學號:

姓名:

## 國立中山大學 97 學年度第2 學期資訊工程學系資工數學

Quiz #2 2009/03/11

Graph an approximate solution curve through the given point or point (x, y) by hand.

1. 
$$4yy' = -9x, (2,2)(15\%)$$

2. 
$$y'=1+y^2$$
,  $(\frac{1}{4}\pi,1)$  (20%)

Find a general solution. Show the steps of derivation.

3. 
$$y' + (x+2)y^2 = 0$$
 (15%)

Find the particular solution. Show the steps of derivation, beginning with the general solution.

4.  $e^{2x}y' = 2(x+2)y^3$ ,  $y(0) = \frac{1}{\sqrt{5}} \approx 0.45$  (20%)

- 5. (Mixing) A tank contains 800 gal of water in which 200 lb of salt is dissolved. Two gallons of fresh water runs in per minute, and 2 gal of the mixture in the tank, kept uniform by stirring, runs out per minute. How much salt is left in the tank after 5 hours? (30%)
  - Let y(t) denote the amount of salt in the tank at time t.