#### Oliver Thomas

# Modelling Nonlinear optics with the Bloch-Messiah reduction

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## Overview

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- What is nonlinear optics?
- Why do we care about it?
- What I have been doing
- Gaussian optics
- Outlook

## Motivation

### The good

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Spontaneous Parametric processes, SPDC, SFWM

- Heralded single photon sources
- Entangled photon pair generation (polarisation, spatial)

### Kerr processes

- Self-Phase modulation (SPM) for generating Bannana states (CV)
- Cross-Phase modulation (XPM) for sensing

#### The bad

 Generating more than two photons -> bad for quantum computing

All Kerr nonlinear processes

- SPM -> Spectral broadening
- XPM -> Unwanted phase shifts on single photons due to propagation of the pump



## What do we mean by nonlinear optics?

 Roughly processes that conserve energy but do not conserve photon number.

$$\vec{P} = \chi^{(1)}\vec{E}_1 + \chi^{(2)}\vec{E}_1\vec{E}_2 + \chi^{(3)}\vec{E}_1\vec{E}_2\vec{E}_3 + \dots$$
 (1)

Here we are going to talk about squeezing, i.e SPDC or SFWM, Hamiltonians are then of the form,

$$\hat{H} = P \hat{a}_S^{\dagger} \hat{a}_I^{\dagger} \hat{a}_P + h.c. \tag{2}$$

$$\hat{H} = P\hat{a}_S^{\dagger}\hat{a}_I^{\dagger}\hat{a}_P\hat{a}_P + h.c. \tag{3}$$

**Note** for the rest of this presentation I will drop the hat notatiaion and using the convention a, b are annihilation operators in modes a & b





## Hamiltonian

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$$\hat{U} = \exp\left[-\frac{i}{\hbar}\left(P\int d\omega_1 \int d\omega_2 f(\omega_1, \omega_2)\hat{a}_1^{\dagger}(\omega_1)\hat{a}_2^{\dagger}(\omega_2) + h.c.\right)\right] \tag{4}$$

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We can do re-write this Hamiltonian as a Schmidt-decomposition using SVD.

$$-\frac{i}{\hbar}Pf(\omega_1,\omega_2) = \sum_k r_k \psi_k(\omega_1)\phi_k(\omega_2)$$
 (5)

Where  $\psi$  &  $\phi$  are unitary matrices,

- ullet with  $\psi_k(\omega_1)$  is the k-th row and  $\omega_1$ -th column of  $u_{(\omega_1,k)}$ ,
- ullet with  $\phi_k(\omega_2)$  is the  $\omega_2$ -th row and k-th column of  $v_{(k,\omega_2)}^\dagger$

$$P'f(\omega_1,\omega_2) = \sum_k r_k u_{(\omega_1,k)} v_{(k,\omega_2)}^{\dagger}$$
 (6)

Recall SVD is defined as,

$$M = U \Sigma V^{\dagger} \tag{7}$$

## Gaussian Optics

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- Using the undelpeted pump approximation we can write the Hamiltonians as terms which are at most quadratic in creation and annihilation operators.
- These are Gaussian transforms, they take Gaussian states to Gaussian states

$$\begin{bmatrix} \vec{b} \\ \vec{b}^{\dagger} \end{bmatrix} = M \begin{bmatrix} \vec{a} \\ \vec{a}^{\dagger} \end{bmatrix} \tag{8}$$

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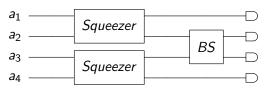


Figure: Two source HOM dip

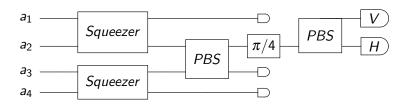


Figure: Type-1 Fusion gate



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