

# Frequency-dependent depletion of secretory vesicle pools modulates bursting in vasopressin neurones of the rat supraoptic nucleus

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## Abstract

*When stimulated, vasopressin neurones discharge lengthy, repeating bursts of action potentials. An increase in the stimulus strength causes both a lengthening of the bursts' active phase and an increase in the intra-burst firing frequency. Here we extend our earlier model [6] for phasic bursting at a constant stimulus. We show that an increase in burst length could be due to a reduction of the co-secretion of an inhibitory factor, dynorphin, and we propose this to be caused by a frequency dependent depletion of the pool of secretory vesicles.*

**Keywords:** *bursting, dense-core granule exocytosis, vasopressin, dehydration, dynorphin, endocrine*

## 1 Introduction

Vasopressin (VP) neurons project from the hypothalamus to the pituitary, where they secrete a hormone (VP), rather than a neurotransmitter, into the blood from their axonal terminals. These cells are activated by the physiological stress of dehydration and discharge lengthy (>20s) bursts of action potentials (APs), each

of which rides on a plateau-potential. The cells steadily depolarize as dehydration progresses, and this increases both the length of the burst's active phase,  $T$ , and the mean intra-burst firing rate,  $\nu$  (typically  $<10\text{Hz}$ ) [1]. The consequence of each of these effects is to increase the secretion of the hormone VP. The same modulation of the discharge pattern can be reproduced *in vitro* by direct depolarization [2]. However,  $T$  can be significantly reduced if the cell is induced to fire at higher frequencies ( $\sim 30\text{Hz}$ ) than the physiological range ( $<20\text{Hz}$ ), *e.g.* by pharmacological block of spike frequency adaptation (SFA) [3]. Thus  $T$  depends non-monotonically on  $\nu$ : increasing at low, physiologically relevant,  $\nu$  and decreasing at high  $\nu$ .

The plateau is thought to be caused by the  $\text{Ca}^{2+}$ -dependent inhibition of a resting  $\text{K}^+$  current [4], (but see also [5]), and is triggered by the  $\text{Ca}^{2+}$  influx that follows several proximal, synaptically evoked, APs. We have proposed [6] that the burst is terminated when the plateau becomes progressively desensitized to  $\text{Ca}^{2+}$ , and that this in turn is mediated by the progressive accumulation of the opioid dynorphin. Dynorphin is an autocrine messenger secreted from the somato-dendritic region of VP cells (figure 1) by dense-core granule exocytosis, and is known to modulate firing: its agonists inhibit bursting, while antagonists prolong burst duration [7]. Naïvely one should expect that if dynorphin secretion followed every spike, then faster firing should result in more rapid accumulation. Thus depolarization should cause bursts to terminate earlier, rather than later and hence dehydration should cause faster firing but shorter bursts, which is in contrast to what occurs experimentally. Here we propose that the releasable pool of dynorphin vesicles becomes depleted as  $\nu$  increases. In consequence the amount of dynorphin available for secretion diminishes, and this in turn slows accumulation and prolongs the active phase despite the increase in  $\nu$ . We further conjecture that the effects of SFA blockade are due to residual release from a non-primed pool.

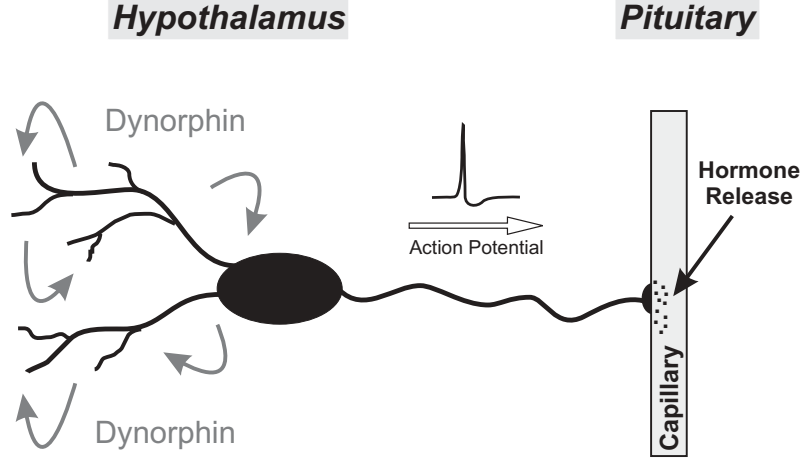


Fig. 1. VP cells project from the hypothalamus to the pituitary where they secrete the hormone vasopressin into the bloodstream. The cells are auto-regulated by secretion of dynorphin, an opioid, from their soma and dendrites. Dynorphin is secreted *via* dense-core granule (DCG) exocytosis and acts through  $\kappa$ -receptors to shift the  $K_d$  of the plateau-potential, and terminate the burst.

## 2 The Model

We quantify the effect on the plateau of the transduction of the  $\kappa$ -opioid receptor activation by dynorphin with the parameter  $D$ . In [6] we proposed that  $D$  is zero when the cell is at rest, is augmented by an amount  $\Delta$  after every spike, and decays exponentially when the cell is quiet, so that

$$\frac{d}{dt}D = -\frac{1}{\tau_D}D \quad \text{and} \quad D = D + \Delta \iff V = V_{thresh}^+ \quad (1)$$

where the decay constant  $\tau_D = 5\text{s}$ , and we choose the threshold  $V_{thresh} = 0$ . To account for known properties of the phasic pattern we further considered that  $D$  facilitated its own action, so that  $\Delta$  depends directly on  $D$ ,

$$\Delta = \alpha + \beta D \quad (2)$$

$\alpha$  is a small constant bias term that breaks the symmetry of the  $D = 0$  state, and  $\beta$  is proportional to the amount of dynorphin secreted by a single AP.  $\beta$  can be interpreted as being the quantity of dynorphin secreted when a  $\kappa$ -receptor is activated.

### 3 Results

In the full model [6], the plateau carries the cell above spike threshold into a repetitive spiking mode, and is sustained by spike-driven  $\text{Ca}^{2+}$ -influx. Within the active phase, firing goes through a brief period of spike-frequency adaptation, but then remains steady until the burst abruptly terminates. Concurrently,  $[\text{Ca}^{2+}]_i$  rapidly attains a steady-state where influx and efflux balance, and only decays at the end of the burst when spiking has ceased.  $D$  acts by shifting the  $K_d$  of the plateau current, and so progressively desensitize the plateau to calcium until it no longer supports repetitive spiking and collapses, thus terminating the active phase.

We simplify the model first by assuming that the active phase terminates when  $D$  reaches some threshold, say  $\bar{D}$ , and second by replacing the full spiking model of equation 1 with a firing-rate model. Equation 1 can then be solved for constant  $\nu$  to give the mean trajectory for  $D(t)$  (see [6])

$$D(t) = \frac{\alpha \nu \tau_D}{1 - \beta \nu \tau_D} \left[ 1 - \exp \left( -\frac{(1 - \beta \nu \tau_D) t}{\tau_D} \right) \right] \quad (3)$$

$T$  can then be found as a function of  $\beta$  for a particular firing rate,  $\nu$ , by setting  $D(T) = \bar{D}$  and inverting equation 3, and is plotted in figure 2. Note that  $T$  increases with decreasing  $\beta$  as expected, and increases asymptotically for small  $\beta$ .

Bursts can therefore become longer with increasing dehydration/depolarization if  $\beta$  decreases as the cell fires faster.

Dynorphin is secreted by dense-core granule exocytosis, and in other neuroendocrine cells the recovery of the releasable pool of vesicles is known to be slow following a secretory event. If refilling after one spike is so slow that it becomes interrupted by the next, then the number of vesicles available for secretion will be significantly smaller than the maximum size of the pool.

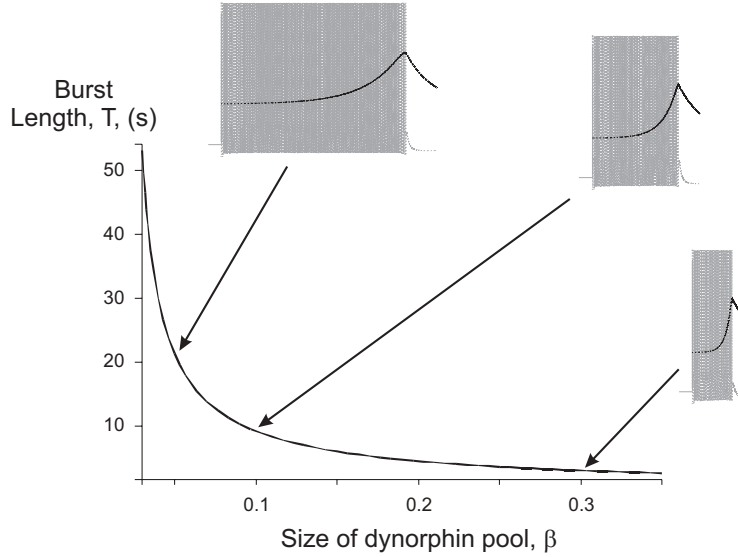


Fig. 2. Length of active phase,  $T$ , as function of quantity of dynorphin secreted,  $\beta$ , for fixed firing frequency,  $\nu$ . Note that  $T$  increases with decreasing  $\beta$ , and increases asymptotically for small  $\beta$ . Voltage traces for three representative bursts are shown (greyscale) with superimposed trajectories for  $D$  (black line). The effect of increasing  $\nu$  is to shift the asymptote leftward (data not shown).

Thus, since  $\beta$  is a measure of the size of the releasable pool, it can become progressively depleted as  $\nu$  increases.

The releasable pool is known to be a small subset (typically  $<10\%$ ) of the docked pool of granules, and movement of granules from the docked to the releasable pool is termed priming. Priming does not involve a physical translocation, but is a chemical step that depends on both calcium and ATP.

The data can be best fit by assuming that  $\beta$  has two components: secretion from a dynamic, primed, pool that empties and then slowly replenishes, and a small constant term, which may correspond to direct secretion from the docked pool. We further find that priming in this model must be a two-stage process, possibly representing transitions from the *Docked Pool (DP)* first to a *Readily Releasable Pool (RRP)* and subsequently to an *Immediately Releasable Pool (IRP)*. Let  $I$  be the concentration in the IRP, and let  $R$ , the concentration in the RRP, be filled from an infinite docked pool. The simplest model is then that the pool is emptied ( $I = 0$ ) following a spike, and refills according to

$$\frac{d}{dt}R = \frac{I_{\infty} - I}{\tau_R} - \frac{R}{\tau_I} \quad (4)$$

$$\frac{d}{dt}I = \frac{R}{\tau_I} \quad (5)$$

The time constants  $\tau_R$  and  $\tau_I$  are unknown, and for so concreteness we have set  $\tau_R = 0.5s$  and  $\tau_I = 0.2s$ , but the model is stable for a range of parameters.

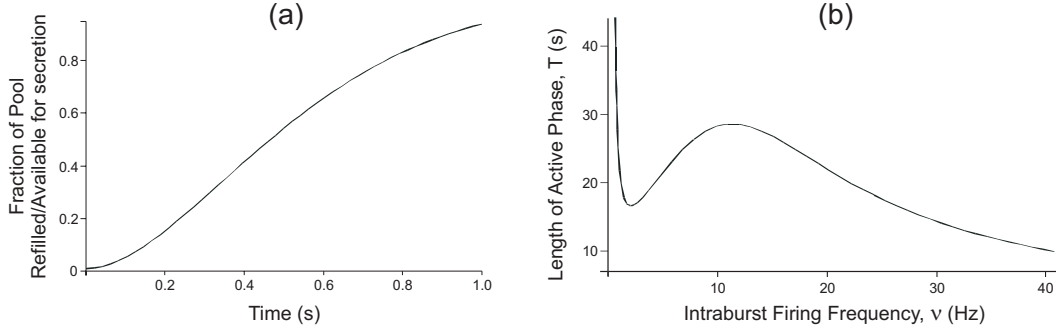


Fig. 3. (a) The fractional filling of the Immediately Releasable Pool,  $I(t)/I_{\infty}$ , as a function of time, see equation 5. (b) Length of active phase,  $T$ , as function of firing frequency,  $\nu$ . Here  $\beta$  is dynamic and decreases as  $\nu$  increases.

Solving for  $I(t)$  we plot the fractional filling of the pool,  $I(t)/I_{\infty}$ , as a function of time in figure 3a. Note that as the firing frequency,  $\nu$ , increases, the concentration in the IRP at each spike will be  $I(\nu^{-1})$ .

We now set  $\beta(\nu) = I(\nu) + \delta$ , where  $\delta$  is a small constant (see above), and following our earlier prescription we plot  $T$  versus  $\nu$  in figure 3b. The model clearly reproduces both the increase in  $T$  seen at low frequencies, and its subsequent decrease at high  $\nu$ . Note also that  $T$  increases asymptotically at very low  $\nu$ , and in fact phasic activity only occurs *in vivo* for  $\nu > \sim 1.5\text{Hz}$  [8]. The increase in  $T$  for intermediate frequencies marks the progressive depletion of the IRP with increasing  $\nu$ . However, the IRP becomes almost fully depleted at high frequency ( $I(\nu) \rightarrow 0$  for  $\nu > 15\text{Hz}$ ) and instead the residual component  $\delta$  starts to dominate, and so secretion from the releasable pool becomes less effectual at high  $\nu$ .

## 4 Conclusions

We have proposed that the concomitant increase of firing rate ( $\nu$ ) and lengthening of the active phase ( $T$ ) observed in vasopressin cells during increasing dehydration/depolarization is caused by depletion of the releasable pool of dense-core granules. We further find that the subsequent decrease in  $T$  at high  $\nu$  is due to a small, residual secretion directly from the docked pool and not from the releasable pool. This model extends our earlier analysis [6] in which we proposed that a slow priming step could account for a transient response that occurs following the sudden onset of a stress.

In essence this model is similar to earlier models of synaptic depression, except that DCG exocytotic dynamics are known to be significantly slower than those of synaptic vesicles. The model could be tested by a manipulation of the priming process, either at the ATP-dependent step, or *via* the use of caged calcium.

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## References

- [1] J.B. Wakerley, D.A. Poulain, and D. Brown. Comparison of firing patterns in oxytocin- and vasopressin-releasing neurones during progressive dehydration. *Brain Research*, 148:425–440, 1978.
- [2] R.D. Andrew and F.E. Dudek. Burst discharge in mammalian neuroendocrine cells involves an intrinsic regenerative mechanism. *Science*, 221(4615):1050–1052, 1983.
- [3] K. Kirkpatrick and C.W. Bourque. Activity dependence and functional role of the apamin-sensitive  $K^+$  current in rat supraoptic neurones *in vitro*. *Journal of Physiology (London)*, 494(2):389–398, 1996.

- [4] Z.H. Li and G.I. Hatton.  $\text{Ca}^{2+}$  release from internal stores: Role in generating depolarizing after-potentials in rat supraoptic neurones. *Journal of Physiology (London)*, 498(2):339–350, 1997.
- [5] M. Ghamari-Langroudi and C.W. Bourque. Flufenamic acid blocks depolarizing afterpotentials and phasic firing in rat supraoptic neurones. *Journal of Physiology (London)*, 545(2):537–542, 2002.
- [6] P. Roper, J. Callaway, and W. Armstrong. Burst initiation and termination in phasic vasopressin cells of the rat SON. 2003.
- [7] C.H. Brown, J.A. Russell, and G. Leng. Opioid modulation of magnocellular neurosecretory cell activity. *Neuroscience Research*, 36:97–120, 2000.
- [8] D.A. Poulain, D. Brown, and J.B. Wakerley. Statistical analysis of patterns of electrical activity in vasopressin- and oxytocin-secreting neurones. In G. Leng, editor, *Pulsatility in Neuroendocrine Systems*, chapter 8, pages 119–154. CRC Press, Inc, Boca Raton, Florida, 1988.