

## The 6th Quiz of Calculus 0507

學號：\_\_\_\_\_ 姓名：\_\_\_\_\_

1. (60%)

$$(1). \int_1^{\infty} \frac{1}{x} dx \quad (2). \int_{-\infty}^{\infty} \frac{e^x}{1+e^{2x}} dx \quad (3). \int_0^{\infty} e^{-x} \sin(2x) dx \quad (4). \int_{-1}^1 \frac{1}{x^2} dx$$

2. (40%) True or False ? If it is true, explain why. If it is false, give a counterexample.

(1). If  $f$  is continuous on  $[1, \infty)$  and  $\lim_{x \rightarrow \infty} f(x) = 0$ , then  $\int_1^{\infty} f(x) dx$  converges.

(2). If  $f$  is continuous on  $[1, \infty)$  and  $\int_1^{\infty} f(x) dx$  diverges, then

$$\lim_{x \rightarrow \infty} f(x) \neq 0$$