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Modelling Nonlinear optics with the Bloch-Messiah reduction

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Overview

Modelling Nonlinear optics with the Bloch-Messia

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- What is nonlinear optics?
- Why do we care about it?
- What I have been doing
- Gaussian optics
- Outlook

Motivation quantum nonlinear optics

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The good

Spontaneous Parametric processes, SPDC, SFWM

- Heralded single photon sources
- Entangled photon pair generation (polarisation, spatial)

Kerr processes

- Self-Phase modulation (SPM), generating Bannana states (CV)
- Cross-Phase modulation (XPM) for sensing

The bad

 Generating more than two photons -> bad for quantum computing

All Kerr nonlinear processes

- SPM -> Spectral broadening
- XPM -> Unwanted phase shifts on single photons due to propagation of the pump

What do we mean by nonlinear optics?

Oliver Thomas, Dara McCutcheon, Will McCutcheon Roughly processes that conserve energy but do not conserve photon number.

$$\vec{P} = \chi^{(1)}\vec{E}_1 + \chi^{(2)}\vec{E}_1\vec{E}_2 + \chi^{(3)}\vec{E}_1\vec{E}_2\vec{E}_3 + \dots$$
 (1)

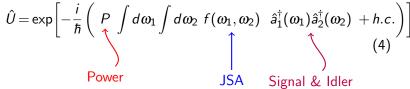
Here we are going to talk about squeezing, i.e SPDC or SFWM, Hamiltonians are then of the form,

$$\hat{H} = A\hat{a}_{S}^{\dagger}\hat{a}_{I}^{\dagger}\hat{a}_{P} + h.c. \tag{2}$$

$$\hat{H} = A\hat{a}_S^{\dagger} \hat{a}_I^{\dagger} \hat{a}_P \hat{a}_P + h.c. \tag{3}$$

Gaussian Optics

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- Using the undelpeted pump approximation we can write the Hamiltonians as terms which are at most quadratic in creation and annihilation operators.
- These are Gaussian transforms, they take Gaussian states to Gaussian states

$$\begin{bmatrix} \vec{b} \\ \vec{b}^{\dagger} \end{bmatrix} = M \begin{bmatrix} \vec{a} \\ \vec{a}^{\dagger} \end{bmatrix} \tag{5}$$

¹These are linear symplectic transforms which conviently can be written as a matrix

Hamilton<u>ian</u>

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Oliver Thomas, Dara McCutcheon, Will McCutcheon We can do re-write this Hamiltonian as a Schmidt-decomposition using SVD.

$$-\frac{i}{\hbar}Pf(\omega_1,\omega_2) = \sum_k r_k \psi_k(\omega_1)\phi_k(\omega_2)$$
 (6)

Where ψ & ϕ are unitary matrices,

- with $\psi_k(\omega_1)$ is the k-th row and ω_1 -th column of $u_{(\omega_1,k)}$,
- ullet with $\phi_k(\omega_2)$ is the ω_2 -th row and k-th column of $v_{(k,\omega_2)}^\dagger$

$$P'f(\omega_1,\omega_2) = \sum_k r_k u_{(\omega_1,k)} v_{(k,\omega_2)}^{\dagger}$$
 (7)

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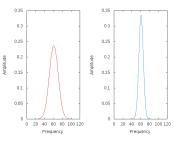
Recall SVD is defined as,

$$M = U\Sigma V^{\dagger} \tag{8}$$

The Joint Spectral Amplitude (JSA)

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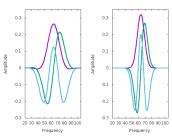


(a) Signal (red) and Idler (blue)

Non-separable JSAs

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(a) Signal (red) and Idler (blue)

Types of Gaussian transformations

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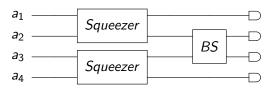


Figure: Two source HOM dip

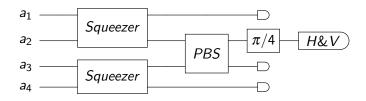
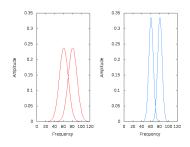


Figure: Type-1 Fusion gate

Two squeezers JSA

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G(4) correlation function

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$$G^{(4)} = \frac{\left\langle \hat{a}_{1}^{\dagger} \hat{a}_{2}^{\dagger} \hat{a}_{3}^{\dagger} \hat{a}_{4}^{\dagger} \hat{a}_{1} \hat{a}_{2} \hat{a}_{3} \hat{a}_{4} \right\rangle}{\left\langle \hat{a}_{1}^{\dagger} \hat{a}_{1} \right\rangle \left\langle \hat{a}_{2}^{\dagger} \hat{a}_{2} \right\rangle \left\langle \hat{a}_{3}^{\dagger} \hat{a}_{3} \right\rangle \left\langle \hat{a}_{4}^{\dagger} \hat{a}_{4} \right\rangle} \tag{9}$$

Outlook

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• There is much to do