## **Chapter Exam**

## **Appendix C-The Basics of Logic Design**

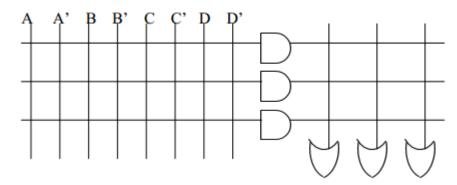
2012/03/06

- 1. In Boolean algebra, there is a Consensus Theorem. Try to prove the following two equations are true. (20%)
  - i)  $X \cdot Y + \sim X \cdot Z + Y \cdot Z = X \cdot Y + \sim X \cdot Z$
  - ii)  $(X + Y) \cdot (\sim X + Z) = (Y + Z)$
- 2. Try to prove De Morgan's Laws using truth table. (20%)

$$\mathbf{A} \cdot \mathbf{B} \equiv \mathbf{\sim} (\mathbf{\sim} \mathbf{A} + \mathbf{\sim} \mathbf{B})$$

$$A + B \equiv \sim (\sim A \cdot \sim B)$$

- **3.** Implement the function  $F(A, B, C, D) = A \cdot B + (\sim C \cdot \sim D)$ .
  - i) 2-input AND and OR gates and inverters. (5%)
  - ii) 2-input NAND gates. (5%)
  - iii) 2-input NOR gates. (5%)
  - iv) An AND/OR PLA. (10%)



- 4. What are the differences between combinational logics and sequential logics? (10%)
- 5. Draw a 1-bit full adder using 2 1-bit half adder in combination logic with the **input** a, b, carry\_in and with the **output** sum, carry\_out. (15%)
- **6.** Using the result of (5) to briefly draw out 32-bit adder. (10%)