Package 'EmpiricalCalibration'

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|---|
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| Description Routines for performing empirical calibration of observational study estimates. By using a set of negative control hypotheses we can estimate the empirical null distribution of a particular observational study setup. This empirical null distribution can be used to compute a calibrated p-value, which reflects the probability of observing an estimated effect size when the null hypothesis is true taking both random and systematic error into account. A similar approach can be used to calibrate confidence intervals, using both negative and positive controls. |
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| calibrateConfidenceInterval calibrateP caseControl cohortMethod computeExpectedSystematicError computeTraditionalCi |

| | computeTraditionalP | 7 |
|-------|-------------------------|----|
| | convertNullToErrorModel | 8 |
| | evaluateCiCalibration | 9 |
| | fitMcmcNull | 10 |
| | fitNull | 11 |
| | fitSystematicErrorModel | 12 |
| | grahamReplication | 13 |
| | plotCalibration | 14 |
| | plotCalibrationEffect | 15 |
| | plotCiCalibration | 16 |
| | plotCiCalibrationEffect | 17 |
| | plotCiCoverage | 18 |
| | plotErrorModel | 19 |
| | plotExpectedType1Error | 20 |
| | plotForest | 22 |
| | plotMcmcTrace | 23 |
| | plotTrueAndObserved | 23 |
| | sccs | 24 |
| | simulateControls | |
| | southworthReplication | 26 |
| Index | | 27 |
| | | |

 ${\tt calibrateConfidenceInterval}$

Calibrate confidence intervals

Description

Calibrate confidence intervals

Usage

2

calibrateConfidenceInterval(logRr, seLogRr, model, ciWidth = 0.95)

Arguments

| logRr | A numeric vector of effect estimates on the log scale. |
|---------|--|
| seLogRr | The standard error of the log of the effect estimates. Hint: often the standard error = (log(<lower 95="" bound="" confidence="" interval="" percent="">) - log(<effect estimate="">))/qnorm(0.025).</effect></lower> |
| mode1 | An object of type systematic Error Model as created by the $\label{thm:model} \textbf{function}.$ |
| ciWidth | The width of the confidence interval. Typically this would be .95, for the 95 percent confidence interval. |

Details

Compute calibrated confidence intervals based on a model of the systematic error.

calibrateP 3

Value

A data frame with calibrated confidence intervals and point estimates.

Examples

```
data <- simulateControls(n = 50 * 3, mean = 0.25, sd = 0.25, trueLogRr = \log(c(1, 2, 4))) model <- fitSystematicErrorModel(data$logRr, data$seLogRr, data$trueLogRr) newData <- simulateControls(n = 15, mean = 0.25, sd = 0.25, trueLogRr = \log(c(1, 2, 4))) result <- calibrateConfidenceInterval(newData$logRr, newData$seLogRr, model) result
```

calibrateP

Calibrate the p-value

Description

calibrateP computes calibrated p-values using the fitted null distribution

Usage

```
calibrateP(null, logRr, seLogRr, ...)
## S3 method for class 'null'
calibrateP(null, logRr, seLogRr, ...)
## S3 method for class 'mcmcNull'
calibrateP(null, logRr, seLogRr, pValueOnly, ...)
```

Arguments

| null | An object of class null created using the fitNull function or an object of class mcmcNull created using the fitMcmcNull function. |
|------------|---|
| logRr | A numeric vector of one or more effect estimates on the log scale |
| seLogRr | The standard error of the log of the effect estimates. Hint: often the standard error = $(\log(< \text{lower bound 95 percent confidence interval>}) - \log(< \text{effect estimate>}))/qnorm(0.025)$ |
| | Any additional parameters (currently none). |
| pValueOnly | If true, will return only the calibrated P-value itself, not the credible interval. |

Details

This function computes a calibrated two-sided p-value as described in Schuemie et al (2014).

Value

The two-sided calibrated p-value.

4 caseControl

Methods (by class)

- null: Computes the calibrated P-value using asymptotic assumptions.
- mcmcNull: Computes the calibrated P-value and 95 percent credible interval using Markov Chain Monte Carlo (MCMC).

References

Schuemie MJ, Ryan PB, Dumouchel W, Suchard MA, Madigan D. Interpreting observational studies: why empirical calibration is needed to correct p-values. Statistics in Medicine 33(2):209-18,2014

Examples

```
data(sccs)
negatives <- sccs[sccs$groundTruth == 0, ]
null <- fitNull(negatives$logRr, negatives$seLogRr)
positive <- sccs[sccs$groundTruth == 1, ]
calibrateP(null, positive$logRr, positive$seLogRr)</pre>
```

caseControl

Odds ratios from a case-control design

Description

Odds ratios from a case-control design

Usage

```
data(caseControl)
```

Format

A data frame with 47 rows and 4 variables:

```
drugName Name of the drug
```

groundTruth Whether the drug is a positive (1) or negative (0) control

logRr The log of the incidence rate ratio

seLogRr The standard error of the log of the incidence rate ratio

Details

A dataset containing the odds ratios (and standard errors) produced using a case-control design. The outcome is upper GI bleeding, the drug of interest (groundTruth = 1) is sertraline. Also included are 46 negative control drugs, for which we believe there to be no causal relation with upper GI bleeding. We used a database of medical records from general practices in the USA, the General Electric (GE) Centricity database, which contains data on 11.2 million subjects. We restricted on study period (start of 1990 through November 2003), age requirements (18 years or older), available time prior to event (180 days), number of controls per case (6), and risk definition window (30 days following the prescription). Controls were matched on age and sex. Cases of upper GI bleeding were identified on the basis of the occurrence of ICD-9 diagnosis codes in the problem list. These

cohortMethod 5

codes pertain to esophageal, gastric, duodenal, peptic, and gastrojejunal ulceration, perforation, and hemorrhage, as well as gastritis and non-specific gastrointestinal hemorrhage. For more information on this set see Schuemie et al (2014).

References

Schuemie MJ, Ryan PB, Dumouchel W, Suchard MA, Madigan D. Interpreting observational studies: why empirical calibration is needed to correct p-values. Statistics in Medicine 33(2):209-18,2014

cohortMethod

Relative risks from a new-user cohort design

Description

Relative risks from a new-user cohort design

Usage

data(cohortMethod)

Format

A data frame with 31 rows and 4 variables:

drugName Name of the drug

groundTruth Whether the drug is a positive (1) or negative (0) control

logRr The log of the incidence rate ratio

seLogRr The standard error of the log of the incidence rate ratio

Details

A dataset containing the relative risks (and standard errors) produced using a new-user cohort design. The outcome is acute liver injury, the drug of interest (groundTruth = 1) is Isoniazid Also included are 30 negative control drugs, for which we believe there to be no causal relation with acute liver injury. We used the Thomson MarketScan Medicare Supplemental Beneficiaries database, which contains data on 4.6 million subjects. We selected two groups (cohorts): (1) all subjects exposed to isoniazid and (2) all subjects having the ailment for which isoniazid is indicated, in this case tuberculosis, and having received at least one drug that is not known to cause acute liver injury. We removed all subjects who belonged to both groups and subjects for which less than 180 days of observation time was available prior to their first exposure to the drug in question. Acute liver injury was identified on the basis of the occurrence of ICD-9-based diagnosis codes from inpatient and outpatient medical claims and was defined broadly on the basis of codes associated with hepatic dysfunction, as have been used in prior observational database studies. The time at risk was defined as the length of exposure + 30 days, and we determined whether subjects experienced an acute liver injury during their time at risk. Using propensity score stratification, the cohorts were divided over 20 strata, and an odds ratio over all strata was computed using a Mantel-Haenszel test. The propensity score was estimated using Bayesian logistic regression using all available drug, condition, and procedure covariates occurring in the 180 days prior to first exposure, in addition to age, sex, calendar year of first exposure, Charlson index, number of drugs, number of visit days, and number of procedures. For more information on this set see Schuemie et al (2014).

References

Schuemie MJ, Ryan PB, Dumouchel W, Suchard MA, Madigan D. Interpreting observational studies: why empirical calibration is needed to correct p-values. Statistics in Medicine 33(2):209-18,2014

compute Expected Systematic Error

Compute the expected systematic error

Description

calibrateP computes calibrated p-values using the fitted null distribution

Usage

```
computeExpectedSystematicError(null)
```

Arguments

null An object of class null created using the fitNull function or an object of class

mcmcNull created using the fitMcmcNull function.

... Any additional parameters (currently none).

Details

This function computes a calibrated two-sided p-value as described in Schuemie et al (2014).

Value

The two-sided calibrated p-value.

```
data(sccs)
negatives <- sccs[sccs$groundTruth == 0, ]
null <- fitNull(negatives$logRr, negatives$seLogRr)
computeExpectedSystematicError(null)</pre>
```

computeTraditionalCi 7

computeTraditionalCi Compute the (traditional) confidence interval

Description

computeTraditionalCi computes the traditional confidence interval based on the log of the relative risk and the standard error of the log of the relative risk.

Usage

```
computeTraditionalCi(logRr, seLogRr, ciWidth = 0.95)
```

Arguments

logRr A numeric vector of one or more effect estimates on the log scale

seLogRr The standard error of the log of the effect estimates. Hint: often the standard

error = (log(<lower bound 95 percent confidence interval>) - log(<effect esti-

mate>))/qnorm(0.025)

ciWidth The width of the confidence interval. Typically this would be .95, for the 95

percent confidence interval.

Value

The point estimate and confidence interval

Examples

```
data(sccs)
positive <- sccs[sccs$groundTruth == 1, ]
computeTraditionalCi(positive$logRr, positive$seLogRr)</pre>
```

computeTraditionalP

Compute the (traditional) p-value

Description

computeTraditionalP computes the traditional two-sided p-value based on the log of the relative risk and the standard error of the log of the relative risk.

Usage

```
computeTraditionalP(logRr, seLogRr)
```

Arguments

logRr A numeric vector of one or more effect estimates on the log scale

seLogRr The standard error of the log of the effect estimates. Hint: often the standard

error = (log(<lower bound 95 percent confidence interval>) - log(<effect esti-

mate>))/qnorm(0.025)

8 convertNullToErrorModel

Value

The two-sided (traditional) p-value.

Examples

```
data(sccs)
positive <- sccs[sccs$groundTruth == 1, ]
computeTraditionalP(positive$logRr, positive$seLogRr)</pre>
```

convertNullToErrorModel

Convert empirical null distribution to systematic error model

Description

This function converts an empirical null distribution, fitted using estimates only for negative controls, into a systematic error distribution that can be used to calibrate confidence intervals in addition to p-values.

Whereas the fitSystematicErrorModel uses positive controls to determine how the error distribution changes with true effect size, this function requires the user to make an assumption. The default assumption, meanSlope = 1 and sdSlope = \emptyset , specify a belief that the error distribution is the same for all true effect sizes. In many cases this assumption is likely to be correct, however, if an estimation method is biased towards the null this assumption will be violated, causing the calibrated confidence intervals to have lower than nominal coverage.

Usage

```
convertNullToErrorModel(null, meanSlope = 1, sdSlope = 0)
```

Arguments

null The empirical null distribution fitted using eith the fitNull or the fitMcmcNull

function.

meanSlope The slope for the mean of the error distribution. A slope of 1 means the error is

the same for different values of the true relative risk.

sdSlope The slope for the log of the standard deviation of the error distribution. A slope

of 0 means the standard deviation is the same for different values of the true

relative risk.

Value

An object of type systematicErrorModel.

```
data(sccs)
negatives <- sccs[sccs$groundTruth == 0, ]
null <- fitNull(negatives$logRr, negatives$seLogRr)
model <- convertNullToErrorModel(null)
positive <- sccs[sccs$groundTruth == 1, ]
calibrateConfidenceInterval(positive$logRr, positive$seLogRr, model)</pre>
```

evaluateCiCalibration 9

evaluateCiCalibration Evaluate confidence interval calibration

Description

evaluateCiCalibration performs a leave-one-out cross-validation to evaluate the calibration confidence intervals.

Usage

```
evaluateCiCalibration(
  logRr,
  seLogRr,
  trueLogRr,
  strata = as.factor(trueLogRr),
  crossValidationGroup = 1:length(logRr),
  legacy = FALSE
)
```

Arguments

logRr A numeric vector of effect estimates on the log scale.

seLogRr The standard error of the log of the effect estimates. Hint: often the standard

error = (log(<lower bound 95 percent confidence interval>) - log(<effect esti-

mate>))/qnorm(0.025).

trueLogRr The true log relative risk.

strata Variable used to stratify the plot. Set strata = NULL for no stratification.

crossValidationGroup

What should be the unit for the cross-validation? By default the unit is a single control, but a different grouping can be provided, for example linking a negative

control to synthetic positive controls derived from that negative control.

legacy If true, a legacy error model will be fitted, meaning standard deviation is linear

on the log scale. If false, standard deviation is assumed to be simply linear.

Details

The empirical calibration is performed using a leave-one-out design: The confidence interval of an effect is computed by fitting a null using all other controls.

Value

A data frame specifying the coverage per strata (usually true effect size) for a wide range of widths of the confidence interval. The result also includes the fraction of estimates that was below and above the confidence interval.

```
## Not run:
data <- simulateControls(n = 50 * 3, mean = 0.25, sd = 0.25, trueLogRr = log(c(1, 2, 4)))
eval <- evaluateCiCalibration(data$logRr, data$seLogRr, data$trueLogRr)
## End(Not run)</pre>
```

10 fitMcmcNull

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Fit the null distribution using MCMC

Description

fitNull fits the null distribution to a set of negative controls using Markov Chain Monte Carlo (MCMC).

Usage

```
fitMcmcNull(logRr, seLogRr, iter = 10000)
```

Arguments

logRr A numeric vector of effect estimates on the log scale

seLogRr The standard error of the log of the effect estimates. Hint: often the standard

error = (log(<lower bound 95 percent confidence interval>) - log(<effect esti-

mate>))/qnorm(0.025)

iter Number of iterations of the MCMC.

Details

This is an experimental function for computing the 95 percent credible interval of a calibrated p-value using Markov-Chain Monte Carlo (MCMC).

Value

An object of type mcmcNull containing the mean and standard deviation (both on the log scale) of the null distribution, as well as the MCMC trace.

```
## Not run:
data(sccs)
negatives <- sccs[sccs$groundTruth == 0, ]
null <- fitMcmcNull(negatives$logRr, negatives$seLogRr)
null
plotMcmcTrace(null)
positive <- sccs[sccs$groundTruth == 1, ]
calibrateP(null, positive$logRr, positive$seLogRr)
## End(Not run)</pre>
```

fitNull 11

| fitNull | Fit the null distribution |
|---------|---------------------------|
| | |

Description

fitNull fits the null distribution to a set of negative controls

Usage

```
fitNull(logRr, seLogRr)
```

Arguments

logRr A numeric vector of effect estimates on the log scale

seLogRr The standard error of the log of the effect estimates. Hint: often the standard

error = (log(<lower bound 95 percent confidence interval>) - log(<effect esti-

mate>))/qnorm(0.025)

Details

This function fits a Gaussian function to the negative control estimates as described in Schuemie et al (2014).

Value

An object containing the parameters of the null distribution.

References

Schuemie MJ, Ryan PB, Dumouchel W, Suchard MA, Madigan D. Interpreting observational studies: why empirical calibration is needed to correct p-values. Statistics in Medicine 33(2):209-18,2014

```
data(sccs)
negatives <- sccs[sccs$groundTruth == 0, ]
null <- fitNull(negatives$logRr, negatives$seLogRr)
null</pre>
```

```
fitSystematicErrorModel
```

Fit a systematic error model

Description

Fit a systematic error model

Usage

```
fitSystematicErrorModel(
  logRr,
  seLogRr,
  trueLogRr,
  estimateCovarianceMatrix = FALSE,
  legacy = FALSE
)
```

Arguments

logRr A numeric vector of effect estimates on the log scale.

seLogRr The standard error of the log of the effect estimates. Hint: often the standard

error = (log(<lower bound 95 percent confidence interval>) - log(<effect esti-

mate >))/qnorm(0.025).

trueLogRr A vector of the true effect sizes.

estimateCovarianceMatrix

Should a covariance matrix be computed? If so, confidence intervals for the

model parameters will be available.

legacy If true, a legacy error model will be fitted, meaning standard deviation is linear

on the log scale. If false, standard deviation is assumed to be simply linear.

Details

Fit a model of the systematic error as a function of true effect size. This model is an extension of the method for fitting the null distribution. The mean and log(standard deviations) of the error distributions are assumed to be linear with respect to the true effect size, and each component is therefore represented by an intercept and a slope.

Value

An object of type systematicErrorModel.

```
 controls <- simulateControls (n = 50 * 3, mean = 0.25, sd = 0.25, trueLogRr = log(c(1, 2, 4))) \\ model <- fitSystematicErrorModel(controls$logRr, controls$seLogRr, controls$trueLogRr) \\ model
```

grahamReplication 13

grahamReplication

Relative risks from an adjusted new-user cohort design

Description

Relative risks from an adjusted new-user cohort design

Usage

data(grahamReplication)

Format

A data frame with 126 rows and 4 variables:

outcomeName Name of the outcome

trueLogRr The log of the true effect size. Only provided for negative and positive controls, is NA for the outcome of interest (GI bleeding).

logRr The log of the incidence rate ratio

seLogRr The standard error of the log of the incidence rate ratio

Details

A dataset containing the incidence rate ratios (and standard errors) produced using a new-user cohort design that compares new-users of dabigatran to new-users of warfarin for the outcome of GI hemorrhage. The dataset includes estimates both for the outcome ofinterest as well as negative and positive control outcomes. Subject are required to have 183 days of continuous observation prior to initiating treatment, be at least 65 years old at index date, and are required to have no prior exposure to warfarin or dabigatran (or any other novel anticoagulant). Furthermore, subjects are required to use the treatment for the indication of atrial fibrillation or atrial flutter, which is enforced by requiring a prior diagnosis of atrial fibrillation or flutter, and no prior diagnosis of other indications. Propensity scores are generated by fitting a model for predicting treatment assignment based on baseline patient characteristics, and are used to perform one-on-one matching. Hazard ratios are estimated through a Cox regression on the matched population. Time-at-risk is defined as starting on the day after initiating treatment and stopping when treatment is stopped, when the outcome occurs, or observation time ends, whichever comes first. The original study (Graham et al 2016) uses the Medicare database. For our replication, we use the Truven Medicare Supplementary Beneficiaries database. We analyze 15,796 dabigatran-exposed and 15,796 warfarin-exposed subjects. For more information on this set see Schuemie et al (2017).

References

Schuemie MJ, Hripcsak G, Ryan PB, Madigan D, Suchard MA. Empirical confidence interval calibration for population-level effect estimation studies in observational healthcare data. Proc Natl Acad Sci U S A. 2018 Mar 13;115(11):2571-2577

Graham DJ, Reichman ME, Wernecke M, Hsueh YH, Izem R, Southworth MR, Wei Y, Liao J, Goulding MR, Mott K, Chillarige Y, MaCurdy TE, Worrall C, Kelman JA. Stroke, Bleeding, and Mortality Risks in Elderly Medicare Beneficiaries Treated With Dabigatran or Rivaroxaban for Nonvalvular Atrial Fibrillation. JAMA Intern Med 176(11):1662-1671, 2016

14 plotCalibration

plotCalibration

Create a calibration plot

Description

plotCalibration creates a plot showing the calibration of our calibration procedure

Usage

```
plotCalibration(
  logRr,
  seLogRr,
  useMcmc = FALSE,
  legendPosition = "right",
  title,
  fileName = NULL
)
```

Arguments

logRr A numeric vector of effect estimates on the log scale

seLogRr The standard error of the log of the effect estimates. Hint: often the standard

error = (log(<lower bound 95 percent confidence interval>) - log(<effect esti-

mate>))/qnorm(0.025)

useMcmc Use MCMC to estimate the calibrated P-value?

legendPosition Where should the legend be positioned? ("none", "left", "right", "bottom",

"top")

title Optional: the main title for the plot

fileName Name of the file where the plot should be saved, for example 'plot.png'. See the

function ggsave in the ggplot2 package for supported file formats.

Details

Creates a calibration plot showing the number of effects with p < alpha for every level of alpha. The empirical calibration is performed using a leave-one-out design: The p-value of an effect is computed by fitting a null using all other negative controls. Ideally, the calibration line should approximate the diagonal. The plot shows both theoretical (traditional) and empirically calibrated p-values.

Value

A Ggplot object. Use the ggsave function to save to file.

```
data(sccs)
negatives <- sccs[sccs$groundTruth == 0, ]
plotCalibration(negatives$logRr, negatives$seLogRr)</pre>
```

plotCalibrationEffect 15

plotCalibrationEffect Plot the effect of the calibration

Description

plotCalibrationEffect creates a plot showing the effect of the calibration.

Usage

```
plotCalibrationEffect(
  logRrNegatives,
  seLogRrNegatives,
  logRrPositives = NULL,
  seLogRrPositives = NULL,
  null = NULL,
  alpha = 0.05,
  xLabel = "Relative risk",
  title,
  showCis = FALSE,
  showExpectedSystematicError = FALSE,
  fileName = NULL
)
```

Arguments

logRrNegatives A numeric vector of effect estimates of the negative controls on the log scale. seLogRrNegatives

The standard error of the log of the effect estimates of the negative controls.

logRrPositives Optional: A numeric vector of effect estimates of the positive controls on the log scale.

seLogRrPositives

Optional: The standard error of the log of the effect estimates of the positive

controls.

null An object representing the fitted null distribution as created by the fitNull or

fitMcmcNull functions. If not provided, a null will be fitted before plotting.

alpha The alpha for the hypothesis test.

xLabel The label on the x-axis: the name of the effect estimate.

title Optional: the main title for the plot

showCis Show 95 percent credible intervals for the calibrated p = alpha boundary.

 $\verb|showExpectedSystematicError||$

Show the expected absolute systematic error. If null is of type mcmcNull the

95 percent credible interval will also be shown.

fileName Name of the file where the plot should be saved, for example 'plot.png'. See the

function ggsave in the ggplot2 package for supported file formats.

Details

Creates a plot with the effect estimate on the x-axis and the standard error on the y-axis. Negative controls are shown as blue dots, positive controls as yellow diamonds. The area below the dashed line indicated estimates with p < 0.05. The orange area indicates estimates with calibrated p < 0.05.

16 plotCiCalibration

Value

A Ggplot object. Use the ggsave function to save to file.

Examples

```
data(sccs)
negatives <- sccs[sccs$groundTruth == 0, ]
positive <- sccs[sccs$groundTruth == 1, ]
plotCalibrationEffect(negatives$logRr, negatives$seLogRr, positive$logRr, positive$seLogRr)</pre>
```

plotCiCalibration

Create a confidence interval calibration plot

Description

plotCalibration creates a plot showing the calibration of our confidence interval calibration procedure

Usage

```
plotCiCalibration(
  logRr,
  seLogRr,
  trueLogRr,
  strata = as.factor(trueLogRr),
  crossValidationGroup = 1:length(logRr),
  legacy = FALSE,
  evaluation,
  legendPosition = "top",
  title,
  fileName = NULL
)
```

Arguments

logRr A numeric vector of effect estimates on the log scale.

seLogRr The standard error of the log of the effect estimates. Hint: often the standard

error = (log(<lower bound 95 percent confidence interval>) - log(<effect esti-

mate>))/qnorm(0.025).

trueLogRr The true log relative risk.

strata Variable used to stratify the plot. Set strata = NULL for no stratification.

crossValidationGroup

What should be the unit for the cross-validation? By default the unit is a single control, but a different grouping can be provided, for example linking a negative control to synthetic positive controls derived from that negative control.

control to synthetic positive controls derived from that negative control.

If true, a legacy error model will be fitted, meaning standard deviation is linear on the log scale. If false, standard deviation is assumed to be simply linear.

legacy

evaluation A data frame as generated by the evaluateCiCalibration function. If pro-

vided, the logRr, seLogRr, trueLogRr, strata, and legacy arguments will be ig-

nored.

legendPosition Where should the legend be positioned? ("none", "left", "right", "bottom",

"top").

title Optional: the main title for the plot

fileName Name of the file where the plot should be saved, for example 'plot.png'. See the

function ggsave in the ggplot2 package for supported file formats.

Details

Creates a calibration plot showing the fraction of effects within the confidence interval. The empirical calibration is performed using a leave-one-out design: The confidence interval of an effect is computed by fitting a null using all other controls. Ideally, the calibration line should approximate the diagonal. The plot shows the coverage for both theoretical (traditional) and empirically calibrated confidence intervals.

Value

A Ggplot object. Use the ggsave function to save to file.

Examples

```
## Not run:
data <- simulateControls(n = 50 * 3, mean = 0.25, sd = 0.25, trueLogRr = log(c(1, 2, 4)))
plotCiCalibration(data$logRr, data$seLogRr, data$trueLogRr)
## End(Not run)</pre>
```

plotCiCalibrationEffect

Plot the effect of the CI calibration

Description

Creates a plot with the effect estimate on the x-axis and the standard error on the y-axis. The plot is trellised by true effect size. Negative and positive controls are shown as blue dots. The area below the dashed line indicated estimates that are statistically significant different from the true effect size (p < 0.05). The orange area indicates estimates with calibrated p < 0.05.

Usage

```
plotCiCalibrationEffect(
  logRr,
  seLogRr,
  trueLogRr,
  legacy = FALSE,
  model = NULL,
  xLabel = "Relative risk",
  title,
  fileName = NULL
)
```

18 plotCiCoverage

Arguments

logRr A numeric vector of effect estimates on the log scale.

seLogRr The standard error of the log of the effect estimates. Hint: often the standard

error = (log(<lower bound 95 percent confidence interval>) - log(<effect esti-

mate>))/qnorm(0.025).

trueLogRr A vector of the true effect sizes.

legacy If true, a legacy error model will be fitted, meaning standard deviation is linear

on the log scale. If false, standard deviation is assumed to be simply linear.

model The fitted systematic error model. If not provided, it will be fitted on the pro-

vided data.

xLabel The label on the x-axis: the name of the effect estimate.

title Optional: the main title for the plot

fileName Name of the file where the plot should be saved, for example 'plot.png'. See the

function ggsave in the ggplot2 package for supported file formats.

Value

A Ggplot object. Use the ggsave function to save to file.

Examples

```
data <- simulateControls(n = 50 * 3, mean = 0.25, sd = 0.25, trueLogRr = log(c(1, 2, 4))) plotCiCalibrationEffect(data$logRr, data$seLogRr, data$trueLogRr)
```

plotCiCoverage

Create a confidence interval coverage plot

Description

plotCiCoverage creates a plot showing the coverage before and after confidence interval calibration at various widths of the confidence interval.

Usage

```
plotCiCoverage(
  logRr,
  seLogRr,
  trueLogRr,
  strata = as.factor(trueLogRr),
  crossValidationGroup = 1:length(logRr),
  legacy = FALSE,
  evaluation,
  legendPosition = "top",
  title,
  fileName = NULL
)
```

plotErrorModel 19

Arguments

logRr A numeric vector of effect estimates on the log scale.

seLogRr The standard error of the log of the effect estimates. Hint: often the standard

error = (log(<lower bound 95 percent confidence interval>) - log(<effect esti-

mate>))/qnorm(0.025).

trueLogRr The true log relative risk.

strata Variable used to stratify the plot. Set strata = NULL for no stratification.

crossValidationGroup

What should be the unit for the cross-validation? By default the unit is a single control, but a different grouping can be provided, for example linking a negative

control to synthetic positive controls derived from that negative control.

legacy If true, a legacy error model will be fitted, meaning standard deviation is linear

on the log scale. If false, standard deviation is assumed to be simply linear.

evaluation A data frame as generated by the evaluateCiCalibration function. If pro-

vided, the logRr, seLogRr, trueLogRr, strata, and legacy arguments will be ig-

nored.

legendPosition Where should the legend be positioned? ("none", "left", "right", "bottom",

"top").

title Optional: the main title for the plot

fileName Name of the file where the plot should be saved, for example 'plot.png'. See the

function ggsave in the ggplot2 package for supported file formats.

Details

Creates a plot showing the fraction of effects above, within, and below the confidence interval. The empirical calibration is performed using a leave-one-out design: The confidence interval of an effect is computed by fitting a null using all other controls. The plot shows the coverage for both theoretical (traditional) and empirically calibrated confidence intervals.

Value

A Ggplot object. Use the ggsave function to save to file.

Examples

```
## Not run:
data <- simulateControls(n = 50 * 3, mean = 0.25, sd = 0.25, trueLogRr = log(c(1, 2, 4)))
plotCiCoverage(data$logRr, data$seLogRr, data$trueLogRr)
## End(Not run)</pre>
```

plotErrorModel P

Plot the systematic error model

Description

plotErrorModel creates a plot showing the systematic error model.

Usage

```
plotErrorModel(
  logRr,
  seLogRr,
  trueLogRr,
  title,
  legacy = FALSE,
  fileName = NULL
)
```

Arguments

logRr A numeric vector of effect estimates on the log scale.

seLogRr The standard error of the log of the effect estimates. Hint: often the standard

error = (log(<lower bound 95 percent confidence interval>) - log(<effect esti-

mate>))/qnorm(0.025).

trueLogRr The true log relative risk.

title Optional: the main title for the plot

legacy If true, a legacy error model will be fitted, meaning standard deviation is linear

on the log scale. If false, standard deviation is assumed to be simply linear.

fileName Name of the file where the plot should be saved, for example 'plot.png'. See the

function ggsave in the ggplot2 package for supported file formats.

Details

Creates a plot with the true effect size on the x-axis, and the mean plus and minus the standard deviation shown on the y-axis. Also shown are simple error models fitted at each true relative risk in the input.

Value

A Ggplot object. Use the ggsave function to save to file.

Examples

```
data <- simulateControls(n = 50 * 3, mean = 0.25, sd = 0.25, trueLogRr = log(c(1, 2, 4))) plotErrorModel(data$logRr, data$seLogRr, data$trueLogRr)
```

plotExpectedType1Error

Plot the expected type 1 error as a function of standard error

Description

plotExpectedType1Error creates a plot showing the expected type 1 error as a function of standard error.

Usage

```
plotExpectedType1Error(
  logRrNegatives,
  seLogRrNegatives,
  seLogRrPositives,
  alpha = 0.05,
  null = NULL,
  xLabel = "Relative risk",
  title,
  showCis = FALSE,
  showEffectSizes = FALSE,
  fileName = NULL
)
```

Arguments

logRrNegatives A numeric vector of effect estimates of the negative controls on the log scale. seLogRrNegatives

The standard error of the log of the effect estimates of the negative controls.

seLogRrPositives

The standard error of the log of the effect estimates of the positive controls.

alpha The alpha (nominal type 1 error) to be used.

null An object representing the fitted null distribution as created by the fitNull

function. If not provided, a null will be fitted before plotting.

xLabel If showing effect sizes, what label should be used for the effect size axis?

title Optional: the main title for the plot

showCis Show 95 percent credible intervals for the expected type 1 error.

showEffectSizes

Show the expected effect sizes alongside the expected type 1 error?

fileName Name of the file where the plot should be saved, for example 'plot.png'. See the

function ggsave in the ggplot2 package for supported file formats.

Details

Creates a plot with the standard error on the x-axis and the expected type 1 error on the y-axis. The red line indicates the expected type 1 error given the estimated empirical null distribution if no calibration is performed. The dashed line indicated the nominal expected type 1 error rate, assuming the theoretical null distribution.

If standard errors are provided for non-negative estimates these will be plotted on the red line as yellow diamonds.

Value

A Ggplot object. Use the ggsave function to save to file.

```
data(sccs)
negatives <- sccs[sccs$groundTruth == 0, ]
positive <- sccs[sccs$groundTruth == 1, ]
plotExpectedType1Error(negatives$logRr, negatives$seLogRr, positive$seLogRr)</pre>
```

plotForest plotForest

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Create a forest plot

Description

plotForest creates a forest plot of effect size estimates.

Usage

```
plotForest(
  logRr,
  seLogRr,
  names,
  xLabel = "Relative risk",
  title,
  fileName = NULL
)
```

Arguments

| logRr | A numeric vector of effect estimates on the log scale |
|----------|--|
| seLogRr | The standard error of the log of the effect estimates. Hint: often the standard error = $(\log(< \text{lower bound 95 percent confidence interval}) - \log(< \text{effect estimate}))/\text{qnorm}(0.025)$ |
| names | A vector containing the names of the drugs or outcomes |
| xLabel | The label on the x-axis: the name of the effect estimate |
| title | Optional: the main title for the plot |
| fileName | Name of the file where the plot should be saved, for example 'plot.png'. See the function ggsave in the ggplot2 package for supported file formats. |

Details

Creates a forest plot of effect size estimates (ratios). Estimates that are significantly different from 1 (alpha = 0.05) are marked in orange, others are marked in blue.

Value

A Ggplot object. Use the ggsave function to save to file.

```
data(sccs)
negatives <- sccs[sccs$groundTruth == 0, ]
plotForest(negatives$logRr, negatives$seLogRr, negatives$drugName)</pre>
```

plotMcmcTrace 23

plotMcmcTrace

Plot the MCMC trace

Description

Plot the MCMC trace

Usage

```
plotMcmcTrace(mcmcNull, fileName = NULL)
```

Arguments

mcmcNull An object of type mcmcNull as generated using the fitMcmcNull function.

fileName Name of the file where the plot should be saved, for example 'plot.png'. See the

function ggsave in the ggplot2 package for supported file formats.

Details

Plot the trace of the MCMC for diagnostics purposes.

Examples

```
## Not run:
data(sccs)
negatives <- sccs[sccs$groundTruth == 0, ]
null <- fitMcmcNull(negatives$logRr, negatives$seLogRr)
plotMcmcTrace(null)
## End(Not run)</pre>
```

 ${\tt plotTrueAndObserved}$

Plot true and observed values

Description

Plot true and observed values, for example from a simulation study.

Usage

```
plotTrueAndObserved(
  logRr,
  seLogRr,
  trueLogRr,
  xLabel = "Relative risk",
  title,
  fileName = NULL
)
```

24 sccs

Arguments

logRr A numeric vector of effect estimates on the log scale.

seLogRr The standard error of the log of the effect estimates. Hint: often the standard

error = (log(<lower bound 95 percent confidence interval>) - log(<effect esti-

mate>))/qnorm(0.025).

trueLogRr A vector of the true effect sizes.

xLabel The label on the x-axis: the name of the effect estimate.

title Optional: the main title for the plot

fileName Name of the file where the plot should be saved, for example 'plot.png'. See the

function ggsave in the ggplot2 package for supported file formats.

Details

Creates a forest plot of effect size estimates (ratios). Estimates that are significantly different from the true value (alpha = 0.05) are marked in orange, others are marked in blue.

Value

A Ggplot object. Use the ggsave function to save to file.

Examples

```
data <- simulateControls(n = 50 * 3, mean = 0.25, sd = 0.25, trueLogRr = log(c(1, 2, 4))) plotTrueAndObserved(data$logRr, data$seLogRr, data$trueLogRr)
```

sccs

Incidence rate ratios from Self-Controlled Case Series

Description

Incidence rate ratios from Self-Controlled Case Series

Usage

data(sccs)

Format

A data frame with 46 rows and 4 variables:

drugName Name of the drug

groundTruth Whether the drug is a positive (1) or negative (0) control

logRr The log of the incidence rate ratio

seLogRr The standard error of the log of the incidence rate ratio

simulateControls 25

Details

A dataset containing the incidence rate ratios (and standard errors) produced using a Self-Controlled Case Series (SCCS) design. The outcome is upper GI bleeding, the drug of interest (groundTruth = 1) is sertraline. Also included are 45 negative control drugs, for which we believe there to be no causal relation with upper GI bleeding. We used a database of medical records from general practices in the USA, the General Electric (GE) Centricity database, which contains data on 11.2 million subjects. We restricted on study period (start of 1990 through November 2003), age requirements (18 years or older), available time prior to event (180 days), and risk definition window (30 days following the prescription). Time 30 days prior to the first prescription was removed to account for possible contra-indications. Cases of upper GI bleeding were identified on the basis of the occurrence of ICD-9 diagnosis codes in the problem list. These codes pertain to esophageal, gastric, duodenal, peptic, and gastrojejunal ulceration, perforation, and hemorrhage, as well as gastritis and non-specific gastrointestinal hemorrhage. For more information on this set see Schuemie et al (2014).

References

Schuemie MJ, Ryan PB, Dumouchel W, Suchard MA, Madigan D. Interpreting observational studies: why empirical calibration is needed to correct p-values. Statistics in Medicine 33(2):209-18,2014

simulateControls

Simulate (negative) controls

Description

Simulate (negative) controls

Usage

```
simulateControls(
  n = 50,
  mean = 0,
  sd = 0.1,
  seLogRr = runif(n, min = 0.01, max = 0.2),
  trueLogRr = 0
)
```

Arguments

n Number of controls to simulate.

mean The mean of the error distribution (on the log RR scale).

sd The standard deviation of the error distribution (on the log RR scale).

seLogRr The standard error of the log of the relative risk. This is recycled for the controls.

The default is to sample these from a uniform distribution.

trueLogRr The true relative risk (on the log scale) used to generate these controls. This is

recycled for the controls.

Details

Generate point estimates given known true effect sizes and standard errors

Examples

```
data <- simulateControls(n = 50 * 3, mean = 0.25, sd = 0.25, trueLogRr = \log(c(1, 2, 4))) plotTrueAndObserved(data$logRr, data$seLogRr, data$trueLogRr)
```

southworthReplication Relative risks from an unadjusted new-user cohort design

Description

Relative risks from an unadjusted new-user cohort design

Usage

data(southworthReplication)

Format

A data frame with 174 rows and 4 variables:

outcomeName Name of the outcome

trueLogRr The log of the true effect size. Only provided for negative and positive controls, is NA for the outcome of interest (GI bleeding).

logRr The log of the incidence rate ratio

seLogRr The standard error of the log of the incidence rate ratio

Details

A dataset containing the incidence rate ratios (and standard errors) produced using a new-user cohort design that compares new-users of dabigatran to new-users of warfarin for the outcome of GI hemorrhage. The dataset includes estimates both for the outcome of interest as well as negative and positive control outcomes. Subjects are required to have 183 days of continuous observation prior to initiating treatment, a prior diagnosis of atrial fibrillation, and are required to have no prior exposure to either dabigatran or warfarin. The study computes an incidence rate ratio without any adjustment for confounders. Time at risk is defined as the time on the drug. The original study (Southworth 2013) uses the 'Mini-Sentinel Database'. For our replication, we use the Optum databases since both databases are US insurance claims databases. We analyzed 5,982 dabigatran-exposed and 19,155 warfarin-exposed subjects. For more information on this set see Schuemie et al (2017).

References

Schuemie MJ, Hripcsak G, Ryan PB, Madigan D, Suchard MA. Empirical confidence interval calibration for population-level effect estimation studies in observational healthcare data. Proc Natl Acad Sci U S A. 2018 Mar 13;115(11):2571-2577

Southworth MR, Reichman ME, Unger EF. Dabigatran and postmarketing reports of bleeding. N Engl J Med 368(14):1272-1274, 2013

Index

```
*Topic datasets
    caseControl, 4
    cohortMethod, 5
    grahamReplication, 13
    southworth {\tt Replication}, {\tt 26}
calibrateConfidenceInterval, 2
calibrateP, 3
caseControl, 4
cohortMethod, 5
{\tt computeExpectedSystematicError}, {\tt 6}
{\tt computeTraditionalCi, 7}
computeTraditionalP, 7
{\tt convertNullToErrorModel}, 8
evaluateCiCalibration, 9, 17, 19
fitMcmcNull, 8, 10
fitNull, 8, 11
fitSystematicErrorModel, 2, 8, 12
grahamReplication, 13
plotCalibration, 14
plotCalibrationEffect, 15
plotCiCalibration, 16
plotCiCalibrationEffect, 17
plotCiCoverage, 18
plotErrorModel, 19
{\tt plotExpectedType1Error, 20}
plotForest, 22
plotMcmcTrace, 23
plotTrueAndObserved, 23
sccs, 24
simulateControls, 25
southworth {\tt Replication}, {\tt 26}
```