

Einfache Gleichungen 1

- 1.** a) $x + 3 = 8$ b) $x + 2 = 12$ c) $x + 9 = 18$
d) $x + 4 = 5$ e) $x + 22 = 44$ f) $x + 28 = 30$
g) $x + 7 = 2$ h) $x + 8 = -4$ i) $x + 2 = -12$
- 2.** a) $x - 1 = 2$ b) $x - 3 = 5$ c) $x - 4 = 11$
d) $x - 8 = 9$ e) $x - 2 = 13$ f) $x - 12 = 22$
g) $x - 7 = -11$ h) $x - 9 = -14$ i) $x - 1 = -19$
- 3.** a) $x \cdot 5 = 15$ b) $x \cdot 2 = 8$ c) $x \cdot 7 = 21$
d) $3 \cdot x = 27$ e) $9 \cdot x = 45$ f) $8 \cdot x = 64$
g) $x \cdot 2 = 4,2$ h) $5 \cdot x = 12,5$ i) $9 \cdot x = 1,8$
- 4.** a) $\frac{x}{2} = 2$ b) $\frac{x}{5} = 1$ c) $\frac{x}{8} = 9$
d) $\frac{x}{5} = 9$ e) $\frac{x}{7} = 7$ f) $\frac{x}{6} = 9$
g) $\frac{x}{10} = 0,3$ h) $\frac{x}{4} = 1,1$ i) $\frac{x}{8} = 0,8$
- 5.** a) $x - 2 = 5$ b) $3 + x = 1$ c) $\frac{x}{12} = -4$
d) $3 \cdot x = 3,6$ e) $x \cdot (-4) = -3,6$ f) $\frac{x}{3} = -1,1$
g) $x + 1,8 = 2,2$ h) $x - 3,6 = 1,5$ i) $-3 \cdot x = -1,5$
- 6.** a) $3 - x = 4$ b) $2 - x = 8$ c) $7 - x = 5$
d) $9 - x = -3$ e) $5 - x = -8$ f) $-3 - x = -1$
g) $-2 - x = 6$ h) $3 - x = 5$ i) $-4 - x = 12$
- 7.** a) $3x + 4 = 16$ b) $2x + 3 = 13$ c) $4 + 5x = 19$
d) $4x - 1 = 15$ e) $9x - 8 = 19$ f) $10x - 15 = 45$
g) $5 - 2x = 15$ h) $3 - 6x = 21$ i) $9 - 5x = -36$
- 8.** a) $\frac{x}{2} - 4 = 3$ b) $3 + \frac{x}{3} = 2$ c) $\frac{x}{5} - 3 = 4$
d) $\frac{x}{5} + 8 = 2$ e) $4 + \frac{x}{8} = 5$ f) $\frac{3x}{4} + 2 = 5$
g) $\frac{2x}{5} - 1 = 5$ h) $-4 + \frac{5x}{6} = 1$ i) $9 + \frac{2x}{9} = 11$
- 9.** a) $\frac{12}{x} = 3$ b) $\frac{6}{x} = 3$ c) $\frac{15}{x} = 15$
d) $\frac{14}{x} = 7$ e) $\frac{16}{x} = 4$ f) $\frac{49}{x} = 7$

Gleichungen mit Additions- und Subtraktionsklammern

- 1.** a) $2x + (3x + 4) = 19$ b) $12x + (3x + 4) + (2x + 3) = 41$
 c) $12x - 4 + (3x + 1) = 27$ d) $8x - 3 + (x + 1) = 2x + 7 + (4x + 3)$
 e) $4 - (3x - 2) + 5x = 4 - (x + 1)$ f) $(4x - 4) - 8 = -(3x - 2)$
- 2.** a) $12x + (13x - 19) - (11x - 15) = 25 - (17 - 13x)$
 b) $(3x + 7) - 6 = 12x - (x + 4) - (4x - 5)$
 c) $(5x - 3) - (2x - 4) = -(x + 3) - (x + 5) + (x + 3)$
 d) $12 - (5x + 8) - (8x - 12) = 14x - 25 - (3x - 8) + (7x + 2)$
 e) $-(3x - 5) - (7x - 24) = 3 + (x + 1) - (2x - 7)$
 f) $12x - (3x + 8) + (39 - 5x) = 14 + (25x - 8) - (41 - x)$
- 3.** a) $12x - 3 - (23x - 48) + (x + 93) = 58x - (24x - 44) + 6$
 b) $-(19x + 51) - (11x + 4) = -(39x + 45) + (8x - 7) - 24$
 c) $24 - (14x - 8) - (3 + 12x) = 4 - (8x + 11)$
 d) $3,7 - (8,1x + 5,4) - (2,6x + 8,3) = -3,1x + (8 - 1,6x)$
 e) $(4,5x + 56) - (2,25x - 7) - (300 - 3x) = -(0,75x - 3)$
 f) $3,5x - 6 - (4 - 2x) = (2,4x - 9,4) - (1,2x - 25,2)$

Gleichungen – Klammer mal Zahl

- 1.** a) $7(x - 2) = 49$ b) $7(5x + 2) + 9 = 58$
 c) $15(8x - 24) = 120$ d) $6(3x - 25) = 12$
 e) $12(5x - 2) = 48 + 12x$ f) $3(4x + 18) = 6x + 108$
- 2.** a) $23(2x + 5) = 6x + 315$ b) $17(5x + 3) = 401 + 35x$
 c) $16(2x - 3) = 5(4x + 16) + 4$ d) $12(8x - 25) = 5(16x + 40) - 20$
 e) $13(20 - 5x) = 15(30 - 5x)$ f) $14(7x - 14) + 3 = 12(8x + 20) + 1$
- 3.** a) $5(3x - 4) = 7(2x - 3)$ b) $3(6x - 9) = 9(2x - 3)$
 c) $8(3x - 5) = 60 + 20x$ d) $5x - 4(2 - 3x) = 22 + 7x$
 e) $3(x + 6) + 2(x + 1) = 40$ f) $8(3x - 5) = 60 + 20x$
- 4.** a) $5x - 4(2 - 3x) = 22 + 7x$ b) $6(1 - 3x) + 7(4x - 3) = 35$
 c) $18q + 3 = 3(6,1q - 5)$ d) $5(x + 1,2) - 4 = 10x + 3$
 e) $4(x + 9) - 34 = 2(x - 4) + 11$ f) $8 - 10x - 2 = 8 - 5(x + 1,4)$

Gleichungen – Klammer mal Klammer

- 1.** a) $(20 + x)(20 - x) = (x + 2)(46 - x)$ b) $(x + 5)(5 - x) = (12 + x)(4 - x) + 1$
 c) $(x - 5)(x + 8) = (x - 2)(x + 1) + 6$ d) $(x + 12)(x + 5) = (x - 8)(x + 7) - 10$
 e) $(x - 8)(x - 15) = (x - 8)(x - 25)$ f) $(x + 9)(x - 17) = (x - 5)(x - 10)$
- 2.** a) $(x + 2)(x - 3) = x(x - 2)$ b) $(2x + 4)(2x - 5) = (4x - 3)(x + 2)$
 c) $(2x - 4)(3 - x) = (x + 4)(2 - 2x)$ d) $x(3x + 2) = (3x - 6)(x + 2)$
 e) $(x - 2)(x + 5) = (x + 6)(x - 1)$ f) $(x - 2)(2x + 3) = (4 - x)(5 - 2x) + 1$
- 3.** a) $(12 - x)(15 + x) = (8 - x)(9 + x)$ b) $(15 - x)(20 + x) = (30 - x)(5 + x)$
 c) $(x + 20)(x - 30) = (x - 10)(x + 40)$ d) $(9 + x)(15 + x) = (3 + x)(5 + x)$
 e) $(2x - 15)(3x + 4) = (6x - 4)(x + 12) - 117$
 f) $(x + 2)(3 - x) = (5 + x)(7 - x) + 2(x + 29)$

Gleichungen mit 1 Variablen – verm. Übungen 1

- 1.** a) $7x - (2x - 9) + (3x + 8) - (5x + 6) = 5$
b) $(4x - 5) - 6 = 12x - (x + 4) - (3x + 7)$

2. a) $14x + (11x - 19) - (13x - 15) = 25 - (17 - 15x)$
b) $26x - (14 + 19x) + (25 + 21x) = 29 - (-23x + 18)$

3. a) $17 - (13 - 9x) + (16x - 9) = (15x - 22) - (7 - 4x)$
b) $12 - (16 - 15x) + (11 - 9x) = (25 - 19x) - (13 - 23x)$

4. a) $7x - [14 - (2x + 5)] = 18 - [3x + (15 - 4x)]$
b) $4x - [7 - (x + 15)] = 11 - [5x - (3x - 17)]$

5. a) $21x - [9 - (5x - 6) + 8x] = 15 - [(4x - 7) - (6x - 5)]$
b) $19 - [13x - (22 + 7x) + 11] = 24x - [(15 - 4x) + (5x - 16)]$

6. a) $12x - [14 - (9x - 11)] = 24x - [18 - (17x + 13)]$
b) $17 - [13x - (15 - 19x) - 21x] = 25 - [(11x - 23) - (18x - 7)]$

7. a) $5(3x - 4) = 7(2x - 3)$ b) $3(6x - 9) = 9(2x - 3)$
c) $8(4x - 3) = 4(5x - 6)$ d) $3(7x - 9) = 4(6x - 7)$

8. a) $8 - 7(3x + 2) = 9x - 6(5x + 1)$
b) $3x - 2(5x - 8) = 9 - 4(3x + 7)$

9. a) $5(3x - 8) + 3(7x + 6) = 6(8x + 3) - 4(2x + 5)$
b) $8(4x + 3) - 5(6x - 5) = 4(9x + 4) - 7(4x - 5)$

10. a) $5(8x + 5) - 4(3x + 4) - 2(11x - 17) = 25 - 3(5x - 7) + 6(3x - 2)$
b) $(2x - 3)7 - (x - 2)6 - (5x + 6)2 = 26 - (3x - 4)4 + (6x - 5)3$

11. a) $(x + 4)(3x - 7) = (x - 2)(3x + 8)$ b) $(x + 5)(x + 2) = (x + 6)(x - 1)$

12. a) $(x - 4)(6 - x) = (x - 3)(8 - x)$ b) $(x + 3)(2x + 5) = (x + 7)(2x - 1)$

13. a) $(x - 2)(x + 3) = (x + 4)(x - 5)$ b) $(x + 1)(4x - 25) = (2x - 5)(2x - 8)$

14. a) $(x + 5)(x - 3) = (x + 6)(x - 2)$ b) $(x - 7)(x - 4) = (x - 5)(x - 2)$

15. a) $(x - 4)(x - 3) = x^2 - 7x + 12$ b) $(2x - 5)(x + 1) = 2x^2 - 3x - 5$

16. a) $(5x - 6)(2x + 3) + (2x + 3)(3x - 2) = 2x(8x + 1)$
b) $(9x - 2)(2x - 5) + (3x + 4)(5x + 3) = 3x(11x - 3)$

17. a) $(3x - 4)(2x - 1) - (3x + 1)(x - 3) = (3x - 1)(x - 1)$
b) $(2x + 1)(3x - 1) - (2x + 11)(2x - 5) = (x - 6)(2x - 3)$

18. a) $(5x - 3)(2x - 3) - 2(4x - 1)(x - 3) = (2x - 3)(x + 5)$
b) $(3x + 1)(4x - 5) - 3(x - 3)(2x - 1) = (6x + 1)(x + 1)$

a) $(x + 3)^2 + (x - 4)^2 = (x - 1)^2 + (x + 2)^2$

19. a) $(x + 3)^2 + (x - 4)^2 = (x - 1)^2 + (x + 2)^2$
b) $(3x + 5)^2 + (2x - 3)^2 = (4x + 1)^2 - 3(x^2 - 1)$

20. a) $(x + 1)^2 - (x - 3)^2 = (x - 2)^2 - (x - 4)^2$
b) $(4x + 3)^2 - (5x - 2)^2 = 6(x + 9) - (3x - 7)^2$

21. a) $(x + 1)(x - 1) - (x - 3)^2 = (x + 4)^2 - (x - 2)(x + 2)$
b) $(x - 3)^2 - (x + 6)(x - 6) = (2x + 3)(2x - 3) - 4(x^2 - 15)$

22. a) $(2x + 1)^2 - (x - 4)^2 = (3x - 2)^2 - (2x + 1)(2x - 1) - 2(x^2 - 7x + 10)$
b) $(2x - 3)^2 + (3x + 5)^2 = (4x + 3)^2 - (3x - 2)(x + 6) - (2x - 7)$

Gleichungen mit 1 Variablen – verm. Übungen 2

1. $5x + 4 - 6x + 8 = 3x + 4 - 8x - 7 + 3x$

2. $18 - x - 15 + x + 2x = 18 - x + 19 + 3x - 1 - x$

3. $x - (x + 3) + x - 5 = 6 - (x - 4) + (x + 1)$

4. $25x + 14 - (3x - 8) = 9x - (6x + 3) - 4x + (2 + 22x)$

5. $5 - [x + 6 - (3 - x)] - 10x = 6x - [(3x + 2) - x] - 17x$

6. $4(x - 3) + 5(x + 6) = 3 - 5(x + 3) + 13x$

7. $5x - (6 - 3x) + 6(3x - 8) = 23x - 4(x - 5) + 6x$

8. $172x + 19(24x - 17) = 207x - 18(61 - 18x) + 96x$

9. $12(x + 13) - 14x + 5(x + 12) - 4(x + 3) = 0$

10. $9x - \{5x - [4x - (3x - 2) - 3] - 4\} = 5x - 6 + x$

11. $x + 15 + 5(2x - 10) = 4x - (5 + x) + 2$

12. $17(3x - 8) - [4x - (3 - x)] = 46x - 1 - 3(x + 2)$

13. $31x - 58 + 4x - 16 = 5x + 24 + 9x - 18 + 4$

14. $52(17x - 28) + 92(44 - 53x) = -51x + 20563 + 29(71x + 1)$

15. $3x + 6(5x + 8) - 6 - (3 + x) - 6(x - 1) - 23x = 0$

16. $2x + 3a - 5b + 4a - x = 4(a + b)$

17. $12x - a - (a - x) = 14x + (a + b) - 3x + b$

18. $a + a^2 - b^2 - x = x - a + a^2 - b^2$

19. $ax + b + 2ax - 12b = 5ax - 3b - 6ax$

20. $(3a - x)^2 = (5a - x)^2$

21. $(5 + x)^2(a - b) = (5 + x)^2(a + b) - 2bx^2$

Gleichungen mit 1 Variablen – verm. Übungen 3

Bestimme die Lösungsmenge zu folgenden Gleichungen.

1. a) $12x - 56 = 16$

b) $5x + 39 = -26$

c) $\frac{4}{5}x + 40 = 48$

d) $\frac{3}{5}x + 4,2 = 7,4$

e) $7x - 4 + 2x = 52 - 5x$

f) $40 - 2x + 5x = 68 + x$

g) $22x + 4(9 - 3x) = 46$

h) $4(3x - 5) + 30 = 46$

2. a) $18x - 75 + 3x + 128 - 7x = 68 - 8x - 25 + 14x$

b) $113x + 73 - 5x - 16 = 23x + 85 - 33x + 45 + 62x + 151$

c) $6x - 2(x - 16) = 5 - 3(11 - x) + 60$

d) $4x - 5(x - 12) = 40 + 9(9 - x) - 11$

e) $\frac{3}{4}(16x + 24) + 6(3x - 4) = \frac{2}{3}(27x + 18) + 6x - 3$

f) $3x - 15 + 2x = 18 + 4x + 25$

3. a) $17x - 33 + 12x - 16 = 4x + 56 + 10x$

b) $-22x + 36 + 18x - 6 = 16x + 55 + 12x - 89$

c) $4x - 22 + 3x - 45 = 8 - 2x + 26 + 5x - 1$

d) $6x + 36 - 2x + 45 = 3x + 88 - 8x + 47$

e) $12x - 66 - 34 + 2x = 8x - 35 + 2x + 99$

f) $-12x + 25 + 6x - 38 = 66 + 2x - 22 + 3x - 12x$

4. a) $66x + 14 - 39 + 12x - 100 = -12x - 47 + 23x + 56$

b) $22x + 48 - 55x - 55x = 36 - 45 + 12x - 43$

c) $-22 + 14x - 33 + 10x - 77 + 25x = 88 - 14x + 65 - 5 + 35$

d) $-78 + 66x - 21x + 20 - 47 + 88x = 10x - 36 - 36x + 90$

e) $55x - 44x - 12x - 12x + 96 = 12x + 99 - 178 - 66x - 30$

f) $-44 - 25x + 29 - 32x - 98x + 14x = -47x + 66 - 58x + 124 + 11$

5. a) $12x - 33 + 20x - 78x + 36 - 48 + 30x - 45x + 558 - 14x - 605 - 58 = 0$

b) $-33x - 44x + 54 - 88 + 12x - 100 + 222x = 12 - 45x + 999 - 10x + 305 + 34$

c) $36x - 78 + 61x - 69 - 78 + 22x - 47x = 369 - 44x + 45 - 12x + 78 + 120x + 11$

d) $-987x - 564 + 55x - 123 + 78 = -987x + 258 - 25x + 478 + 255$

e) $16x^2 - 56x + 22 - 851 - 951 + 357x = 16x^2 + 698 - 14x + 548 - 20x - 11$

f) $-65a + 58 - 36a + 587 - 33a = 698 + 14a - 587a + 698 - 32a + 191$

6. a) $-789v + 258 - 11v + 456 - 894 = 336v + 201 - 45v + 710$

b) $66z + 587 - 65z + 32z - 784 = -35z + 368 - 45z + 125 - 12$

c) $-47y + 569 - 45y - 55y + 231 = -147y + 987 - 36y + 444 + 89$

d) $665m - 478 - 365m + 884 - 320m = 6987 - 358 - 12m - 3365 + 6$

e) $-254a + 369 - 258 + 458a - 369 = -540a + 3320 + 142$

f) $-258x + 5873 - 3369 + 368x - 897 - 321x + 33 = 1007$