

# UNIT 4

## CHAPTER 2

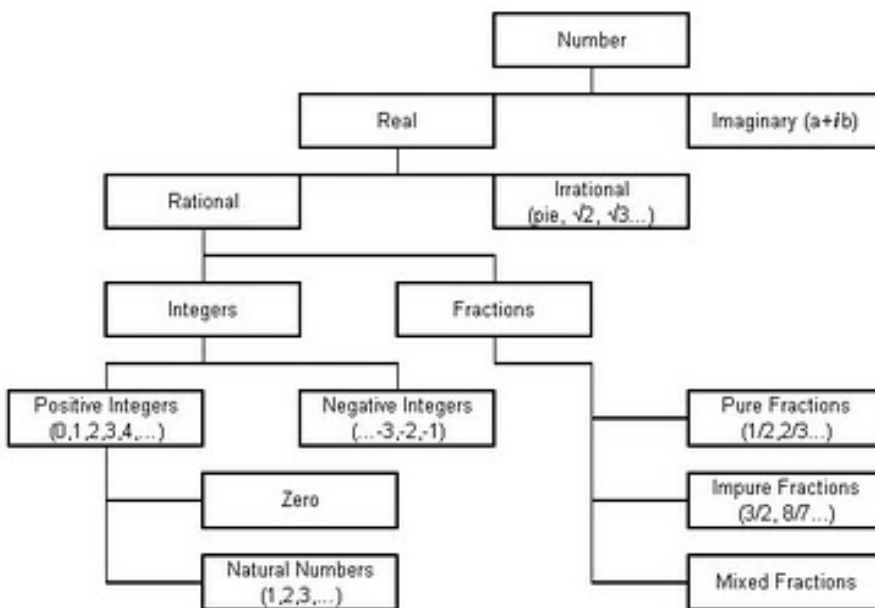
### NUMBER SYSTEM

### BASIC CONCEPT BUILDER

**Classification of the numbers:**

The concept of numbers is made clear from the number tree. The basics of number tree is given below.

- Number Tree –**



**Essential definitions are given below**

**Real Number:** - The real numbers include all of the measuring numbers. All the numbers on a number line starting from  $-\infty$  to  $+\infty$  are real numbers.

**Imaginary Number:** - Number with square root of negative number is called imaginary number. These numbers are in the form of  $a + ib$ .

**Rational Number:** - A rational number is a number that can be expressed as a fraction  $(p/q)$  with an integer numerator and a non-zero natural number denominator. A number repeated after a decimal is a recurring number. *All recurring numbers are rational numbers.*

**Conversion of Recurring number to p/q form -**

Find the number  $1.45454545\dots$  in the form of  $p/q$ .

Let  $x = 1.454545\dots$

$$\begin{aligned}
 100x &= 145.454545\dots \\
 100x - x &= 145.454545\dots - 1.454545\dots \\
 99x &= 144 \\
 X &= 145/99
 \end{aligned}$$

**Irrational Number:** - In mathematics, an **irrational number** is any real number which cannot be expressed as a fraction  $m/n$ , where  $m$  and  $n$  are integers, with  $n$  non-zero and is therefore not a rational number.

**Integers:** - The **integers** are formed by the natural numbers including 0 (0, 1, 2, 3, ...) together with the negatives of the non-zero natural numbers (-1, -2, -3, ...). Viewed as subset of the real numbers, they are numbers that can be written without a fractional or decimal component, and fall within the set  $\{\dots -2, -1, 0, 1, 2 \dots\}$ .

**Fractions:** - A **fraction** is a number that can represent part of a whole.

**Proper Fraction:** Value of the fraction is less than 1. These are in the form of  $\frac{1}{2}$ ,  $\frac{2}{3}$ ,  $\frac{3}{4}$  ..

**Improper Fraction:** - Value of the fraction is greater than 1. These are in the form of  $\frac{3}{2}$ ,  $\frac{4}{3}$  ...

**Mixed Fraction:** - When an integer is given before proper fraction then number is called mixed fraction. Numbers of the form  $2\frac{3}{4}$ .

**Whole Number:** All non negative numbers including Zero.  $W \sim (0, 1, 2, 3, 4, \dots)$

**Natural Numbers:** - All the number starting from 1.  $N \sim (1, 2, 3, 4, \dots)$

Natural Numbers = Whole Number - Zero

**Prime and Composite Numbers** - A number which has two factors 1 and itself is a prime number. 2 is the only even prime number and that prime numbers greater than 3 are of the form  $6k \pm 1$ , or  $4k \pm 1$  where  $k$  is a natural number.. Here the converse is not true.i.e. all those numbers in the above mentioned form are not necessarily the prime number.

**Co-Prime Numbers (Relatively Prime Numbers):-**

Pair of numbers that do not have any common factor except 1 are known as Co-prime numbers.

Remember:-

1. One is co-prime with any other number. (1,2) , (1,3) ...
2. Two Consecutive numbers are always co-prime.
3. A prime number is co-prime with all numbers except its multiple.
4. Two prime numbers are always co-prime.