

Regular Expressions

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Regular Expression



Pattern matching

What happens if, at a Unix/Linux shell prompt, you type

and press return?

• Suppose the current directory contains files called regfla.tex, regfla.aux, regfla.log, regfla.dvi, and regfla.aux. What happens if you type

and press return?

Alphabets



An alphabet is specified by giving a finite set, Σ , whose elements are called symbols. For us, any set qualifies as a possible alphabet, so long as it is finite.

Examples:

- $\Sigma_1 = \{0,1,2,3,4,5,6,7,8,9\}$ 10-element set of decimal digits.
- $\Sigma_2 = \{a,b,c,...,x,y,z\}$ 26-element set of lower-case characters of the English language
- $\Sigma_3 = \{S \mid S \subseteq \Sigma_1\}$ 2^{10} -element set of all subsets of the alphabet of decimal digits.

Non-Example:

• $\mathbb{N} = \{0,1,2,3,...\}$ –set of all non-negative whole numbers is not an alphabet, because it is infinite

String over an Alphabet



A string of length n (\geq 0) over an alphabet Σ is just an ordered n-tuple of elements of Σ , written without punctuation.

- Example: if $\Sigma = \{a, b, c\}$, then a, ab, aac, and bbac are strings over Σ of lengths one, two, three and four respectively
- This string is called sentence or word

N.B. there is a unique string of length zero over Σ , called the null string (or empty string) and denoted ϵ

Regular Language



- A language is a set of strings over an alphabet. Thus
 - $\{a, ab, baa\}$ is a language over $\Sigma = \{a, b\}$
 - $\{0, 111\}$ is a language over $\Sigma = \{0, 1\}$
- The number of symbols in a string is called the length of the string. For a string w its length is represented by $|\mathbf{w}|$.

 A Regular Language is a subset of all languages that can be defined by regular expressions

Regular Expression



- Each regular expression is a notation for a regular language.
- If A is a regular expression, then we write L(A) to the language denoted by A
- Single character: 'c'
 - $L(c) = \{c\}$ (for any $c \in \Sigma$)
- Concatenation: AB (where A and B are regular expression)
 - $L(AB) = \{ab \mid a \in L(A) \text{ and } b \in L(B)\}$
 - Example: if A = i and B = f then $L(AB) = L(i ' f') = {i ' f'}$
- Union:
 - $L(A \mid B) = L(A) \cup L(B)$ = $\{s \mid s \in L(A) \text{ or } s \in L(B)\}$
 - Example: L('if' | 'then' | 'else') = {"if", "then", "else"}

Regular Expression



- So far, we do not have a notation for infinite languages
- Iteration: A*
 - $L(A^*) = {```' \mid L(A) \mid L(AA) \mid L(AAA) \mid ...}$
 - Example: $L(0*) = {\text{``'}, \text{``0''}, \text{``00''}, \text{``000''}, \dots}$
- Epsilon: &
 - L(e) = {""}
- If (A) is a regular expression same as the regular expression A

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Notational Conveniences



Regular Definition is a sequence of the definitions of the form

$$\begin{array}{ccc} \mathbf{d}_1 & & \rightarrow \mathbf{r}_1 \\ \mathbf{d}_2 & & \rightarrow \mathbf{r}_2 \end{array}$$

where d_i is a distinct name and r_i is a regular expression over symbols in

$$\Sigma \cup \{d_1, d_2, \dots d_{i-1}\}$$

Example

Notational Conveniences



- One or more instances: $r^+ = rr^*$
- Zero or one instance: \mathbf{r} ? = $\mathbf{r} \mid \boldsymbol{\epsilon}$
- Character classes:

- Any single character denoted by dot sign: .
- Negated character class: [^aeiou]
- Number of repetition: [a f]{3}

Precedence of RE



- The order is (high to low)
 - Closure (*)
 - Concatenation
 - Alternation

Example:

- ab | cd means (ab) | (cd)
- a | bc*d means (a | (b(c*)d))

Examples



- Keywords
 - if, while, for,
- Identifiers

Integers

- Whitespace: non-empty sequence of blanks, newlines, tabs
 - ('\n' | '\t' | '')+

Examples



Float

String constants

$$\left(\begin{bmatrix} a-2A-2 & 0-9 \end{bmatrix} \right) \left[\begin{bmatrix} a-2A-2 \end{bmatrix} \right) *$$

Special Characters in RE



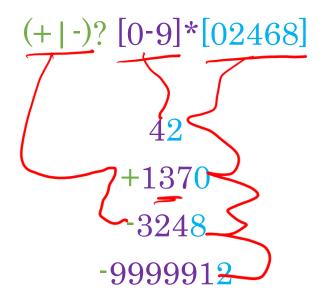
• If you want to match 1+2=3, you need to use a backslash (\) to escape the + as this character has a special meaning (Match one or more of the previous).

• To match the 1+2=3 as one string you would need to use 1 + 2=3

Apply Regular Expression



- Suppose our Σ is all ASCII characters.
- A regular expression for even number is



Apply Regular Expression



- Suppose our $\Sigma = \{a, @, ...\}$ where a represents "some letter."
- A regular expression for email addresses is

$$a^{+} (.a^{+})^{*} @ a^{+} (.a^{+})^{+}$$

szk461@cse.psu.edu

first.middle.last@mail.site.org

my.president@whitehouse.gov

Build a Regular Expression



- L = {w | w is a binary string which does not contain two consecutive 0s or two consecutive 1s anywhere}
 - E.g., w = 01010101 is in L, while w = 10010 is not in L
- Goal: Build a regular expression for L
- Four cases for w:
 - Case A: w starts with O and |w| is even
 - Case B: w starts with 1 and |w| is even
 - Case C: w starts with O and |w| is odd
 - Case D: w starts with 1 and |w| is odd
- Since L is the union of all 4 cases
 - Reg Exp for $L = (01)^* \mid (10)^* \mid 0(10)^* \mid 1(01)^* \checkmark$

• Regular expression for four cases:

• Case A: (01)*

• Case B: (10)*

• Case C: 0(10)*

• Case D: 1(01)*

- If we introduce ε then the regular expression can be simplified to:
 - Reg Exam for $L = (\epsilon \mid 1) (01)^* (\epsilon \mid 0)$

Build a Regular Expression



• $\Sigma = \{a, b, c\}$, a string that has a symbol in the middle that is neither its start not its end symbol, and its and start symbols are different, for e.g., abbbbbc or bcccca

• Given an alphabet $\Sigma = \{a, b\}$, a string with a's followed by b's with both the number of a's and b's being equal.

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Reading and Exercises



Reading

Chapter: 2.1 (Michael Scott Book)

Exercises

• Exercises: 2.1, and 2.3 (Michael Scott Book)