

```
> #1
> expr :=  $\frac{x^4 - x^3 - 11x^2 + 9x + 18}{x^4 - 3x^3 - 7x^2 + 27x - 18} : \frac{x^3 - 9x^2 + 26x - 24}{x^3 - 8x^2 + 19x - 12}$ 
```

(1)

```
> simplify(expr)

$$\frac{x+1}{x-1}$$

```

(2)

```
> #2
> expr := (2x - 1) · (3x2 + 5) · (5x + 2) :
> collect(expr, x)

$$30x^4 - 3x^3 + 44x^2 - 5x - 10$$

```

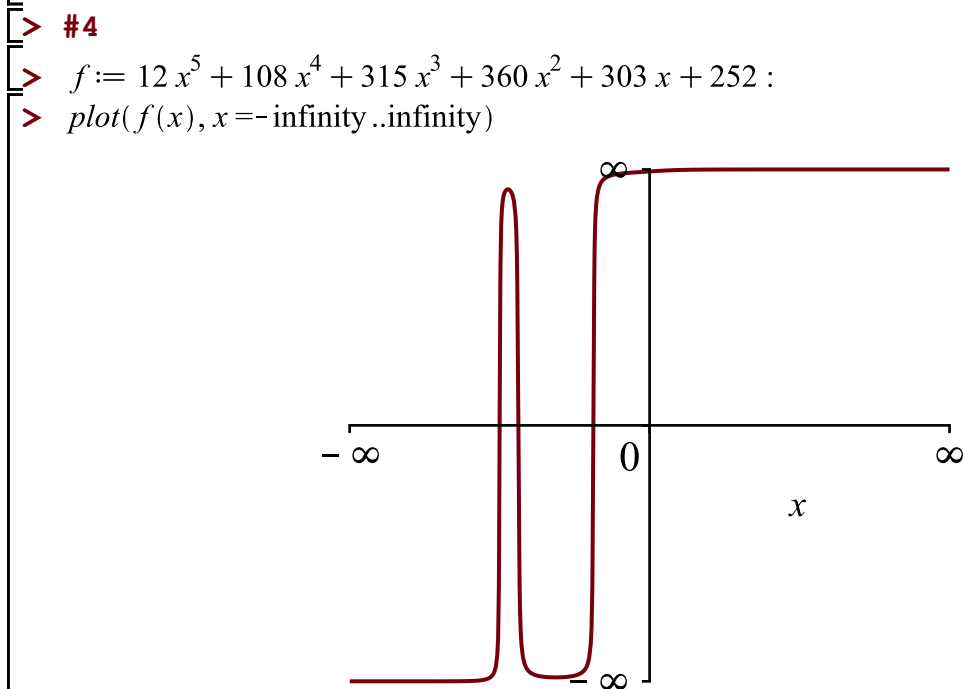
(3)

```
> #3
> expr := 14x4 - 46x3 - 82x2 + 138x + 120 :
> factor(expr)

$$2(7x + 5)(x - 4)(x^2 - 3)$$

```

(4)



```
> fsolve(f)
-4., -3.500000000, -1.500000000
```

(5)

```
> #5
> expr :=  $\frac{5x^4 + 7x^3 + 5x - 4}{(x^2 + 4) \cdot (x - 2)^2 \cdot (x^2 - 1)}$  :
> convert(expr, parfrac)

$$\frac{13}{10(x-1)} + \frac{-19x-23}{20(x^2+4)} + \frac{11}{90(x+1)} - \frac{17}{36(x-2)} + \frac{71}{12(x-2)^2}$$

```

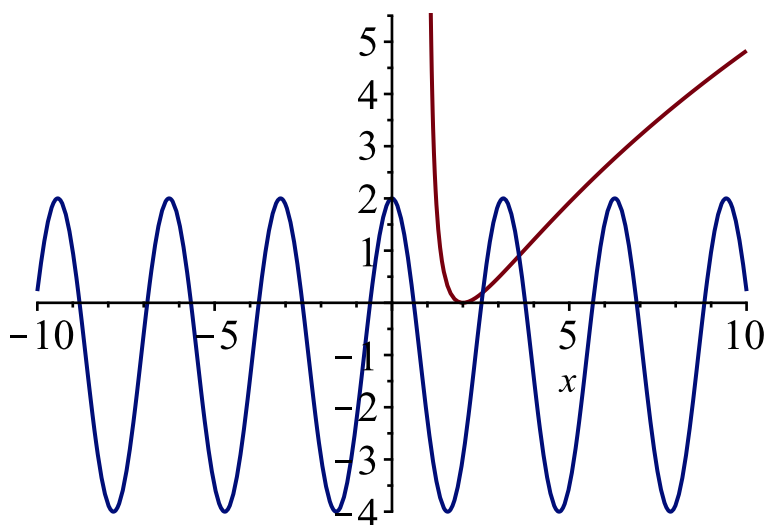
(6)

```
> #6
```

```

> f1 := ln2(x - 1) :
> f2 := 3 cos(2 x) - 1 :
> f := f1 = f2 :
> plot([f1, f2], x = -10 .. 10);

```



```

> fsolve(f, x = -infinity .. infinity)

```

2.561721559

(7)

```

> #7

```

```

> expr := (5 n - 2) / (2 n - 1) :

```

```

> solve([|5/2 - expr| < 0.1, n ≥ 1], n)

```

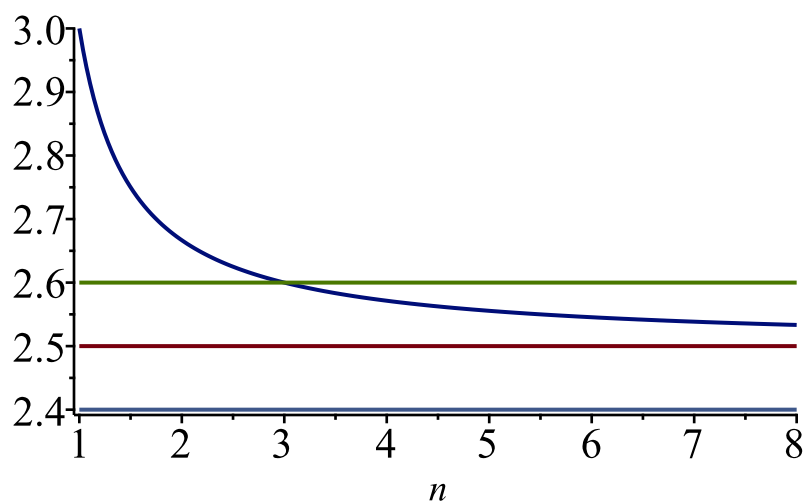
{3. < n}

(8)

```

> plot([5/2, expr, 5/2 + 0.1, 5/2 - 0.1], n = 1 .. 8)

```



```

> #8.1

```

```

> expr := n * (sqrt(n^2 + 1) - sqrt(n^2 - 1)) :

```

```

> limit(expr, n = infinity)

```

1

(9)

> #8.2

> $\text{expr} := \left(\frac{3n^2 - 6n + 7}{3n^2 + 20n - 1} \right)^{1-n} :$

> $\text{limit}(\text{expr}, n = \text{infinity})$

$$e^{\frac{26}{3}}$$

(10)

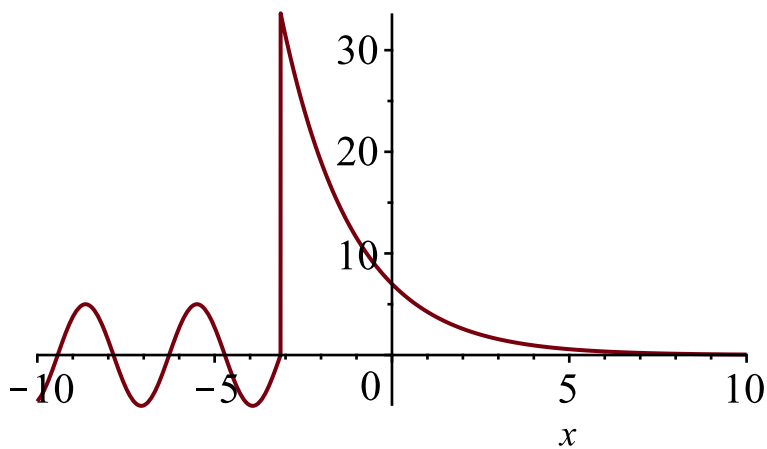
> #9.1

> $f := \text{piecewise}(x < -\text{Pi}, 5 \cdot \sin(2x), x \geq -\text{Pi}, 7 \cdot e^{-0.5x})$

$$f := \begin{cases} 5 \sin(2x) & x < -\pi \\ 7 e^{-0.5x} & -\pi \leq x \end{cases}$$

(11)

> $\text{plot}(f, x = -10..10)$



> #9.2

> $\text{limit}(f, x = -\text{Pi}, \text{left})$

$$0.$$

(12)

> $\text{limit}(f, x = -\text{Pi}, \text{right})$

$$33.67334167$$

(13)

> $\text{limit}(f, x = \text{infinity}, \text{left})$

$$0.$$

(14)

> $\text{limit}(f, x = -\text{infinity}, \text{right})$

$$-5..5.$$

(15)

> #9.3

> $f_{\text{diff}} := \text{diff}(f, x)$

$$f_{\text{diff}} := \begin{cases} 10. \cos(2. x) & x < -3.141592654 \\ \text{Float(undefined)} & x = -3.141592654 \\ -3.500000000 e^{-0.5000000000 x} & -3.141592654 < x \end{cases}$$

(16)

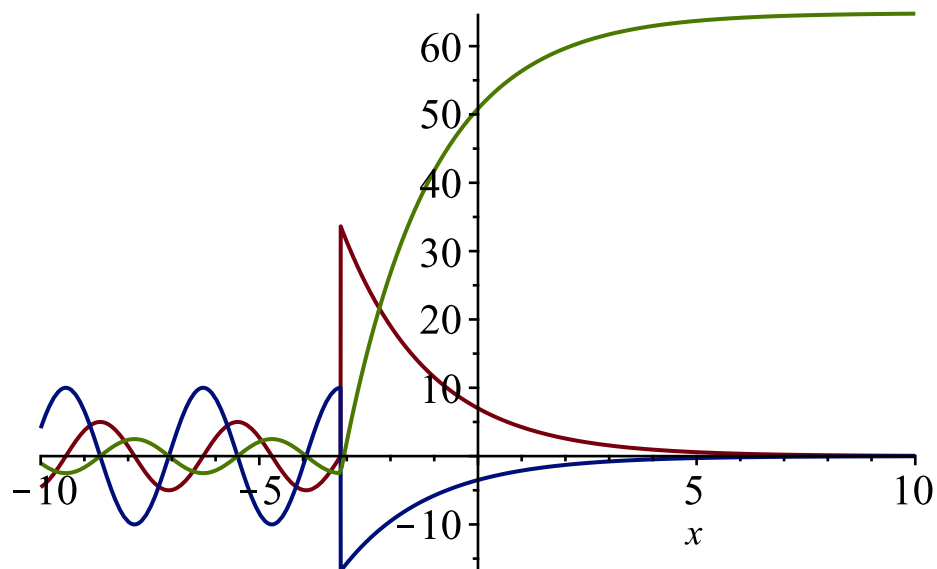
> $f_{\text{int}} := \text{int}(f, x)$

$$f_{\text{int}} := \begin{cases} -2.500000000 \cos(2. x) & x \leq -3.141592654 \\ -14. e^{-0.5000000000 x} + 64.84668333 & -3.141592654 < x \end{cases}$$

(17)

> #9.4

```
> plot([f, fdiff, fint], x=-10..10)
```



```
> #9.5
```

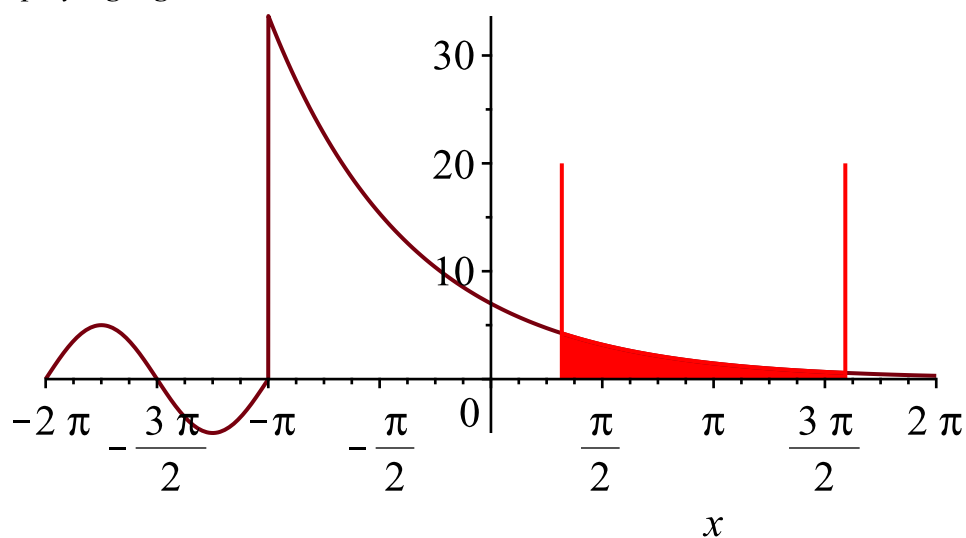
```
> g1 := plot(f) :
```

```
> g2 := plot(f, x=1..5, color=red, filled=true) :
```

```
> a1 := plot([1, z, z=0..20], color=red) :
```

```
> a2 := plot([5, z, z=0..20], color=red) :
```

```
> plots[display](g1, g2, a1, a2);
```



```
> int(f, x=1..5)
```

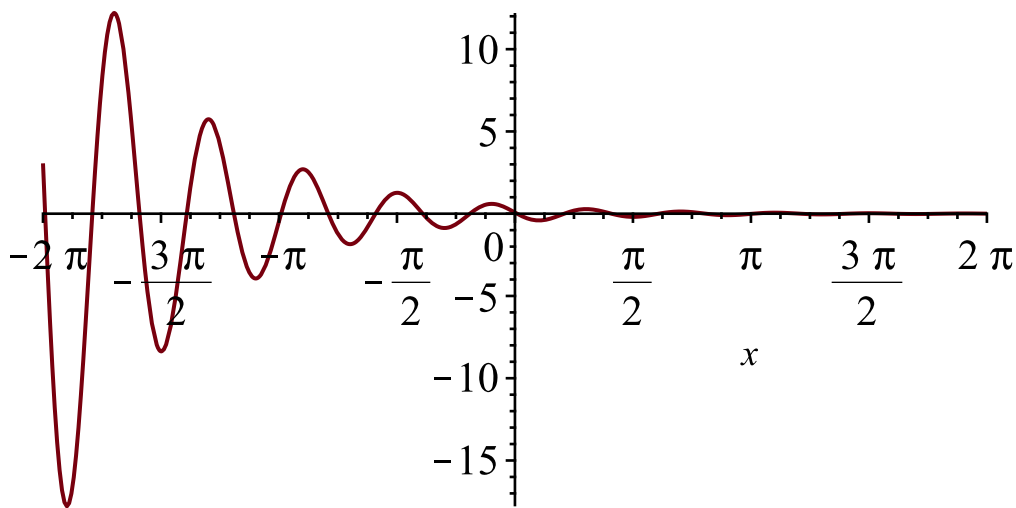
7.342239255

(18)

```
> #10.1
```

```
> f := 0.5 * exp(-0.6 * x) * sin(5 * x + 3) :
```

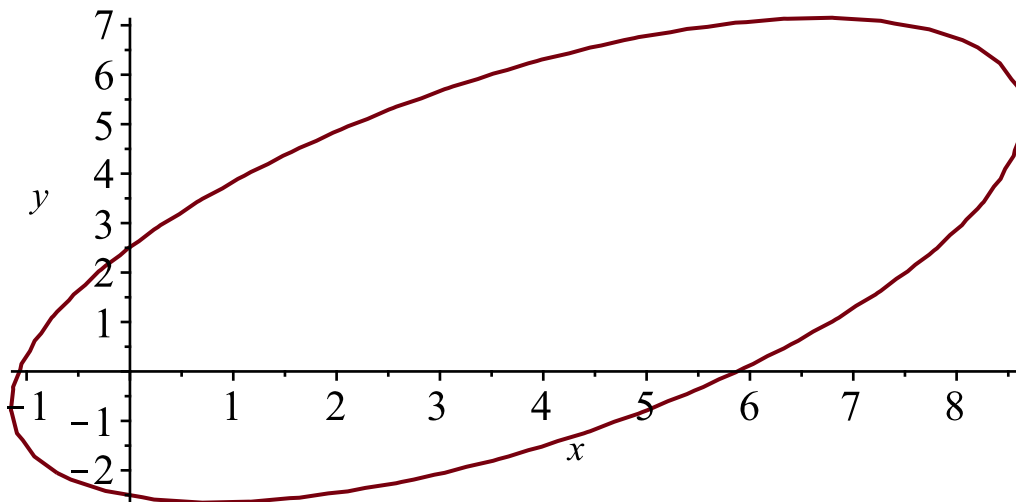
```
> plot(f, x)
```



> #10.2

> $f := 5x^2 - 6x \cdot y + 5y^2 - 24x - 32 = 0 :$

> `plots[implicitplot](f, x=-10..10, y=-10..10)`



> $M := \text{Matrix}([[5, -3], [-3, 5]])$

$$M := \begin{bmatrix} 5 & -3 \\ -3 & 5 \end{bmatrix}$$

(19)

> `LinearAlgebra[Eigenvectors](M)`

$$\begin{bmatrix} 2 \\ 8 \end{bmatrix}, \begin{bmatrix} 1 & -1 \\ 1 & 1 \end{bmatrix}$$

(20)

> `LinearAlgebra[Normalize](Matrix([1, 1]), 2)`

$$\begin{bmatrix} \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{bmatrix}$$

(21)

> `LinearAlgebra[Normalize](Matrix([-1, 1]), 2)`

$$\begin{bmatrix} -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \end{bmatrix}$$

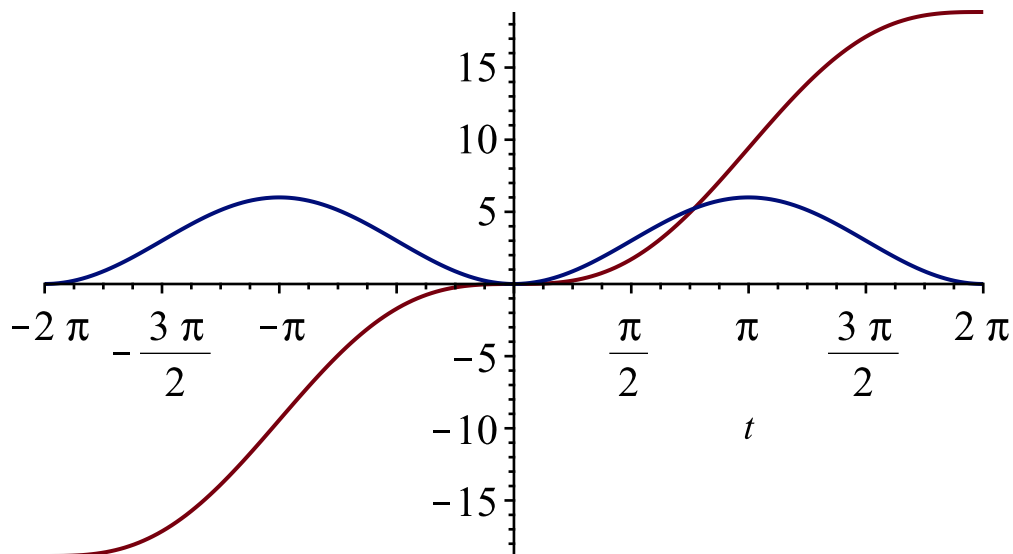
(22)

```
> X :=  $\frac{\sqrt{2}}{2} \cdot x + \frac{\sqrt{2}}{2} \cdot y$ :
```

```
> Y :=  $-\frac{\sqrt{2}}{2} \cdot x + \frac{\sqrt{2}}{2} \cdot y$ :
```

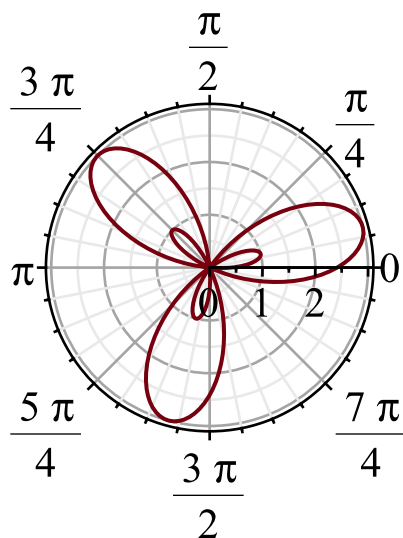
```
> #10.3
```

```
> plot([2 · (t + sin(t)), 2 · (1 − cos(t))])
```



```
> #10.4
```

```
> plots[polarplot](1 + 2 sin(3 x +  $\frac{\text{Pi}}{4}$ ), x)
```



```
>
```