




# ODINN.jl: Scientific machine learning glacier modelling

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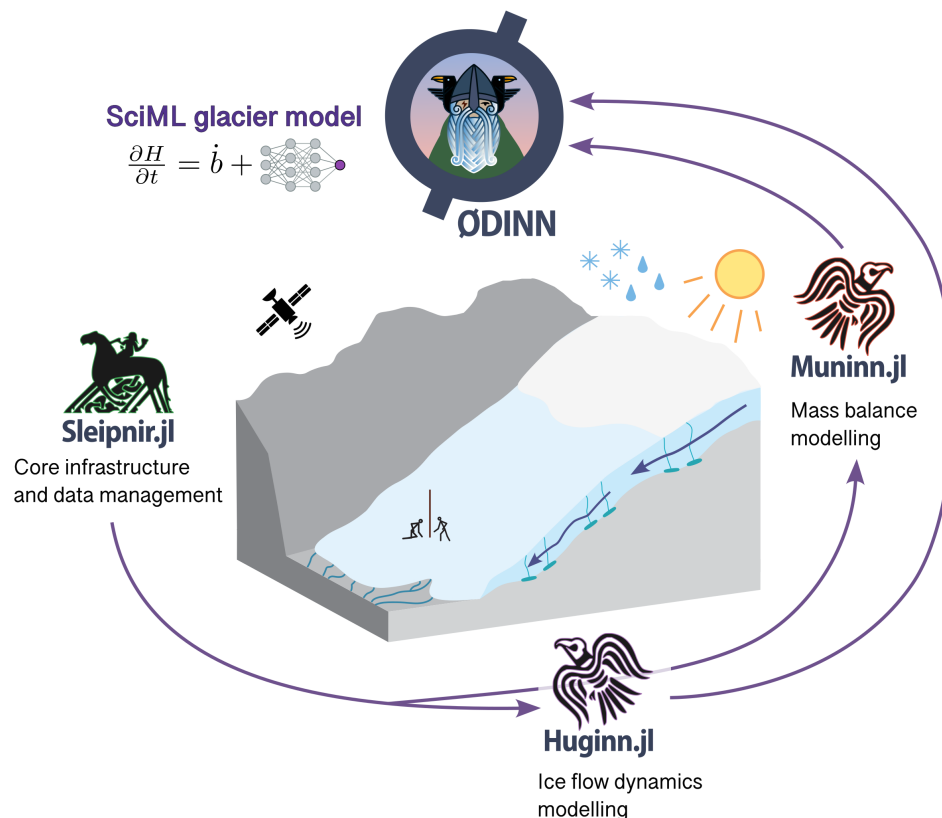
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## Summary

ODINN.jl is a glacier model leveraging scientific machine learning (SciML) methods to perform forward and inverse simulations of large-scale glacier evolution. It can simulate both surface mass balance and ice flow dynamics through a modular architecture which enables the user to easily modify model components. For this, ODINN.jl is in fact an ecosystem composed of multiple packages, each one handling a specific task:

- **Sleipnir.jl**: Handles all the basic types, functions and datasets, common through the whole ecosystem, as well as data management tasks.
- **Muninn.jl**: Handles surface mass balance processes, via different types of models.
- **Huginn.jl**: Handles ice flow dynamics, by solving the ice flow partial differential equations (PDEs) using numerical methods. It can accommodate multiple types of ice flow models.
- **ODINN.jl**: Acts as the interface to the whole ecosystem, and provides the necessary tools to differentiate and optimize any model component. It can be seen as the SciML layer, enabling different types of inverse methods, using hybrid models combining differential equations with data-driven models.
- Splitting large Julia ([Bezanson et al., 2017](#)) packages into smaller, focused subpackages is a good practice that enhances maintainability, usability, and collaboration. Modular design simplifies debugging, testing, and updates by isolating functionalities, while users benefit from faster precompilation and reduced memory overhead by loading only the subpackages they need. This approach also lowers the barrier for new contributors, fosters clearer dependency management, and ensures scalability as projects grow, ultimately making the ecosystem more robust and adaptable. The ODINN ecosystem extends beyond this suite of Julia packages, by leveraging the data preprocessing tools of the Open Global Glacier Model (OGGM, [Maussion et al. \(2019\)](#)). We do so via an auxiliary Python library named **Gungnir**, which is responsible for downloading all the necessary data to force and initialize the model, such as glacier outlines from the Randolph Glacier Inventory (RGI Consortium ([2023](#)), RGI), digital elevation models (DEMs), ice thickness observations from **GlaThiDa** ([Consortium, 2020](#)), ice surface velocities from different studies ([Millan et al., 2022](#)), and many different sources of climate reanalyses and projections ([Eyring et al., 2016](#); [Lange, 2019](#)). This implies that ODINN.jl, like OGGM, is virtually capable of simulating any of the ~274,000 glaciers on Earth ([RGI Consortium, 2023](#)).



**Figure 1:** Figure 1: Overview of the ODINN.jl ecosystem.

ODINN.jl provides a high-level user-friendly interface, enabling the user to swap and replace most elements of a glacier simulation in a very modular fashion. The main elements of a simulation, such as the Parameters, a Model and a Simulation (i.e. a Prediction or an Inversion), are all objects that can be easily modified and combined. In a few lines of code, the user can automatically retrieve all necessary information for most glaciers on Earth, compose a Model based on a specific combination of surface mass balance and ice flow models, and incorporate data-driven models (e.g. a neural network) to parametrize specific physical processes of any of these components. Both forward and reverse simulations run in parallel using multiprocessing, leveraging Julia's speed and performance. Graphics Processing Unit (GPU) compatibility is still not ready, due to the difficulties of making everything compatible with automatic differentiation (AD). Nonetheless, it is planned for future versions.

The most unique aspect of ODINN.jl is its differentiability and capabilities of performing all sorts of different hybrid modelling. Since the whole ecosystem is differentiable, we can optimize almost any model component, providing an extremely powerful framework to tackle many scientific problems (Bolibar et al., 2023). ODINN.jl can optimize, separately or together, in a steady-state or transient way:

- The initial or intermediate state of glaciers (i.e. their ice thickness) or the equivalent ice surface velocities.
- Model parameters (e.g. the Glen coefficient  $A$  related to ice viscosity in a 2D Shallow Ice Approximation (Hutter, 1983)), in a gridded or scalar format. This can be done for multiple time steps where observations (e.g. ice surface velocities) are available.
- The parameters of a regressor (e.g. a neural network), used to parametrize a subpart or one or more coefficients of an ice flow or surface mass balance mechanistic model.

67 This enables the exploration of empirical laws describing physical processes of glaciers,  
68 leveraging Universal Differential Equations (UDEs, Christopher Rackauckas et al. (2021)).

69 For this, it is necessary to differentiate (that is, computing gradients or derivatives) through  
70 complex code, including numerical solvers, which is a non-trivial task (Sapienza et al., 2024).  
71 We use reverse differentiation based on the adjoint method to achieve this. We have two  
72 strategies for computing both the adjoint and the required vector-jacobian products (VJPs):  
73 (1) manual adjoints, which have been implemented using AD via Enzyme.jl (Moses et al.,  
74 2021), as well as fully manual implementations of the discrete and continuous adjoints; and  
75 (2) automatic adjoints using SciMLSensitivity.jl (Chris Rackauckas et al., 2019), providing  
76 both continuous and discrete versions and available with different AD back-ends. These two  
77 approaches are complementary, with the manual adjoints being ideal for high-performance  
78 tasks, and serving as a ground truth for benchmarking and testing automatic adjoint methods  
79 from SciMLSensitivity.jl.

80 Beyond all these inverse modelling capabilities, ODINN.jl can also act as a more conventional  
81 forward glacier model, simulating glaciers in parallel, and easily customizing almost every  
82 possible detail of the simulation. Its high modularity, combined with the easy access to a vast  
83 array of datasets coming from OGGM, makes it very easy to run simulations, even with a  
84 simple laptop. Huginn.jl is responsible for the ice flow dynamics models, with an architecture  
85 capable of integrating and easily swapping various models. Models based on partial differential  
86 equations (PDEs) are solved using DifferentialEquations.jl (Christopher Rackauckas &  
87 Nie, 2017), which provides access to a huge amount of numerical solvers. For now, we have  
88 implemented a 2D Shallow Ice Approximation (SIA, Hutter (1983)), but in the future we plan to  
89 incorporate other models, such as the Shallow Shelf Approximation (SSA, Weis et al. (1999)).  
90 Validation of numerical forward simulations are evaluated in the test suite based on exact  
91 analytical solutions of the SIA equation for some simpler cases (Bueler et al., 2005). In terms  
92 of surface mass balance, Muninn.jl incorporates for now simple temperature-index models.  
93 Nonetheless, the main addition of the upcoming version will be the machine learning-based  
94 models from the MassBalanceMachine (Sjursen et al., 2025), which will become the de-facto  
95 solution. Frontal ablation (i.e. calving) and debris cover are not available for now, but we plan  
96 to add it to future versions of the model.

## 97 Statement of need

98 ODINN.jl addresses the need for a glacier model that combines the physical interpretability of  
99 mechanistic approaches with the flexibility and data-assimilation capabilities of data-driven  
100 methods (Bolibar et al., 2023). By integrating both paradigms, it enables targeted inverse  
101 methods to learn parametrizations of glacier processes, capturing unknown physics while  
102 preserving the physically grounded structure of glacier dynamics through differential equations.

103 While purely mechanistic and purely data-driven glacier models already exist (e.g. Gagliardini  
104 et al. (2013), Maussion et al. (2019), Rounce et al. (2023), Bolibar et al. (2022)), they  
105 often lack the flexibility needed to fully exploit the growing wealth of glacier observations, such  
106 as ice surface velocities, ice thickness, surface topography, surface mass balance or climate  
107 reanalyses. Existing empirical laws do not always link directly to these observables, making  
108 their calibration challenging. Approaches based on differentiable programming and functional  
109 inversions offer a path forward, allowing the derivation of new empirical relationships from  
110 carefully chosen proxies and providing a framework to test hypotheses about poorly understood  
111 physical processes such as basal sliding, creep, or calving.

112 Improving the representation of these complex processes is crucial for accurate projections of  
113 glacier evolution and their impacts on freshwater availability and sea-level rise (IPCC, 2021).  
114 To this end, ODINN.jl provides a unified modelling ecosystem that supports both advanced  
115 inverse methods for model calibration and efficient, modular forward simulations for large-scale  
116 glacier studies.

117 Developing such a framework places demanding requirements on scientific software. Inefficient  
 118 or monolithic implementations can hinder progress, emphasizing the importance of open-  
 119 source, community-driven tools that follow modern software engineering practices. The Julia  
 120 programming language provides two key advantages in this context: it resolves the two-language  
 121 problem by offering Python-like high-level expressiveness with C-level performance (Bezanson et  
 122 al., 2017), and it enables source-code differentiability, essential for gradient-based optimization  
 123 in inverse modelling.

124 With ODINN.jl, our goal is to provide a robust and future-proof modelling environment  
 125 that bridges the gap between physical understanding and data-driven discovery. Its modular  
 126 architecture, thorough testing, and continuous integration (CI) ensure reproducibility and  
 127 reliability, while its open design invites collaborations and both methodological and applied  
 128 advancements across the glaciological and Earth system modelling communities.

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