# The Accuracy of KNN, SVM, SVDD, neural network and DBSCAN, k-means for Determining the Cancer by Gene-expression Signatures And the Arrhythmia Types

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# **Abstract**

Nowadays, using machine to give an early diagnosis of a cancer type is widely studied. In this paper, based on the gene-expression dataset on Synapse.org, we compare the performance of machine learning techniques, including data preprocessing, e.g., Principal components analysis (PCA), Autoencoder (AE), classification, e.g., k-nearest neighbors (KNN), support vector machine (SVM), neural network (NN), and clustering for dealing with unknown types, e.g., k-means, density-based spatial clustering of applications with noise (DBSCAN).

The result of gene dataset shows that, with PCA reducing the dimension of the dataset to 32, use KNN for classifying the known types, and finally apply DBSCAN on the remaining data, the accuracy of predicting can reach about 94%, which beats the other methods out. In the other way, the result of arrhythmia dataset shows that, with raw data, use KNN and k-means, the highest accuracy of predicting can reach about 53%.

The source code can be found in here.

## 1 Introduction

Over the years, machine learning methods for early predict various disease are widely used in medical field. [1] [2] From diabetes [3], heart disease [4], to lung adenocarcinoma [5] etc., machine learning methods is universally studied attributed to the promising perspective. With a well-built database of disease and a well-choose combination of machine learning mathods, within seconds, a

machine may determine the type of disease that this person may have by collecting the data from the person, and thereby achieve the goal of personalized medicine. As a result, machine learning methods have become a popular tool for medical researchers.

In real application, besides from the konwn diseases in the train data, there're numerous unkown types of diseases. When a new type of disease appears, how shall the machine results? In ideal situation, this new type of disease should be reported as an unkonwn type, which can be done by the combination of classification and clustering. However, how to choose the proper machine learning methods is a hot potato, since the different combinations of machine learning methods have different performance.

In this work, the dataset on Synapse.org is used, which contains 20531 RNA sequences and 3 types of cancer in the train data, i.e., kidney renal clear cell carcinoma (KIRC), breast invasive carcinoma (BRCA), lung adenocarcinoma (LUAD), and 2 new types in test data, i.e., colon adenocarcinoma (COAD), prostate adenocarcinoma (PRAD). And also, the dataset of arrhythmia is included, which caintains 8 types in train data, and 5 new types in test data. To find out which techniques is more suitable to fit these two datasets, this work examines the the accuracy of the combinations of some major machine learning techniques, including PCA, AE, KNN, SVM, NN, k-means, DBSCAN.

# 2 Related works

# Data preprocess

Autoencoder (AE): An AE is a type of neural network used for unsupervised learning and dimensionality reduction. It is designed to learn efficient representations or encodings of input data by training the network to reconstruct its own inputs. The AE consists of an encoder and a decoder. The encoder compresses the input data into a lower-dimensional representation, often called the latent space or code. The decoder then aims to reconstruct the original input data from this compressed representation. By learning a compact representation of the input data, AEs can capture important features and discard noise or irrelevant information [6]. This makes them effective in tasks such as image [7] [8] [9] or text classification [10] [11], where reducing the dimensionality of the data can improve performance.

**Principal components analysis (PCA):** PCA is a statistical technique used for dimensionality reduction and data exploration. It aims to transform a dataset with a large number of variables into a lower-dimensional space while preserving the most important information. PCA accomplishes this by identifying the principal components, which are linear combinations of the original variables. Applications of PCA span various fields, including image [12] [13] and signal processing [14] [15], genetics [16] [17]. It is particularly useful in scenarios where the dataset is high-dimensional and the interpretation and visualization of the data are challenging.

# Classification algorithm

k-nearest neighbors (KNN) classification algorithm: The KNN classification algorithm is a supervised learning method which is first developed by Fix and Hodges [18]. The idea of KNN is based on the idiom, "birds of a feather flock together". By picking the k-nearest neighbors of a data point, the unkonwn class label can be determined. Lots of works [19] [20] [21] show the fact that KNN performs well for prediction of diabetes disease.

**support vector machine (SVM):** Given a set of training datas, where each data is labeled as a binary class, such as 0 and 1, SVM training algorithm creates a model that assigns new examples to the binay labels by mak-

ing it a non-probabilistic binary linear classifier. In addition, accroding to [22] [23], SVM can also use a method called kernel trick to effectively perform non-linear classification by implicitly mapping its inputs into a high-dimensional feature space. The idea of kernel trick is transform the data into higher dimension. In ideal situation, the dataset which is not linear separable becomes linear separable. Fig 1 illurates this case.

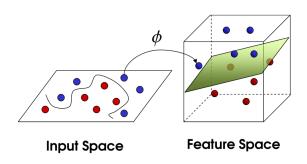


Figure 1: An example of SVM kernel trick

neural network (NN): Neural network have been used in many fields to deal with intricate datas. With input layer, hidden layer and output layer constructed by neurons, each data in dataset is processed while passing through neurons, layer by layer. After the processing, the outcome can be used to predict. Using back propogation, the accuracy of predictions increase in each training. In order to construct the hidden layer more efficient, NAS(Neural Arcitecture Searching) is used to search suitable structure for hidden layer, increasing the accuracy. According to [24][25], many neural network have been constructed and trained already, with high efficiency and accuracy in prediction of diabetes.

# Clustering algorithm

**k-means:** K-means is a popular and easily implemented clustering method in machine learning and data analysis. With n data points in a dataset, k-means algorithm partition them into k distinct clusters. The algorithm works iteratively and converges to a solution by minimizing the sum of squared distance between the data points and the center of their cluster. K-means is a useful algorithm

for clustering data, which is widely applied on many researches, e.g. [26], [27], [28].

Density-based spatial clustering of applications with noise (DBSCAN): DBSCAN is a data clustering algorithm proposed by Ester et al. [29] DBSCAN is particularly effective in discovering clusters of arbitrary shapes and handling noise in the data. Unlike k-means need user specify how many clusters, DBSCAN determine the clusters and noise automatically by the density of data points. This characteristic makes it particularly useful when addressing the datasets where the number of cluster is unkonwn. DBSCAN is the major clustering algorithm in machine learning field, since the ability to discover the number of clusters automatically. And the variants of DBSCAN [30] is also developed widely.

# **3 Main Process**

The pesudo code of the proposed algorithm to process the dataset is shown below and Fig 2 illurates the process of this algorithm:

### Algorithm 1 The Main Algorithm

Require: Dataset

- 1 Data, Labels ← Dataset
- 2  $Data' \leftarrow preprocess(Data)$
- 3 Konwns, Unkonwns  $\leftarrow$  classify(Data')
- 4 Clusters ← clustering(Unkonwns)
- 5 Accuracy ← calacc((Konwns, Clusters), Labels)

First, preprocess the dataset, e.g. normalize, apply PCA, apply AE. Second, classify the data after preprocessing. In the experiment, we use PCA and AE to reduce the dimension down to 32 and 30 in arrhythmia dataset and gene expression cancer RNA-Seq dataset, respectively. With this step, the konwn types and the unknown types will be separated by a certain criterion. This criterions will be varied depending on the classification algorithm. For KNN, the criterion is distance and probability. More specifically, assume a data point x, and the knearest data points are  $p_1, ..., p_k$ . Only those points whose distance between x smaller than L will be marked valid. Denote the valid data points as  $p_1', ..., p_n'$ , and the corresponding labels are  $l_1, ..., l_n$ . If this data point satisifies

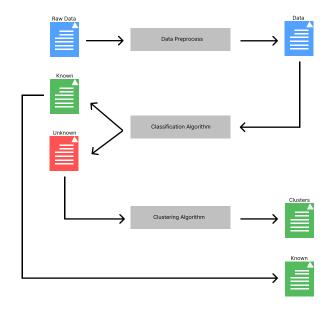


Figure 2: A figure about the main algorithm

Eq 1, mark it as unkown type.

$$\frac{\arg\max_{t \in \text{types}\{N(t)\}}}{n} < P \tag{1}$$

where P is a manually set probability and N(t) is the number of type t in those n valid data points.

As for SVM, the criterion born in the designed. Since SVM is meant to be a binary classifier, the SVM classification algorithm must be redesigned. As shown in Algo 2.

On the other hands, neural network classifier has another criterion. First, train a neural network that classify the "konwn" and "unknown". Here "kown" means the types in train data, and "unkown" means the reverse. Then train the other neural network to classify the "konwn" data. The detail is in Algo 3.

After classifying, the konwn types and unkonwn types are separated. The data marked as unkonwn types will be thrown into clustering algorithm, e.g., DBSCAN, k-means. Subsequently, the process is completed.

### Algorithm 2 The SVM Multi-classification Algorithm

```
Require: Train Data, Labels, Test Data
Assumption: Length(Train Data) = Length(Labels) =
    N, Length(Test Data) = M
  1 for t in Known Types do
       for i in [1, N] do
  2
           if Labels[i] \neq t then
  3
  4
               Labels'[i] = +1
  5
  6
               Labels'[i] = -1
           end if
        end for
  8
       SVM[t].fit(Train Data, Labels')
11 for t in Known Types do
12
       for i in [1, M] do
           if SVM[t].predict() = +1 then
13
               Test Labels[i] = t
 14
 15
           else
               Test Labels[i] = UNKNOWN
 16
 17
           end if
 18
        end for
   end for
```

# 4 Experiment result

The experiment result of arrhythmia dataset is shown in Table 1. And the result of gene expression cancer RNA-Seq data set is in Table 2.

From the result, the fact that SVM performs worse than KNN can be seen. The main reason is because the mult-classification SVMs method designed here can't separate well in most of types. Fig 3 illurates the situation. For type 1 SVM, the negative/positive classification makes the data hard to separate, and also for type 2, 3, etc. This happens even when the kernel trick is applied, though the kernel trick sometimes ease the pain.

In the other hand, KNN performs extraordinarily. In arrhythmia dataset, KNN with k-means in raw data gets 53.1646% accuracy, which is the highest accuracy comparing to others methods. And in gene expression cancer RNA-Seq dataset, KNN with k-means in PCA data gets 94.8795%. And KNN with DBSCAN performs well too. This method shows similar performance in these two

# Algorithm 3 Neural Network Classification

**Require:** Train Data, Labels, Test Data **Assumption:** Length(Train Data) = Length(Labels) = N, Length(Test Data) = M1 Binary NN.train(Train Data, Labels)

2 Mutli-Classification NN.train(Train Data, Labels)

3 Just Knowns, Unkonwns = Binary NN.predict(Test Data)

4 Knowns = Mutli-Classification NN.predict(Just Knowns)

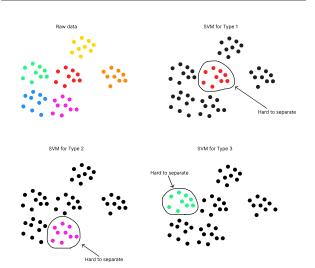


Figure 3: An example that mult-classification SVMs fail

datasets, which also gets 94.5783% in gene expression cancer RNA-Seq dataset PCA data.

# 5 Conclusion

In this study, we present a framework of algorithm to deal with the dataset containing out-of-knowledge data. And with in this algorithm, multiple major machine learning techniques are used, e.g., for preprocess, PCA, AE, normalization; for classification, KNN, SVM, SVDD, NN, as for clustering, DBSCAN, k-means, NN-chain. Among the various combinations, PCA + KNN + k-means performs outstanding in gene expression cancer RNA-Seq dataset, and raw data + KNN + k-means performs the best in arrhythmia dataset. Accidently, SVM performs

Table 1: COMPARISON OF CLASSIFICATION TECHNIQUES. (ARRHYTHMIA DATASET)

Method	Raw		Normalized		PCA-32		PCA-32 Normalized		AE-32		AE-32 Normalized	
	Search (s)	acc	Search (s)	acc	Search (s)	acc	Search (s)	acc	Search (s)	acc	Search (s)	acc
KNN-Brute-Force + DBSCAN	0.0285	$47.4684 \pm 0$	0.0254	$46.8354 \pm 0$	0.0070	$38.6076 \pm 0$	0.0071	$42.4051 \pm 0$	0.0071	$37.9747 \pm 0$	0.0071	$44.3038 \pm 0$
SVM (linear) + DBSCAN	1.7269	$25.9494 \pm 0$	8.9285	$35.4430 \pm 0$	0.2186	$32.2785 \pm 0$	0.8162	$29.7468 \pm 0$	0.2169	$31.6456 \pm 0$	0.1552	$27.8481 \pm 0$
SVM (polynomial) + DBSCAN	0.9993	$25.9494 \pm 0$	1.6100	$25.3165 \pm 0$	0.1997	$1.2658 \pm 0$	0.4577	$33.5443 \pm 0$	0.2402	$30.3797 \pm 0$	0.4924	$30.2785 \pm 0$
SVM (RBF) + DBSCAN	0.9915	$25.9494 \pm 0$	1.4681	$22.7848 \pm 0$	1.4328	$0.6329 \pm 0$	11.9417	$30.3797 \pm 0$	13.5147	$22.1519 \pm 0$	24.7346	$34.1772 \pm 0$
SVM (sigmoid) + DBSCAN	3.5272	$28.4810 \pm 0$	6.4731	$20.2532 \pm 0$	1.5779	$30.3797 \pm 0$	0.9797	$36.0759 \pm 0$	0.5284	$22.1519 \pm 0$	0.8430	$24.6835 \pm 0$
KNN-Brute-Force + kmeans	0.0236	$53.1646 \pm 0$	0.0343	$50.6329 \pm 0$	0.0068	$43.0380 \pm 0$	0.0069	$43.0380 \pm 0$	0.0069	$36.0759 \pm 0$	0.0080	$41.7722 \pm 0$
SVM (linear) + kmeans	1.7719	$25.3165 \pm 0$	37.9747	$37.9747 \pm 0$	0.2317	$25.3165 \pm 0$	0.8932	$27.8481 \pm 0$	0.2331	$24.0506 \pm 0$	0.1596	$20.2532 \pm 0$
SVM (polynomial) + kmeans	1.0456	$25.3165 \pm 0$	1.4942	$26.5823 \pm 0$	0.2326	$14.5570 \pm 0$	0.4094	$28.4810 \pm 0$	0.2033	$24.0506 \pm 0$	0.4884	$25.3165 \pm 0$
SVM (RBF) + kmeans	34.5382	$8.8608 \pm 0$	43.0936	$29.7468 \pm 0$	110.589	$0.6329 \pm 0$	112.945	$1.2658 \pm 0$	38.7497	$22.7848 \pm 0$	14.1561	$27.2152 \pm 0$
SVM (sigmoid) + kmeans	4.0277	$22.6582 \pm 0$	8.0918	$17.7848 \pm 0$	0.7529	$25.3165 \pm 0$	0.7967	$12.0253 \pm 0$	0.6921	$17.7215 \pm 0$	0.4013	$28.4810 \pm 0$

Table 2: Comparison of Classification Techniques. (Gene expression cancer RNA-Seq dataset)

Method	Raw		Normalized		PCA-30		PCA-30 Normalized		AE-30		AE-30 Normalized	
	Search (s)	acc	Search (s)	acc	Search (s)	acc	Search (s)	acc	Search (s)	acc	Search (s)	acc
KNN-Brute-Force + DBSCAN	14.5101	$59.0361 \pm 0$	10.3013	$66.5663 \pm 0$	0.0224	$94.5783 \pm 0$	0.0237	$78.3133 \pm 0$	0.0258	$64.4578 \pm 0$	0.0235	$59.3373 \pm 0$
SVM (linear) + DBSCAN	124.593	$61.7470 \pm 0$	610.6730	$9.9398 \pm 0$	0.6466	$9.9398 \pm 0$	0.1193	$10.5422 \pm 0$	0.1407	$63.2530 \pm 0$	0.1122	$13.5542 \pm 0$
SVM (polynomial) + DBSCAN	81.6495	$61.7470 \pm 0$	86.6406	$1.2048 \pm 0$	0.2585	$64.4578 \pm 0$	0.3012	$61.1446 \pm 0$	0.2013	$63.2530 \pm 0$	0.2056	$50.3012 \pm 0$
SVM (RBF) + DBSCAN	X	not converge	X	not converge	12.5077	$9.9398 \pm 0$	3.8838	$63.2530 \pm 0$	5.0461	$40.3614 \pm 0$	11.4194	$49.6988 \pm 0$
SVM (sigmoid) + DBSCAN	X	not converge	X	not converge	0.6372	$71.6867 \pm 0$	0.8222	$65.9639 \pm 0$	0.6236	$44.2771 \pm 0$	0.2273	$38.2530 \pm 0$
KNN-Brute-Force + kmeans	22.754	$\textbf{74.0964} \pm \textbf{0}$	6.36577	$53.6145 \pm 0$	0.0212	$94.8795 \pm 0$	0.0214	$84.9398 \pm 0$	0.0214	$42.1687 \pm 0$	0.0220	$65.9639 \pm 0$
SVM (linear) + kmeans	136.408	$61.7470 \pm 0$	664.2860	$9.9398 \pm 0$	0.5914	$9.9398 \pm 0$	0.1077	$10.5422 \pm 0$	0.1274	$63.2530 \pm 0$	0.1084	$13.2530 \pm 0$
SVM (polynomial) + kmeans	81.4276	$61.7470 \pm 0$	81.1669	$63.8554 \pm 0$	0.2003	$64.4578 \pm 0$	0.2167	$25.3012 \pm 0$	0.1780	$63.2530 \pm 0$	0.1930	$50.3012 \pm 0$
SVM (RBF) + kmeans	1772.32	$9.9398 \pm 0$	1800.6	$9.9398 \pm 0$	1.3625	$9.9398 \pm 0$	1.3848	$9.9398 \pm 0$	11.1729	$39.7590 \pm 0$	4.7882	$28.6145 \pm 0$
SVM (sigmoid) + kmeans	190.866	$26.5060 \pm 0$	81.7487	$63.8554 \pm 0$	0.8287	$65.9639 \pm 0$	0.4269	$65.9639 \pm 0$	0.9908	$28.9157 \pm 0$	0.2360	$39.4578 \pm 0$

bad in these two dataset. The main cause is the defect of the multi-classification SVMs design, which make some SVMs hard to separate the target types. However, by customize the kernel for each SVMs, the problem may ease. In the same time, the increasing number of parameters can be fine-tuned by metaheuristic algorithms, e.g., simulated annealing, genetic algorithm, etc. We will develope a refinement design on multi-classification SVMs, to enhance the accuracy on these datasets.

# 6 Contribution

- Hsieh Cheng-Han: KNN, SVM, DBSCAN, paper, ppt
- Hsu Ting-Hao:
- Sun Shih-Yu: SVM, k-means, paper
- Lu Che-Yuan:
- Huang Chia-Yen:

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