

# Collinear and Non-Collinear Second Harmonic Generation in BBO Crystal.

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# Non-linear optics

- Low intensities of electric field

$$P(t) = \varepsilon_0 \chi^{lin} E(t)$$

- Very high intensity of light

$$P(t) = P\{E(t)\}$$

Several non-linear effects appears

Second harmonic generation	(SHG)
Third harmonic generation	(THG)
High harmonic generation	(HHG)
Sum frequency generation	(SFG)
Optical parametric generation	(OPG)

...

# Goal of the project

- To use nonlinear processes for frequency conversion of the broadband fs pulses
- Find the best configuration for broadband SHG
- Determine spectral limits for common non-linear crystals
- Both theoretical and experimental approach

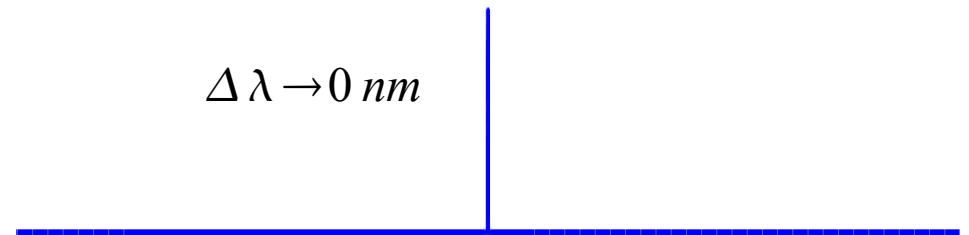
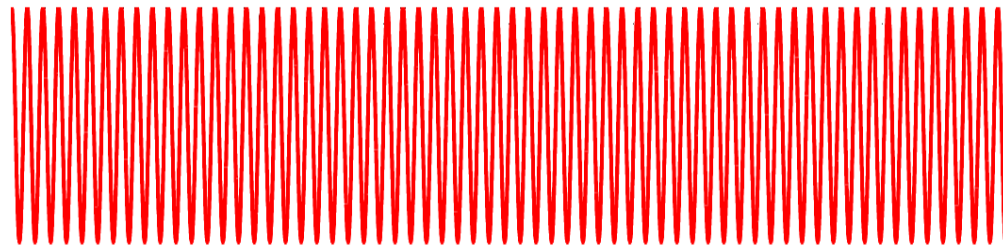
# Properties of ultra-short laser pulses

Electromagnetic wave

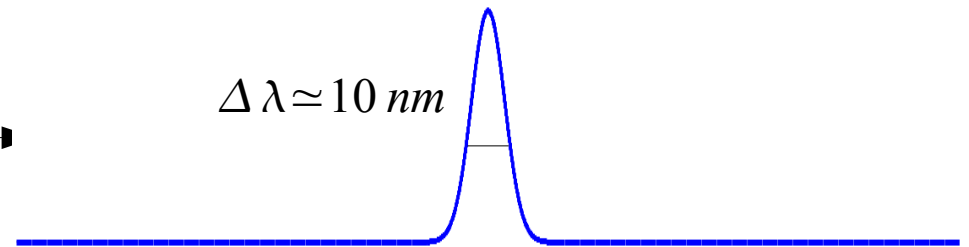
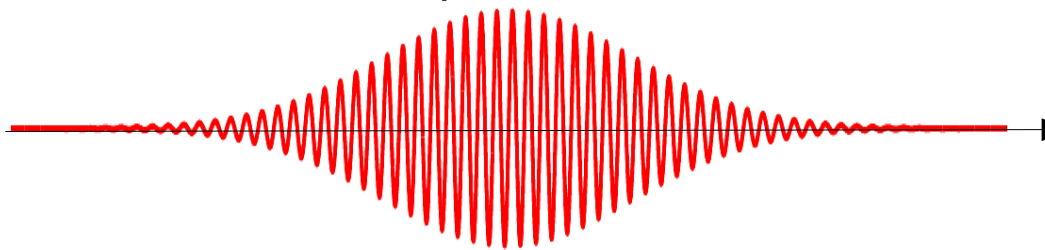
continuous wave

$$\Delta \omega \Delta \tau = 2 \pi k$$

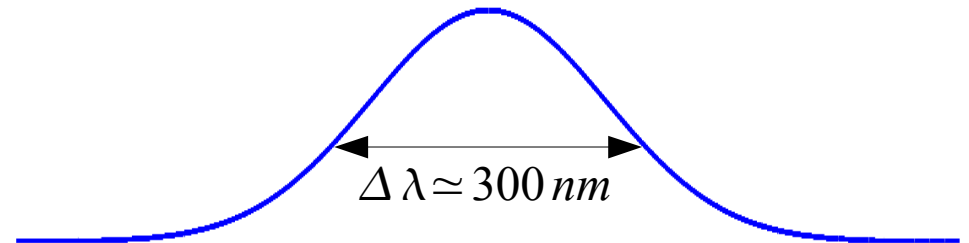
Spectra



150 fs pulse



5 fs pulse



# Second harmonic generation

- Conservation of energy holds automatically

$$\omega_1 + \omega_1 = \omega_2$$

- Conservation of momentum implies a necessary condition:

$$\vec{k}_1 + \vec{k}_1 = \vec{k}_2$$

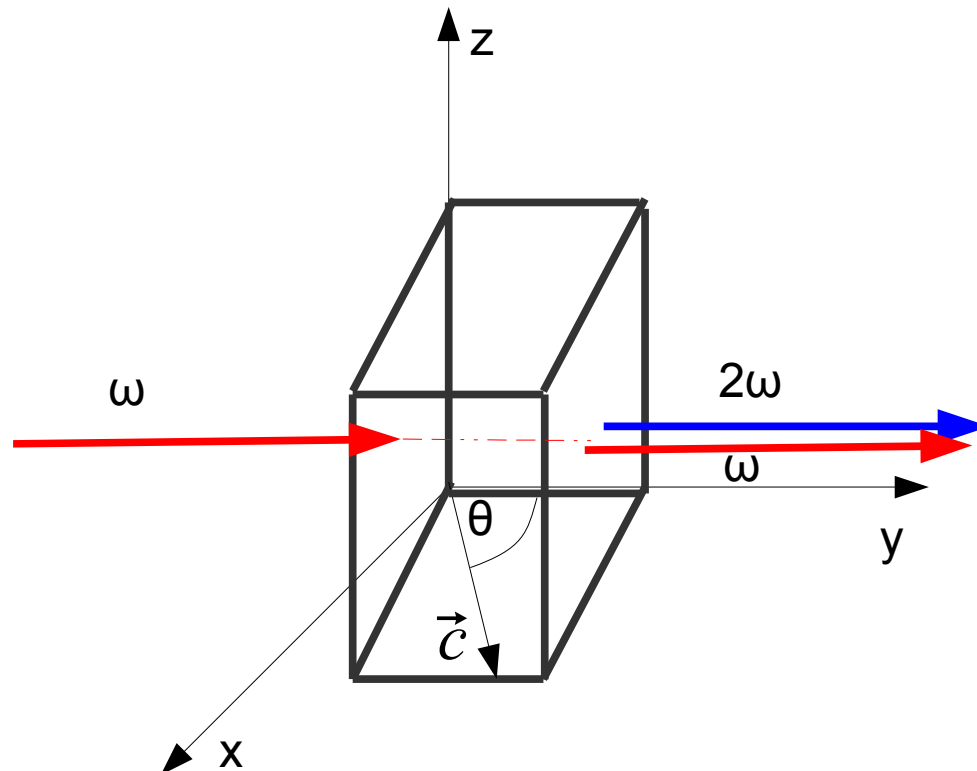
Phase velocities of fundamental beam and second harmonic have to be synchronized

$$\begin{aligned}\vec{v}_f(\omega_1) &= \vec{v}_f(\omega_2) \\ n(\omega_1) &= n(\omega_2)\end{aligned}$$

Possible only in the birefringent crystals

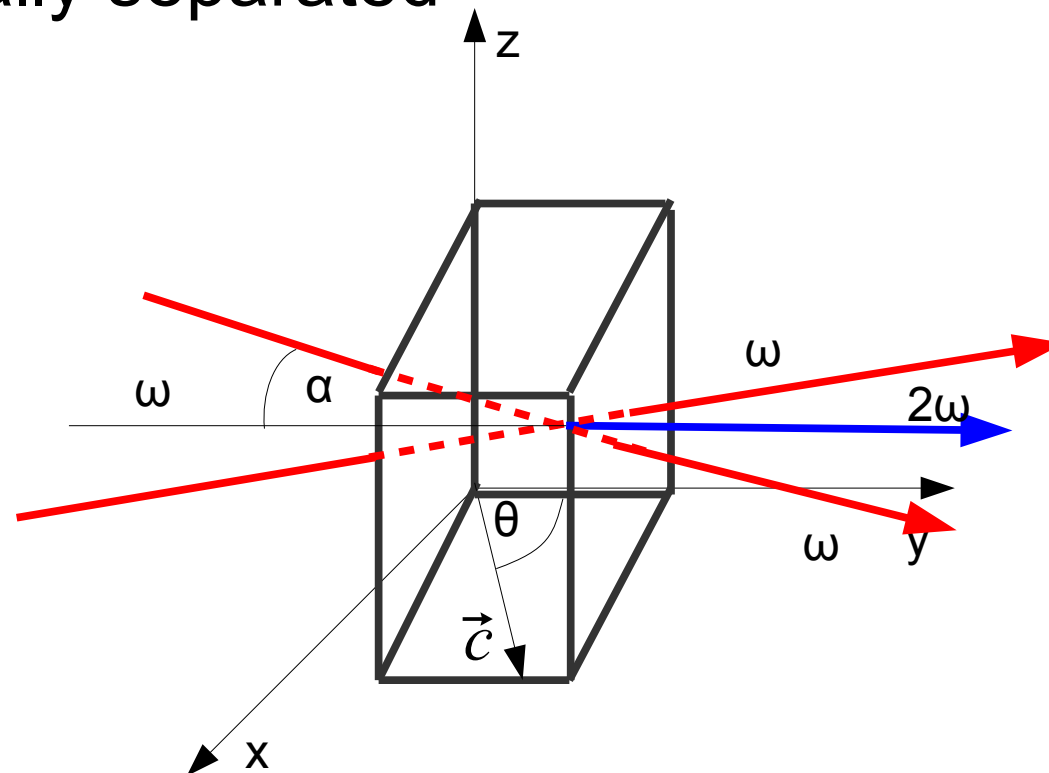
# Collinear second harmonic generation (SHG)

- The only one incoming fundamental beam
- Simple geometry
- The rest of fundamental beam has to be filtered



# Non-collinear second harmonic generation

- We can choose non-collinear angle  $\alpha$  in order to optimize SHG
- The fundamental beam and the second harmonic are automatically separated





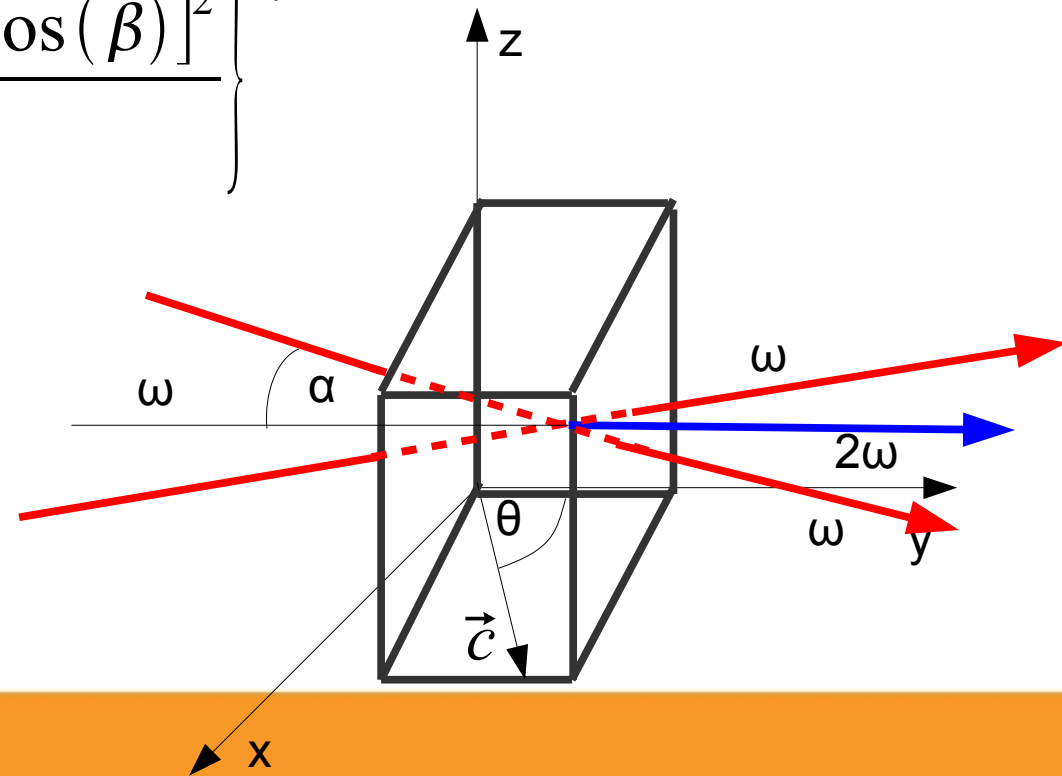
# Theoretical approach

$$I_{2\omega}(l) = \frac{32\pi^3\omega^2}{c^3 n^2(\omega)n(2\omega)} \left| \hat{e}(2\omega) \chi^{(2)}(2\omega) : \hat{e}_\omega \hat{e}_\omega \right| l^2 \left[ \frac{\sin(\Delta k l/2)}{\Delta k l/2} \right]^2 I_\omega^2(0)$$

$$\sin(\theta_{pm}) = \frac{n_e(\lambda_c)}{\eta_o(\lambda_b)\cos(\alpha) + \eta_o(\lambda_a)\cos(\beta)}$$

$$\times \left\{ \frac{\eta_o^2(\lambda_c) - [\eta_o(\lambda_b)\cos(\alpha) + \eta_o(\lambda_a)\cos(\beta)]^2}{n_o^2(\lambda_c) - n_e^2(\lambda_c)} \right\}^{1/2}$$

$$\beta = \arcsin \left[ \frac{\eta_o(\lambda_b)}{\eta_o(\lambda_a)\sin(\alpha)} \right]$$



# Results – collinear mode

$\lambda = 786 \text{ nm}$ :

- BBO

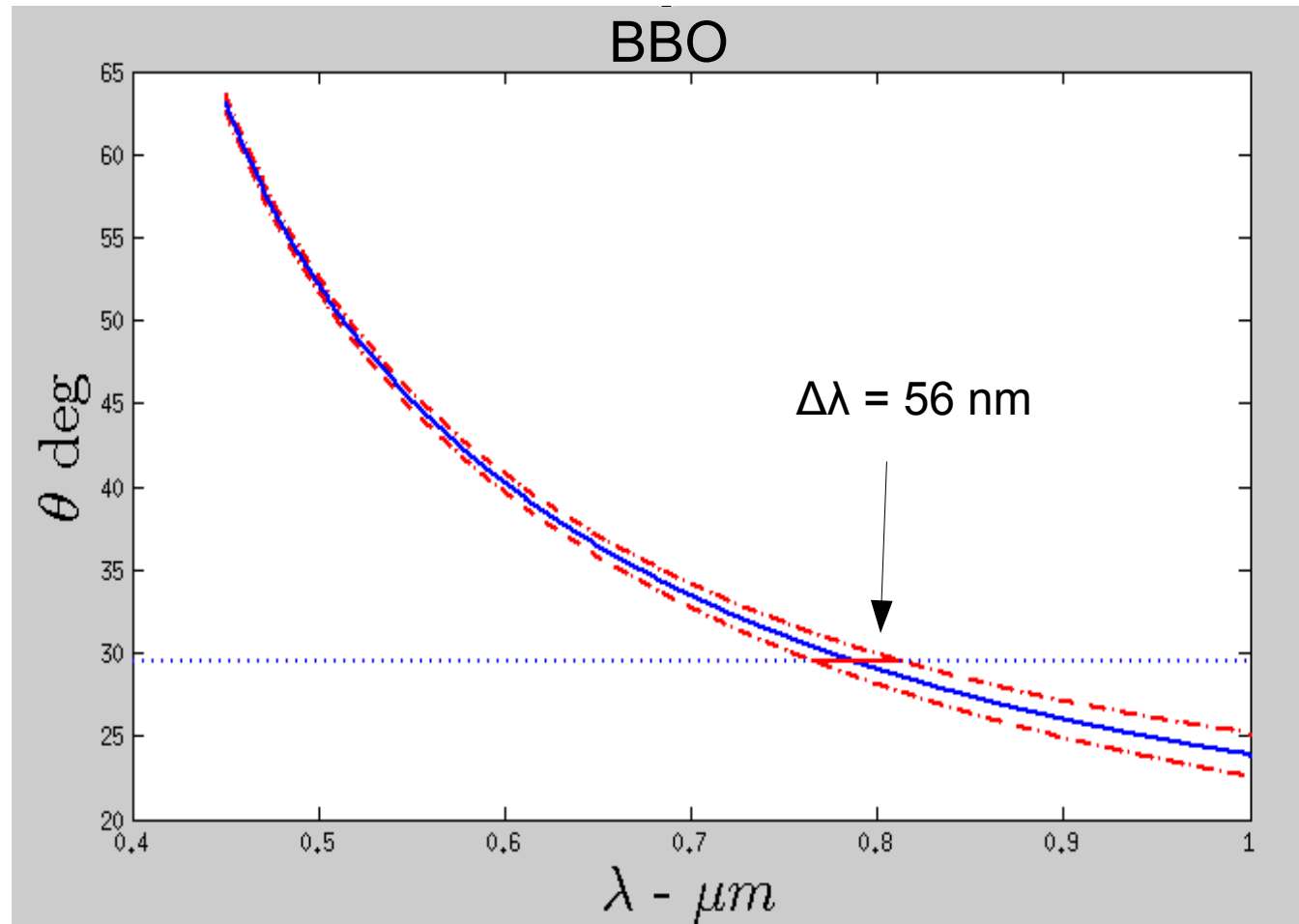
$\Delta\lambda = 56 \text{ nm}$

$\Delta t \approx 40 \text{ fs}$

- KDP

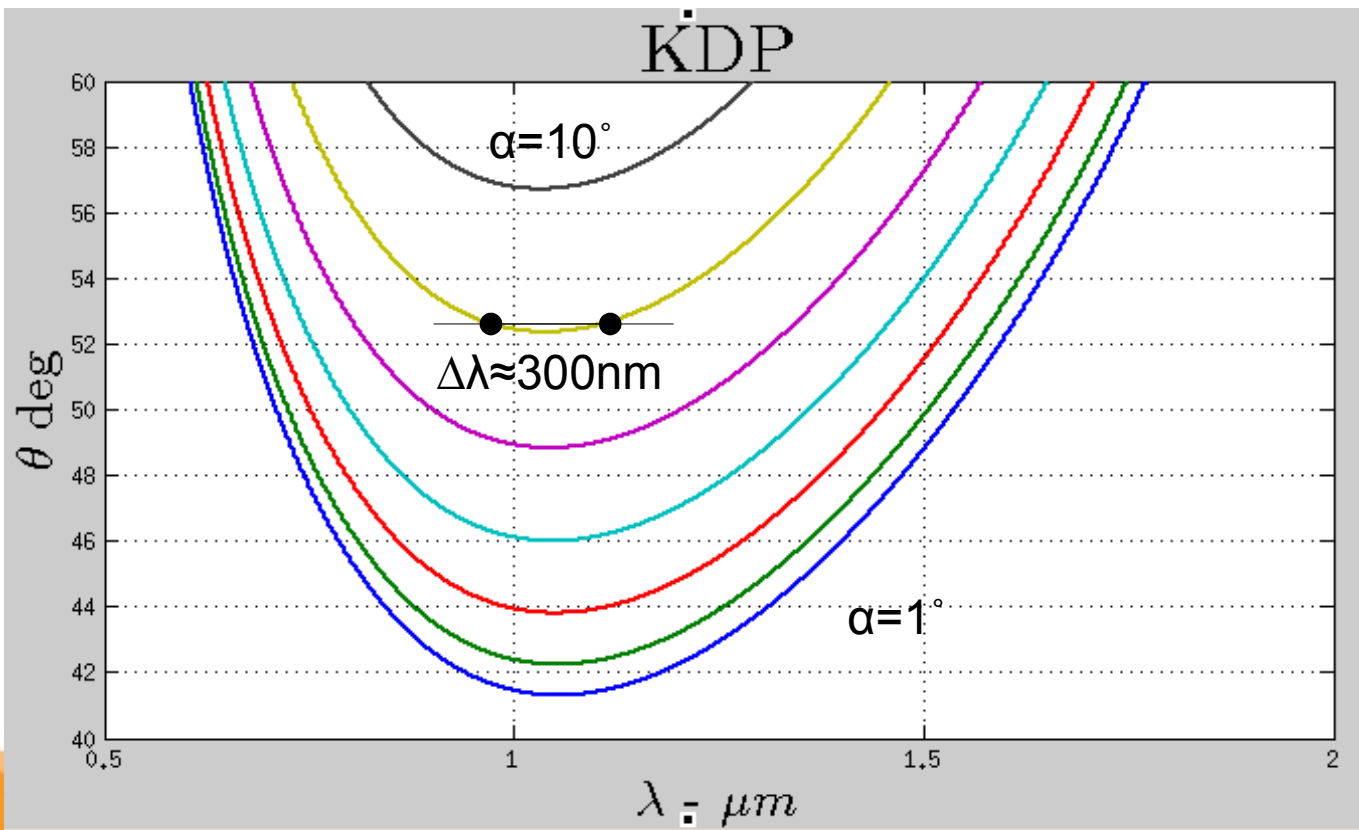
$\Delta\lambda = 120 \text{ nm}$

$\Delta t \approx 20 \text{ fs}$



# Results – non-collinear mode

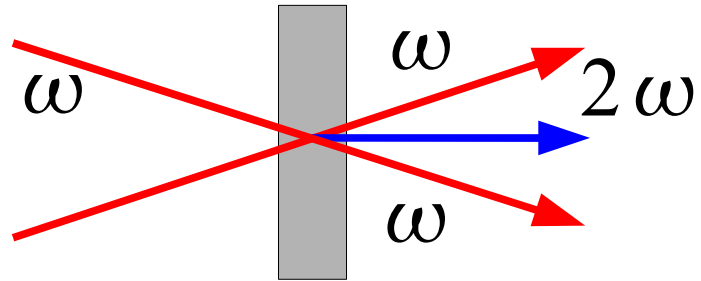
- Both BBO and KDP are suitable for broadband SHG in the near IR region
- Wavelength ideal for broadband SHG slowly varies with  $\alpha$ .



KDP  
 $\lambda_b \approx 1100\text{nm}$   
BBO  
 $\lambda_b \approx 1500\text{nm}$   
LBO  
 $\lambda_b \approx 1400\text{nm}$

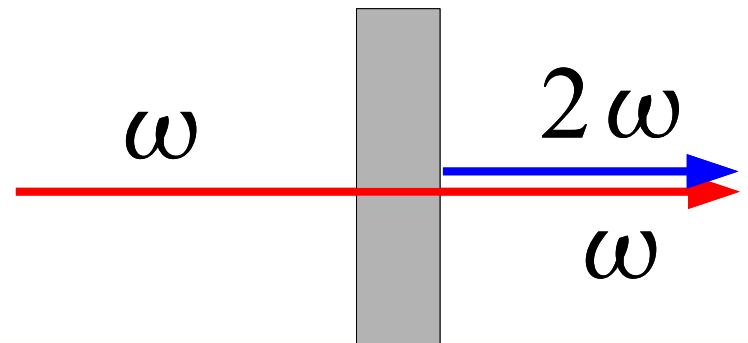
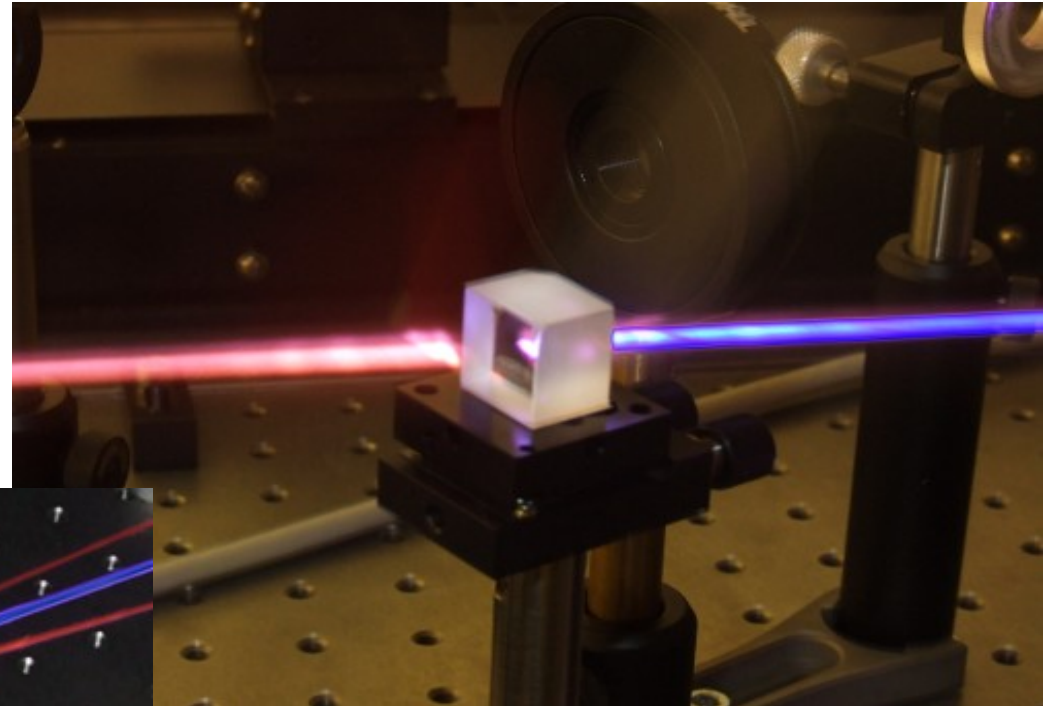
# Experimental results

$$\lambda = 786\text{nm}$$



Non-collinear generation

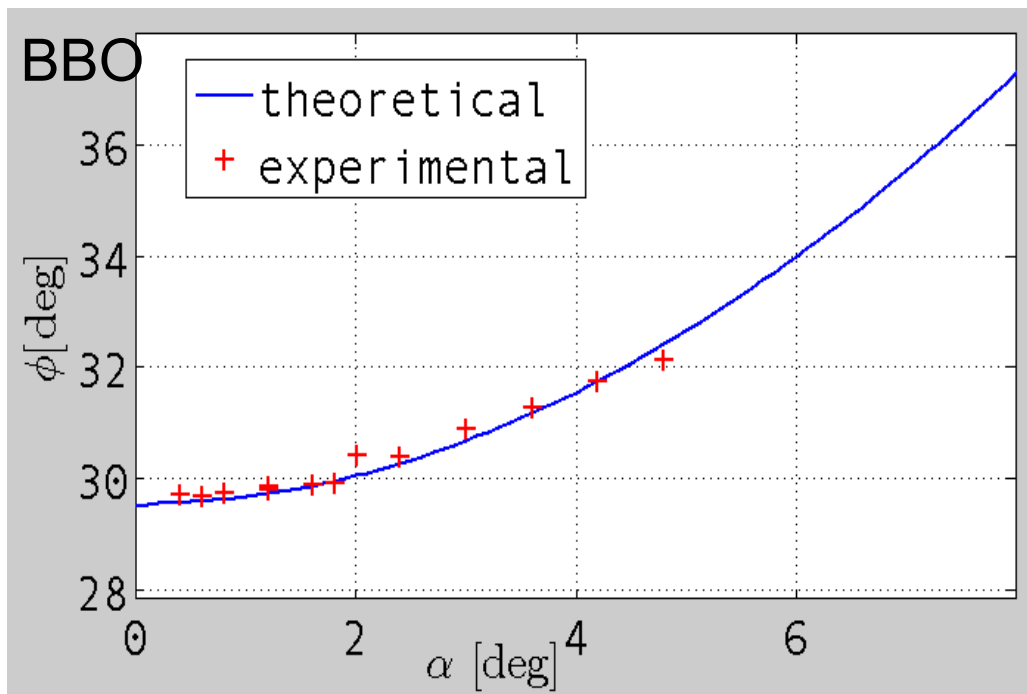
Collinear generation



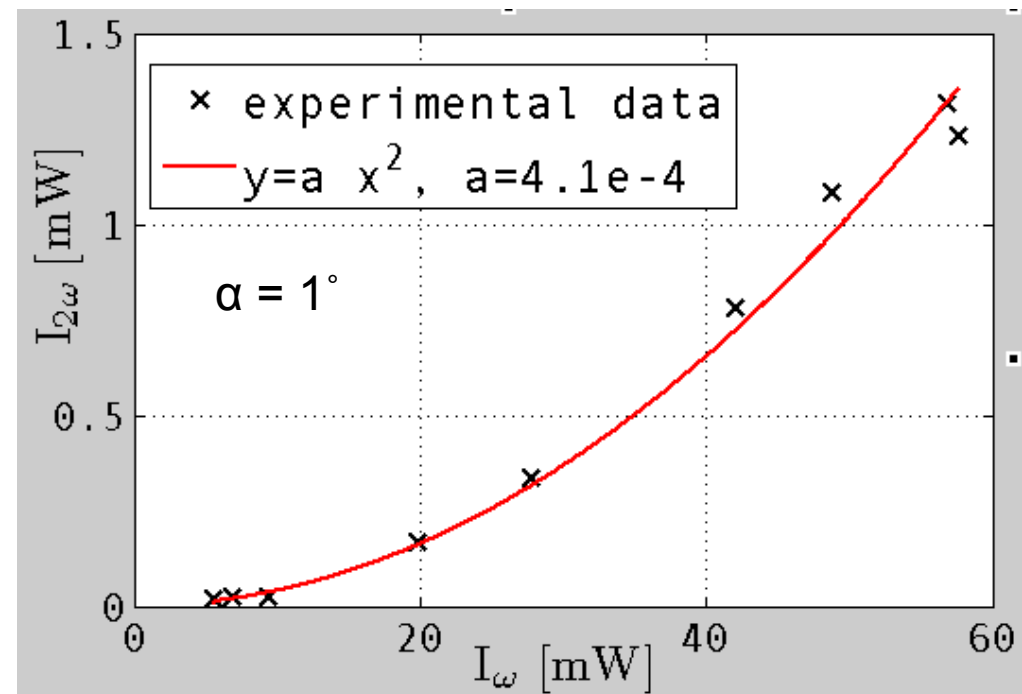
$$\eta_{max} = 0.2$$

# Non-collinear phase matching

Comparison of the theoretically calculated phase matching angle with the measured data



Power of the second harmonic depending on the power of the fundamental beam



# SHG of ultra-short visible pulses

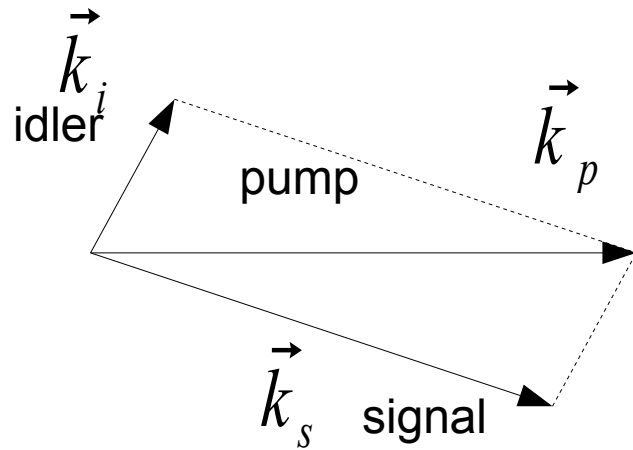
- BBO, LBO, KDP do not offer broadband SHG with a visible light.
- Possibilities:
  - try different nonlinear crystals
  - try different polarization of interacting beams
  - try different nonlinear process:

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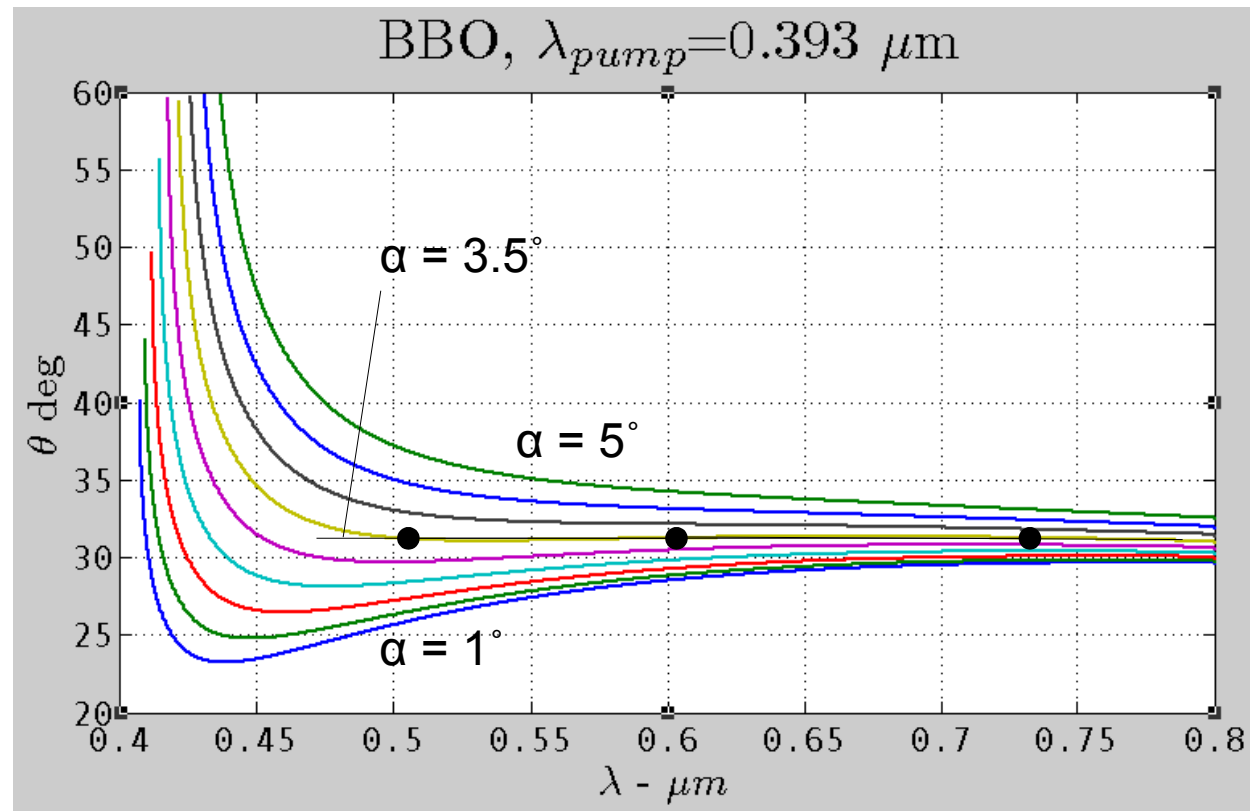
Other type of frequency conversion:  
Parametric processes

# Optical parametric generation



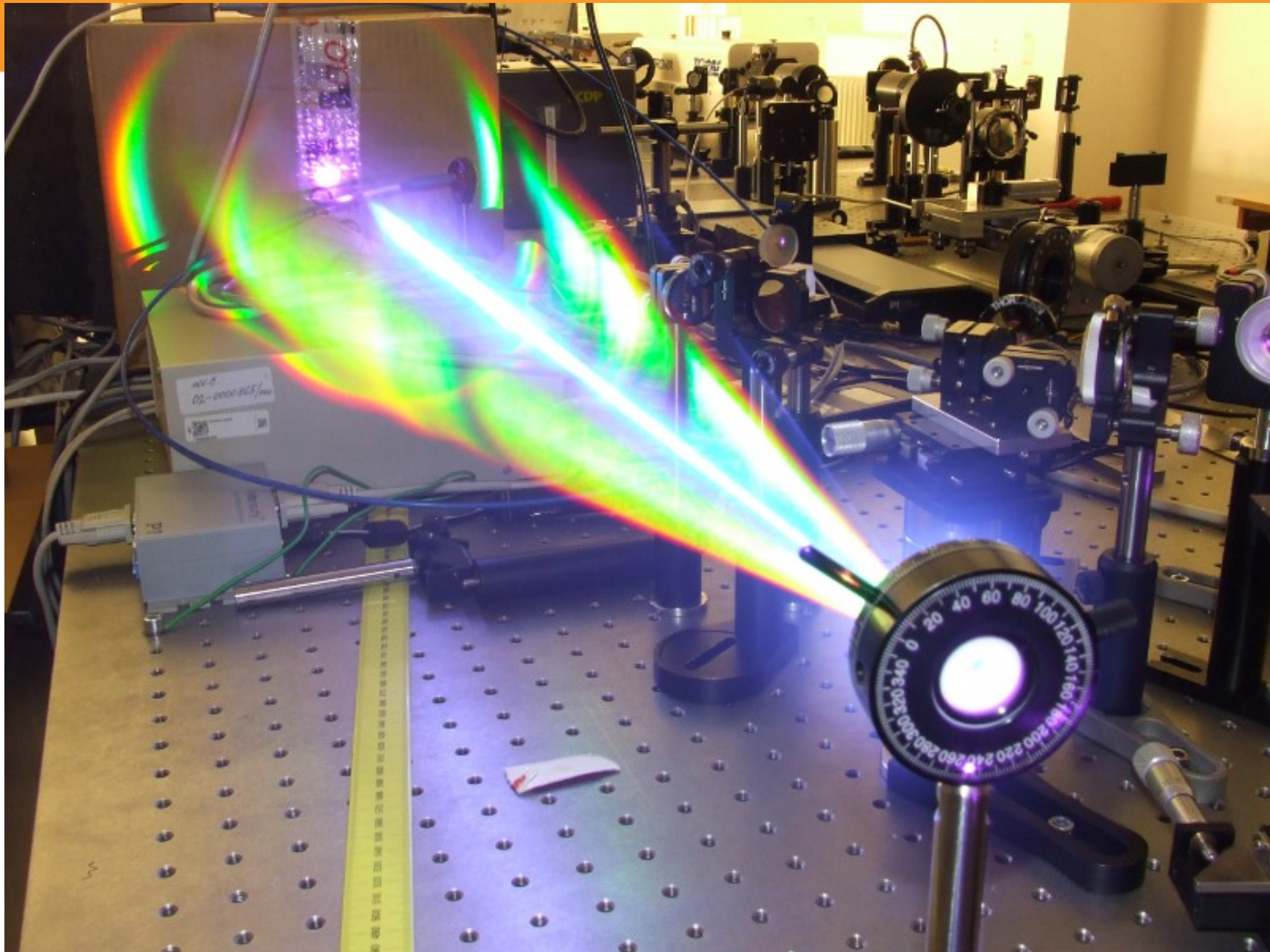
$$\vec{k}_p = \vec{k}_i + \vec{k}_s$$
$$\omega_p = \omega_i + \omega_s$$

BBO,  $\lambda_p = 393\text{nm}$ :  
Phase matching for  $\alpha = 3.5^\circ$ :  
 $\Delta\lambda \approx 300\text{nm}$ ,  $\Delta t \approx 4\text{fs}$ .



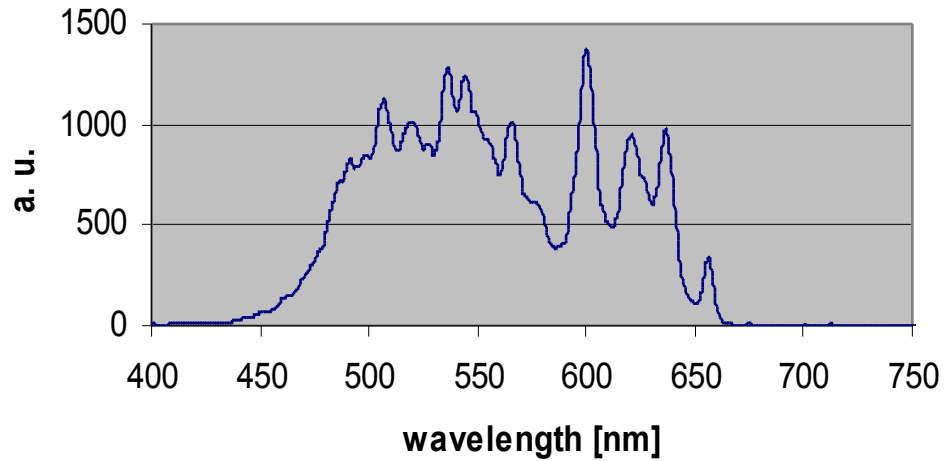


# Parametric scattering

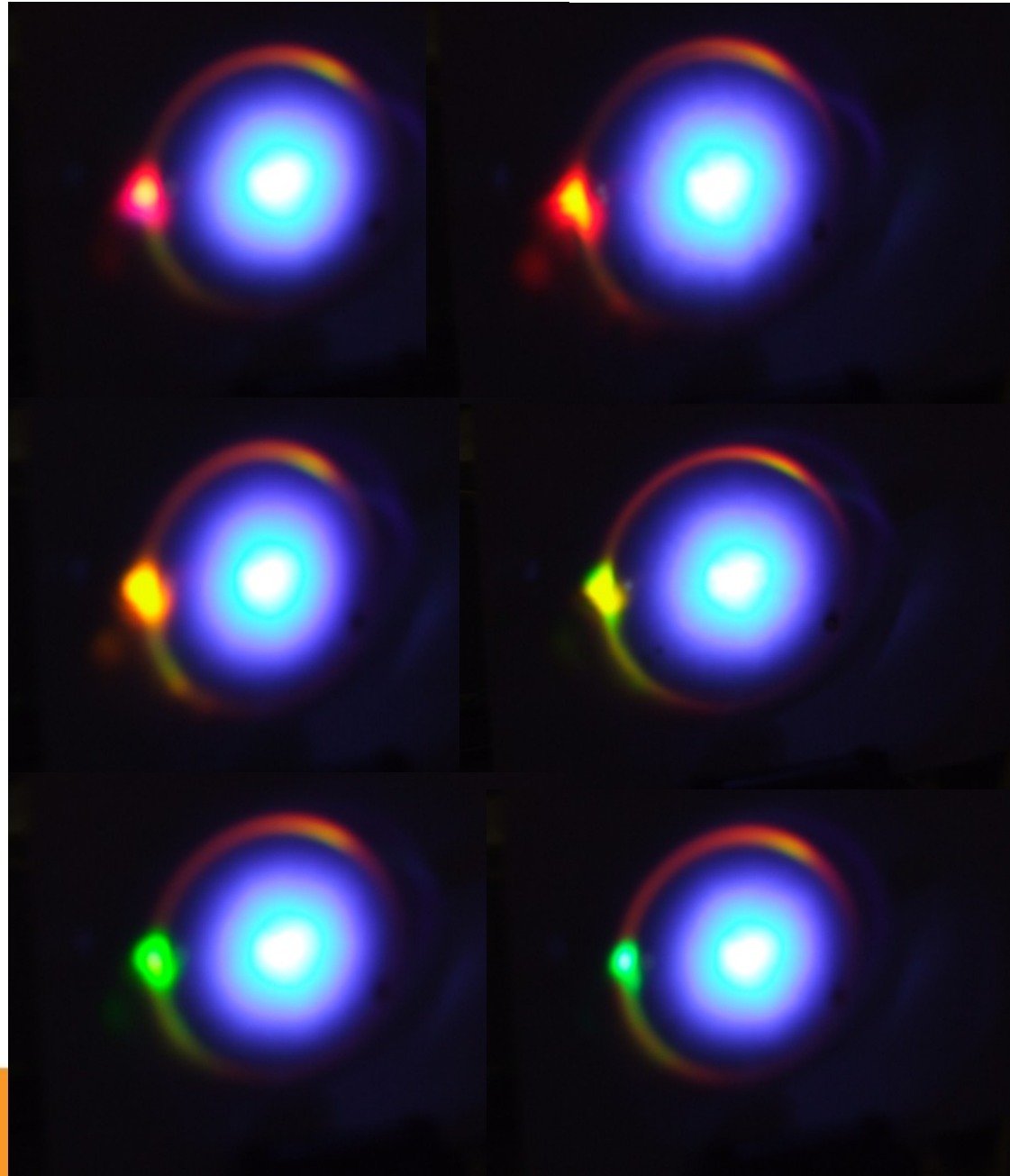
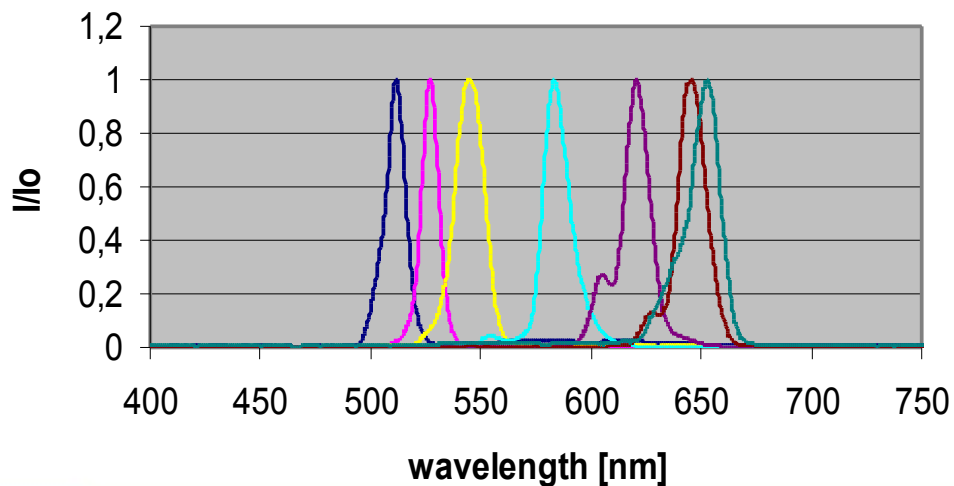


# The hottest news from the lab

Supercontinuum in glass



OPA



# Conclusion

- We have determined the maximum bandwidth for the collinear and non-collinear SHG in the most common nonlinear crystals (BBO, LBO, KDP)
- Calculated phase matching angles of crystals are in a very good agreement with the experiment
- We are able to convert bandwidth of 150 nm via parametric amplification

# Acknowledgements

Petr Hříbek

Thank you for your attention



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