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Modelling Nonlinear optics with the Bloch-Messiah reduction

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Overview

Modelling Nonlinear optics with the Bloch-Messia

- What is nonlinear optics?
- Why do we care about it?
- What I have been doing
- Gaussian optics
- Outlook

Motivation quantum nonlinear optics

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The good

Spontaneous Parametric processes, SPDC, SFWM

- Heralded single photon sources
- Entangled photon pair generation (polarisation, spatial)

Kerr processes

- Self-Phase modulation (SPM), generating Bannana states (CV)
- Cross-Phase modulation (XPM) for sensing

The bad

Spontaneous parametric processes

- Generating more than two photons -> bad for quantum computing
- Understanding filtering
 All Kerr nonlinear processes
 - SPM -> Spectral broadening
 - XPM -> Unwanted phase shifts on single photons due to propagation of the pump

What do we mean by nonlinear optics?

Oliver Thomas, Dara McCutcheon, Will McCutcheon Roughly processes that conserve energy but do not conserve photon number.

$$\vec{P} = \chi^{(1)}\vec{E}_1 + \chi^{(2)}\vec{E}_1\vec{E}_2 + \chi^{(3)}\vec{E}_1\vec{E}_2\vec{E}_3 + \dots$$
 (1)

Here we are going to talk about squeezing, i.e SPDC or SFWM, Hamiltonians are then of the form,

$$\hat{H} = A\hat{a}_{S}^{\dagger}\hat{a}_{I}^{\dagger}\hat{a}_{P} + h.c. \tag{2}$$

$$\hat{H} = A\hat{a}_S^{\dagger}\hat{a}_I^{\dagger}\hat{a}_P\hat{a}_P + h.c. \tag{3}$$

Gaussian Optics

Thomas, Dara McCutcheon, Will McCutcheon Using the undelpeted pump approximation we can write the Hamiltonians as terms which are at most quadratic in creation and annihilation operators.

$$\hat{U} = \exp\left[-\frac{i}{\hbar} \left(P \int d\omega_1 \int d\omega_2 \ f(\omega_1, \omega_2) \ \hat{a}_s^{\dagger}(\omega_1) \hat{a}_i^{\dagger}(\omega_2) + h.c. \right) \right]$$
Power

JSA Signal & Idler

 These are Gaussian transforms, they take Gaussian states to Gaussian states ¹

$$\begin{bmatrix} \vec{b} \\ \vec{b}^{\dagger} \end{bmatrix} = \mathbf{M} \begin{bmatrix} \vec{a} \\ \vec{a}^{\dagger} \end{bmatrix} \tag{5}$$

¹These are linear symplectic transforms which conviently can be written as a matrix

Types of Gaussian transformations

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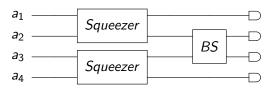


Figure: Two source HOM dip

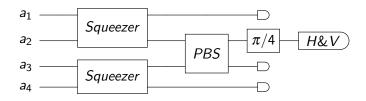


Figure: Type-1 Fusion gate

Reducing the size of the state-space

Oliver Thomas, Dara McCutcheon, Will We can re-write the Hamiltonian using a Schmidt-decomposition as,

$$P'F(\omega_1,\omega_2) = \sum_k r_k \psi_k(\omega_1) \phi_k(\omega_2)$$
 (6)

Where r_k is the Schmidt number, $\psi \& \phi$ are unitaries.

To solve this numerically we discretize the function and the Schmidt-decomposition is then the Singular value decomposition (SVD) of the JSA (F).

$$P'\mathbf{F}_{(\omega_1,\omega_2)} = \sum_{k} r_k \mathbf{U}_{(\omega_1,k)} \mathbf{V}_{(k,\omega_2)}^{\dagger}$$
 (7)

- ullet with $\psi_k(\omega_1)$ is the k-th row and ω_1 -th column of $oldsymbol{\mathsf{U}}_{(\omega_1,k)}$,
- with $\phi_k(\omega_2)$ is the ω_2 -th row and k-th column of $\mathbf{V}^{\dagger}_{(k,\underline{\omega}_2)}$

Joint Spectral Amplitudes (JSAs)

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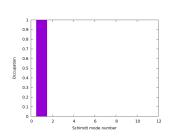


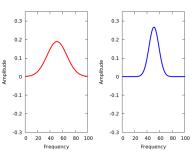
¹Moving to the rotating frame...

Seperable JSAs Schmidt modes

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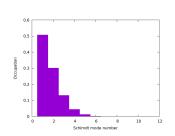
(a) Signal (red) and Idler (blue)

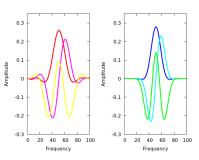
Non-separable JSAs

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Non-separable JSAs Schimdt modes

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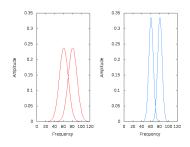


(a) Signal (red) and Idler (blue)

Two squeezers JSA

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Correlations in a HOM dip

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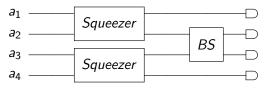


Figure: Two source HOM dip

G(4) correlation function

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$$G^{(4)} = \frac{\left\langle \hat{a}_{1}^{\dagger} \hat{a}_{2}^{\dagger} \hat{a}_{3}^{\dagger} \hat{a}_{4}^{\dagger} \hat{a}_{1} \hat{a}_{2} \hat{a}_{3} \hat{a}_{4} \right\rangle}{\left\langle \hat{a}_{1}^{\dagger} \hat{a}_{1} \right\rangle \left\langle \hat{a}_{2}^{\dagger} \hat{a}_{2} \right\rangle \left\langle \hat{a}_{3}^{\dagger} \hat{a}_{3} \right\rangle \left\langle \hat{a}_{4}^{\dagger} \hat{a}_{4} \right\rangle} \tag{8}$$

Where,

$$a_i = \sum_j a_i(\omega_j) \tag{9}$$

Meaning we sum over all of the spectral modes of the spatial modes (1,2,3,4) seperately. We end up with,

$$G^{(4)} = 1 - \left(\frac{2 \mid cosh(r) \mid^2}{\mid cosh(r) \mid^2 + \mid sinh(r) \mid^2} sin(\theta) cos(\theta)\right)^2$$
 (10)

G(4) correlation function

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Summary

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Outlook

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