples: int, float, bool, char
  - Composite types: struct types; arrays; pointer types; function types ...

# Memory units for storing types

- Terminology in use with current 32-bit computers:
  - Nibble: 4 bits (a hex digit)
  - Byte: 8 bits
  - Half-word: 16 bits
  - Word: 32 bits
  - Double word: 64 bits
  - Quad word: 128 bits

# Integer types

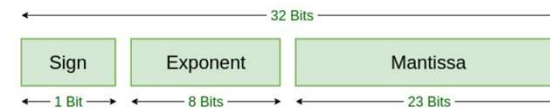


- In most languages, integer types are finite in size.
- For example, Java
  - byte: 8-bits; short: half-word; int: a word; long: a double word
- So,  $a + b$  may overflow the finite range.
  - E.g.,  $(2^{32} - 1) + 1 \rightarrow 0$
- There's also a difference between signed and unsigned representations

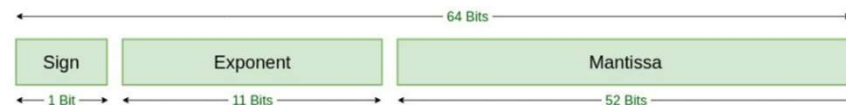
# Floating point types



- Model real numbers, but only as approximations
- Single precision (float): 32 bits, double precision (double): 64 bits
- IEEE Standard 754 Floating Point Numbers are represented using three components
  - The sign of Mantissa
  - Exponent
  - Mantissa



Single Precision  
IEEE 754 Floating-Point Standard



Double Precision  
IEEE 754 Floating-Point Standard

# Boolean and Character (omit)



- Boolean: true, false
  - Could be implemented as bits, but often as bytes
  - Advantage: increase readability
- Character
  - Stored as numeric codings (e.g., ASCII, ISO 8859-1, Unicode: Java, JavaScript, C#)
  - UTF-8, UTF-16, UTF-32

# Enumeration types



- Enumeration (C/C++):
  - `enum day {Monday, Tuesday, Wednesday, Thursday, Friday, Saturday, Sunday};`
  - `enum day myDay = Wednesday;`
  - In C/C++ the above values of this type are 0, ..., 6.
- More powerful in Java:  
`enum day {Monday, ..., Sunday};`  
`for (day d : day.values())`  
`System.out.println(d);`

# Records and Structure



- Usually laid out contiguously
- Possible holes for alignment
- Compilers may re-arrange field to minimize holes

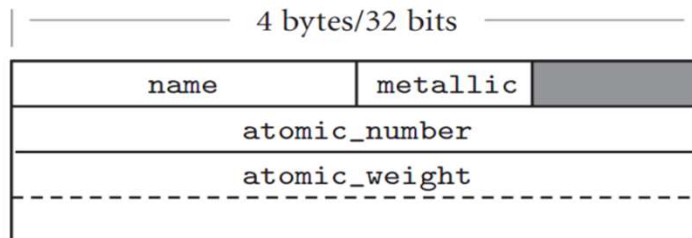
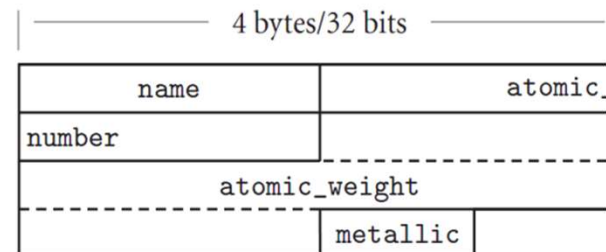
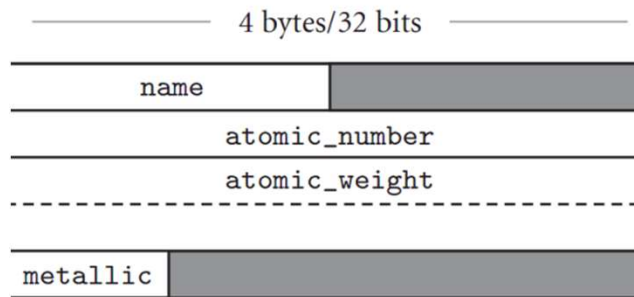
```
struct id {  
    int i;  
    double d;};  
struct id x;  
x.i, x.d
```



# Records and Structure



```
struct element {  
    char name[2];  
    int atomic_number;  
    double atomic_weight;  
    _Bool metallic;}  
}
```



Possible  
Memory Layouts

1

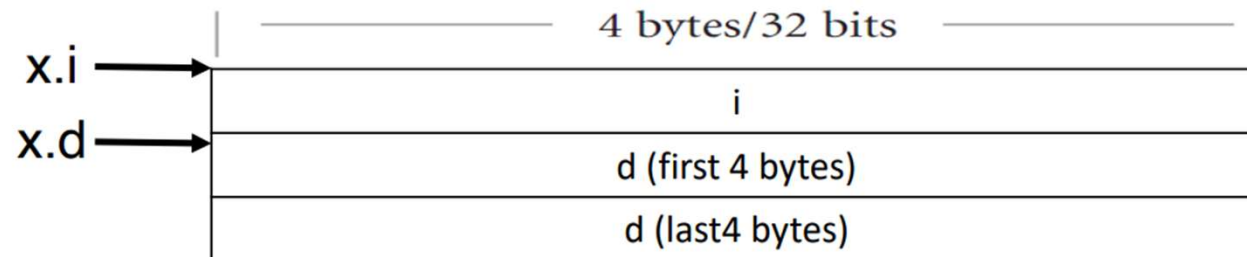
# Records and Structure



Usually laid out contiguously

```
struct id {  
    int i;  
    double d;};  
struct id x;  
x.i, x.d
```

A possible memory layout:



Each field has a separate piece of memory

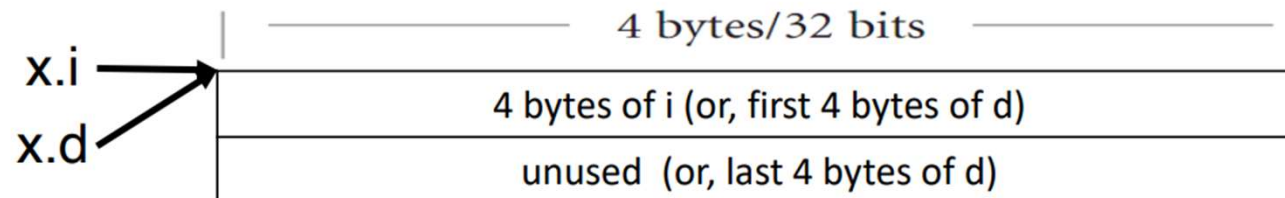
# Union Types



Laid out in shared memory

```
union id {  
    int i;  
    double d;};  
union id x;  
x.i = 1;  
y = 1.0 + x.d;
```

A possible memory layout:



All fields share the same piece of memory

# Union Types

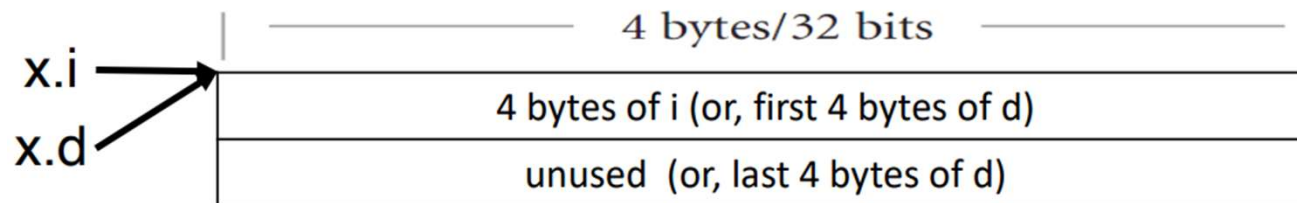
Not type safe:

x.d will read the binary

0x00000001,???????? as a double

```
union id {  
    int i;  
    double d;};  
union id x;  
x.i = 1;  
y = 1.0 + x.d;
```

A possible memory layout:



How can we make it type safe?

# Discriminated Union Types



A combination of a tag (like an enum) and a payload per possibility (like a union).

```
enum Kind {isInt, isFloat}
struct intorreal {
    enum Kind which;
    union U {int a; float p} u;
} ir;
float x = 1.0;
if (ir.which == isInt) ir.u.a = 1;
if (ir.which == isFloat) x = x + ir.u.p;
```

**Still not type safe: type system doesn't enforce tag check** Ⓜ

# Sum Types



Many functional programming languages support type-safe sum types

Haskell

Tag

(possibly empty)  
payload type

```
data intorreal = isInt Int | isFloat Float
-- given u has type intorreal
case u of
  isInt i -> i + 1
  isFloat f -> f + 1.0
```

Type safe: type is checked under each case statement (the only way to read from a value with the sum type)

# Sum Types are General



Haskell

Tag

```
data day = Monday | Tuesday | Wednesday |  
         Thursday | Friday | Saturday | Sunday  
-- Given d has type day  
case d of  
  Monday -> ...  
  Tuesday -> ...  
  ...
```

A generalization of Enumeration type



# Sum Types and Product Types

Sum Types: alternation of types

Product Types: concatenation of types (such as?)  
(records and structures are product types)

```
enum Color {Red, Blue}
enum Shape {Circle, Rectangle}
struct ColoredShape {enum color c;enum shape s}
```

Analogy:

Values  
of color

Values  
of shape

Values of  
coloredShape

$$\begin{aligned} & (\text{Red} + \text{Blue}) * (\text{Circle} + \text{Rectangle}) \\ &= (\text{Red} * \text{Circle}) + (\text{Red} * \text{Rectangle}) + (\text{Blue} * \text{Circle}) + (\text{Blue} * \text{Rectangle}) \end{aligned}$$



# Array



## Lifetime and array size

- Global lifetime, static shape
- Local lifetime, static shape
- Local lifetime, Dynamic shape

```
int A[10];
```

```
int f() {  
    int A[10];  
    ... }
```

```
int f(int n) {  
    int A[n];  
    ... }
```

# C Array

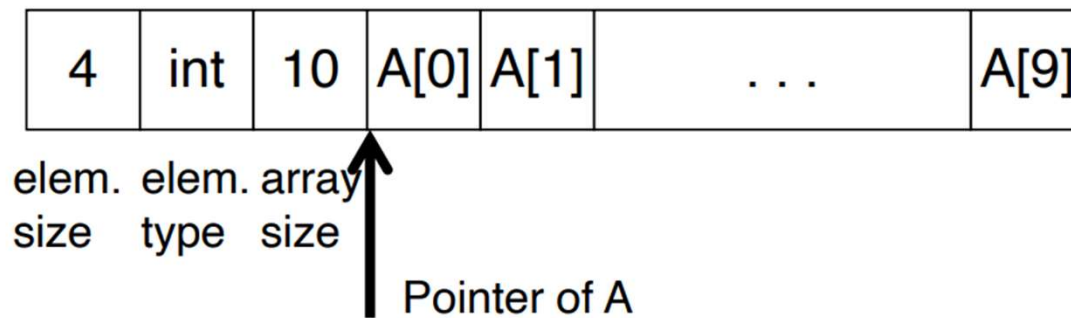
- Static/Stack/Heap allocated
- Size statically/dynamically determined
- Array bounds not checked (buffer overflow)

# Java Array



- Heap allocated
- Size dynamically determined
- Array size is part of stored data (Dope Vector)
- Array bounds checked

# Dope Vectors



Address of A[i]?

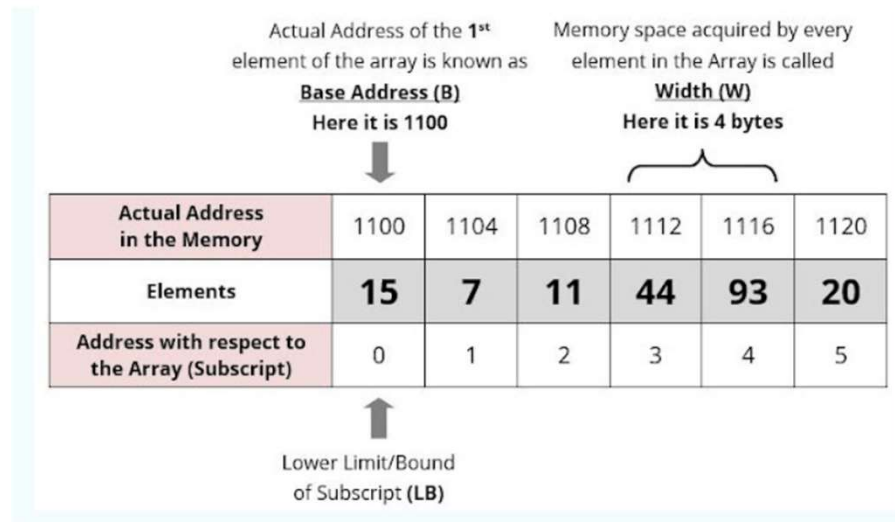
$A + 4 \cdot i$

Bound check?

$0 \leq i < 10$

Benefit: the array may change dynamically

# Address Calculation (one dimension Array)



$$\begin{aligned}\text{Address of } A[3] &= B + W * (i - LB) \\ &= 1100 + 4 * (3 - 0) = 1112\end{aligned}$$

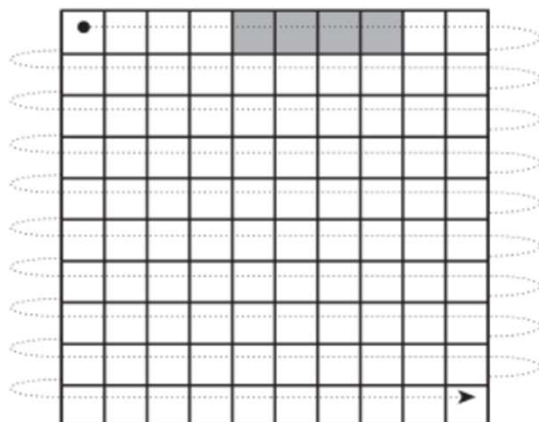
# Memory Layout

One-dimensional arrays

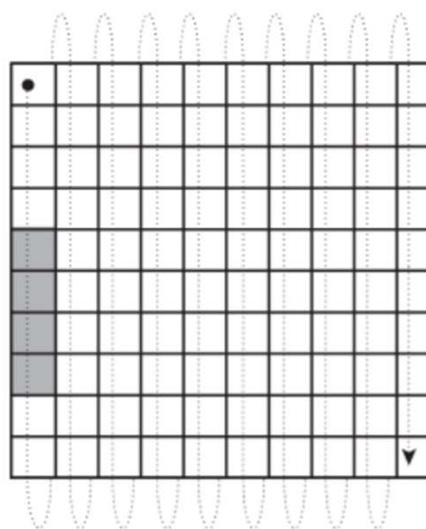


Two-dimensional arrays

```
int[][] A = new int[10][100]
```

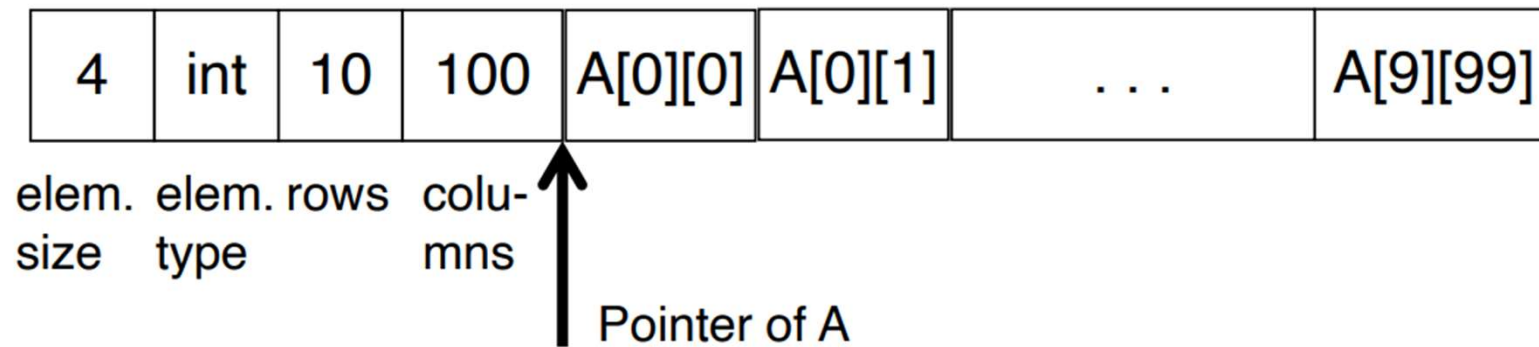


Row-major order



Column-major order

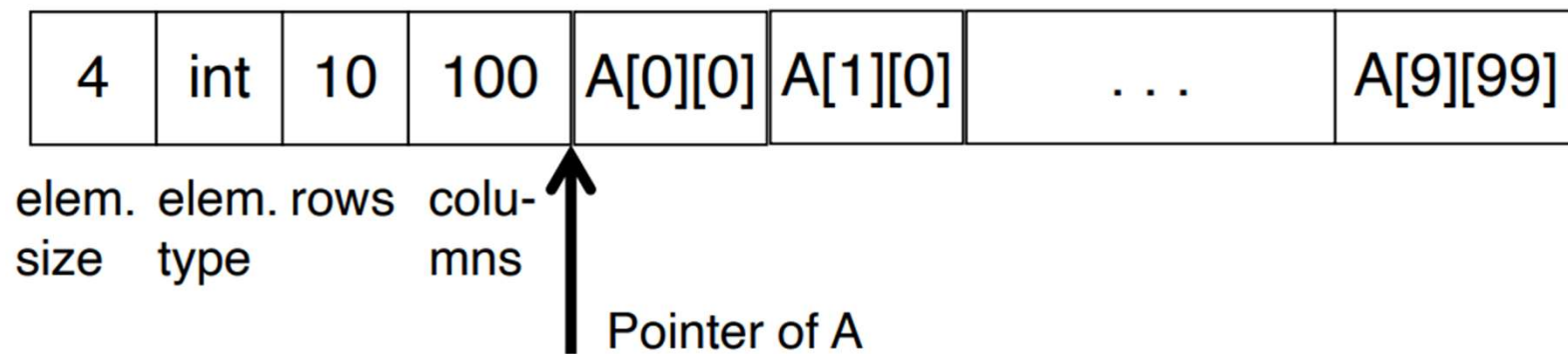
# Address Calculation (Row Major)



Address of A[i][j]?  
Bound check?

$$A + 4(i*100+j)$$
$$0 \leq i < 10, 0 \leq j < 100$$

# Address Calculation (Column Major)



Address of A[i][j]?  
Bound check?

$$A + 4(j*10+i)$$
$$0 \leq i < 10, 0 \leq j < 100$$



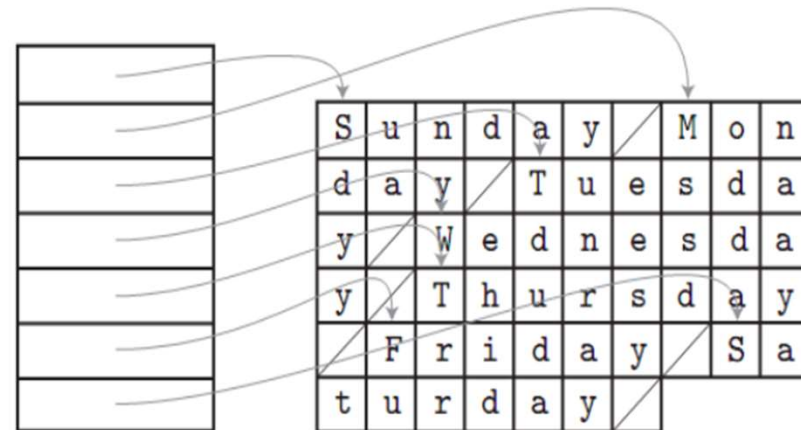
# Memory Layout



## Row-Pointer Layout

```
int[][] B = new int[10][]  
B[0] = new int[100]  
B[1] = new int[50]
```

S	u	n	d	a	y	/			
M	o	n	d	a	y	/			
T	u	e	s	d	a	y	/		
W	e	d	n	e	s	d	a	y	/
T	h	u	r	s	d	a	y	/	
F	r	i	d	a	y	/			
S	a	t	u	r	d	a	y	/	



# Pointers



What are they?

- A set memory addresses and operations on them
- Values: legal addresses, and a special value, nil

```
int x=20;  
int* p = &x;
```

address	
7084	7080
7080	20

p  
x

# Pointers



Operations: assignment, dereferencing, arithmetic

```
int x=20;  
int* p = &x;  
int y=*p;
```

```
int a[3] = {1,2,3};  
int x = *(a+1) //same as a[1]
```

## Uses

- Indirect addressing (access arbitrary address)
- Manage dynamic storage (heap)

# Pointers vs. References



- Pointers: `int *p;`
- References: `int &p;`

Value Model vs. Reference Model: `A = B`

- Value model: the value of B is copied to A
- Reference model: A is an alias of B (same memory)
- Java: primitive types follow value model; objects follow reference model

# References



- Restricted pointers: cannot be used as value or operated in any way
- Not directly visible to the programmer No explicit data type

```
double r=2.3;
```

```
double& s=r; //s is an alias of r (share memory)
```

```
double *p = &r; //p has value: address of r
```

```
s += 1; *p += 1;
```

# References

## Uses

- ~~Indirect addressing (access arbitrary address)~~
- Manage dynamic storage (heap)

Alias of existing variable

# The Nil Pointer Problem

*“I call it my billion-dollar mistake. It was the invention of the null reference in 1965. ... This has led to innumerable errors, vulnerabilities, and system crashes, which have probably caused a billion dollars of pain and damage in the last forty years.”*

C.A.R. Hoare, 2009

How to avoid it?

# String



- Now so fundamental, directly supported.
- In C, a string is a 1D array with the string value terminated by a NUL character (value = 0).
- In Java, Perl, Python, a string variable can hold an unbounded number of characters
- Libraries of string operations and functions.



# Function Type



- Pascal example:
  - `function newton(a, b: real; function f: real): real;`
  - Know that `f` returns a real value, but the arguments to `f` are unspecified.
- Strongly typed functional language
  - Functions are first class
  - Accepts functions as arguments and return functions as results

# Function Type

- ML:  $T1 \rightarrow T2$ 
  - $\rightarrow$  is right-associative
    - $T1 \rightarrow T2 \rightarrow T3$  is the same as  $T1 \rightarrow (T2 \rightarrow T3)$
  - Examples:
    - $\text{int} \rightarrow \text{int} \rightarrow \text{int}$
    - $\text{int} \rightarrow (\text{int} \rightarrow \text{int}) \rightarrow \text{int}$
    - $(\text{int} \rightarrow \text{int}) \rightarrow (\text{int} \rightarrow \text{int})$

# Subtypes



- S is a subtype of T if S extends or implements T
- A subtype is a type that has certain constraints placed on its values or operations.

# Type Conversions

- A type conversion is usually done by a conversion function
  - e.g., `3 + 5.0`; `3 + "hello"`
- A *widening* conversion if the result type permits more bits
  - E.g., in C, `byte b = 23`; `int i = (int) b`;
- A type conversion is a *narrowing* conversion if the result type permits fewer bits, thus potentially losing information.
  - in C, `int i = 1911`; `byte b = (byte) i`;
- *implicit* narrowing conversions may be harmful
  - Why?