

ME 599/699 Robot Modeling & Control

Fall 2021

Planning As Search

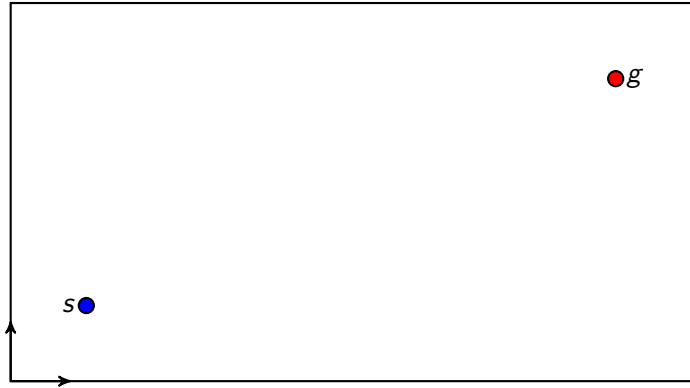
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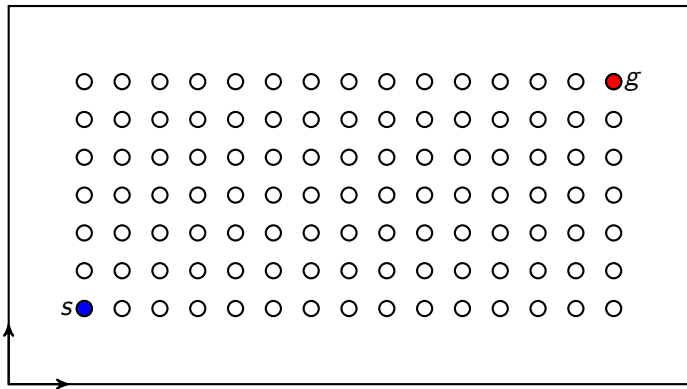
Web: <https://www.engr.uky.edu/~hap>

Graph Search



s = start, g = goal

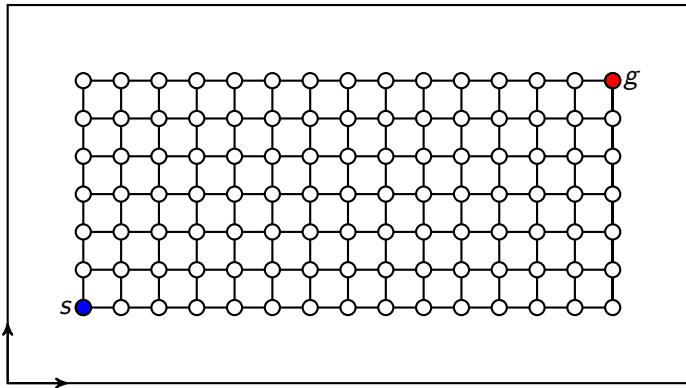
Graph Search



s = start, g = goal

Define nodes

Graph Search

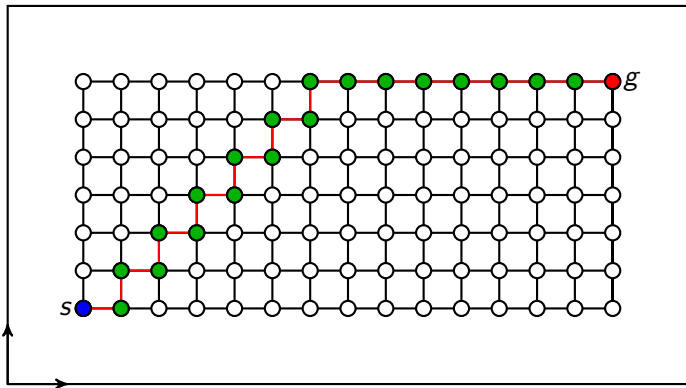


s = start, g = goal

Define nodes

Define edges

Graph Search



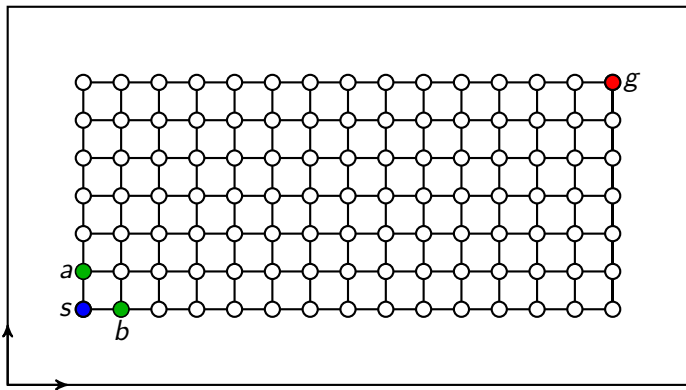
s = start, g = goal

Define nodes

Define edges

Find path(s)

Graph Search



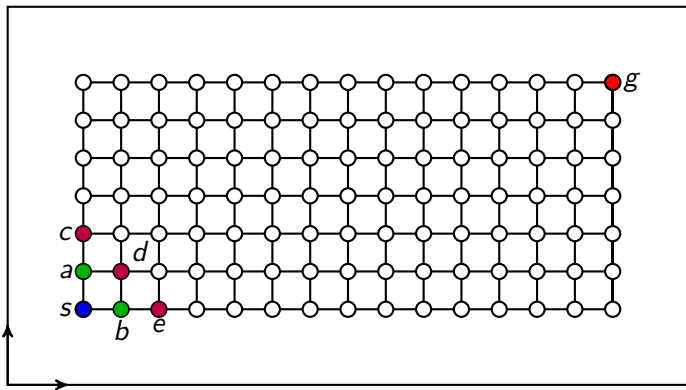
s = start, g = goal

Define nodes

Define edges

Let's focus on the nodes close to s

Graph Search



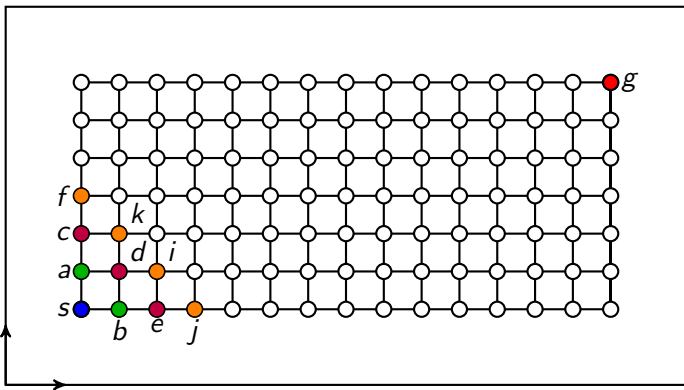
s = start, g = goal

Define nodes

Define edges

Let's focus on the nodes close to s

Graph Search



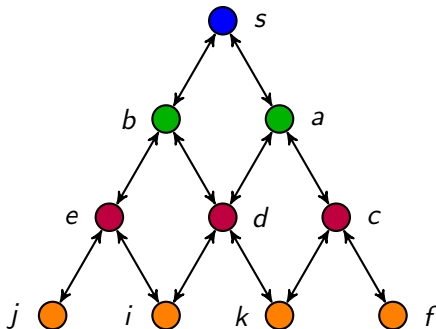
s = start, g = goal

Define nodes

Define edges

Let's focus on the nodes close to s

Graph As Seen From Start



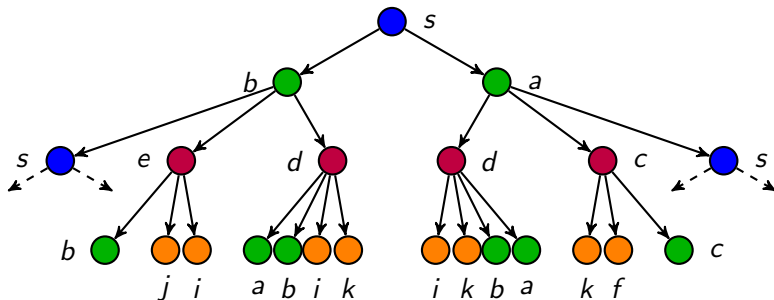
The undirected edges are equivalent to directed edges going forwards and back between two nodes.

We will use a search tree to **traverse** paths in this undirected graph.

Search Tree

The root of the search tree is node s .

This tree depicts the possible paths starting from s .



Each 'layer' contains the nodes reached after taking a step from a node in a preceding layer.

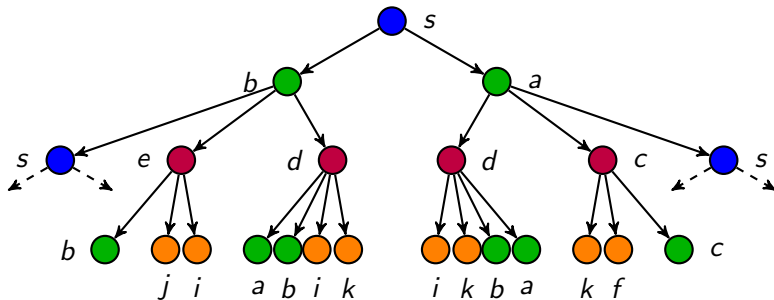
Each layer has a depth, starting at 0 for s on top.

Node s appears at depth 0 and 2; b at 1 and 3, etc.

Search Tree

The root of the search tree is node s .

This tree depicts the possible paths starting from s .



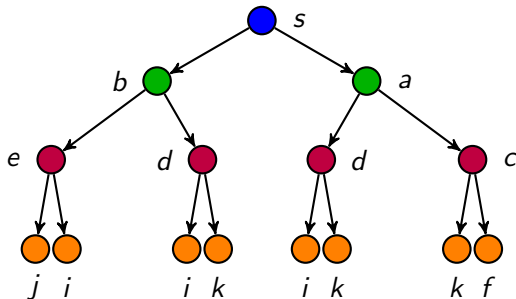
The actual tree is much larger, with infinite depth.

For example, the tree recursively repeats itself whenever s appears at some depth.

Search Tree

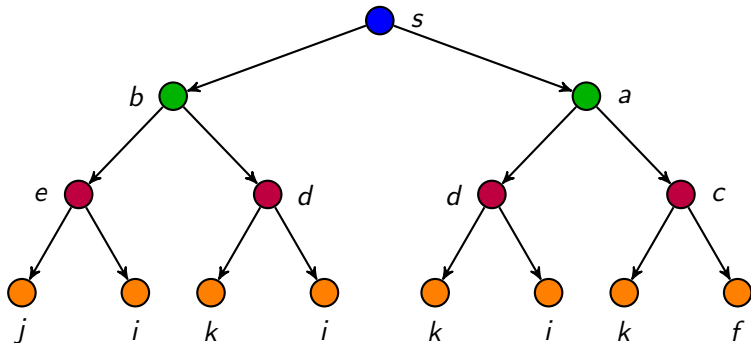
The root of the search tree is node s .

This tree depicts the possible paths starting from s .



If the edges in the graph were directed, we would never return to nodes located at smaller depths, simplifying the tree.

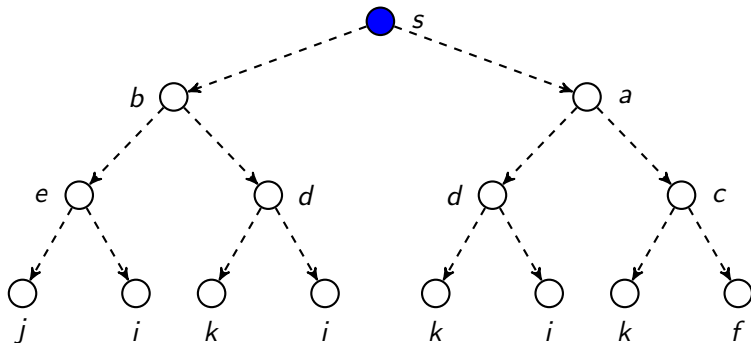
Search Tree



If a path exists from s to g , it is one of the possible paths in this search tree.

The key question is: how do we enumerate all the possible paths starting from s ?

Search Algorithms



Search algorithms avoid representing all paths, or the entire tree, at one go.

Instead, the search tree is incrementally traversed.

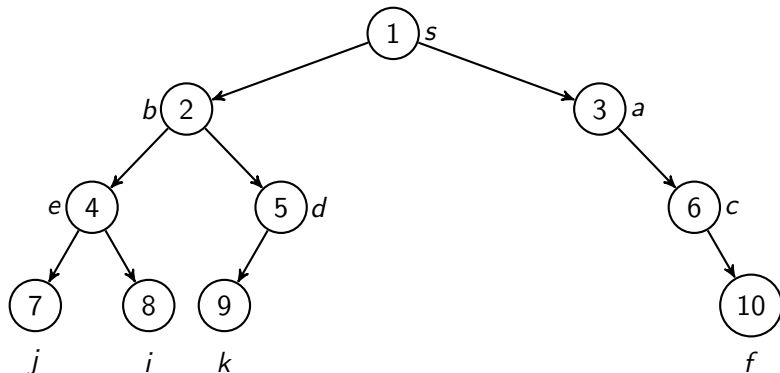
Start with root node, and no other nodes/edges.

Search Algorithms

Search algorithms differ in the order in which paths are evaluated, which boils down to the order in which unvisited successor states are checked for being the goal.

- ▶ Uninformed Search: Only know the successors at each node
 - ▶ Breadth First Search: Adds successors to end of list (Queue: first in first out)
 - ▶ Depth First Search: Adds successors to start of list (Stack: first in last out)
- ▶ Informed Search: Use an estimate of potential value of a node to order unvisited nodes (neither FIFO nor FILO).

Breadth-First Search



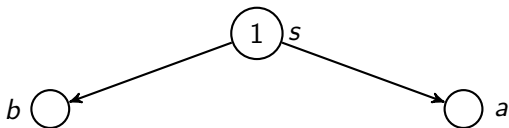
Order of visiting nodes under BFS. 'Row-by-row'

Breadth-First Search



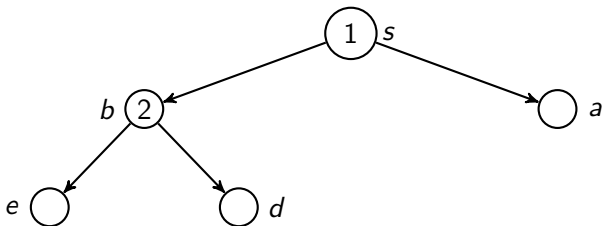
What the search tree looks like as it is built

Breadth-First Search



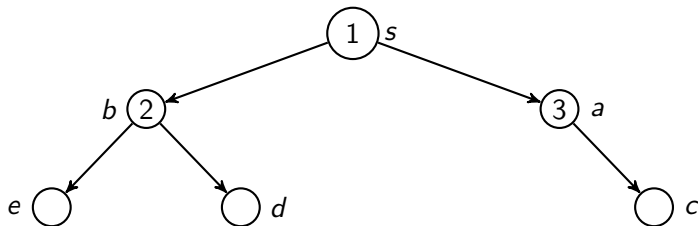
What the search tree looks like as it is built

Breadth-First Search



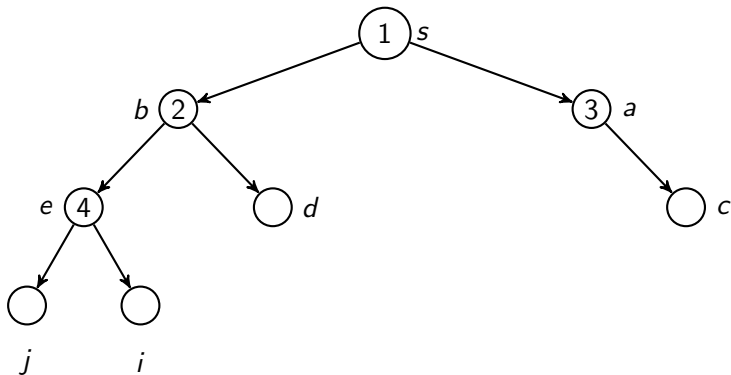
What the search tree looks like as it is built

Breadth-First Search



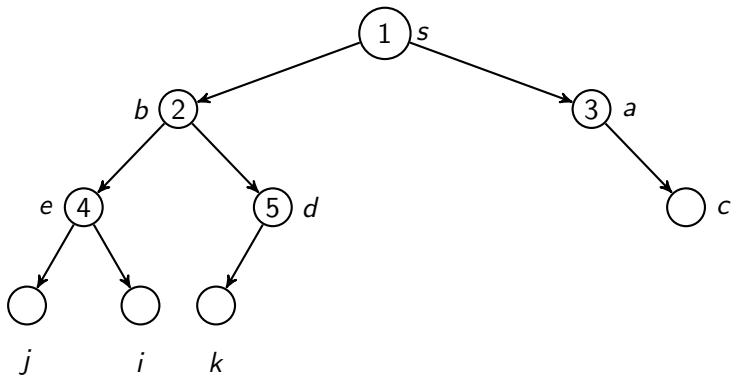
What the search tree looks like as it is built

Breadth-First Search



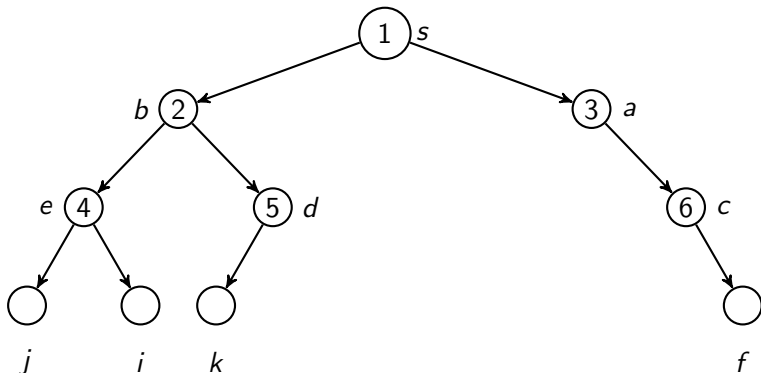
What the search tree looks like as it is built

Breadth-First Search



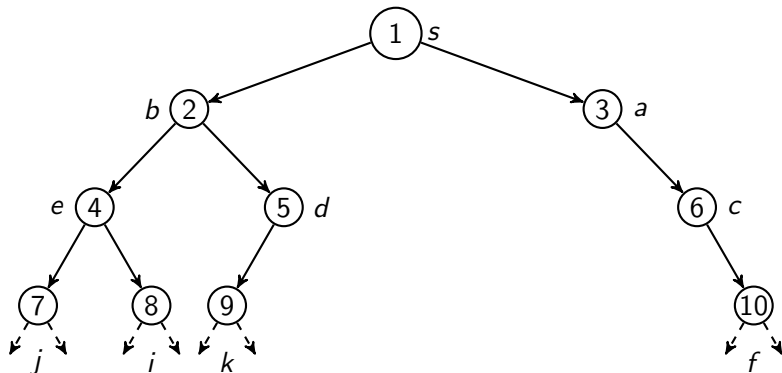
What the search tree looks like as it is built

Breadth-First Search



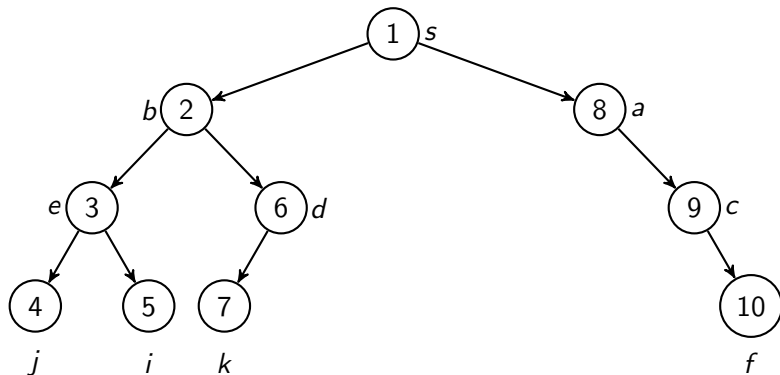
What the search tree looks like as it is built

Breadth-First Search



What the search tree looks like as it is built

Depth-First Search



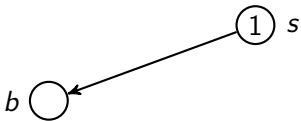
Order of visiting nodes under DFS. 'Column-by-column'

Depth-First Search



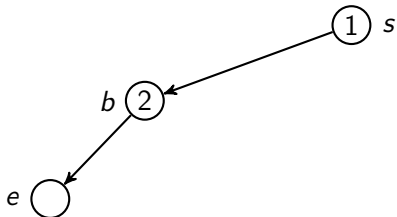
What the search tree looks like

Depth-First Search



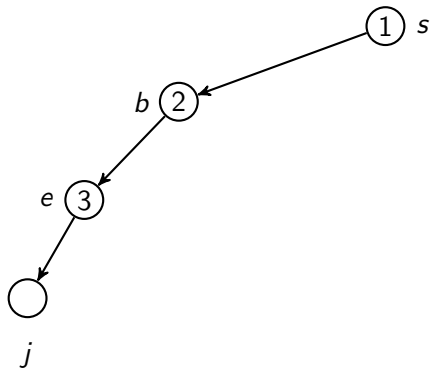
What the search tree looks like

Depth-First Search



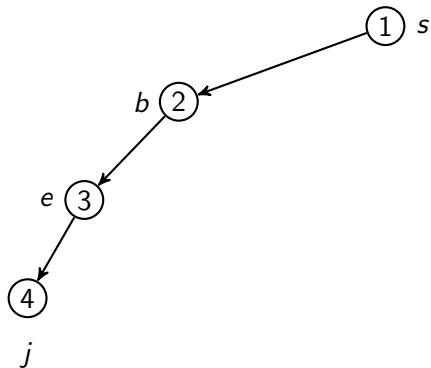
What the search tree looks like

Depth-First Search



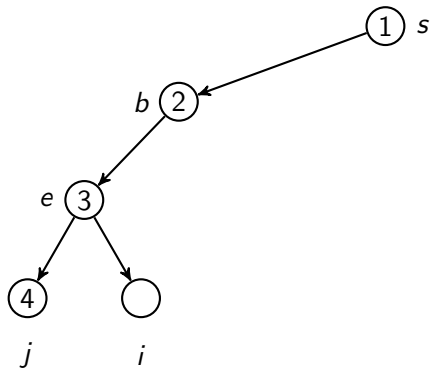
What the search tree looks like

Depth-First Search



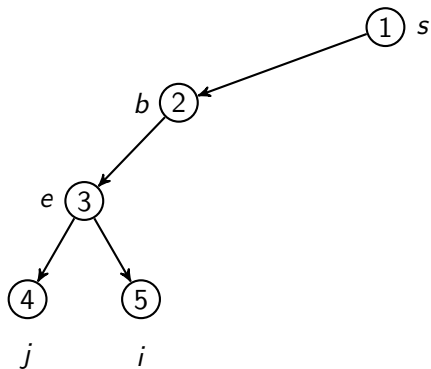
What the search tree looks like

Depth-First Search



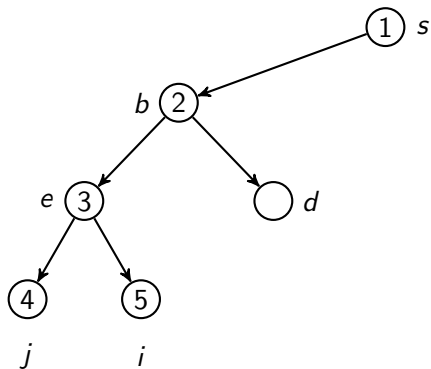
What the search tree looks like

Depth-First Search



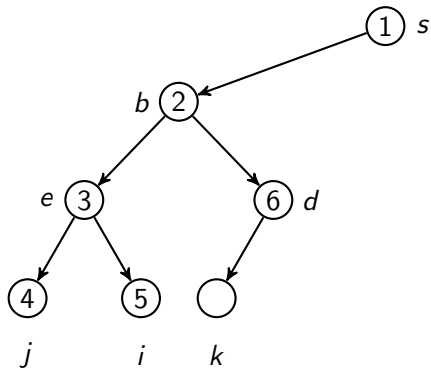
What the search tree looks like

Depth-First Search



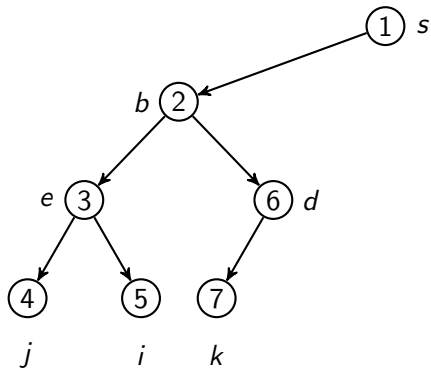
What the search tree looks like

Depth-First Search



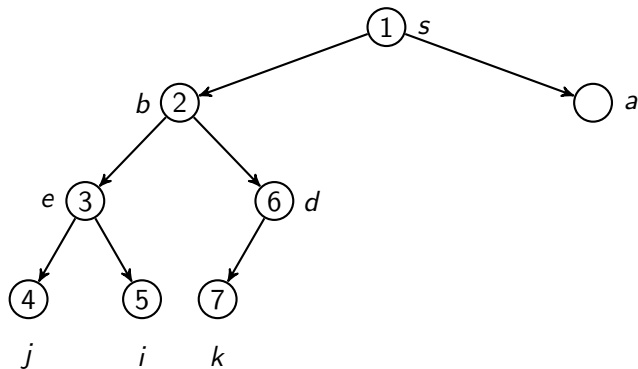
What the search tree looks like

Depth-First Search



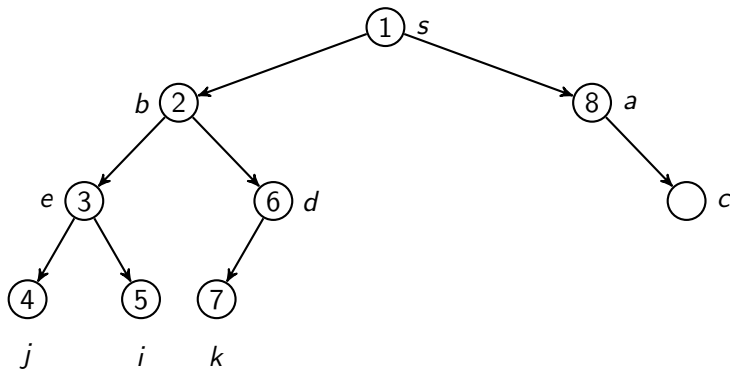
What the search tree looks like

Depth-First Search



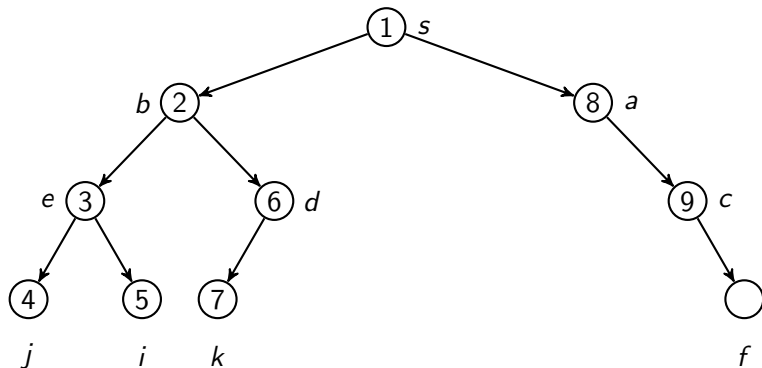
What the search tree looks like

Depth-First Search



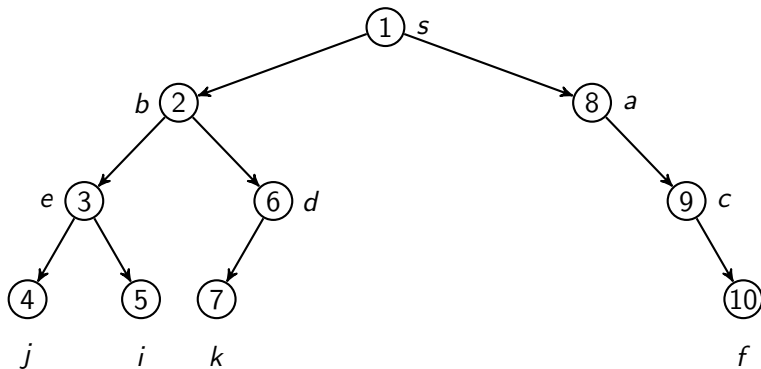
What the search tree looks like

Depth-First Search



What the search tree looks like

Depth-First Search



What the search tree looks like

Informed Search

- ▶ Breadth-First Search will find the goal, but it is slow when there are many successor states
- ▶ Depth-First Search might get stuck in loops, due to its implementation using recursion.
- ▶ While DFS and BFS creates an order between groups of successor nodes, they don't have a clear way to order the nodes within a group of successors
- ▶ Some estimate of how likely a node will lead to the goal would be a useful way to break ties
- ▶ This idea leads to informed search, where the estimate for each node is provided by a *heuristic* function

Two IS Algorithms

There are two quantities we can assign to a node:

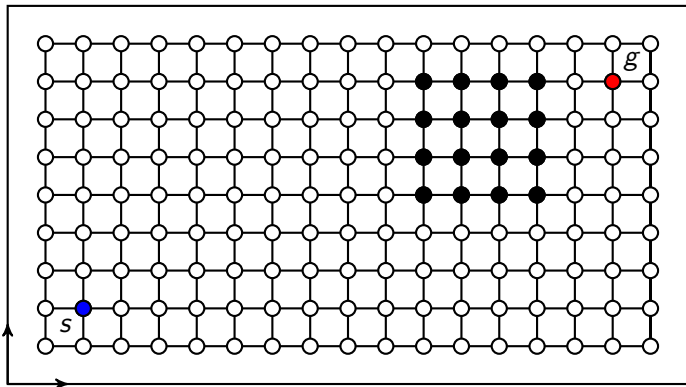
- ▶ The lowest cost $c(n)$ of the path – given the search tree uncovered so far – from root s to node n .
- ▶ The **estimated** least cost over all paths from n to goal g . We don't know this least-cost path, but we let estimate $h(n)$ be a guess of its true value $h^*(n)$ (unknown to us).

These quantities lead to two algorithms:

1. Best-First Search: order using $c(n)$
2. A*: order using $c(n) + h(n)$. Guaranteed performance when

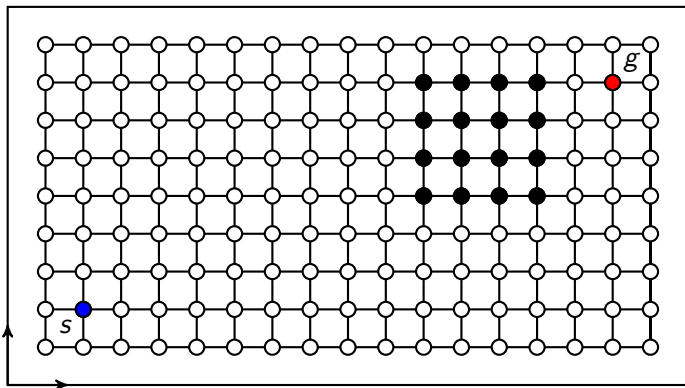
$$h(n) \leq h^*(n).$$

Motion Planning Discrete Space



Black nodes are 'obstacle' nodes

Motion Planning Discrete Space



Black nodes are 'obstacle' nodes

While we 'see' the graph all at once, our algorithms deal with this graph using a search tree