



Data Structures [R1UC308B]

Module-VII: Queue

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Introduction to Queue

- ▶ A Queue is a fundamental concept in computer science used for storing and managing data in a specific order.
- ▶ It follows the principle of "First in, First out" (FIFO), where the first element added to the queue is the first one to be removed.
- ▶ Queues are commonly used in various algorithms and applications for their simplicity and efficiency in managing data flow.



Figure: Structure of Queue



Operations on Queue

- ▶ Create - Creating the queue with initial values.
- ▶ Add - enqueue() – Insertion of elements at rear to the queue.
- ▶ Delete - dequeue() – Removal of elements at front from the queue.
- ▶ Full - isFull() – Validates if the queue is full.
- ▶ Empty - isEmpty() – Checks if the queue is empty.
- ▶ peek() or front()- Acquires the data element available at the front node of the queue without deleting it.
- ▶ rear() – This operation returns the element at the rear end without removing it.
- ▶ size(): This operation returns the size of the queue i.e. the total number of elements it contains at present.



Implementation of queues

- ▶ Array
- ▶ Linked List



Array implementation of queues



//Queue using Array

```
class Queue {  
    int queue[];  
    int front, rear, capacity;  
  
    Queue(int size) {  
        front = rear = -1;  
        capacity = size;  
        queue = new int[capacity];  
    }  
  
    // insert an element into the queue  
    void enqueue(int item) {  
        // check if the queue is full  
        if (capacity-1 == rear) {  
            System.out.println("Queue is full");  
        }  
    }  
}
```




```
        return;
    }
    // insert element at the rear
    else {
        queue[++rear] = item;
        if(front==-1) front=0;
    }
    return;
}
```

```
//remove an element from the queue
int dequeue() {
    // check if queue is empty
    if (front==-1 || rear<front) {
        System.out.println("Queue is empty");
        return Integer.MIN_VALUE;
    }
}
```



```
else {  
    int temp=queue[front++];  
    System.out.printf("Item "+temp+" is deQueued\n");  
    return temp;  
}
```

```
}
```

```
    public boolean isEmpty() {  
return (front== -1 || rear < front);  
}
```

```
    public boolean isFull() {  
return (rear == capacity - 1);  
}
```

```
// print queue elements
```



```
void queueDisplay()
{
    int i;
    if (front == -1 || rear < front) {
        System.out.println("Queue is Empty");
        return;
    }

    // traverse front to rear and print elements
    System.out.printf("Elements of the Queue are: ");
    for (i = front; i < rear; i++) {
        System.out.printf("%d , ", queue[i]);
    }
    System.out.printf(" %d\n", queue[i]);
    return;
}
```



```
// print front of queue
void queueFront()
{
    if (front == -1) {
        System.out.println("Queue is Empty");
        return;
    }
    System.out.printf("Front Element of the queue: %d\n", front);
    return;
}

void queueRear()
{
    if (front == -1) {
        System.out.println("Queue is Empty");
        return;
    }
    System.out.printf("Rear Element of the queue: %d\n", rear);
    return;
}
```



```
        return;
    }
    int queueSize()
    {
        int size=0;
        if (front == -1 || rear<front) return size;
        if(front<=rear)
            size=rear-front+1;
        return size;
    }
}
```

```
public class QueueArray {
    public static void main(String[] args) {
        // Create a queue of capacity 4
        Queue q = new Queue(4);
```



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```
System.out.println("Initial Queue(capacity=4):");  
// print Queue elements  
System.out.println("Display():");  
q.queueDisplay();  
System.out.printf("Size():%d\n",q.queueSize());  
  
// inserting elements in the queue  
System.out.println("enqueue(10):");  
q.enqueue(10);  
q.queueDisplay();  
System.out.printf("Size():%d\n",q.queueSize());  
  
System.out.println("enqueue(30):");  
q.enqueue(30);  
q.queueDisplay();  
System.out.printf("Size():%d\n",q.queueSize());
```



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```
System.out.println("enqueue(50):");  
q.enqueue(50);  
q.queueDisplay();  
System.out.printf("Size():%d\n",q.queueSize());  
  
System.out.println("enqueue(70):");  
q.enqueue(70);  
q.queueDisplay();  
System.out.printf("Size():%d\n",q.queueSize());  
  
// insert element in the queue  
System.out.println("enqueue(90):");  
q.enqueue(90);  
q.queueDisplay();  
System.out.printf("Size():%d\n",q.queueSize());  
  
System.out.println("deQueue():");
```



```
q.deQueue();  
q.queueDisplay();  
System.out.printf("Size():%d\n",q.queueSize());  
  
System.out.println("deQueue():");  
q.deQueue();  
q.queueDisplay();  
System.out.printf("Size():%d\n",q.queueSize());  
  
System.out.println("enqueue(100):");  
q.enqueue(100);  
q.queueDisplay();  
System.out.printf("Size():%d\n",q.queueSize());  
  
System.out.println("enqueue(110):");  
q.enqueue(110);  
q.queueDisplay();
```




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```
System.out.printf("Size():%d\n",q.queueSize());

System.out.println("enqueue(120):");
q.enqueue(120);
q.queueDisplay();
System.out.printf("Size():%d\n",q.queueSize());

System.out.println("Front():");
q.queueFront();
System.out.println("Rear():");
q.queueRear();
}
}
```



Linked implementation of queues



//Queue using Linked List

```
class QueueLL {  
private Node front, rear;  
private int queueSize; // queue size
```

```
//linked list node  
private class Node {  
int data;  
Node next;  
}
```

```
//default constructor - initially front & rear are null; s  
public QueueLL() {  
front = null;  
rear = null;  
queueSize = 0;
```



```
}  
//check if the queue is empty  
public boolean isEmpty() {  
    return (queueSize == 0);  
}  
  
//Remove item from the front of the queue.  
public int dequeue() {  
    if (isEmpty()) {  
        System.out.println("\nQueue is empty");  
    }  
    int data = front.data;  
    front = front.next;  
    queueSize--;  
    if (isEmpty()) { //queueSize is 0 after dequeue.  
        rear = null;  
    }  
}
```



```
System.out.println("Element " + data+ " removed from the queue");  
return data;  
}
```

```
//Add data at the rear of the queue.  
public void enqueue(int data) {  
    Node New_Node=new Node();  
    if(New_Node==null) {  
        System.out.println("\nQueue is full");  
    }  
    New_Node.data=data;  
    New_Node.next=null;  
  
    if (isEmpty()){  
        front = rear=New_Node;  
    }  
}
```



```
else {
rear.next=New_Node;
rear=New_Node;
}
queueSize++;
System.out.println("Element " + data+ " added to the queue"
}
//print front and rear of the queue
public void print_frontRear() {
if(front!=null)
System.out.println("Front of the queue:" + front.data
+ "\nRear of the queue:" + rear.data);
}
}

class QueueLink{
public static void main(String a[]){
```



```
QueueLL queue = new QueueLL();  
queue.enqueue(6);  
queue.enqueue(3);  
queue.print_frontRear();  
queue.enqueue(12);  
queue.enqueue(24);  
queue.dequeue();  
queue.dequeue();  
queue.enqueue(9);  
queue.print_frontRear();  
}  
}
```



Circular queues

- ▶ A Circular Queue is an extended version of a normal queue where the last element of the queue is connected to the first element of the queue forming a circle.
- ▶ The operations are performed based on FIFO (First In First Out) principle. It is also called 'Ring Buffer'.
- ▶ In a normal Queue, we can insert elements until queue becomes full. But once queue becomes full, we can not insert the next element even if there is a space in front of queue.



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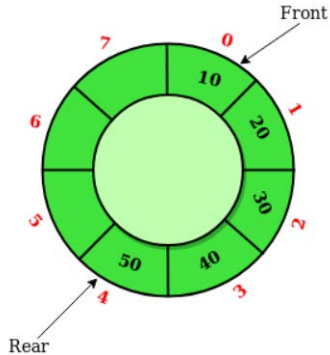


Figure: Circular Queue



//Circular Queue using Array

```
class QueueA
```

```
{  
    int queue[];  
    int front;  
    int rear;  
    int capacity;
```

```
    QueueA(int size) {  
        front = rear = -1;  
        capacity = size;  
        queue = new int[capacity];  
    }
```

```
    // insert an element into the queue
```



```
void enqueue(int item) {  
    // check if the queue is full  
    if (front == ((rear+1)%capacity)) {  
        System.out.println("Queue is full");  
        return;  
    }  
    // insert element at the rear  
    else {  
        rear= (rear==capacity-1?0:++rear);  
        //rear=((rear+1)%capacity);  
        queue[rear] = item;  
        if(front==-1) front=0;  
        queueDisplay();  
    }  
    return;  
}
```



```
//remove an element from the queue
int deQueue() {
    // check if queue is empty
    if (front == -1) {
        System.out.println("Queue is empty");
        return -1;
    }
    else {
        int temp=queue[front];
        if(front==rear)
            front=rear=-1;
        else
            front=(front==capacity-1?0:++front);
        //front=((front+1)%capacity);
        System.out.printf("Item "+temp+" is deQueued\n");
        queueDisplay();
        return temp;
    }
}
```



```
}

}

// print queue elements
void queueDisplay()
{
    int i;
    if (front == -1) {
        System.out.println("Queue is Empty");
        return;
    }

    // traverse front to rear and print elements
    System.out.println("Queue is:");
    if(front<=rear)
        for (i = front; i < rear; i++)
```



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```
System.out.printf(" %d , ", queue[i]);
else {
    for (i = front; i < rear+capacity; i++)
        System.out.printf(" %d , ", queue[i%capacity]);
    //for (i = 0; i < rear; i++)
    //System.out.printf(" %d , ", queue[i]);
}
System.out.printf(" %d \n", queue[rear]);

return;
}

// print front of queue
void queueFront()
{
    if (front == -1) {
        System.out.println("Queue is Empty");
```



```
        return;
    }
    System.out.printf("Front Element of the queue: %d\n", front);
    return;
}

void queueRear()
{
    if (front == -1) {
        System.out.println("Queue is Empty");
        return;
    }
    System.out.printf("Rear Element of the queue: %d\n", rear);
    return;
}

int queueSize()
```



```
{
    int size=0;
    if (front == -1) return size;

    if(front<=rear)
        size=rear-front+1;
    else
        size=capacity-(front-rear-1);
    return size;
}

public class QueueC {
    public static void main(String[] args) {
        // Create a queue of capacity 4
        QueueA q = new QueueA(4);
```




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```
System.out.println("Initial Queue(capacity=4):");  
// print Queue elements  
System.out.println("Display():");  
q.queueDisplay();  
System.out.printf("Size():%d\n",q.queueSize());  
  
// inserting elements in the queue  
System.out.println("enqueue(10):");  
q.enqueue(10);  
System.out.printf("Size():%d\n",q.queueSize());  
  
System.out.println("enqueue(30):");  
q.enqueue(30);  
System.out.printf("Size():%d\n",q.queueSize());  
  
System.out.println("enqueue(50):");  
q.enqueue(50);
```



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```
System.out.printf("Size():%d\n",q.queueSize());
```

```
System.out.println("enqueue(70):");
```

```
q.enqueue(70);
```

```
System.out.printf("Size():%d\n",q.queueSize());
```

```
// insert element in the queue
```

```
System.out.println("enqueue(90):");
```

```
q.enqueue(90);
```

```
System.out.printf("Size():%d\n",q.queueSize());
```

```
System.out.println("dequeue():");
```

```
q.dequeue();
```

```
System.out.printf("Size():%d\n",q.queueSize());
```

```
System.out.println("dequeue():");
```

```
q.dequeue();
```



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```
System.out.printf("Size():%d\n",q.queueSize());
```

```
System.out.println("enqueue(100):");
```

```
q.enqueue(100);
```

```
System.out.printf("Size():%d\n",q.queueSize());
```

```
System.out.println("enqueue(110):");
```

```
q.enqueue(110);
```

```
System.out.printf("Size():%d\n",q.queueSize());
```

```
System.out.println("enqueue(120):");
```

```
q.enqueue(120);
```

```
System.out.printf("Size():%d\n",q.queueSize());
```

```
System.out.println("Front():");
```

```
q.queueFront();
```

```
System.out.println("Rear():");
```



```
q.queueRear();
```

```
}
```

```
}
```



//Circular Queue using Linked List

```
class QueueCLL {  
private Node front, rear;  
private int queueSize; // queue size  
  
//linked list node  
private class Node {  
int data;  
Node next;  
}  
  
//default constructor - initially front & rear are null;  
//size=0; queue is empty  
public QueueCLL() {  
front = null;  
rear = null;
```



```
queueSize = 0;
}
//check if the queue is empty
public boolean isEmpty() {
return (queueSize == 0);
}

//Add data at the rear of the queue.
@SuppressWarnings("unused")
public void enqueue(int data) {
Node New_Node=new Node();
if(New_Node==null) {
System.out.println("Queue is full");
}
New_Node.data=data;
if (isEmpty()){
front = rear=New_Node;
```



```
rear.next=front;
}
else {
New_Node.next=front;
rear.next=New_Node;
rear=New_Node;
}
queueSize++;
System.out.println("Element " + rear.data+ " added to the c
}

//Remove item from the front of the queue.
public int dequeue() {
if (isEmpty()) {
System.out.println("Queue is empty");
}
int data = front.data;
```



```
front = front.next;  
rear.next=front;  
queueSize--;  
if (isEmpty()) { //queueSize is 0 after dequeue.  
front=rear = null;  
}
```

```
System.out.println("Element " + data+ " removed from the queue");  
return data;  
}
```

```
//print front and rear of the queue  
public void print_frontRear() {  
if(front!=null)  
System.out.println("Front of the queue:" + front.data  
+ "\nRear of the queue:" + rear.data);  
}
```




```
void queueDisplay()
{
    Node temp;
    if (front == null) {
        System.out.println("Queue is Empty");
        return;
    }

    // Traverse front to rear and print elements
    System.out.printf("Elements of the Queue: ");
    for (temp = front; temp != rear; temp=temp.next) {
        System.out.printf("%d , ", temp.data);
    }
    System.out.printf(" %d\n", rear.data);
    return;
}
```



```
class QueueCirLL{  
public static void main(String a[]){  
QueueCLL q = new QueueCLL();  
System.out.println("Display():");  
q.queueDisplay();  
System.out.println("enqueue(6):");  
q.enqueue(6);  
q.queueDisplay();  
System.out.println("enqueue(3):");  
q.enqueue(3);  
q.queueDisplay();  
System.out.println("enqueue(12):");  
q.enqueue(12);  
q.queueDisplay();  
System.out.println("enqueue(24):");  
q.enqueue(24);
```



```
q.queueDisplay();  
System.out.println("dequeue():");  
q.dequeue();  
q.queueDisplay();  
System.out.println("dequeue():");  
q.dequeue();  
q.queueDisplay();  
System.out.println("enqueue(9):");  
q.enqueue(9);  
q.queueDisplay();  
System.out.println("frontRear():");  
q.print_frontRear();  
}  
}
```



Double Ended queue

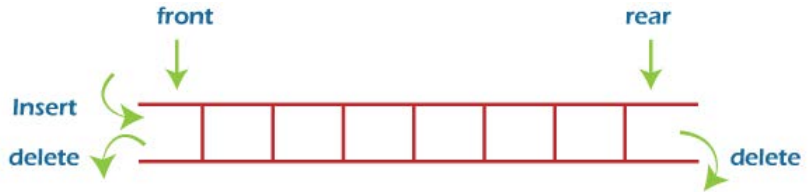


Figure: Deque

- Deque or Double Ended Queue is a generalized version of Queue data structure that allows insert and delete at both ends.



- ▶ `push-front()` - Inserts the element at the beginning.
- ▶ `push-back()` - Adds element at the end.
- ▶ `pop-front()` - Removes the first element from the deque.
- ▶ `pop-back()` - Removes the last element from the deque.
- ▶ `front()` - Gets the front element from the deque.
- ▶ `back()` - Gets the last element from the deque.



//De-queue using circular array

/*Operations on Deque:

void Push_Front(int key);

void Push_Rear(int key);

void Pop_Front();

void Pop_Rear();

bool isFull();

bool isEmpty();

int getFront();

int getRear();*/

class DequeCirArr {

static int queue[];

static int front;

static int rear;

static int capacity;



```
public DequeCirArr(int size)
{
    front = -1;
    rear = -1;
    capacity = size;
    queue = new int[capacity];
}

// Checks whether Deque is full or not.
boolean isFull()
{
    return ((front == 0 && rear == capacity - 1)
    || front == rear + 1);
}

// Checks whether Deque is empty or not.
boolean isEmpty() { return (front == -1); }
```



```
// Inserts an element at front
void Push_Front(int key)
{
    // check whether Deque is full or not
    if (isFull()) {
        System.out.println("Overflow");
        return;
    }

    // If queue is initially empty
    if (front == -1) {
        front = 0;
        rear = 0;
    }
    // front is at first position of queue
    else if (front == 0)
```




```
front = capacity - 1;
else // decrement front end by '1'
front--;
// insert current element into Deque
queue[front] = key;
}

// function to insert element at rear end of Deque.
void Push_Rear(int key)
{
if (isFull()) {
System.out.println(" Overflow ");
return;
}

// If queue is initially empty
if (front == -1) {
```



```
front = 0;
rear = 0;
}
// rear is at last position of queue
else if (rear == capacity - 1)
rear = 0;
// increment rear end by '1'
else
rear++;
// insert current element into Deque
queue[rear] = key;
}

// Deletes element at front end of Deque
void Pop_Front()
{
// check whether Deque is empty or not
```



```
if (isEmpty()) {  
    System.out.println("Queue Underflow\n");  
    return;  
}  
  
// Deque has only one element  
if (front == rear) {  
    front = -1;  
    rear = -1;  
}  
else  
    // back to initial position  
    if (front == capacity - 1)  
        front = 0;  
    else // increment front by '1' to remove current  
        // front value from Deque  
        front++;
```



}

```
// Delete element at rear end of Deque
```

```
void Pop_Rear()
```

```
{
```

```
if (isEmpty()) {
```

```
System.out.println(" Underflow");
```

```
return;
```

```
}
```

```
// Deque has only one element
```

```
if (front == rear) {
```

```
front = -1;
```

```
rear = -1;
```

```
}
```

```
else if (rear == 0)
```

```
rear = capacity - 1;
```



```
else  
rear--;  
}
```

```
// Returns front element of Deque  
int getFront()  
{  
    // check whether Deque is empty or not  
    if (isEmpty()) {  
        System.out.println(" Underflow");  
        return -1;  
    }  
    return queue[front];  
}
```

```
// function return rear element of Deque  
int getRear()
```



```
{
// check whether Deque is empty or not
if (isEmpty()) {
System.out.println(" Underflow");
return -1;
}
return queue[rear];
}

// print queue elements
static void DequeDisplay()
{
    int i;
    if (front == -1) {
        System.out.println("Queue is Empty");
        return;
    }
}
```



```
//traverse front to rear and print elements
System.out.println("Queue is:");
if(front<=rear) {
    for (i = front; i < rear; i++)
        System.out.printf(" %d , ", queue[i]);
}
else {
    for (i = front; i < rear+capacity; i++)
        System.out.printf(" %d , ", queue[i%capacity]);
    //for (i = 0; i < rear; i++)
    //System.out.printf(" %d , ", queue[i]);
}
System.out.printf(" %d \n", queue[rear]);

return;
}
```



```
public static void main(String[] args)
{

DequeCirArr dq = new DequeCirArr(5);

// Function calls
System.out.println("Initial Queue(capacity=5):");
DequeDisplay();
System.out.println("Insert element at rear: 5 ");
dq.Push_Rear(5);
DequeDisplay();

System.out.println("Insert element at rear: 10 ");
dq.Push_Rear(10);
DequeDisplay();
```




```
dq.Pop_Rear();  
System.out.println("After delete rear element: ");  
DequeDisplay();  
  
System.out.println("Insert element at front: 15 ");  
dq.Push_Front(15);  
DequeDisplay();  
  
System.out.println("Insert element at front: 20 ");  
dq.Push_Front(20);  
DequeDisplay();  
  
System.out.println("Insert element at rear: 30 ");  
dq.Push_Rear(30);  
DequeDisplay();
```



```
System.out.println("Insert element at rear: 40 ");  
dq.Push_Rear(40);  
DequeDisplay();
```

```
System.out.println("Insert element at rear: 50 ");  
dq.Push_Rear(50);  
DequeDisplay();
```

```
System.out.println("Insert element at front: 60 ");  
dq.Push_Front(60);  
DequeDisplay();
```

```
dq.Pop_Front();  
System.out.println("After delete front element:");  
DequeDisplay();
```

```
System.out.println("get front element: "+ dq.getFront());
```



```
System.out.println("get rear element : "+ dq.getRear());  
}  
}
```



Priority Queue

- ▶ A priority queue is a type of queue that arranges elements based on their priority values.
- ▶ Elements with higher priority values are typically retrieved or removed before elements with lower priority values.
- ▶ Each element has a priority value associated with it.
- ▶ When we add an item, it is inserted in a position based on its priority value.
- ▶ There are several ways to implement a priority queue, including using an array, linked list, heap, or binary search tree.
- ▶ Binary heap being the most common method to implement.



- ▶ The reason for using Binary Heap is simple, in binary heaps, we have easy access to the min (in min heap) or max (in max heap) and binary heap being a complete binary tree are easily implemented using arrays.
- ▶ Since we use arrays, we have cache friendliness advantage also.
- ▶ Priority queues are often used in real-time systems, where the order in which elements are processed is not simply based on the fact who came first (or inserted first), but based on priority.
- ▶ Priority Queue is used in algorithms such as Dijkstra's algorithm, Prim's algorithm, Kruskal's algorithm and Huffman Coding.



Thank you

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