# Object Oriented Programming with Applications Lecture 9

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#### Lecture 9

- C# style
- Problem Sheet 6 overview
- Example: solving 1D heat equation with finite differences

#### Prgramming style

Just like natural languages, each programming language has it's unique style. While we may be "translating" literary from a different language that we know (C++, R, Matlab, Python?) when we first learn a new language, it's important to develop a style shared by other coders using a given language (C#) in our case). It leads to more coherence and optimal use of language features.

Again, this is a highly subjective and each developer/team/organization will have their own conventions, but there are some common themes which we will briefly discuss in today's lecture.

#### General principles

- Simplicity Meet the expectation of your users with simple classes and simple methods.
- Clarity Ensure that each class, interface, method variable and object has a clear purpose. Explain where, when, why and how to use each.
- Completeness Provide the minimum functionality that any reasonable user would expect to find and use. Create complete documentation; document all features and functionality.
- Consistency Similar entities should look and behave the same;
- Robustness Provide predictable, documented behaviour in response to errors and expectations. Do not hide errors and do not force clients to detect errors.

#### General principles

- When working with an existing codebase try to adapt to it's style to assure consistency.
- Do it right the first time aim to write clear and readable code from the start of a project.
- No standard is perfect conventions are very useful and provide a lot of clarity, but they may not be suitable in certain situations (e.g. improving efficiency). When you deviate from a convention strive for as much clarity and consistency as possible and document why you've done so.
- Style checking tools there are tools (e.g. FXcop, Mono.Gendarme, Resharper) that can help enforce consistent style automatically by analyzing the code and displaying warnings/errors.

#### Formatting - whitespaces

Use a single space to separate the keywords, parentheses, and curly braces in control flow statements:

```
for (...)
   //...
if (...)
   //...
else if (...)
    //...
else
   //...
```

#### Formatting - whitespaces

Use a single space on either side of a binary operators, after commas and semicolons and between parameter list in method declaration:

```
double length = Math.Sqrt(x * x + y * y);
for (int i = 0; i < 100; i++)
{
    //...
}
Vector NormalizeVector(double x, double y, double z)
{
    //...
}</pre>
```

### Formatting - indentation

Use indented block statements:

#### Formatting - indentation

Break long statements into multiple lines and use indentation to group together similar elements

# Class organization

#### Organise class into regions

- Public properties
- Private fields
- Constructors
- Public methods
- Private Methods

#### Naming

Use meaningful names, define constants

```
if (a < 65)
   y = 65 - a;
else
VS
if (age < RetirementAge)</pre>
    yearsToRetirement = RetirementAge - age;
else
    yearsToRetirement = 0
```

#### Naming

- Name according to meaning, not type type information can be inferred from usage and context (e.g. no GetSumDouble())
- ...but suffix custom exception types with "Exception" e.g. "RootFindingException"
- Use familiar names use words that exist in the terminology of target domain (e.g. when designing an online shop use "Customer" rather than "Client")
- Use complete words ("Message" rather than "Msg")
- Use nouns to name classes and variables and verbs to name methods
- Avoid excessively long names
- Use **PascalCase** for namespaces, classes, structures, properties, enumeration and methods
- Use **camelCase** for variables and method parameter names
- Prefix interfaces with "I" (e.g. "IComparable")

#### The Elements of C# Style

We've only discussed the most basic examples of C# style.

These slides have been based on the book "The Elements of C# Style" by Kenneth Baldwin, Andrewy Grey and Trevor Misfeldt.

Please refer to it for a much more detailed treatment of the subject if you're interested in more details.

#### Problem Sheet 6

Available at: https://github.com/OOPA2018/ Problem-sheets/blob/master/ProblemSheet6.pdf

We would like to solve (approximate solution to):

$$\frac{\partial u}{\partial t} - \frac{1}{2} \frac{\partial^2 u}{\partial x^2} = 0$$
 on  $(0, T] \times (-R, R)$ ,

subject to  $u(\cdot, -R) = u(\cdot, R) = 0$  and  $u(0, \cdot) = u_0(\cdot)$  given.

Let

$$\delta_{\tau}f(t,x) := \frac{f(t,x) - f(t-\tau,x)}{\tau} \approx \frac{\partial f}{\partial t}(t,x)$$
$$\Delta_{h}f(t,x) := \frac{f(t,x+h) - 2f(t,x) - f(t,x-h)}{h^{2}} \approx \frac{\partial^{2} f}{\partial x^{2}}(t,x).$$

Using Taylor's theorem you can check that if f is smooth and has bounded derivatives then

$$igg| \delta_{ au} f(t,x) - rac{\partial f}{\partial t}(t,x) igg| \le c au$$
 $igg| \Delta_h f(t,x) - rac{\partial^2 f}{\partial x^2}(t,x) igg| \le c h^2,$ 

with c depending on f.

Let  $K \in \mathbb{N}$  and  $J \in \mathbb{N}, J > 1$  be given and set  $\tau = \frac{T}{K}$  and  $h := \frac{2R}{J-1}$ . Let  $\nu$  be a solution to

$$\delta_{\tau}v - \frac{1}{2}\Delta_{h}v = 0 \text{ on } M_{T},$$

with  $v(\cdot, -R) = v(\cdot, R) = 0$  and  $v(0, \cdot) = u_0(\cdot)$ , where  $M_T$  is

$$\{(t,x): t=\tau, 2\tau, \ldots, T, x=-R+h, -R+2h, \ldots, R-2h, R-h\}.$$

This v should be a good approximation of the heat equation.

To implement this on a computer:

Let  $v^{k,j} := v(k\tau, -R + jh)$  and let us collect what we know:

- 1 k runs from 1 to K and j runs from 0 to J-1.
- 2  $v^{k,0} = v^{k,J-1} = 0$  for all k = 1, ..., K (boundary conditions).
- $v^{0,j} = u_0(-R+jh)$  for all  $j = 0, \dots, J-1$  (initial condition).

$$\frac{v^{k,j} - v^{k-1,j}}{\tau} - \frac{1}{2} \frac{v^{k,j+1} - 2v^{k,j} + v^{k,j-1}}{h^2} = 0$$

for k = 1, ..., K and j = 1, ..., J - 1.

Consider  $v^k$  as a column vector of length J with entries  $v^{k,j}$ .

Then  $k = 1, \ldots, K$ 

$$\frac{v^k - v^{k-1}}{\tau} + Av^k = 0$$

if we take A to be

$$\begin{pmatrix} h^{-2} & 0 & 0 & 0 & \cdots & 0 & 0 \\ -\frac{1}{2}h^{-2} & h^{-2} & -\frac{1}{2}h^{-2} & 0 & \cdots & 0 & 0 \\ 0 & -\frac{1}{2}h^{-2} & h^{-2} & -\frac{1}{2}h^{-2} & \cdots & 0 & 0 \\ \vdots & \ddots & \ddots & \ddots & \ddots & \vdots & \vdots \\ 0 & \cdots & 0 & -\frac{1}{2}h^{-2} & h^{-2} & -\frac{1}{2}h^{-2} & 0 \\ 0 & 0 & \cdots & 0 & -\frac{1}{2}h^{-2} & h^{-2} & -\frac{1}{2}h^{-2} \\ 0 & 0 & \cdots & 0 & 0 & h^{-2} \end{pmatrix}.$$

At each time step k we have to solve

$$(I - \tau A)v^k = v^{k-1}.$$

This is a linear system.

Let  $S := I + \tau A$ . Then we are solving  $Sv^k = v^{k-1}$ .

#### Our code will need:

- 1 Problem information: T, R,  $u_0$ .
- 2 Discretization information: K and J.
- 3 One vector to represent  $v^{k-1}$ , call it v01d.
- 4 One vector to represent  $v^k$ , call it vNew.
- 5 The sparse matricies A and S.
- 6 A linear solver. We will use iterative solver for sparse matricies.

```
class HeatEq1DFinDiffSolver
    // problem parameters
    private double T;
    private double R; // we are solving on (0,T) \times (-R,R) with 0 bdry cond.
    private Func<double, double> initialCondition;
    // discretization parameters
    private int J; // number of steps in space
    private int K; // number of steps in time
    private double h:
    // needed for work
    private Matrix<double> A;
    private Matrix<double> S;
    // for solving linear system iteratively;
    Iterator<double> monitor:
    BiCgStab solver;
```

We need to construct the finite difference matrix A.

With MathNet.Numerics this can be done by creating a function  $(i,j)\mapsto A_{ij}$ . E.g.  $(1,1)\mapsto h^{-2}$ .

So we write the function

```
Func<int, int, double> matrixEntry = (i, j) =>
{
    if (i == j) // diagonal entry
        return 1.0/(h*h);
    else if (i > 0 && j == i + 1)
        return -1.0 / (2 * h * h);
    else if (i < J - 1 && j == i - 1)
        return -1.0 / (2 * h * h);
    else
        return 0;
};</pre>
```

#### And then create A:

```
A = Matrix<double>.Build.Sparse(J, J, matrixEntry);
```

#### Now the matrix S:

```
double tau = T / K;
Matrix<double> I = Matrix<double>.Build.SparseIdentity(J);
S = (I - tau*A);
```

#### Iterative solver:

We must discretize the initial condition:

```
public Vector<double> ApproxInitialCondition()
{
    Vector<double> u0 = Vector<double>.Build.Dense(J);
    for (int i = 0; i < J; ++i)
        u0[i] = initialCondition(-R + i * h);
    return u0;
}</pre>
```

And we solve by iterating through the time-steps:

```
public Vector<double> Solve()
   SetUpSolver();
   Vector<double> uOld = ApproxInitialCondition();
   Vector<double> uNew = Vector<double>.Build.Dense(J):
   for (int k = 0; k < K; k++)
       // Must solve ( I - tau * A ) * uNew = uOld i.e. S * uNew = uOld
       uNew = S.SolveIterative(uOld, solver, monitor);
       uOld = uNew:
       Console.Write("Step {0}, ", k);
   Console.WriteLine():
   return uNew;
```