Deep Learning Cheat Sheet

Evaluation Metrics

$$\begin{aligned} &\operatorname{Accuracy} = \frac{TP + TN}{TP + TN + FP + FN} \\ &\operatorname{Error\ Rate} = 1 - accuracy \\ &\operatorname{Precision} = \frac{TP}{TP + FP} \\ &\operatorname{TPR} = \frac{TP}{TP + FN} & \operatorname{FPR} = \frac{FP}{FP + TN} \\ &\operatorname{TNR} = \frac{TN}{TN + FP} & \operatorname{FNR} = \frac{FN}{FN + TP} \\ &\operatorname{F1-score} = \frac{2 \cdot Precision \cdot TPR}{Precision + TPR} \\ &\operatorname{Specificity} = \frac{TP}{TN + FP} \\ &\operatorname{AUC} = \int_0^1 TPR \cdot dFPR \\ &\operatorname{Macro\ Average} = \frac{1}{n} \sum_{i=1}^n avg_i \\ &\operatorname{Micro\ Average} = \frac{\sum_{i=1}^n TP_i}{\sum_{i=1}^n TP_i} \end{aligned}$$

Bias & Variance

 $\mathbf{Bias}(h_{\theta}) = \mathbb{E}[h_{\theta}, D] - f$ $\mathbf{Var}(h_{\theta}) = \mathbb{E}[(h_{\theta}, D - \mathbb{E}[h_{\theta}, D])^2]$ $\mathbf{MSE} = \mathrm{Bias}(h_{\theta})^2 + \mathrm{Var}(h_{\theta}) + \sigma^2$ Underfitting Overfitting

high bias, low variance

low bias, high variance

Data Preparation

Min-max [0,1]:
$$x' = \frac{(x - x_{min})}{(x_{max} - x_{min})}$$

Min-max [-1,1]: $x' = 2 \cdot min \ max(x) - 1$ min-max doesn't handle outliers.

Z-norm: $x' = \frac{(x-\mu)}{}$

Scaling & Centering

Scaling improves the numerical stability, the convergence speed and accuracy of the learning algorithms. Centering improves the robustness of the learning algorithms

Activation Functions

Sigmoid -

 $\sigma(z) = \frac{1}{1+e^{-z}}$ — Smooth and differentiable. Used in output layers for binary classifica-

— Hyperbolic Tangent (tanh) —

 $f(z) = \tanh(z)$ — Smooth, differentiable, output centered around 0. Used in LSTM.

Rectified Linear Unit (ReLU)

 $f(z) = \max(0, z)$ — Non-linear, used as a standard, but has dying units problem for z < 0.

Leaky ReLU — where :

 $f(z) = \begin{cases} z & \text{if } z \ge 0 \\ \alpha z & \text{if } z < 0 \end{cases}$ — Addresses dying — $\hat{y}(i) = h_{\theta}(x(i))$ is the prediction of the model, units problem with a small α (typical $\alpha = 0.01$).

—— Exponential Linear Unit (ELU) —

$$f(z) = \begin{cases} z & \text{if } z \ge 0 \\ \alpha(e^z - 1) & \text{if } z < 0 \end{cases}$$
— Similar to Leaky ReLU but more computationally expensive.

 $f(z_i) = \frac{e^{z_i}}{\sum_{j=0}^{K-1} e^{z_j}}$ — Used in the last layer for multi-class classification, outputs a probability distribution.

Universal Approximation Theorem

A feedforward network with a linear output layer and at least one hidden layer with a non-linear activation function (e.g. sigmoid) can approximate a large class of functions $f: \mathbb{R}^n \to \mathbb{R}^m$ with arbitrary accuracy, provided that the network is given enough hidden units.

Curse of Dimensionality

when the dimensionality increases, the volume of the space increases so fast that the available data become sparse. This sparsity is problematic for any method that requires statistical significance. In order to obtain a statistically sound and reliable result, the amount of data needed to support the reamount of data needed to support the result often grows exponentially with the dimensionality $\nabla_w J_{CE}(w,b) = \frac{1}{m} \sum_{i=1}^m (\hat{y}(i) - y(i)) \cdot x(i)$ $\nabla_b J_{CE}(w,b) = \frac{1}{m} \sum_{i=1}^m (\hat{y}(i) - y(i))$

Gradient Descent

- 1: Initialize parameter vector θ_0
- 2: repeat
- Compute the gradient of the cost function at current position $\theta_t : \nabla_{\theta} J(\theta_t)$
- Update the parameter vector by moving against the gradient : $\theta_{t+1} = \theta_t$ - $\alpha \cdot \nabla_{\theta} J(\theta_t)$
- where α is the learning rate.
- 6: **until** change in θ is small

—— MSE –

$$J_{MSE}(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (\hat{y}(i) - y(i))^2$$

- -y(i) is the true outcome,
- m is the number of training examples.

$$\nabla_w J_{MSE}(w,b) =$$

$$\frac{1}{m} \sum_{i=1}^{m} \hat{y}(i) \cdot (1 - \hat{y}(i)) \cdot (\hat{y}(i) - y(i)) \cdot x(i)$$

$$\nabla_b J_{MSE}(w,b) =$$

$$\frac{1}{m} \sum_{i=1}^{m} \hat{y}(i) \cdot (1 - \hat{y}(i)) \cdot (\hat{y}(i) - y(i))$$

- Cross Entropy -

$$J_{CE}(\theta) = -\sum_{i=1}^{m} y(i) \cdot \log h_{\theta}(x(i)) + (1 - y(i)) \cdot \log(1 - h_{\theta}(x(i)))$$

where:

- $p_{\theta}(y(i) \mid x(i))$ is the probability model parameterized by $\bar{\theta}$, predicting the $\mathbf{a}^{[l]} = \sigma^{[l]}(\mathbf{z}^{[l]})$ probability of the true class y(i) given $\mathbf{z}^{[l]} = \mathbf{W}^{[l]} \cdot \mathbf{a}^{[l-1]} + \mathbf{b}^{[l]}$ with $\mathbf{a}^{[0]} = \mathbf{x}$ the input x(i).
- m is the number of observations or data points in the dataset.

$$\nabla_{w} J_{CE}(w,b) = \frac{1}{m} \sum_{i=1}^{m} (\hat{y}(i) - y(i)) \cdot x(i)$$
$$\nabla_{b} J_{CE}(w,b) = \frac{1}{m} \sum_{i=1}^{m} (\hat{y}(i) - y(i))$$

Gradient Descent Variants

-BGD

Smooth, not wiggling, strictly decreasing cost, many epochs needed, choose larger learning rate, no out-of-core support all data in RAM (m), easy to parallelise.

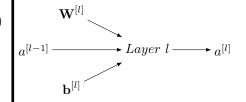
— SGD —

Wiggling, needs smoothing, wiggles around minimum, not necessarily decreasing cost, few epochs needed, choose smaller learning rate, out-of-core support - not all data to be kept in RAM of a single machine, not easy to parallelise.

- MBGD -

Slightly wiggling, wiggles around minimum. typically decreasing cost, less epochs than BGD, more than SGD needed, choose medium learning rate (dependent on model), out-of-core support - not all data to be kept in RAM of a single machine, easy to parallelise.

Compute Graph



$$\mathbf{W}^{[l]} = \begin{pmatrix} w_{11} & \cdots & w_{1n^{[l-1]}} \\ \vdots & \ddots & \vdots \\ w_{n^{[l]}1} & \cdots & w_{n^{[l]}n^{[l-1]}} \end{pmatrix}$$

$$\mathbf{a}^{[l]} = \begin{pmatrix} a_1 \\ \vdots \\ a_{n^{[l]}} \end{pmatrix}$$

$$\mathbf{b}^{[l]} = \begin{pmatrix} b_1 \\ \vdots \\ b_{n^{[l]}} \end{pmatrix}$$

$$\mathbf{a}^{[l]} = \sigma^{[l]}(\mathbf{z}^{[l]})$$

$$\mathbf{z}^{[l]} = \mathbf{W}^{[l]} \cdot \mathbf{a}^{[l-1]} + \mathbf{b}^{[l]} \quad \text{with } \mathbf{a}^{[0]} = \mathbf{x}$$

Backpropagation

- Matrix Notation

$$\begin{split} \frac{\partial L}{\partial \mathbf{z}^{[l]}} &= \frac{\partial L}{\partial \mathbf{a}^{[l]}} * \frac{d\sigma^{[l]}(\mathbf{z}^{[l]})}{dz} \\ \frac{\partial L}{\partial \mathbf{W}^{[l]}} &= \frac{\partial L}{\partial \mathbf{z}^{[l]}} \cdot \left(\mathbf{a}^{[l-1]}\right)^T \\ \frac{\partial L}{\partial \mathbf{b}^{[l]}} &= \frac{\partial L}{\partial \mathbf{z}^{[l]}} \\ \frac{\partial L}{\partial \mathbf{a}^{[l-1]}} &= \left(\mathbf{W}^{[l]}\right)^T \cdot \frac{\partial L}{\partial \mathbf{z}^{[l]}} \\ \frac{\partial L}{\partial \mathbf{z}^{[l]}} &= \hat{\mathbf{y}} - \mathbf{y} \end{split}$$

- Full Batch

$$\begin{split} \frac{\partial L}{\partial \mathbf{Z}^{[l]}} &= \frac{\partial L}{\partial \mathbf{A}^{[l]}} * \frac{d\sigma^{[l]}(\mathbf{Z}^{[l]})}{dz} \\ \frac{\partial L}{\partial \mathbf{W}^{[l]}} &= \frac{\partial L}{\partial \mathbf{Z}^{[l]}} \cdot \left(\mathbf{A}^{[l-1]}\right)^T \\ \frac{\partial L}{\partial \mathbf{b}^{[l]}} &= \frac{1}{m} \cdot \frac{\partial L}{\partial \mathbf{Z}^{[l]}} \cdot \begin{pmatrix} \vdots \\ \vdots \\ \vdots \end{pmatrix} \\ \frac{\partial L}{\partial \mathbf{A}^{[l-1]}} &= \left(\mathbf{W}^{[l]}\right)^T \cdot \frac{\partial L}{\partial \mathbf{Z}^{[l]}} \\ \frac{\partial L}{\partial \mathbf{Z}^{[l]}} &= \hat{\mathbf{Y}} - \mathbf{Y} \end{split}$$

Batch Normalization

$$\begin{split} \frac{\partial L}{\partial \gamma} &= \frac{1}{m} \cdot \sum_{i=1}^{m} \frac{\partial L}{\partial \hat{a}^{(i)}} \cdot \frac{\partial \hat{a}^{(i)}}{\partial \gamma} \\ &= \frac{1}{m} \cdot \sum_{i=1}^{m} \frac{\partial L}{\partial \hat{a}^{(i)}} \cdot \hat{a}^{(i)} \\ \frac{\partial L}{\partial \beta} &= \sum_{i=1}^{m} \frac{\partial L}{\partial \hat{a}^{(i)}} \cdot \frac{\partial \hat{a}^{(i)}}{\partial \beta} \\ &= \sum_{i=1}^{m} \frac{\partial L}{\partial \hat{a}^{(i)}} \end{split}$$

Vanishing Exploding Gradient

Xavier & Heu Initialization

Sets the initial weights of a layer to values Uses a running average of gradients to Modify the loss function to include a pedrawn from a uniform distribution with smooth the optimization path. a range that depends on the number of input and output units in the layer. Specifically, the range is set to [-r, r], where $r = \sqrt{\frac{6}{n_{in} + n_{out}}}$, and n_{in} is the number Nesterov variant: of input units and n_{out} is the number of output units. This range was chosen because it ensures that the variance of the outputs of each layer remains constant. which helps to prevent the vanishing or exploding gradient problem.

Batch Normalization –

We calculate the average μ_r and standard deviation σ_r over the m column vectors z_r of the mini-batch according to:

$$\mu_r = \frac{1}{m} \sum_{i=1}^m z_r^{[l](i)}$$

$$\sigma_r = \sqrt{\frac{1}{m} \sum_{i=1}^m (z_r^{[l](i)} - \mu_r)^2}$$

Now, the actual normalization of the logit matrix is as follows:

$$\hat{Z}_r^{[l]} = \frac{Z_r^{[l]} - \mu_r}{\sigma_r + \epsilon}$$

Finally, two addition parameter vectors are introduced that rescale the logits according $m_t \leftarrow \beta_1 m_{t-1} + (1-\beta_1) \nabla_{\theta} J(\theta_{t-1})$ to:

$$\tilde{Z}_r^{[l]} = \gamma^{[l]} \cdot \hat{Z}_r^{[l]} + \beta^{[l]}$$

— Non Saturating Activation Function — To alleviate the saturation of sigmoid and tanh, we can use the ReLU activation function. It still suffer from dying units problem (when the input is negative, the gradient is 0).

Gradient Clipping

If gradients values exceed a certain threshold, they are "clipped" or rescaled to a **Exponential scheduling** : $\alpha(t)$ smaller value. This prevents the gradients $\alpha_0 \cdot 10^{-t/T}$ from becoming too large and helps to Power stabilize the training process.

Optimizers

- Momentum

$$m_t \leftarrow \beta m_{t-1} + \alpha \nabla_{\theta} J(\theta)$$
$$\theta_t \leftarrow \theta_{t-1} - m_t$$

$$m_t \leftarrow \beta m_{t-1} + \alpha \nabla_{\theta} J(\theta_{t-1} - \beta m_{t-1})$$

$$\theta_t \leftarrow \theta_{t-1} - m_t$$

— AdaGrad —

Scaling down the gradient vector along the steepest dimensions.

$$s_{t} \leftarrow s_{t-1} + \nabla_{\theta} J(\theta_{t-1}) \cdot \nabla_{\theta} J(\theta_{t-1})$$
$$\theta_{t} \leftarrow \theta_{t-1} - \frac{\alpha}{\sqrt{s_{t}} + \epsilon} \cdot \nabla_{\theta} J(\theta_{t-1})$$

RMS Prop

A variant of AdaGrad using an exponentially decaying average of squared gradients.

$$s_{t} \leftarrow \beta s_{t-1} + (1 - \beta) \nabla_{\theta} J(\theta_{t-1}) \cdot \nabla_{\theta} J(\theta_{t-1})$$
$$\theta_{t} \leftarrow \theta_{t-1} - \frac{\alpha}{\sqrt{s_{t} + \epsilon}} \cdot \nabla_{\theta} J(\theta_{t-1})$$

— Adam -

Combines momentum and RMSProp to adapt the learning rate for each parameter.

$$m_{t} \leftarrow \beta_{1} m_{t-1} + (1 - \beta_{1}) \nabla_{\theta} J(\theta_{t-1})$$

$$s_{t} \leftarrow \beta_{2} s_{t-1} + (1 - \beta_{2}) \nabla_{\theta} J(\theta_{t-1}) \cdot \nabla_{\theta} J(\theta_{t-1})$$

$$\hat{m}_{t} \leftarrow \frac{m_{t}}{1 - \beta_{1}^{t}}$$

$$\hat{s}_{t} \leftarrow \frac{s_{t}}{1 - \beta_{2}^{t}}$$

$$\theta_{t} \leftarrow \theta_{t-1} - \frac{\alpha}{\sqrt{\hat{s}_{t}} + \epsilon} \cdot \hat{m}_{t}$$

- Scheduler ·

Strategies to adjust the learning rate during training: Performance scheduling

scheduling : $\alpha(t)$ $\alpha_0 \cdot \left(1 + \frac{t}{T}\right)^{-c}$, where c is typically set to 1.

Regularization

- Weight Penalty -

nalty to big weights:

$$J(\theta) = J_0(\theta) + \lambda \cdot \Omega(W)$$

where $\Omega(W)$ is the penalty term:

- L1:
$$\Omega(W) = ||W||_1 = \sum |W_{ji}|$$

- L2: $\Omega(W) = \frac{1}{2}||W||_2^2 = \frac{1}{2}\sum (W_{ii}^2)$

——— Dropout -

Randomly drop neurons during training:

- Each neuron has probability p of being dropped.
- Typical p:50
- During testing, scale weights by 1-p.

- Early Stopping -

Stop training when validation error increases:

- Track validation error during training.
- Save model parameters when validation error improves.
- Stop if no improvement for a set number of steps.

Convolutional Neural Networks Features colors, terrain texture, size, presence of - Premier CNN utilisé avec succès pour straight lines, border 1. Extracting localized low-level features 2. Incrementally allowing the system to - Utilisation de couches de convolution appropriately bind together features and their relationships 3. Gradually building up overall spatial invariance — Pooling layer — Maxpooling after a convolution layer eliminates non-maximal values : it is a form of non-linear down-sampling that reduces computation for upper layers and provides a "summary" of the statistics of features in lower lavers. Convolution layer — Different kernel sizes (3x3, 5x5, 7x7, etc.) allow the identification of features at different scales. Multiple layers of 3x3 kernels can implement other kernel sizes. The CONV layer's parameters consist of a set of learnable filters. Every filter is small - Réduction des paramètres grâce à des spatially (along width and height) but couches 1x1 convolutions (depth projecextends through the full depth of the input tion) volume. We can compute the spatial size of the output volume as a function of the input volume size (W), the receptive field size - Introduction des residual connections pour of the Conv Layer neurons (F), the stride with which they are applied (S), and the (gradient highway) amount of zero padding used (P) on the border. ——Input Volume — Size: $W_1 \times H_1 \times D_1$ — Hyperparameters — **K**: Number of conv filters **F**: Filter size (spatial extent) S: Stride P: The amount of zero padding Output Volume - $\begin{aligned} \mathbf{W2} &: \big\lfloor \frac{W_1 - F + 2P}{S} \big\rfloor + 1 \\ \mathbf{H2} &: \big\lfloor \frac{H_1 - F + 2P}{S} \big\rfloor + 1 \\ \mathbf{Size} &: W_2 \times H_2 \times K \end{aligned}$ Parameters —

```
(MNIST).
(pooling).
couche.
```

DeepCNN LeNet5 la reconnaissance des chiffres manuscrits suivies de couches de sous-échantillonnage — AlexNet — - Introduction des CNN profonds avec huit couches apprises. Utilisation de ReLUUtilisation de Dropout - Utilisation de Data Augmentation - VGGnet -Profondeur accrue avec 16 à 19 couches. Introduction de l'utilisation de petits filtres 3x3 dans toutes les couches de convolution. — GoogleNet – - Introduction des Inceptions Modules plusieurs tailles de filtres dans chaque injection of gradient at early stages ResNet assurer la rétropropagation du gradient Résolution du problème de gradient vanishing dans les réseaux très profonds. Batch Normalization Xavier He Initialization Bottleneck layers 1x1x64 Pattern -"Pattern"l.

- [Ajouter ici une brève description de l'innovation ou du concept clé lié au réseau

```
Keras CNN
                                        Data Augmentation
                                       Principle

    Model -

                                       Types
def build model():
                                      Strategies
    visible = Input(shape=(32, 32,
                                       Keras
    # first feature extractor
    conv1 = Conv2D(32, kernel_size
    =3, activation='relu')(visible)
                                         Transfer Learning
    drop1 = Dropout(0.2)(conv1)
                                       Principle
    pool1 = MaxPooling2D(pool_size
                                      Keras Code
MobileNet
    =(2, 2))(drop1)
    flat1 = Flatten()(pool1)
    # second feature extractor
                                       Strategies
    conv2 = Conv2D(32, kernel_size
    =6. activation='relu')(visible)
    drop2 = Dropout(0.2)(conv2)
                                        RNN
    pool2 = MaxPooling2D(pool_size
                                      Use Case
Model Category
    =(2, 2))(drop2)
    flat2 = Flatten()(pool2)
                                       Recurrence Net
    # merge feature extractors
                                      Single Laver
    merge = concatenate([flat1,
                                       Many to Many
    flat2])
    # interpretation laver
                                       Un exemple par catégorie
    hidden1 = Dense(100, activation=
                                       Stacked RNN
    'relu')(merge)
    # prediction output
    output = Dense(n_classes,
                                        LSTM
    activation='softmax')(hidden1)
                                       Long Term Memory Unit Cell
    model = Model(inputs=visible.
    outputs=output, name='
                                       Gates
    exp2 functional')
                                       Backprop
    return model
                                       \overline{\text{Keras}}
clf = build_model()
                                       GRE
clf.compile(loss='
    categorical_crossentropy',
    optimizer='adam', metrics=[
                                         Word Embedding
    accuracy'])
                                       Word
                                       Training

    Data Augmentation -

datagen = ImageDataGenerator(
                                        Sentiment Classification
        rotation_range=20,
        width_shift_range=0.2,
                                       Strategy
        height_shift_range=0.2,
                                       Architecture
        horizontal_flip=True,
        shear_range=0.2,
        zoom_range=0.2,
                                         Autoencoder
        fill_mode='nearest')
                                       Definition
train_generator = datagen.flow(
                                       Use Case
   X train, Y train, batch size
    =128)
test_generator = datagen.flow(X_test
                                        GenRNN
   , Y_test, batch_size=128)
                                       Many to Many
checkpoint_filepath = clf.name + '.
                                       Many to One
   keras'
             — Training —
                                         Attention
                                       Sequence to Sequence
history = clf.fit(
   train_generator,
                                       Attention
    steps_per_epoch=100,
    epochs=15,
    validation_data=test_generator,
                                         Transformer
    validation_steps=10,
                                       High-Level Architecture
    callbacks = [ModelCheckpoint(
    checkpoint_filepath,
                                       Self-Attention
```

Full Architecture

save_best_only=True)]

It introduces $(F \times F \times D_1) \times K$ weights

Discrete Continuous

plus K biases.