Deep Learning Cheat Sheet

Evaluation Metrics

$$\begin{aligned} &\operatorname{Accuracy} = \frac{TP + TN}{TP + TN + FP + FN} \\ &\operatorname{Error\ Rate} = 1 - accuracy \\ &\operatorname{Precision} = \frac{TP}{TP + FP} \\ &\operatorname{TPR} = \frac{TP}{TP + FN} & \operatorname{FPR} = \frac{FP}{FP + TN} \\ &\operatorname{TNR} = \frac{TN}{TN + FP} & \operatorname{FNR} = \frac{FN}{FN + TP} \\ &\operatorname{F1-score} = \frac{2 \cdot Precision \cdot TPR}{Precision + TPR} \\ &\operatorname{Specificity} = \frac{TP}{TN + FP} \\ &\operatorname{AUC} = \int_0^1 TPR \cdot dFPR \\ &\operatorname{Macro\ Average} = \frac{1}{n} \sum_{i=1}^n avg_i \\ &\operatorname{Micro\ Average} = \frac{\sum_{i=1}^n TP_i}{\sum_{i=1}^n TP_i} \end{aligned}$$

Bias & Variance

 $\mathbf{Bias}(h_{\theta}) = \mathbb{E}[h_{\theta}, D] - f$ $\mathbf{Var}(h_{\theta}) = \mathbb{E}[(h_{\theta}, D - \mathbb{E}[h_{\theta}, D])^2]$ $\mathbf{MSE} = \mathrm{Bias}(h_{\theta})^2 + \mathrm{Var}(h_{\theta}) + \sigma^2$ Underfitting Overfitting

high bias, low variance

low bias, high variance

Data Preparation

Min-max [0,1]:
$$x' = \frac{(x - x_{min})}{(x_{max} - x_{min})}$$

Min-max [-1,1]: $x' = 2 \cdot min \ max(x) - 1$ min-max doesn't handle outliers.

Z-norm: $x' = \frac{(x-\mu)}{}$

Scaling & Centering

Scaling improves the numerical stability, the convergence speed and accuracy of the learning algorithms. Centering improves the robustness of the learning algorithms

Activation Functions

Sigmoid -

 $\sigma(z) = \frac{1}{1+e^{-z}}$ — Smooth and differentiable. Used in output layers for binary classifica-

— Hyperbolic Tangent (tanh) —

 $f(z) = \tanh(z)$ — Smooth, differentiable, output centered around 0. Used in LSTM.

Rectified Linear Unit (ReLU)

 $f(z) = \max(0, z)$ — Non-linear, used as a standard, but has dying units problem for z < 0.

Leaky ReLU — where :

 $f(z) = \begin{cases} z & \text{if } z \ge 0 \\ \alpha z & \text{if } z < 0 \end{cases}$ — Addresses dying — $\hat{y}(i) = h_{\theta}(x(i))$ is the prediction of the model, units problem with a small α (typical $\alpha = 0.01$).

—— Exponential Linear Unit (ELU) —

$$f(z) = \begin{cases} z & \text{if } z \ge 0 \\ \alpha(e^z - 1) & \text{if } z < 0 \end{cases}$$
— Similar to Leaky ReLU but more computationally expensive.

 $f(z_i) = \frac{e^{z_i}}{\sum_{j=0}^{K-1} e^{z_j}}$ — Used in the last layer for multi-class classification, outputs a probability distribution.

Universal Approximation Theorem

A feedforward network with a linear output layer and at least one hidden layer with a non-linear activation function (e.g. sigmoid) can approximate a large class of functions $f: \mathbb{R}^n \to \mathbb{R}^m$ with arbitrary accuracy, provided that the network is given enough hidden units.

Curse of Dimensionality

when the dimensionality increases, the volume of the space increases so fast that the available data become sparse. This sparsity is problematic for any method that requires statistical significance. In order to obtain a statistically sound and reliable result, the amount of data needed to support the reamount of data needed to support the result often grows exponentially with the dimensionality $\nabla_w J_{CE}(w,b) = \frac{1}{m} \sum_{i=1}^m (\hat{y}(i) - y(i)) \cdot x(i)$ $\nabla_b J_{CE}(w,b) = \frac{1}{m} \sum_{i=1}^m (\hat{y}(i) - y(i))$

Gradient Descent

- 1: Initialize parameter vector θ_0
- 2: repeat
- Compute the gradient of the cost function at current position $\theta_t : \nabla_{\theta} J(\theta_t)$
- Update the parameter vector by moving against the gradient : $\theta_{t+1} = \theta_t$ - $\alpha \cdot \nabla_{\theta} J(\theta_t)$
- where α is the learning rate.
- 6: **until** change in θ is small

—— MSE –

$$J_{MSE}(\theta) = \frac{1}{2m} \sum_{i=1}^{m} (\hat{y}(i) - y(i))^2$$

- -y(i) is the true outcome,
- m is the number of training examples.

$$\nabla_w J_{MSE}(w,b) =$$

$$\frac{1}{m} \sum_{i=1}^{m} \hat{y}(i) \cdot (1 - \hat{y}(i)) \cdot (\hat{y}(i) - y(i)) \cdot x(i)$$

$$\nabla_b J_{MSE}(w,b) =$$

$$\frac{1}{m} \sum_{i=1}^{m} \hat{y}(i) \cdot (1 - \hat{y}(i)) \cdot (\hat{y}(i) - y(i))$$

- Cross Entropy -

$$J_{CE}(\theta) = -\sum_{i=1}^{m} y(i) \cdot \log h_{\theta}(x(i)) + (1 - y(i)) \cdot \log(1 - h_{\theta}(x(i)))$$

where:

- $p_{\theta}(y(i) \mid x(i))$ is the probability model parameterized by $\bar{\theta}$, predicting the $\mathbf{a}^{[l]} = \sigma^{[l]}(\mathbf{z}^{[l]})$ probability of the true class y(i) given $\mathbf{z}^{[l]} = \mathbf{W}^{[l]} \cdot \mathbf{a}^{[l-1]} + \mathbf{b}^{[l]}$ with $\mathbf{a}^{[0]} = \mathbf{x}$ the input x(i).
- m is the number of observations or data points in the dataset.

$$\nabla_{w} J_{CE}(w,b) = \frac{1}{m} \sum_{i=1}^{m} (\hat{y}(i) - y(i)) \cdot x(i)$$
$$\nabla_{b} J_{CE}(w,b) = \frac{1}{m} \sum_{i=1}^{m} (\hat{y}(i) - y(i))$$

Gradient Descent Variants

-BGD

Smooth, not wiggling, strictly decreasing cost, many epochs needed, choose larger learning rate, no out-of-core support all data in RAM (m), easy to parallelise.

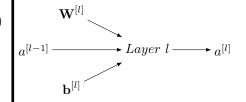
— SGD —

Wiggling, needs smoothing, wiggles around minimum, not necessarily decreasing cost, few epochs needed, choose smaller learning rate, out-of-core support - not all data to be kept in RAM of a single machine, not easy to parallelise.

- MBGD -

Slightly wiggling, wiggles around minimum. typically decreasing cost, less epochs than BGD, more than SGD needed, choose medium learning rate (dependent on model), out-of-core support - not all data to be kept in RAM of a single machine, easy to parallelise.

Compute Graph



$$\mathbf{W}^{[l]} = \begin{pmatrix} w_{11} & \cdots & w_{1n^{[l-1]}} \\ \vdots & \ddots & \vdots \\ w_{n^{[l]}1} & \cdots & w_{n^{[l]}n^{[l-1]}} \end{pmatrix}$$

$$\mathbf{a}^{[l]} = \begin{pmatrix} a_1 \\ \vdots \\ a_{n^{[l]}} \end{pmatrix}$$

$$\mathbf{b}^{[l]} = \begin{pmatrix} b_1 \\ \vdots \\ b_{n^{[l]}} \end{pmatrix}$$

$$\mathbf{a}^{[l]} = \sigma^{[l]}(\mathbf{z}^{[l]})$$

$$\mathbf{z}^{[l]} = \mathbf{W}^{[l]} \cdot \mathbf{a}^{[l-1]} + \mathbf{b}^{[l]} \quad \text{with } \mathbf{a}^{[0]} = \mathbf{x}$$

- Matrix Notation

$$\begin{split} \frac{\partial L}{\partial \mathbf{z}^{[l]}} &= \frac{\partial L}{\partial \mathbf{a}^{[l]}} * \frac{d\sigma^{[l]}(\mathbf{z}^{[l]})}{dz} \\ \frac{\partial L}{\partial \mathbf{W}^{[l]}} &= \frac{\partial L}{\partial \mathbf{z}^{[l]}} \cdot \left(\mathbf{a}^{[l-1]}\right)^T \\ \frac{\partial L}{\partial \mathbf{b}^{[l]}} &= \frac{\partial L}{\partial \mathbf{z}^{[l]}} \\ \frac{\partial L}{\partial \mathbf{a}^{[l-1]}} &= \left(\mathbf{W}^{[l]}\right)^T \cdot \frac{\partial L}{\partial \mathbf{z}^{[l]}} \end{split}$$

Full Batch

$$\begin{split} \frac{\partial L}{\partial \mathbf{Z}^{[l]}} &= \frac{\partial L}{\partial \mathbf{A}^{[l]}} * \frac{d\sigma^{[l]}(\mathbf{Z}^{[l]})}{dz} \\ \frac{\partial L}{\partial \mathbf{W}^{[l]}} &= \frac{\partial L}{\partial \mathbf{Z}^{[l]}} \cdot \left(\mathbf{A}^{[l-1]}\right)^T \\ \frac{\partial L}{\partial \mathbf{b}^{[l]}} &= \frac{1}{m} \cdot \frac{\partial L}{\partial \mathbf{Z}^{[l]}} \cdot \begin{pmatrix} \vdots \\ \vdots \\ \vdots \end{pmatrix} \\ \frac{\partial L}{\partial \mathbf{A}^{[l-1]}} &= \left(\mathbf{W}^{[l]}\right)^T \cdot \frac{\partial L}{\partial \mathbf{Z}^{[l]}} \end{split}$$

■ Batch Normalization

$$\begin{split} \frac{\partial L}{\partial \gamma} &= \frac{1}{m} \cdot \sum_{i=1}^{m} \frac{\partial L}{\partial \hat{a}^{(i)}} \cdot \frac{\partial \hat{a}^{(i)}}{\partial \gamma} \\ &= \frac{1}{m} \cdot \sum_{i=1}^{m} \frac{\partial L}{\partial \hat{a}^{(i)}} \cdot \hat{a}^{(i)} \\ \frac{\partial L}{\partial \beta} &= \sum_{i=1}^{m} \frac{\partial L}{\partial \hat{a}^{(i)}} \cdot \frac{\partial \hat{a}^{(i)}}{\partial \beta} \\ &= \sum_{i=1}^{m} \frac{\partial L}{\partial \hat{a}^{(i)}} \end{split}$$

Vanishing Exploding Gradient

Xavier & Heu Initialization

drawn from a uniform distribution with smooth the optimization path. a range that depends on the number of input and output units in the layer. Specifically, the range is set to [-r, r], where $r = \sqrt{\frac{6}{n_{in} + n_{out}}}$, and n_{in} is the number Nesterov variant: of input units and n_{out} is the number of output units. This range was chosen because it ensures that the variance of the outputs of each layer remains constant. which helps to prevent the vanishing or exploding gradient problem.

— Batch Normalization –

We calculate the average μ_r and standard deviation σ_r over the m column vectors z_r of the mini-batch according to:

$$\mu_r = \frac{1}{m} \sum_{i=1}^m z_r^{[l](i)}$$

$$\sigma_r = \sqrt{\frac{1}{m} \sum_{i=1}^m (z_r^{[l](i)} - \mu_r)^2}$$

Now, the actual normalization of the logit matrix is as follows:

$$\hat{Z}_r^{[l]} = \frac{Z_r^{[l]} - \mu_r}{\sigma_r + \epsilon}$$

Finally, two addition parameter vectors are introduced that rescale the logits according $m_t \leftarrow \beta_1 m_{t-1} + (1-\beta_1) \nabla_{\theta} J(\theta_{t-1})$ to:

$$\tilde{Z}_r^{[l]} = \gamma^{[l]} \cdot \hat{Z}_r^{[l]} + \beta^{[l]}$$

— Non Saturating Activation Function — To alleviate the saturation of sigmoid and tanh, we can use the ReLU activation function. It still suffer from dving units problem (when the input is negative, the gradient is 0).

— Gradient Clipping —

If gradients values exceed a certain threshold, they are "clipped" or rescaled to a **Exponential scheduling** : $\alpha(t)$ smaller value. This prevents the gradients $\alpha_0 \cdot 10^{-t/T}$ from becoming too large and helps to Power stabilize the training process.

Optimizers

- Momentum

Sets the initial weights of a layer to values Uses a running average of gradients to Modify the loss function to include a pe-

$$m_t \leftarrow \beta m_{t-1} + \alpha \nabla_{\theta} J(\theta)$$
$$\theta_t \leftarrow \theta_{t-1} - m_t$$

$$m_t \leftarrow \beta m_{t-1} + \alpha \nabla_{\theta} J(\theta_{t-1} - \beta m_{t-1})$$

$$\theta_t \leftarrow \theta_{t-1} - m_t$$

— AdaGrad —

Scaling down the gradient vector along the steepest dimensions.

$$s_{t} \leftarrow s_{t-1} + \nabla_{\theta} J(\theta_{t-1}) \cdot \nabla_{\theta} J(\theta_{t-1})$$
$$\theta_{t} \leftarrow \theta_{t-1} - \frac{\alpha}{\sqrt{s_{t}} + \epsilon} \cdot \nabla_{\theta} J(\theta_{t-1})$$

RMS Prop

A variant of AdaGrad using an exponentially decaying average of squared gradients.

$$s_{t} \leftarrow \beta s_{t-1} + (1 - \beta) \nabla_{\theta} J(\theta_{t-1}) \cdot \nabla_{\theta} J(\theta_{t-1})$$
$$\theta_{t} \leftarrow \theta_{t-1} - \frac{\alpha}{\sqrt{s_{t} + \epsilon}} \cdot \nabla_{\theta} J(\theta_{t-1})$$

- Adam

Combines momentum and RMSProp to adapt the learning rate for each parameter.

$$s_{t} \leftarrow \beta_{2}s_{t-1} + (1 - \beta_{2})\nabla_{\theta}J(\theta_{t-1}) \cdot \nabla_{\theta}J(\theta_{t-1})$$

$$\hat{m}_{t} \leftarrow \frac{m_{t}}{1 - \beta_{1}^{t}}$$

$$\hat{s}_{t} \leftarrow \frac{s_{t}}{1 - \beta_{2}^{t}}$$

$$\theta_{t} \leftarrow \theta_{t-1} - \frac{\alpha}{\sqrt{\hat{s}_{t}} + \epsilon} \cdot \hat{m}_{t}$$

- Scheduler ·

Strategies to adjust the learning rate during training: Performance scheduling

scheduling $\alpha(t)$ $\alpha_0 \cdot \left(1 + \frac{t}{T}\right)^{-c}$, where c is typically set to 1.

Regularization

Weight Penalty -

nalty to big weights:

$$J(\theta) = J_0(\theta) + \lambda \cdot \Omega(W)$$

where $\Omega(W)$ is the penalty term:

- L1:
$$\Omega(W) = ||W||_1 = \sum |W_{ji}|$$

- L2: $\Omega(W) = \frac{1}{2}||W||_2^2 = \frac{1}{2}\sum (W_{ii}^2)$

——Dropout -

Randomly drop neurons during training:

- Each neuron has probability p of being dropped.
- Typical p:50
- During testing, scale weights by 1-p.

- Early Stopping -

Stop training when validation error increases:

- Track validation error during training.
- Save model parameters when validation error improves.
- Stop if no improvement for a set number of steps.

CNN

Convolutional Laver Pooling Layer

Unbalanced Dataset

Bayesian Approach Discrete Continuous Medical Test

DeepCNN

Conf2D Params MaxPooling LeNet5 AlexNet VGGnet GoogleNet ResNetPattern

Feature Visualization

Data Preparation Network Compile Evaluate Activation Map

- Data Augmentation

Principle
Types
Strategies
Keras

Functional API

Sequential vs Functionals Architecture 1 Architecture 2 Architecture 3

Transfer Learning

Principle Keras Code MobileNet Strategies

RNN

Use Case
Model Category
Recurrence Net
Single Layer
Many to Many
Un exemple par catégorie
Stacked RNN

LSTM

Long Term Memory Unit Cell Gates Backprop Keras GRE

Word Embedding

Word Training

Sentiment Classification

Strategy Architecture

Autoencoder

Definition Use Case

GenRNN

Many to Many Many to One

Attention

Sequence to Sequence Attention

Transformer

High-Level Architecture