

# <sup>1</sup> ODINN.jl: Scientific machine learning glacier modelling

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## <sup>12</sup> Summary

<sup>13</sup> ODINN.jl is a glacier model leveraging scientific machine learning (SciML) methods to perform  
<sup>14</sup> forward and inverse simulations of large-scale glacier evolution. It can simulate both surface  
<sup>15</sup> mass balance and ice flow dynamics through a modular architecture which enables the user to  
<sup>16</sup> easily modify model components.

<sup>17</sup> The most unique aspect of ODINN.jl is its differentiability and capabilities of performing  
<sup>18</sup> all sorts of different hybrid modelling. Since the whole ecosystem is differentiable (where  
<sup>19</sup> differentiable means the ability to compute model derivatives with respect to parameters  
<sup>20</sup> ([Shen et al., 2023](#))), we can optimize almost any model component, providing an extremely  
<sup>21</sup> powerful framework to tackle many scientific problems ([Bolibar et al., 2023](#)). ODINN.jl can  
<sup>22</sup> optimize, separately or together, in a steady-state (time-independent simulation) or transient  
<sup>23</sup> (time-dependent simulation) way the following model parameters:

- The initial or intermediate state of glaciers (i.e. their ice thickness) or the equivalent ice surface velocities.
- Model parameters (e.g. the Glen coefficient A related to ice viscosity in a 2D Shallow Ice Approximation ([Hutter, 1983](#))), in a gridded or scalar format. This can be done for multiple time steps where observations (e.g. ice surface velocities) are available.
- The parameters of a statistical regressor (e.g. a neural network), used to parametrize a subpart or one or more coefficients of an ice flow or surface mass balance mechanistic model. This enables the exploration of empirical laws describing physical processes of glaciers, leveraging Universal Differential Equations (UDEs, Christopher Rackauckas et al. ([2021](#))).

<sup>34</sup> For this, it is necessary to differentiate (that is, computing gradients or derivatives) through  
<sup>35</sup> complex code, including numerical solvers, which is a non-trivial task ([Sapienza et al., 2024](#)).  
<sup>36</sup> We use reverse differentiation based on the adjoint method to achieve this. We have two  
<sup>37</sup> strategies for computing both the adjoint and the required vector-jacobian products (VJPs):  
<sup>38</sup> (1) manual adjoints, which have been implemented using AD via Enzyme.jl ([Moses et al.,](#)  
<sup>39</sup> [2021](#)), as well as fully manual implementations of the spatially discrete and spatially continuous  
<sup>40</sup> VJPs; and (2) automatic adjoints using SciMLSensitivity.jl ([Chris Rackauckas et al., 2019](#)),  
<sup>41</sup> available with different AD back-ends for the VJPs computation. These two approaches are  
<sup>42</sup> complementary, with the manual adjoints being ideal for high-performance tasks by providing  
<sup>43</sup> more control on the implementation, and serving as a ground truth for benchmarking and

44 testing automatic adjoint methods from SciMLSensitivity.jl.  
45 Beyond all these inverse modelling capabilities, ODINN.jl can also act as a more conventional  
46 forward glacier model, simulating glaciers in parallel, and easily customizing different model  
47 parametrizations and choices within the simulation. Its high modularity, combined with the easy  
48 access to a vast array of datasets coming from OGGM, makes it very easy to run simulations,  
49 even with a simple laptop. Multiple ice flow dynamics models can be easily swapped, thanks  
50 to a modular architecture (see Software design). Models based on partial differential equations  
51 (PDEs) are solved using DifferentialEquations.jl (Christopher Rackauckas & Nie, 2017),  
52 which provides access to a huge amount of numerical solvers. For now, we have implemented  
53 a 2D Shallow Ice Approximation (SIA, Hutter (1983)), but in the future we plan to incorporate  
54 other models, such as the Shallow Shelf Approximation (SSA, Weis et al. (1999)). Validation  
55 of numerical forward simulations are evaluated in the test suite based on exact analytical  
56 solutions of the SIA equation (Bueler et al., 2005). Multiple surface mass balance models are  
57 available, based on simple temperature-index models. Nonetheless, the main addition of the  
58 upcoming version will be the machine learning-based models from the MassBalanceMachine  
59 (Sjursen et al., 2025), which will provide further mass balance models.

## 60 Statement of need

61 ODINN.jl addresses the need for a glacier model that combines the physical interpretability of  
62 mechanistic approaches with the flexibility and data-assimilation capabilities of data-driven  
63 methods (Bolibar et al., 2023). By integrating both paradigms, it enables targeted inverse  
64 methods to learn parametrizations of glacier processes, capturing unknown physics while  
65 preserving the physically grounded structure of glacier dynamics through differential equations.  
66 While purely mechanistic and purely data-driven glacier models already exist (e.g. Gagliardini  
67 et al. (2013), Maussion et al. (2019), Rounce et al. (2023), Bolibar et al. (2022)), they  
68 often lack the flexibility needed to fully exploit the growing wealth of glacier observations, such  
69 as ice surface velocities, ice thickness, surface topography, surface mass balance or climate  
70 reanalyses. Existing empirical laws do not always link directly to these observables, making  
71 their calibration challenging. Approaches based on differentiable programming and functional  
72 inversions offer a path forward, allowing the derivation of new empirical relationships from  
73 carefully chosen proxies and providing a framework to test hypotheses about poorly understood  
74 physical processes such as basal sliding, creep, or calving.  
75 Improving the representation of these complex processes is crucial for accurate projections of  
76 glacier evolution and their impacts on freshwater availability and sea-level rise (IPCC, 2021).  
77 To this end, ODINN.jl provides a unified modelling ecosystem that supports both advanced  
78 inverse methods for model calibration and efficient, modular forward simulations for large-scale  
79 glacier studies.  
80 Developing such a framework places demanding requirements on scientific software. Inefficient  
81 codes and irreproducible implementations can severely restrict progress, emphasizing the  
82 importance of open-source, community-driven tools that follow modern research software  
83 engineering (RSE) practices (Combemale et al., 2023). For this end, software should support  
84 modular and adaptable design patterns that enable prototyping and augmentation of existing  
85 pipelines (Nyenh et al., 2024). The Julia programming language provides two key advantages in  
86 this context: it solves the two-language problem by offering Python-like high-level expressiveness  
87 with C-level performance (Bezanson et al., 2017), and it enables source-code differentiability,  
88 essential for modular gradient-based optimization in inverse modelling and setting the foundation  
89 for a strong ecosystem where hybrid modelling, and particularly UDEs, can thrive. With  
90 ODINN.jl, our goal is to provide a robust and future-proof modelling framework that bridges  
91 the gap between physical understanding and data-driven discovery. Its modular architecture,  
92 thorough testing, and continuous integration (CI) ensure reproducibility and reliability, while its  
93 open design invites collaborations and both methodological and applied advancements across

94 the glaciological and Earth system modelling communities.

## 95 Software design

96 ODINN.jl is in fact an ecosystem composed of multiple packages, each one handling a specific  
97 task:

- 98     ▪ Sleipnir.jl: Handles all the basic types, functions and datasets, common through the  
99         whole ecosystem, as well as data management tasks.
- 100     ▪ Muninn.jl: Handles surface mass balance processes, via different types of models.
- 101     ▪ Huginn.jl: Handles ice flow dynamics, by solving the ice flow partial differential equations  
102         (PDEs) using numerical methods. It can accommodate multiple types of ice flow models.
- 103     ▪ ODINN.jl: Acts as the interface to the whole ecosystem, and provides the necessary tools  
104         to differentiate and optimize any model component. It can be seen as the SciML layer,  
105         enabling different types of inverse methods, using hybrid models combining differential  
106         equations with data-driven models.

107 Splitting large Julia ([Bezanson et al., 2017](#)) packages into smaller, focused subpackages is  
108 a good practice that enhances maintainability, usability, and collaboration. Modular design  
109 simplifies debugging, testing, and updates by isolating functionalities, while users benefit from  
110 faster precompilation and reduced memory overhead by loading only the subpackages they  
111 need. This approach also lowers the barrier for new contributors, fosters clearer dependency  
112 management, and ensures scalability as projects grow, ultimately creating a robust and  
113 adaptable software ecosystem. The ODINN ecosystem extends beyond this suite of Julia  
114 packages, by leveraging the data preprocessing tools of the Open Global Glacier Model (OGGM,  
115 Maussion et al. ([2019](#))). We do so via an auxiliary Python library named Gungnir, which  
116 is responsible for generating all the necessary data to force and initialize the model, such as  
117 glacier outlines from the Randolph Glacier Inventory (RGI Consortium ([2023](#)), RGI), digital  
118 elevation models (DEMs), ice thickness observations from GlaThiDa ([Consortium, 2020](#)), ice  
119 surface velocities from different studies ([Millan et al., 2022](#)), and different sources of climate  
120 reanalyses and projections ([Eyring et al., 2016](#); [Lange, 2019](#)). This implies that ODINN.jl,  
121 like OGGM, is virtually capable of simulating any of the ~274,000 glaciers on Earth ([RGI  
122 Consortium, 2023](#)).

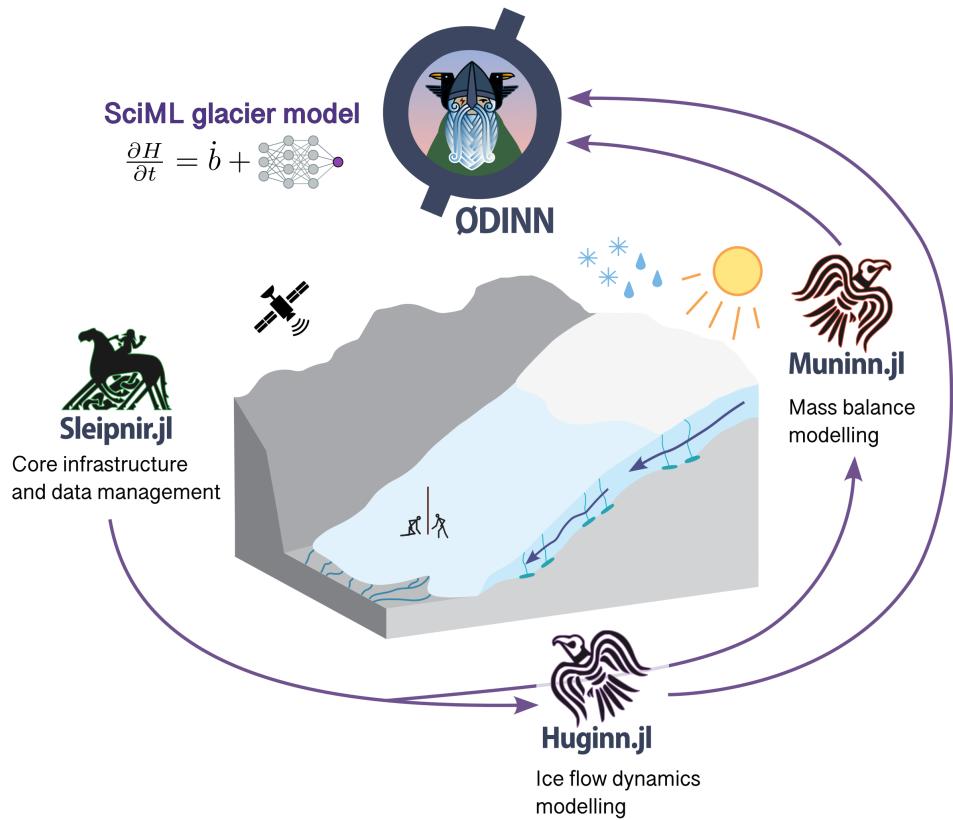


Figure 1: Overview of the ODINN.jl ecosystem.

123    ODINN.jl provides a high-level user-friendly interface, enabling the user to swap and replace  
 124    most elements of a glacier simulation in a very modular fashion. The main elements of a  
 125    simulation, such as the Parameters, a Model and a Simulation (i.e. a Prediction or an  
 126    Inversion), are all objects that can be easily modified and combined. In a few lines of  
 127    code, the user can automatically retrieve all necessary information for most glaciers on Earth,  
 128    compose a Model based on a specific combination of surface mass balance and ice flow models,  
 129    and incorporate data-driven models (e.g. a neural network) to parametrize specific physical  
 130    processes of any of these components. Both forward and inverse simulations run in parallel  
 131    using multiprocessing, leveraging Julia's speed and performance. Graphics Processing Unit  
 132    (GPU) compatibility is still not ready, due to the difficulties of making GPU architectures  
 133    compatible with automatic differentiation (AD). Nonetheless, it is planned for future versions.

## Research impact statement

134    ODINN.jl has so far been used to explore the use of UDEs to invert hidden empirical laws in a  
 135    synthetic glacier setup, where a prescribed rheological law was successfully recovered using  
 136    a neural network (Bolibar et al., 2023). This proof-of-concept then served as a backbone  
 137    to create the current complex architecture of ODINN.jl, finalized with the recent 1.0 release.  
 138    The main changes and scientific goals of this large software development investment, are the  
 139    capacity to now apply these methods to large-scale remote sensing data for multiple glaciers,  
 140    which will enable the exploration of new glacier basal sliding laws directly from heterogeneous  
 141    observations, which remains a long-standing problem in glaciology (Minchew & Joughin, 2020).  
 142  
 143    Additionally, ODINN.jl will be soon used as part of a newly funded 4-year project, to simulate

<sup>144</sup> past and future glacier changes in several catchments in the Andes and the Alps. These model  
<sup>145</sup> outputs will then be combined with a hydrological model, to investigate the impacts of glacier  
<sup>146</sup> retreat on the hydrological regimes and drought mitigation under different climate change  
<sup>147</sup> scenarios.

<sup>148</sup> With these two research venues, ODINN.jl will be developed and used to pursue both  
<sup>149</sup> fundamental research on glacier sliding laws, as well as applied research to assess the impact  
<sup>150</sup> of glacier retreat on freshwater availability and drought mitigation.

## <sup>151</sup> AI usage disclosure

<sup>152</sup> Generative AI, via GitHub copilot, has been used to partially generate some of the docstrings  
<sup>153</sup> for the documentation, and to assist in the coding of some tests and helper functions.

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## <sup>167</sup> References

- <sup>168</sup> Bezanson, J., Edelman, A., Karpinski, S., & Shah, V. B. (2017). Julia: A Fresh Approach to  
<sup>169</sup> Numerical Computing. *SIAM Review*, 59(1), 65–98. <https://doi.org/10.1137/141000671>
- <sup>170</sup> Bolibar, J., Rabatel, A., Gouttevin, I., Zekollari, H., & Galiez, C. (2022). Nonlinear sensitivity  
<sup>171</sup> of glacier mass balance to future climate change unveiled by deep learning. *Nature  
Communications*, 13(1), 409. <https://doi.org/10.1038/s41467-022-28033-0>
- <sup>172</sup> Bolibar, J., Sapienza, F., Maussion, F., Lguensat, R., Wouters, B., & Pérez, F. (2023). Universal  
<sup>173</sup> differential equations for glacier ice flow modelling. *Geoscientific Model Development*,  
<sup>174</sup> 16(22), 6671–6687. <https://doi.org/10.5194/gmd-16-6671-2023>
- <sup>175</sup> Bueler, E., Lingle, C. S., Kallen-Brown, J. A., Covey, D. N., & Bowman, L. N. (2005).  
<sup>176</sup> Exact solutions and verification of numerical models for isothermal ice sheets. *Journal of  
Glaciology*, 51(173), 291–306. <https://doi.org/10.3189/172756505781829449>
- <sup>177</sup> Combemale, B., Gray, J., & Rumpe, B. (2023). Research software engineering and the  
<sup>178</sup> importance of scientific models. *Software and Systems Modeling*, 22(4), 1081–1083.  
<https://doi.org/10.1007/s10270-023-01119-z>
- <sup>179</sup> Consortium, G. (2020). *Glacier Thickness Database 3.1.0*. World Glacier Monitoring Service,  
<sup>180</sup> Zurich, Switzerland.
- <sup>181</sup> Eyring, V., Bony, S., Meehl, G. A., Senior, C. A., Stevens, B., Stouffer, R. J., & Taylor, K.  
<sup>182</sup> E. (2016). Overview of the Coupled Model Intercomparison Project Phase 6 (CMIP6)
- <sup>183</sup>

- 186 experimental design and organization. *Geoscientific Model Development*, 9(5), 1937–1958.  
187 <https://doi.org/10.5194/gmd-9-1937-2016>
- 188 Gagliardini, O., Zwinger, T., Gillet-Chaulet, F., Durand, G., Favier, L., Fleurian, B. de,  
189 Greve, R., Malinen, M., Martín, C., Råback, P., Ruokolainen, J., Sacchettini, M., Schäfer,  
190 M., Seddik, H., & Thies, J. (2013). Capabilities and performance of Elmer/Ice, a new-  
191 generation ice sheet model. *Geoscientific Model Development*, 6(4), 1299–1318. <https://doi.org/10.5194/gmd-6-1299-2013>
- 192 Hutter, K. (1983). *Theoretical Glaciology*. Springer Netherlands. <https://doi.org/10.1007/978-94-015-1167-4>
- 193 IPCC. (2021). *Climate Change 2021: The Physical Science Basis. Contribution of Working  
194 Group I to the Sixth Assessment Report of the Intergovernmental Panel on Climate Change:  
195 Vols. In Press*. Cambridge University Press. <https://doi.org/10.1017/9781009157896>
- 196 Lange, S. (2019). WFDE5 over land merged with ERA5 over the ocean (W5E5). GFZ Data  
197 Services. <https://doi.org/10.5880/PIK.2019.023>
- 198 Maussion, F., Butenko, A., Champollion, N., Dusch, M., Eis, J., Fourteau, K., Gregor, P.,  
199 Jarosch, A. H., Landmann, J., Oesterle, F., Recinos, B., Rothenpieler, T., Vlug, A., Wild, C.  
200 T., & Marzeion, B. (2019). The Open Global Glacier Model (OGGM) v1.1. *Geoscientific  
201 Model Development*, 12(3), 909–931. <https://doi.org/10.5194/gmd-12-909-2019>
- 202 Millan, R., Mouginot, J., Rabatel, A., & Morlighem, M. (2022). Ice velocity and thickness of  
203 the world's glaciers. *Nature Geoscience*, 15(2), 124–129. <https://doi.org/10.1038/s41561-021-00885-z>
- 204 Minchew, B., & Joughin, I. (2020). Toward a universal glacier slip law. *Science*, 368(6486),  
205 29–30. <https://doi.org/10.1126/science.abb3566>
- 206 Moses, W. S., Churavy, V., Paehler, L., Hückelheim, J., Narayanan, S. H. K., Schanen, M.,  
207 & Doerfert, J. (2021). Reverse-mode automatic differentiation and optimization of GPU  
208 kernels via enzyme. *Proceedings of the International Conference for High Performance  
209 Computing, Networking, Storage and Analysis*. <https://doi.org/10.1145/3458817.3476165>
- 210 Nyenah, E., Döll, P., Katz, D. S., & Reinecke, R. (2024). Software sustainability of global  
211 impact models. *Geoscientific Model Development Discussions*, 2024, 1–29. <https://doi.org/10.5194/gmd-2024-97>
- 212 Rackauckas, Chris, Innes, M., Ma, Y., Bettencourt, J., White, L., & Dixit, V. (2019).  
213 DiffEqFlux.jl - A Julia Library for Neural Differential Equations. *arXiv:1902.02376 [Cs,  
214 Stat]*. <http://arxiv.org/abs/1902.02376>
- 215 Rackauckas, Christopher, Ma, Y., Martensen, J., Warner, C., Zubov, K., Supekar, R., Skinner,  
216 D., Ramadhan, A., & Edelman, A. (2021). *Universal Differential Equations for Scientific  
217 Machine Learning*. arXiv. <https://doi.org/10.48550/arXiv.2001.04385>
- 218 Rackauckas, Christopher, & Nie, Q. (2017). DifferentialEquations.jl – A Performant and  
219 Feature-Rich Ecosystem for Solving Differential Equations in Julia. *Journal of Open  
220 Research Software*, 5, 15. <https://doi.org/10.5334/jors.151>
- 221 RGI Consortium. (2023). *Randolph Glacier Inventory - A Dataset of Global Glacier Outlines,  
222 Version 7*. National Snow; Ice Data Center. <https://doi.org/10.5067/F6JMOVY5NAVZ>
- 223 Rounce, D. R., Hock, R., Maussion, F., Hugonnet, R., Kochtitzky, W., Huss, M., Berthier,  
224 E., Brinkerhoff, D., Compagno, L., Copland, L., Farinotti, D., Menounos, B., & McNabb,  
225 R. W. (2023). Global glacier change in the 21st century: Every increase in temperature  
226 matters. *Science*, 379(6627), 78–83. <https://doi.org/10.1126/science.abo1324>
- 227 Sapienza, F., Bolibar, J., Schäfer, F., Groenke, B., Pal, A., Boussange, V., Heimbach,  
228 P., Hooker, G., Pérez, F., Persson, P.-O., & Rackauckas, C. (2024). *Differentiable*

- 233      *Programming for Differential Equations: A Review.* arXiv. <http://arxiv.org/abs/2406.09699>
- 234
- 235      Shen, C., Appling, A. P., Gentine, P., Bandai, T., Gupta, H., Tartakovsky, A., Baity-Jesi, M., Fenicia, F., Kifer, D., Li, L., Liu, X., Ren, W., Zheng, Y., Harman, C. J., Clark, M., Farthing, M., Feng, D., Kumar, P., Aboelyazeed, D., ... Lawson, K. (2023). Differentiable modelling to unify machine learning and physical models for geosciences. *Nature Reviews Earth & Environment*, 1–16. <https://doi.org/10.1038/s43017-023-00450-9>
- 236
- 237
- 238
- 239
- 240      Sjursen, K. H., Bolibar, J., Meer, M. van der, Andreassen, L. M., Biesheuvel, J. P., Dunse, T., Huss, M., Maussion, F., Rounce, D. R., & Tober, B. (2025). Machine learning improves seasonal mass balance prediction for unmonitored glaciers. *EGUsphere*, 1–39. <https://doi.org/10.5194/egusphere-2025-1206>
- 241
- 242
- 243
- 244      Weis, M., Greve, R., & Hutter, K. (1999). Theory of shallow ice shelves. *Continuum Mechanics and Thermodynamics*, 11(1), 15–50. <https://doi.org/10.1007/s001610050102>
- 245

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